# Relative Universe 

A special theory of gravitation
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#### Abstract

Gravitation is the relative density of space-time caused by the mass of an object. There are three aspects of gravitation. First, it is related to an object. Gravitation can cause changes in the velocity of an object. Second, it is related to a photon, gravitation can change the frequency of a photon. Third, it is related to differences in the result of observation. Different observers of the same object can yield different results. Gravitation causes differences in the period of an event, differences in the length of an object, and differences in the mass or energy of an object.


Keywords: Expanding universe, Pseudo movement, Relative universe, Special theory of gravitation.

## 1. INTRODUCTION

According to Newtonian mechanics, gravitation is the force that every object exerts on every other object. The value of the gravitational force is directly proportional to the product of their masses and inversely proportional to the square of the distance between them.


Figure 1
$F=G \frac{m_{1} m_{2}}{r^{2}}$
Where
$F$ is the force between two objects.
$G$ is the gravitational constant.
$m_{l}$ and $m_{2}$ are the masses of the objects.
$r$ is the distance between the two objects.
If the value of object $m_{1}$ is much higher than object $m_{2}$, there is an equation for gravitation.
$g=G \frac{m_{1}}{r^{2}}$
Where
g is gravitation.
2. POTENTIAL ENERGY AND KINETIC ENERGY


Figure 2
$\mathrm{O}_{1}$ is Observer1, $\mathrm{O}_{2}$ is Observer2, $\mathrm{P}_{1}$ is Position1, $\mathrm{P}_{2}$ is Position2, and $h$ is the height between $\mathrm{P}_{1}$ and $\mathrm{P}_{2}$. An object with mass $m$ is dropped at position $\mathrm{P}_{1}$. The initial velocity $V$ is $V_{I}=0$. The object then free-falls to position $\mathrm{P}_{2}$. At $\mathrm{P}_{2}$ the velocity of the object is $V_{2}=V$.

The object has potential and kinetic energy. Potential energy is energy held by an object because of its height. Kinetic energy is a form of energy held because of its motion.
$E_{p}=m g h$
$E_{p}$ is potential energy, $m$ is the mass of the object, $g$ is gravitation and $h$ is the height of the object.
$E_{k}=\frac{1}{2} m v^{2}$
$E_{k}$ is kinetic energy, $m$ is the mass of the object, and $v$ is the velocity of the object.
When the object is dropped from a height there is a change in energy from potential energy to kinetic energy.
When the position of the object is at $\mathrm{P}_{1} E_{p}=m g h$ and $E_{k}=0$ because $V=0$.
When the position of the object is at $\mathrm{P}_{2} E_{p}=0$ because $h=0$ and $E_{k}=\frac{1}{2} m v^{2}$.
The total energy consisting of potential energy and kinetic energy is constant. There are only changes in the forms of energy.
$m g h_{1}+\frac{1}{2} m v_{1}^{2}=m g h_{2}+\frac{1}{2} m v_{2}^{2}$

## Relative Universe

## 3. DIFFERENCE IN TOTAL ENERGY DUE TO DIFFERENCE IN OBSERVER POSITION

According to Einstein's special theory of relativity, mass is equivalent to energy, $E=m c^{2}$, where $E$ is the energy of an object, $m$ is the mass of an object, and $c$ is the speed of light. The total energy of an object consists of rest mass energy and kinetic energy. When the speed of an object is much less than the speed of light then Newton's equation for kinetic energy $E_{k}=\frac{1}{2} m v^{2}$ is still valid.


Figure 3
See Figure 3
Observer $\mathrm{O}_{1}$ is at position $\mathrm{P}_{1}$, and observer $\mathrm{O}_{2}$ is at position $\mathrm{P}_{2}$.
From the viewpoint of observer $\mathrm{O}_{1}$ when the position of the object is at $\mathrm{P}_{1}$.
$h=0$ and $v=0$.
Therefore
$E_{r}=m c^{2}$, where $E_{r}$ is the rest energy.
$E_{p}$ is potential energy $=m g h$. Because $h=0$ then $E_{\mathrm{p}}=0$,
$E_{k}=\frac{1}{2} m v^{2}$, and because $v=0$ then $E_{k}=0$
The total energy $=m c^{2}+m g h+\frac{1}{2} m v^{2}=m c^{2}$ or $E_{t}=E_{r}$
When the position of the object is at P 2 .
$h=-h$ and $v=v$
$E_{r}=m c^{2}$
$E_{p}=-m g h$,
and $E_{k}=\frac{1}{2} m v^{2}$
The total energy $=m c^{2}-m g h+\frac{1}{2} m v^{2}=m c^{2}$ or $E_{t}=E_{r}$

## Relative Universe

because $m g h=\frac{1}{2} m v^{2}$.

From the viewpoint of observer $\mathrm{O}_{2}$ when the position of the object is at $\mathrm{P}_{1}$ :
$h=h$ and $v=0$
$E_{p}=m g h$,
and $E_{k}=\frac{1}{2} m v^{2} E_{\mathrm{k}}=0$ because $v=0$.
And total energy $=m c^{2}+m g h+\frac{1}{2} m v^{2}=m c^{2}+m g h$ or $E_{t}=E_{r}+E_{p}$, because $v=0$.
When the position of the object is at $\mathrm{P}_{2}$,
$h=0$ and $v=v$.
$E_{p}=m g h, E_{\mathrm{p}}=0$
and $E_{k}=\frac{1}{2} m v^{2}$
and total energy $=m c^{2}+m g h+\frac{1}{2} m v^{2}=m c^{2}+\frac{1}{2} m v^{2}$, because $h=0$
or total energy $E_{t}=E_{r}+E_{k}$
or total energy $E_{t}=E_{r}+E_{p}$
because $m g h=\frac{1}{2} m v^{2}$ or $E_{p}=E_{k}$.

