

Title Fermat's Last Theorem

Author Barry Foster

Abstract Fermat's Last Theorem states that there are no natural numbers A, B, C, and n such that $A^n = B^n + C^n$ is true.

This effort examines the attributes of the numbers in the equation to show that natural numbers for A, B, and C cannot satisfy it, irrational numbers are required.

Proof The proposition was first stated as a theorem by Pierre de Fermat around 1637 in the margin of a copy of Arithmetica.

<https://en.wikipedia.org/wiki/Arithmetica>

Fermat added that he had a proof that was too large to fit in the margin and because he had done likewise for other since-proved theorems there has since been a search to find a proof.

This effort uses the fact that the nth root of a number is irrational unless the number is a number raised to the nth power.

Consider the natural numbers A, B, C and n where $A > B > C$ and $n > 2$.

Assume Fermat's Last Theorem is true.

$$\begin{aligned}
 \text{Then } A^n &= B^n + C^n \\
 &= (B^n - C^n) + 2C^n \\
 &= 2C^n + 2(B^n - C^n)/2 \\
 &= 2(C^n + (B^n - C^n)/2) \\
 &= 2^{1/n} (C^n + (B^n - C^n)/2)^{1/n}
 \end{aligned}$$

Thus A is the product of 2 numbers which are nth roots namely $2^{1/n}$ and a larger one $(C^n + (B^n - C^n)/2)^{1/n}$.

These numbers are irrational as is their product.

The conclusions are that the theorem is true and the margin probably *wasn't* big enough.