

A STATIC, STABLE UNIVERSE: CURVATURE-COSMOLOGY

DAVID F. CRAWFORD

School of Physics (Retired), University of Sydney, NSW, 2006, Australia

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ABSTRACT

Curvature-cosmology is a tired-light cosmology that predicts a well-defined static and stable universe. Since it is a complete challenge to the big bang paradigm, it can only be judged by its agreement with direct cosmological observations. It predicts a universe of a hydrogen plasma with a temperature of 2.456×10^9 K [observed: 2.62×10^9 K] and a cosmic background radiation temperature of 2.736 K [observed: 2.725 K]. It has only one parameter which is the density of the cosmic plasma. In addition this paper provides a new simpler raw data analysis for Type Ia supernova which provides excellent predictions for the redshift variation of Type I supernova light curve width and magnitude. A new discovery is intrinsic magnitude distribution. The analysis of 746,922 quasars provides important cosmological information on the distribution on intrinsic magnitudes and the density distribution of quasars. Other major observations that are shown to be consistent with Curvature-cosmology are: Tolman surface density, galaxy clusters, angular size, galaxy distributions, X-ray background radiation, and quasar variability. It does not need inflation, dark matter or dark energy.

Subject headings: Cosmology—supernova—quasars

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		1. INTRODUCTION	
		<p>This paper describes Curvature-cosmology that is based on two hypothesis, Curvature-redshift and Curvature-pressure, and shows excellent agreement with observations. This new paradigm challenges the big bang paradigm to see which provides the best agreement with cosmological observations. Following the precepts of Thomas S. Kuhn (Kuhn 1970) it is essential that each paradigm must be judged using its own analysis. That is observations of non-static behavior observed within the old paradigm cannot be used to invalidate the new paradigm. They must be evaluated within the new paradigm to have any validity.</p> <p>Nearby Type Ia supernova are well known to have essentially identical light curves that make excellent cosmological probes. The observational evidence for their time dilation has a long history with notable papers being</p>	

by Goldhaber et al. (2001, 1996); Blondin et al. (2008). More recent contributions are by Kowalski et al. (2008); Wood-Vasey et al. (2008); Kessler et al. (2009a); Amanullah et al. (2010); Conley et al. (2011); Betoule et al. (2014); Scolnic et al. (2018). All of these recent papers use the SALT2 Guy et al. (2010, 2007) method to determine the widths and peak flux densities of the supernova and they have used the Λ CDM expansion cosmology to determine absolute magnitudes. These papers show that type Ia supernova observations provide the major contribution to cosmological models.

The common attribute of all Λ CDM, cosmologies is that they are based on the assumption that the universe is expanding (Peebles 1993). An early alternative was the steady-state theory of Hoyle, Bondi and Gold Hoyle (1962) (described with later extensions by Hoyle et al. (2000)) that required continuous creation of matter. However steady-state theories have serious difficulties in explaining the cosmic microwave background radiation. This left Λ CDM as the dominant cosmology but still subject to criticism.

Lal (2010) and Joseph (2010); Ellis (1984); Lerner (1991); Disney (2000); van Flandern (1991) and Peebles (2020, 2022) have continued major earlier criticisms of Λ CDM cosmologies. Whereas most of these criticisms have been of a theoretical nature, this paper concentrates on whether observational data supports a static cosmological model, Curvature-cosmology.

Table 14 provides a list of the important cosmological characteristics predicted by Curvature-cosmology and shows their excellent agreement with the observations.

The analysis of 746,922 quasars provides important cosmological information on the distribution on intrinsic magnitudes and the density distribution of quasars. The intrinsic magnitude distribution appears to be due to the elimination of photons that have energies larger than the ionisation energy of hydrogen.

A crucial property of Curvature-cosmology is that the observed magnitude is the sum of an intrinsic magnitude, which is what would be observed by a nearby observer and a cosmological magnitude which describes the change in the average energy of the photons due to their trajectory through the universe.

This paper has four major parts where the first part is this introduction and the second part presents a new static cosmology, Curvature-cosmology. It is an addition to general relativity and fully accepts it as the best gravitational theory.

The third part provides a new analysis of Type Ia supernova that is a much simpler method than does the current standard SALT2 method. It analyzes raw Type Ia supernova data in order to measure their light curve widths and their peak flux densities. These results are compared with the standard SALT2 method and it shows that the SALT2 method is possibly flawed and that Curvature-cosmology has a better agreement with observations.