| Observer | Total energy |  | Difference in the <br> total energy |
| :--- | :--- | :--- | :--- |
|  | Position object at $\mathrm{P}_{1}$ | Position object at $\mathrm{P}_{2}$ |  |
| $\mathrm{O}_{1}$ | $E_{t}=E_{r}$ | $E_{t}=E_{r}+E_{k}-E_{p}=E_{r}$ | No |
| $\mathrm{O}_{2}$ | $E_{t}=E_{r}+E_{p}$ | $E_{t}=E_{r}+E_{k}$ or $E_{t}=E_{r}+E_{p}$ <br> Because $E_{k}=E_{p}$ | No |
| Difference in the <br> total energy | Yes | Yes |  |

Table 1
We can see that the cause of the difference in total energy is the position of the observer, not the position of the object

## Relative Universe

## 4. LIGHT AND GRAVITATION



Figure 4

When light is directed from position $\mathrm{P}_{1}$ to $\mathrm{P}_{2}$, there is a change in the frequency of the light. Observer $\mathrm{O}_{2}$ at position $\mathrm{P}_{2}$ will detect a higher frequency of light than the frequency detected by observer $\mathrm{O}_{1}$ at position $\mathrm{P}_{1}$

From the viewpoint of observer $\mathrm{O}_{1}$ at position $\mathrm{P}_{1}$
$v=v_{1}$
$T_{1}=\frac{1}{v_{1}}$
$\lambda_{1}=\frac{c}{v_{1}}$
$E_{1}=h v_{1}$

From the viewpoint of observer $\mathrm{O}_{2}$ at position $\mathrm{P}_{2}$
$v=v_{2}$
$T_{2}=\frac{1}{v_{2}}$
$\lambda_{2}=\frac{c}{v_{2}}$
$E_{2}=h v_{2}$
$\mathrm{v}_{1}<\mathrm{v}_{2}, \lambda_{1}>\lambda_{2}, T_{1}>T_{2}$, and $E_{1}<E_{2}$
$v$ is the light frequency.
$h$ is the Planck constant

## Relative Universe

$\lambda$ is the light wavelength.
$T$ is the wave period of light.
Compared to observer $\mathrm{O}_{1}$ at position 1, observer $\mathrm{O}_{2}$ at position 2 observes that the wave period of the light is slower, the wavelength is shorter and the energy is higher.

| Observer | Wavelength | Frequency | Period | Energy |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{O}_{1}$ | $\lambda_{1}$ | $v_{1}$ | $T_{1}$ | $E_{1}=h v_{1}$ |
| $\mathrm{O}_{2}$ | $\lambda_{2}$ | $v_{2}$ | $T_{2}$ | $E_{2}=h v_{2}$ |
| Comparison | $\lambda_{1}>\lambda_{2}$ | $v_{1}<v_{2}$ | $T_{1}>T_{2}$ | $E_{1}<E_{2}$ |

Table 2
Note that the light observed by observers $\mathrm{O}_{1}$ and $\mathrm{O}_{2}$ is the same light and from the same source. The difference in wavelength, frequency and period is due to differences in the position of the observers.

## 5. GRAVITATION AS THE RELATIVE DENSITY OF SPACE-TIME

There are three aspects of gravitation. First, related to an object, gravitation can cause changes in the velocity of an object. Second, related to photons, gravitation can change the frequency of photons. Third, related to the difference in the result of observation. Different observers of the same object observation can yield different results. Gravitation causes differences in the period of an event, differences in the length of an object, and differences in the mass or energy of an object.

From sections 3 and 4 we see that there are differences in the total energy of objects and differences in wavelength, frequency, period, and energy of photons. The differences are because of the difference in the position of observers. I introduce gravitation $d$ as the relative density of space-time. The value of $d$ is the ratio of the total energy of an object observed from different positions. The value of $d$ is relative. The closer the position of the observer to a high-mass object the higher the value of $d$. Figure 5 is the visualization of the relative density of space-time $d$. Darker color means a higher value of relative density of space-time $d$. The closer the position to the high-mass object the darker the color.


Figure 5

## Relative Universe

$d$ is the relative value of space-time density. It can be seen as the relative value of total energy, relative time interval, or relative length of an object.

There is an object with mass observed by observer $\mathrm{O}_{1}$ at position 1 and observer $\mathrm{O}_{2}$ at position 2. Observer $\mathrm{O}_{1}$ concludes that the mass of the object is $m_{1}$ while observer $\mathrm{O}_{2}$ concludes that the mass of the object is $m_{2}$. The relative space-time density from position 1 to position 2 is
$d_{\text {relative from position } 1 \text { to position } 2}=\frac{m_{\text {mass observed by observer } 1}}{m_{\text {mass observed by observer } 2}}$
Or $d_{12}=\frac{m_{1}}{m_{2}}$
and because mass is equal to energy, $E=m c^{2}$ then $E_{1}=m_{1} c^{2}$ and $E_{2}=m_{2} c^{2}$. Therefore the relative space-time density from position 1 to position 2 is
$d_{12}=\frac{E_{1}}{E_{2}}$
There is an event with a time interval observed by observer $\mathrm{O}_{1}$ at position 1 and observer $\mathrm{O}_{2}$ at position 2. Observer $\mathrm{O}_{1}$ concludes that the time interval of the event is $t_{1}$, while Observer $\mathrm{O}_{2}$ concludes that the time interval of the event is $t_{2}$. The relative space-time density from position 1 to position 2 is
$d_{12}=\frac{t_{\text {time interval observed by observer } 2}}{t_{\text {time interval observed by observer } 1}}$
Or $d_{12}=\frac{t_{2}}{t_{1}}$
There is an object with length observed by observer $\mathrm{O}_{1}$ at position 1 and observer $\mathrm{O}_{2}$ at position 2. Observer $\mathrm{O}_{1}$ concludes that the length of the object is $l_{1}$, while Observer $\mathrm{O}_{2}$ concludes that the length of the object is $l_{2}$. The relative space-time density from position 1 to position 2 is
$d_{12}=\frac{l_{\text {lengt }} \text { of object observed by observer } 2}{l_{\text {length of object observed by observer } 1}}$
Or $d_{12}=\frac{l_{2}}{l_{1}}$
Other formulas for relative space - time density are
$d_{12}=\frac{1}{d_{21}}$ and $d_{21}=\frac{1}{d_{12}}$
$d_{31}=d_{32} \cdot d_{21}$
$d_{11}=d_{22}=1$
With boundary
$0<d_{x y}<\infty$

## 6. CALCULATION OF RELATIVE DENSITY OF SPACE-TIME

Two-Step Calculation


Figure 6
P and Q are objects with mass. 1, 2 and 3 are the positions of observers and the relative density of space-time.
Relative density of space-time from position 3 to 2
Calculation from position 2
Let:
$E_{t}=$ Total energy of object Q
$d_{32}=$ Relative Density of Space-time from position 3 to 2
$E_{p}=$ Potential energy of object Q
$m_{2}=$ Relative mass of object Q observed from position 2
$M_{2}=$ Relative mass of object P observed from position 2
$r_{22}=$ Relative distance from object P to position 2 observed from position 2
$r_{32}=$ Relative distance from object P to position 3 observed from position 2
$-\frac{G M m}{r}=$ Gravitational potential energy.
$d_{32}=\frac{E_{t \text { observed by observer from position } 3}}{E_{t \text { observed by observer from position } 2}}$
or
$d_{32}=\frac{E_{t 3}}{E_{t 2}}$
$E_{t 2}=m_{2} c^{2}$
$E_{t 3}=m_{2} c^{2}+E_{p(\text { from position 3 to 2) }}$
$E_{p}=-\left(\frac{G M_{2} m_{2}}{r_{22}}-\frac{G M_{2} m_{2}}{r_{32}}\right)$
$E_{p}=\frac{G M_{2} m_{2}}{r_{32}}-\frac{G M_{2} m_{2}}{r_{22}}$
$E_{p}=G M_{2} m_{2}\left(\frac{1}{r_{32}}-\frac{1}{r_{22}}\right)$
$E_{p}=G M_{2} m_{2}\left(\frac{r_{22}-r_{32}}{r_{22} r_{32}}\right)$
$d_{32}=\frac{E_{t 3}}{E_{t 2}}$
$d_{32}=\frac{E_{t 2}+E_{p}}{E_{t 2}}$
$d_{32}=\frac{m_{2} c^{2}+G M_{2} m_{2}\left(\frac{r_{22}-r_{32}}{r_{22} r_{32}}\right)}{m_{2} c^{2}}$
$d_{32}=1+\frac{G M_{2}\left(r_{22}-r_{32}\right)}{r_{22} r_{32} c^{2}}$

## Calculation from position 1

$d_{21}=$ Relative density of space-time from position 2 to position 1.
$m_{1}=$ Relative mass of object Q observed from position 1.
$M_{1}=$ Relative mass of object P observed from position 1.
$r_{21}=$ Relative distance from object P to position 2 observed from position 1.
$r_{31}=$ Relative distance from object P to position 3 observed from position 1.
$M_{2}=d_{21} M_{1}$
$r_{22}=\frac{r_{21}}{d_{21}}$
$r_{32}=\frac{r_{31}}{d_{21}}$
$d_{32}=1+\frac{G M_{2}\left(r_{22}-r_{32}\right)}{r_{22} r_{32} c^{2}}$
Substituting $M_{2}$ to $M_{1}, r_{22}$ to $r_{21} r_{22}$, and $r_{32}$ to $r_{31}$
$d_{32}=1+\frac{G d_{21}^{3} M_{1}\left(r_{21}-r_{31}\right)}{d_{21} r_{21} r_{31} c^{2}}$
$d_{32}=1+\frac{G d_{21}^{2} M_{1}\left(r_{21}-r_{31}\right)}{r_{21} r_{31} c^{2}}$

Multi-Step Calculation


Figure 7
$M$ is an object with mass. $0,1,2,3,4,5,6,7, \ldots n$ are the positions of observers and the relative density of space-time Let:
$d_{n 0}=$ Relative density of space-time from position n to position 0.
$d_{10}=$ Relative density of space-time from position 1 to position 0.
$d_{21}=$ Relative density of space-time from position 2 to position 1.
$d_{n(n-1)}=$ Relative density of space-time from position n to position $(\mathrm{n}-1)$.
$M_{0}=$ Relative mass of object M observed from position 0.
$M_{1}=$ Relative mass of object M observed from position 1.
$M_{(n-1)}=$ Relative mass of object M observed from position (n-1).
$n \rightarrow \infty$.
$d_{n 0}=d_{10} \cdot d_{21} \cdot d_{32} \cdot d_{43} \cdot d_{54} \cdot d_{65} \ldots d_{n(n-1)}$
For brevity let
$P_{n 0}=\frac{G M_{0}\left(r_{00}-r_{n 0}\right)}{r_{00} r_{n 0} c^{2}}$
$P_{10}=\frac{G M_{0}\left(r_{00}-r_{10}\right)}{r_{00} r_{10} c^{2}}$
$P_{21}=\frac{G M_{1}\left(r_{11}-r_{21}\right)}{r_{11} r_{21} c^{2}}$
$P_{32}=\frac{G M_{2}\left(r_{22}-r_{32}\right)}{r_{22} r_{32} c^{2}}$
$P_{n(n-1)}=\frac{G M_{n-1}\left(r_{(n-1)(n-1)}-r_{n(n-1)}\right)}{r_{(n-1)(n-1)} r_{n(n-1)} c^{2}}$

## Relative Universe

For simplicity let
$P_{10}=P_{21}=P_{32}=\ldots=P_{n(n-1)}$
$P_{10}+P_{21}+P_{32}+\ldots+P_{n(n-1)}=P_{n 0}$
$n=\frac{P_{n 0}}{P_{10}}$ or $P_{10}=\frac{P_{n 0}}{n}$
Relative density d from position 1 to position 0
$d_{10}=1+\frac{G M_{0}\left(r_{00}-r_{10}\right)}{r_{00} r_{10} c^{2}}=1+P_{10}$
And furthermore.
$d_{21}=1+\frac{G M_{1}\left(r_{11}-r_{21}\right)}{r_{11} r_{21} c^{2}}=1+\frac{G d_{10}^{2} M_{0}\left(r_{10}-r_{20}\right)}{r_{10} r_{20} c^{2}}=1+d_{10}^{2} P_{21}=1+d_{10}^{2} P_{10}$
$d_{32}=1+\frac{G M_{2}\left(r_{22}-r_{32}\right)}{r_{22} r_{32} c^{2}}=1+\frac{G d_{20}^{2} M_{0}\left(r_{20}-r_{30}\right)}{r_{20} r_{30} c^{2}}=1+\frac{G d_{21}^{2} d_{10}^{2} M_{0}\left(r_{20}-r_{30}\right)}{r_{20} r_{30} c^{2}}=1+d_{10}^{4} P_{32}=1+d_{10}^{4} P_{10}$
$d_{n(n-1)}=1+\frac{G M_{(n-1)}\left(r_{(n-1)(n-1)}-r_{n(n-1)}\right)}{r_{n(n-1)} r_{(n-1)(n-1)} c^{2}}=1+\frac{G\left(d_{(n-1) 0}^{2}\right) M_{0}\left(r_{(n-1) 0}-r_{n 0}\right)}{r_{(n-1) 0} r_{n 0} c^{2}}$
$=1+\frac{G\left(d_{(n-1)(n-2)}^{2}\right)\left(d_{(n-2)(n-3)}^{2}\right)\left(d_{(n-3)(n-4)}^{2}\right) \ldots d_{10}^{2} M_{0}\left(r_{n 0}-r_{(n-1) 0}\right)}{r_{n 0} r_{(n-1) 0} c^{2}}=1+d_{10}^{2(n-1)} P_{n(n-1)}$ $=1+d_{10}^{2(n-1)} P_{10}$
$d_{n 0}=d_{10} \cdot d_{21} \cdot d_{32} \cdot d_{43} \cdot d_{54} \cdot d_{65} \ldots d_{n(n-1)}$
$d_{n 0}=\left(1+P_{10}\right)\left(1+d_{10}^{2} P_{10}\right)\left(1+d_{10}^{4} P_{10}\right) \ldots\left(1+d_{10}^{2 n} P_{10}\right)$
Consider
$e^{y}=\left(1+Z_{1}\right)\left(1+Z_{2}\right)\left(1+Z_{3}\right)\left(1+Z_{4}\right) \ldots\left(1+Z_{n}\right)$
Where
$Z_{x} \rightarrow 0$ and
$\sum_{x=1}^{x=n} Z_{x}=y$
$d_{n 0}=\left(1+P_{10}\right)\left(1+d_{10}^{2} P_{10}\right)\left(1+d_{10}^{4} P_{10}\right) \ldots\left(1+d_{10}^{2(n-1)} P_{10}\right)$
Let
$A=P_{10}+d_{10}^{2} P_{10}+d_{10}^{4} P_{10}+d_{10}^{6} P_{10}+\ldots+d_{10}^{2(n-1)} P_{10}$
$d_{10}^{2} A=d_{10}^{2} P_{10}+d_{10}^{4} P_{10}+d_{10}^{6} P_{10}+\ldots+d_{10}^{2(n-1)} P_{10}+d_{10}^{2 n} P_{10}$
$d_{10}^{2} A-A=d_{10}^{2 n} P_{10}-P_{10}$
$A\left(d_{10}^{2}-1\right)=d_{10}^{2 n} P_{10}-P_{10}$

## Relative Universe

$A=\frac{d_{10}^{2 n} P_{10}-P_{10}}{d_{10}^{2}-1}$
$A=\frac{d_{10}^{2 n} P_{10}-P_{10}}{\left(1+P_{10}\right)^{2}-1}$
$A=\frac{d_{10}^{2 n} P_{10}-P_{10}}{\left(1+2 P_{10}+P_{10}^{2}\right)-1}$
$A=\frac{d_{10}^{2 n} P_{10}-P_{10}}{\left(2 P_{10}+P_{10}^{2}\right)}$
$P_{10}^{2}$ can be ignored because it is much smaller than $2 P_{10}$.
$A=\frac{d_{10}^{2 n} P_{10}-P_{10}}{2 P_{10}}$
$A=\frac{d_{10}^{2 n}-1}{2}$
Substituting
$d_{10}=1+P_{10}$
$A=\frac{\left(1+P_{10}\right)^{2 n}-1}{2}$
Substituting
$P_{10}=\frac{P_{n 0}}{n}$
$A=\frac{\left(1+\frac{P_{n 0}}{n}\right)^{2 n}-1}{2}=\frac{e^{\left(2 P_{n 0}\right)}-1}{2}$
$A=P_{10}+d_{10}^{2} P_{10}+d_{10}^{4} P_{10}+d_{10}^{6} P_{10}+\ldots+d_{10}^{2(n-1)} P_{10}$
$d_{n 0}=\left(1+P_{10}\right)\left(1+d_{10}^{2} P_{10}\right)\left(1+d_{10}^{4} P_{10}\right) \ldots\left(1+d_{10}^{2(n-1)} P_{10}\right)$
$d_{n 0}=e^{A}$
Substituting
$A=\frac{e^{\left(2 P_{n 0}\right)}-1}{2}$
$d_{n 0}=e^{\left(\frac{e^{\left(2 P_{n 0}\right)}-1}{2}\right)}$
Where
$P_{n 0}=\frac{G M_{0}\left(r_{00}-r_{n 0}\right)}{r_{00} r_{n 0} c^{2}}$
For $r_{00} \rightarrow \infty$ the equation for $P_{n 0}$ can be simplified to
$P_{n 0}=\frac{G M_{0}}{r_{n 0} c^{2}}$

## Relative Universe

## 7. RELATIVE DENSITY OF SPACE-TIME FROM MERCURY PLANET TO EARTH.

Let
$G=$ Gravitational constant $=6.67384 \times 10^{-1} \mathrm{~m}^{3} \mathrm{~kg}^{-1} \mathrm{~s}^{-2}$
$M_{e}=$ Mass of the sun observed from Earth $=1.98847 \times 10^{30} \mathrm{~kg}$
$r_{m e}=$ Distance from the sun to Mercury observed from Earth $=5.74 \times 10^{10} \mathrm{~m}$ or $0.574 \times 10^{11} \mathrm{~m}$
$r_{e e}=$ Distance from the sun to Earth observed from Earth $=1.496 \times 10^{11} \mathrm{~m}$ or $14.496 \times 10^{10} \mathrm{~m}$
$c=$ Speed of light $=3 \times 10^{8} \mathrm{~ms}^{-1}$
The relative density d of space-time from Mercury planet to Earth is
$d_{\text {mercury eart }}=d_{m e}=e^{\left(\frac{e^{(2 P m e)}-1}{2}\right)}$
$P_{m e}=\frac{G M_{e}\left(r_{e e}-r_{m e}\right)}{r_{e e} r_{m e} c^{2}}$
$P_{m e}=\frac{6.67384 \times 10^{-1} 1.98847 \times 10^{30}\left(1.496 \times 10^{11}-0.574 \times 10^{11}\right)}{1.496 \times 10^{11} \times 5.74 \times 10^{10} \times 9 \times 10^{16}}$
$P_{m e}=\frac{12.2356136 \times 10^{30}}{77.28336 \times 10^{37}}$
$P_{m e}=1.58321 \times 10^{-8}$
$d_{m e}=e^{\left(\frac{e^{\left(2 \times 1.58321 \times 10^{-8}\right)}-1}{2}\right)}$
Consider
$e^{n}=1+n$
if $|n| \ll 1$
$d_{m e}=e^{\left(\frac{1+\left(2 \times 1.58321 \times 10^{-8}\right)-1}{2}\right)}$
$d_{m e}=e^{\left(\frac{2 \times 1.58321 \times 10^{-8}}{2}\right)}$
$d_{m e}=e^{1.58321 \times 10^{-8}}$
$d_{m e}=1+1.58321 \times 10^{-8}$
If light with a frequency of $5 \times 10^{14} \mathrm{~Hz}$ is emitted from Earth's orbit, then when it reaches Mercury's orbit, its frequency is $(1+$ $\left.1.58321 \times 10^{-8}\right) \times 5 \times 10^{14} \mathrm{~Hz}=\left(5 \times 10^{14}+7,91605 \times 10^{6}\right) \mathrm{Hz}$ indicating gravitational blueshift. If light with a frequency of $5 \times$ $10^{14} \mathrm{~Hz}$ is emitted from Mercury's orbit, then when it reaches Earth's orbit, its frequency is $5 \times 10^{14} /\left(1+1.58321 \times 10^{-8}\right) \mathrm{Hz}=$ $\left(5 \times 10^{14}-7,91605 \times 10^{6}\right) \mathrm{Hz}$ indicating gravitational redshift.

If a ball with a mass of 2 kgs is dropped from Earth's orbit toward the sun when it reaches Mercury's orbit, its total mass is $(1+$ $\left.1.58321 \times 10^{-8}\right) \times 2 \mathrm{kgs}=\left(2+3,16642 \times 10^{-8}\right) \mathrm{kgs}$. The velocity of the ball when it reaches Mercury's orbit is
$m_{e}=$ Mass of the ball at Earth's orbit $==\left(2+3,16642 \times 10^{-8}\right) \mathrm{kgs}$
$m_{m}=$ Mass of the ball at Mercury's orbit $=2 \mathrm{kgs}$
$V=$ Velocity of the ball at mercury orbit
$c=$ Velocity of light $=3 \times 10^{8} \mathrm{~m} / \mathrm{s}$

## Relative Universe

$m_{m}=\frac{m_{e}}{\sqrt{1-\frac{V^{2}}{c^{2}}}}$
$m_{m}^{2}=\frac{m_{e}^{2}}{1-\frac{V^{2}}{c^{2}}}$
$1-\frac{V^{2}}{c^{2}}=\frac{m_{e}^{2}}{m_{m}^{2}}$
$-\frac{V^{2}}{c^{2}}=\frac{m_{e}^{2}}{m_{m}^{2}}-1$
$\frac{V^{2}}{c^{2}}=1-\frac{m_{e}^{2}}{m_{m}^{2}}$
$V^{2}=\left(1-\frac{m_{e}^{2}}{m_{m}^{2}}\right) c^{2}$
$V^{2}=\left(1-\frac{2^{2}}{\left(2+3,16642 \times 10^{-8}\right)^{2}}\right) c^{2}$
$V^{2}=\left(1-\frac{4}{\left(4+12.66568 \times 10^{-8}+10.02622 \times 10^{-16}\right)}\right) c^{2}$
$10.02622 \times 10^{-16}$ is very small compared to $12.66568 \times 10^{-8}$ and can be ignored.
$V^{2}=\left(1-\frac{4}{\left(4+12.66568 \times 10^{-8}\right)}\right) c^{2}$
$12.66568 \times 10^{-8}$ is very small compared to 4 so equation can be modified.
$V^{2}=\left(1-\frac{4-12.66568 \times 10^{-8}}{4}\right) c^{2}$
$V^{2}=\left(\frac{12.66568 \times 10^{-8}}{4}\right) c^{2}$
$V^{2}=3,16642 \times 10^{-8} c^{2}$
$V=\sqrt{3,16642 \times 10^{-8}} \times 3 \times 10^{8}$
$V=1.7794 \times 10^{-4} \times 3 \times 10^{8}$
$V=5.33883 \times 10^{4} \mathrm{~m} / \mathrm{s}$
Because the value of $P_{m e}$ is very small, the calculation using the classic method will result in the same result.
$E_{k}=E_{p}$
$\frac{1}{2} \mathrm{~m} v^{2}=-\left(\frac{G M m}{r_{e}}-\frac{G M m}{r_{m}}\right)$
$\frac{1}{2} \mathrm{~m} v^{2}=\frac{G M m}{r_{m}}-\frac{G M m}{r_{e}}$
$\frac{1}{2} \mathrm{~m} v^{2}=G M m\left(\frac{1}{r_{m}}-\frac{1}{r_{e}}\right)$
${ }_{2}^{1} \mathrm{~m} v^{2}=G M m\left(\frac{r_{e}-r_{m}}{r_{e} r_{m}}\right)$

$$
\begin{aligned}
& \frac{1}{2} v^{2}=G M\left(\frac{r_{e}-r_{m}}{r_{e} r_{m}}\right) \\
& v^{2}=2 G M\left(\frac{r_{e}-r_{m}}{r_{e} r_{m}}\right) \\
& v^{2}=\frac{2 \times 6.67384 \times 10^{-11} 1.98847 \times 10^{30}\left(1.496 \times 10^{11}-0.574 \times 10^{11}\right)}{1.496 \times 10^{11} \times 5.74 \times 10^{10}} \\
& v^{2}=\frac{24.47122 \times 10^{30}}{8.587041 \times 10^{21}} \\
& v^{2}=2.8497845 \times 10^{9} \\
& V=5.33883 \times 10^{4} \mathrm{~m} / \mathrm{s}
\end{aligned}
$$

In addition, there are differences in the results between observers on Earth and observers on Mercury.

| Object of the observations | Result from Earth | Calculation from Mercury | Calculation result from Mercury |
| :---: | :---: | :---: | :---: |
| Mass of the sun | $1.98847 \times 10^{30} \mathrm{~kg}$ | $\begin{aligned} & \left(1+1.58321 \times 10^{-8}\right) \times \\ & 1.98847 \times 10^{30} \mathrm{~kg} \end{aligned}$ | $\begin{aligned} & 1.98847 \times 10^{30} \mathrm{~kg}+ \\ & 3.14817 \times 10^{22} \mathrm{~kg} \end{aligned}$ |
| Distance from Mercury to the sun | $5.79 \times 10^{10} \mathrm{~m}$ | $\frac{5.79 \times 10^{10}}{1+1.58321 \times 10^{-8}} \mathrm{~m}$ | $5.79 \times 10^{10} . \mathrm{m}-366 \mathrm{~m}$ |
| Diameter of the sun | $1.3927 \times 10^{9} . \mathrm{m}$ | $\frac{1.3927 \times 10^{9}}{1+1.58321 \times 10^{-8}}$ | $1.3927 \times 10^{9} . \mathrm{m}-22.05 \mathrm{~m}$ |
| Average rotating the sun on axis | 27 days $=2.3328 \times 10^{6} \mathrm{~S}$ | $\frac{2.3328 \times 10^{6}}{1+1.58321 \times 10^{-8}} \mathrm{~s}$ | 27 days -0.036 s |
| Mass of the universe | $1.73 \times 10^{53} \mathrm{~kg}$ | $\begin{aligned} & \left(1+1.58321 \times 10^{-8}\right) \mathrm{x} \\ & 1.73 \times 10^{53} \mathrm{~kg} \end{aligned}$ | $\begin{aligned} & 1.73 \times 10^{53} \mathrm{~kg}+ \\ & 2.739 \times 10^{45} \mathrm{~kg} \end{aligned}$ |
| Diameter of the universe | $93.016 \times 10^{9}$ light years | $\frac{93.016 \times 10^{9}}{1+1.58321 \times 10^{-8}}$ light years | $93.016 \times 10^{9}$ light years 1472.64 light years |

Table 3

## 8. LARGER DENSITY OBJECT



Figure 8
The object Q has a mass 2 times that of the Sun and a diameter of 3 km . Observer O 1 at position 0 is at a relative distance from object Q.
$M_{0}=3.976941 \times 10^{30} \mathrm{~kg}$

## Relative Universe

$r_{n 0}=3000 \mathrm{~m}$
$G=$ Gravitational constant $=6.67384 \times 10^{-1} \mathrm{~m}^{3} \mathrm{~kg}^{-1} \mathrm{~s}^{-2}$
$c=$ Speed of light $=3 \times 10^{8} \mathrm{~ms}^{-1}$
$P_{n 0}=\frac{G M_{0}}{r_{n 0} c^{2}}$
$P_{n 0}=\frac{6.67384 \times 10^{-1} \times 3.976941 \times 10^{30}}{3 \times 10^{3} \times 9 \times 10^{16}}$
$P_{n 0}=0.983017$
$d_{n 0}=e^{\left(\frac{e^{\left(2 P_{n 0}\right)}-1}{2}\right)}$
$d_{n 0}=e^{\left(\frac{e^{(2 \times 0.983017)}-1}{2}\right)}$
$d_{n 0}=e^{\left(\frac{e^{(1.966035)}-1}{2}\right)}$
$d_{n 0}=e^{\left(\frac{7.142301-1}{2}\right)}$
$d_{n 0}=e^{3.07115}$
$d_{n 0}=21.5669$
Rounded
$d_{n 0}=22$
If light with a frequency of $5 \times 10^{14} \mathrm{~Hz}$ is emitted from position 0 toward object Q , then when it reaches position n its frequency is $22 \times 5 \times 10^{14} \mathrm{~Hz}=1.10 \times 10^{16} \mathrm{~Hz}$. If light with a frequency of $5 \times 10^{14} \mathrm{~Hz}$ is emitted from position n , then when it reaches position 0 , its frequency is $5 \times 10^{14} / 22 \mathrm{~Hz}=22.73 \times 10^{12} \mathrm{~Hz}$.

For the result of object observations from position 0 and position n see the table below.

| Object of the observations | Result from position 0 | Result from position 0 |
| :--- | :--- | :--- |
| Mass of the object Q | $3.976941 \times 10^{30} \mathrm{~kg}$ | $22 \times 3.976941 \times 10^{30} \mathrm{~kg}=8.74927 \times 10^{31}$ |
| Diameter of the sun | $1.3927 \times 10^{9} . \mathrm{m}$ | $1.3927 \times 10^{9} / 22 \mathrm{~m}=6.3305 \times 10^{7} . \mathrm{m}$ |
| Average rotating the sun on axis | 27 days $=2.3328 \times 10^{6} \mathrm{~s}$ | $2.3328 \times 10^{6} / 22 \mathrm{~s}=1.0604 \times 10^{5} . \mathrm{s}$ |
| Mass of the universe | $1.73 \times 10^{53} \mathrm{~kg}$ | $22 \times 1.73 \times 10^{53} \mathrm{~kg}=3.806 \times 10^{54} \mathrm{~kg}$ |
| Diameter of the universe | $93.016 \times 10^{9}$ light years | $93.016 \times 10^{9} / 22=4.228 \times 10^{9}$ light years |

Table 4

## 9. RELATIVE UNIVERSE

From Tables 3 and 4, we can conclude that the observation of mass, length, and rotation period of an object differs depending on the position of the observer on Earth, Mercury, and other places. There are many places in the universe, and the values of the relative density of space-time differ from one place to another. Therefore, the mass, length, and period of an object differ between them. The result is that there are no absolute values of mass, length, and period of objects in the universe, only relative values. The mass and diameter of the universe are relative values observed from Earth. There are many places outside Earth with a relative value of $d$ lower than 1 , such as a location far from the star at the edge of our galaxy, or a value of $d$ much larger than 1 , as at a location at the neutron star.

## Relative Universe

## 10. LOCALIZATION PRINCIPLE

Observer $\mathrm{O}_{1}$ and observer $\mathrm{O}_{2}$ are at different positions, with $\mathrm{O}_{1}$ at position $\mathrm{P}_{1}$ and $\mathrm{O}_{2}$ at position $\mathrm{P}_{2}$. Let the relative density from $\mathrm{P}_{1}$ to $\mathrm{P}_{2}$ be $d_{12}=1.6$ or $d_{21}=\frac{1}{d_{12}}=\frac{1}{1.6}=0.625$.

They observe the object's carbon-12 atomic mass, quartz crystal vibration, and hydrogen atom Bohr radius at each position:

Observer $\mathrm{O}_{1}$ 's results:
Carbon-12 atomic mass $=12 \mathrm{amu}$ (atomic mass unit)
Quartz crystals vibrate at 32768 times per second
Hydrogen Bohr radius $=1.00054 \AA$ (Ångström)

Observer $\mathrm{O}_{2}$ 's results:
Carbon-12 atomic mass $=12 \mathrm{amu}$
Quartz crystals vibrate at 32,768 times per second
Hydrogen Bohr radius $=1.00054 \AA$
Localization principle: Every observer has the same result when they observe an object of the same kind at the same position.

But if observer $\mathrm{O}_{1}$ at position $\mathrm{P}_{1}$ observes objects at position $\mathrm{P}_{2}$ with $d_{12}=1.6$ the results are:
Carbon-12 atomic mass $=d_{21} \times 12 \mathrm{amu}=1.6 \times 12 \mathrm{amu}=19.2 \mathrm{amu}$
Quartz crystals vibrate at $d_{12} \times 32,768$ times per second $=1.6 \times 32768=52,428$ times per second
Hydrogen Bohr radius $=\frac{1}{d_{12}} \times 1.00054 \AA=\frac{1}{1.6} \times 1.00054 \AA=0.62534 \AA$

And if observer $\mathrm{O}_{2}$ at position $\mathrm{P}_{2}$ observes objects at position $\mathrm{P}_{1}$ with $d_{21}=0.625$ the results are:
Carbon-12 atomic mass $=d_{21} \times 12 \mathrm{amu}=0.625 \times 12 \mathrm{amu}=7.5 \mathrm{amu}$
Quartz crystals vibrate at $d_{21} \times 32,768$ times per second $=0.625 \times 32768=20,480$ times per second
Hydrogen Bohr radius $=\frac{1}{d_{21}} \times 1.00054 \AA=\frac{1}{0.625} \times 1.00054 \AA=1.600864 \AA$

## Relative Universe

## 11. PSEUDO MOVEMENT



Figure 9
Observer $\mathrm{O}_{1}$ stays still at position $\mathrm{P}_{1}$, observer $\mathrm{O}_{2}$ stays still at position $\mathrm{P}_{2}$ and observer $\mathrm{O}_{3}$ moves from position $\mathrm{P}_{2}$ to position $\mathrm{P}_{1}$. Object A and object B do not move.
$S_{I}=$ Distance from position A to position B as observed by Observer $\mathrm{O}_{1}$
$S_{2}=$ Distance from position A to position B as observed by Observer $\mathrm{O}_{2}$
$\Delta S=$ Pseudo distance difference.
$\Delta \mathrm{T}=$ Time required by observer $\mathrm{O}_{3}$ to travel from position $\mathrm{P}_{2}$ to position $\mathrm{P}_{1}$.
$V_{p}=$ Pseudo movement
$S_{2}=\frac{1}{d_{21}} S_{1}$
$d_{21}>1$ Because gravity is toward position $\mathrm{O}_{2}$, then
$S_{1}>S_{2}$
$\Delta S=S_{1}-S_{2}$.
$V_{p}=\frac{\Delta S}{\Delta T}$
When Observer $\mathrm{O}_{3}$ was at position $\mathrm{P}_{2}$ he saw the distance from A to B as $\mathrm{S}_{2}$. When Observer $\mathrm{O}_{3}$ arrived at Position $\mathrm{P}_{1}$ he saw the distance from A to B as $\mathrm{S}_{1}$. Then Observer $\mathrm{O}_{3}$ observed the pseudo distance difference between A and B as $\Delta \mathrm{S}$, and the pseudo movement as $V_{p}=\frac{\Delta S}{\Delta T}$.


Figure 10
Observer $\mathrm{O}_{1}$ stays still at position $\mathrm{P}_{1}$, while observer $\mathrm{O}_{2}$ stays still at position $\mathrm{P}_{2}$. Object A and object B do not move. There are two objects C and D moving away from O 2 .

From the viewpoint of Observer $\mathrm{O}_{1}$.
$S_{1 \text { begi }}=$ Distance of object A and object B when objects C and D begin to move away from observer $\mathrm{O}_{2}$.
$S_{1 \text { end }}=$ Distance of object A and object B after objects C and D end moving away from observer $\mathrm{O}_{2}$.
Because there is no change in gravitation at Observer $\mathrm{O}_{1}$, there is no change in relative density.
$d_{e n d \text { begin }}=d_{e b}=1$
$S_{1 e n d}=\frac{1}{d_{e b}} S_{1 \text { beg }}$
$S_{1 \text { end }}=S_{1 \text { begin }}$

From the viewpoint of observer $\mathrm{O}_{2}$.
$S_{2 \text { begin }}=$ Distance of object A and object B when objects C and D begin to move away from observer $\mathrm{O}_{2}$.
$S_{2 e n d}=$ Distance of object A and object B after objects C and D end moving away from observer $\mathrm{O}_{2}$.
$\Delta S_{2}=$ Pseudo distance difference.
$\Delta \mathrm{T}=$ Time interval of objects C and D moving away from observer $\mathrm{O}_{2}$
$V_{p}=$ Pseudo movement
Because of the change in the distance of objects C and D to $\mathrm{P}_{2}$ the relative density at position $\mathrm{P}_{2}$ changes.
$d_{\text {end begin }}=d_{e b}<1$ Because objects C and D moving away from O 2 .
$S_{2 e n d}=\frac{1}{d_{a b}} S_{2 b e g}$
$S_{2 e n d}>S_{2 \text { beg }}$

## Relative Universe

$\Delta S_{2}=S_{2 e n}-S_{2 \text { begi }}$
$V_{p}=\frac{\Delta S_{2}}{\Delta T}$
Observer $\mathrm{O}_{2}$ saw that there is a pseudo distance difference with value $\Delta S_{2}$, and the value of pseudo movement as $V_{p}=\frac{\Delta S_{2}}{\Delta T}$ is different from the result from Observer $\mathrm{O}_{1}$ that there is no change in the distance between object A and object B

## 12. EXPANDING UNIVERSE

Since the Big Bang, our universe continues to expand. Every galaxy moves away from each other. According to section 10 the relative density caused by objects moving away from the observer is $d_{\text {end begin }}=d_{e b}<1$. Let an observer on Earth observe the distance of galaxy A to galaxy B
$S_{\text {begin }}=$ Distance of galaxy A and galaxy B at the beginning of observation
$S_{\text {end }}=$ Distance of galaxy A and galaxy B at the end of observation
$v_{p}=$ Pseudo velocity of the expanding universe.
$\Delta \mathrm{T}=$ Time interval of observation.
$v_{t}=$ Total velocity of the expanding universe seen by an observer.
$v_{r}=$ Real velocity of the expanding universe.
$d_{e b}<1$ so there is pseudo movement.
$S_{e n d}=\frac{1}{d_{e b}} S_{b e g i n}$
$S_{\text {end }}>S_{\text {begin }}$
$\Delta S=S_{\text {end }}-S_{\text {begin }}$
$V_{p}=\frac{\Delta S}{\Delta T}$
$v_{t}=v_{r}+v_{p}$
Pseudo-movement is part of the total velocity of the expanding universe seen by an observer. Pseudo-movement makes the total velocity of expansion faster than it should be.

## 13. DECREASING THE UNIVERSE'S MASS

There is another consequence of the expanding universe: the mass of the universe is decreasing
Let
$M_{b}=$ The mass of the universe at the beginning of observation.
$M_{e}=$ The mass of the universe at the end of observation.
$d_{e n d \text { begin }}=d_{e b}<1$ because the universe is expanding.
Then
$M_{e}=d_{e b} M_{b}$,

## Relative Universe

and $M_{e}<M_{b}$
Therefore the mass of the universe is decreasing because of the expansion of the universe.

## 14. CONCLUSIONS

1. Gravitation is the relative density of space-time.
2. Gravitation can affect the observation results of the same object.

3 There is pseudo movement between two objects due to changes in the value of the relative density of the observer.

## REFERENCES

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