The fourth part provides a discussion of most of the important cosmological observations and discusses their results in the context of Curvature-cosmology. The fifth part provides a summary of the results.

This paper is the culmination of many years of work and is a complete re-synthesis of many approaches that I have already published (Crawford 1987a,b, 1991, 1995,

1998, 1999a,b, 2006, 2009a,b). These papers are cited to show the convoluted and historic path of Curvature-cosmology. Because hypotheses and notations have changed and evolved, direct references to these earlier versions of the theory would be misleading and all relevant results are published in this paper.

For convenience it is assumed that the wavelength dependence of a band can be replaced by a single value, λ , which is the mean wavelength for that band. The index (above) is provided to assist the rapid access to all labels with a mouse click and to return with "backspace".

2. PART A: CURVATURE-COSMOLOGY THEORY.

2.1. Introduction

Curvature-cosmology is a static tired-light cosmology which is based on the two hypothesized of Curvature-redshift which is based on the propagation of a wave in of curved space-time and Curvature-pressure which opposes the mutual gravitational attraction in hot gases.

It uses the Friedmann equations with an additional term that stabilizes the solution. This term called Curvature-pressure is a reaction of high-speed particles back on the material producing the curved space-time. This sense of this reaction is to reduce the curvature.

The basic cosmological model is one in which the cosmic plasma dominates the mass distribution and hence the curvature of space-time. In this first-order model, the gravitational effects of stars and galaxies are neglected. The geometry is that of a three-dimensional "surface" of a four-dimensional hyper-sphere, which is common to most cosmologies.

For a static universe, there is no ambiguity in the definition of distances and times. One can use a universal cosmic time and define distances in light travel times or any other convenient measure. In a statistical sense Curvature-cosmology obeys the perfect cosmological principle of being the same at all places and at all times.

Curvature-cosmology makes quite specific predictions that can be refuted. Thus, any observations that unambiguously show changes in the universe with time would invalidate it. In Curvature-cosmology, there is a continuous process in which some of the cosmic gas will aggregate to form galaxies and then stars. The galaxies and stars will evolve and eventually all their material will be returned to the cosmic plasma. Thus, a characteristic of Curvature-cosmology is that although individual galaxies will be born, live and die, the overall population will be statistically the same for all characteristics.

2.2. Derivation of Curvature-redshift

The derivation of Curvature-redshift is based on the fundamental hypothesis of Einstein's general theory of relativity that space is curved. As a consequence, the trajectories of initially parallel, point particles, geodesics, will move closer to each other, or further apart as time increases. Consequently in space with a positive curvature, the cross-sectional area of a bundle of geodesics will slowly decrease.

In applying this idea to photons, we assume that a photon is described in quantum mechanics as a localized wave where the geodesics correspond to the rays of the

wave. Note that this wave is quite separate from an electromagnetic wave that corresponds to the effects of many photons. It is fundamental to the hypothesis that we can consider the motion in space of individual photons.

Because the curvature of space causes the focusing of a bundle of geodesics, this focusing also applies to a wave. As the photon progresses, the cross-sectional area of the wave associated with it will decrease. However, in quantum mechanics' properties such as angular momentum are computed by an integration of a radial coordinate over the volume of the wave and will be affected by the focusing.

However, angular momentum is a quantized parameter that for photons has a fixed value. The solution to this dilemma is that, from symmetry, the photon splits into two very low-energy photons and a third that has the same direction as the original photon and nearly all the energy.

Since in quantum mechanics protons and other particles are considered as waves, a similar process will also apply to them. It is argued that protons and other particles will interact with curved space to lose energy by the emission of very low-energy photons.

The *equation for geodesic deviation* can be written [Misner, Thorne, & Wheeler \(1973\)](#) as

$$\frac{d^2\xi}{dr^2} = -\frac{\xi}{R^2},$$

where ξ is a distance normal to the trajectory and r is measured along the trajectory. The quantity $1/R^2$ is the Gaussian curvature at the point of consideration.

Assume that a photon can be described by a localized wave packet that has finite extent both along and normal to its trajectory. This economic description is sufficient for the following derivation. From quantum mechanics the frequency of a photon with energy E is $\nu = E/h$ and its wavelength as $\lambda = hc/E$. The derivation requires that the wavelength is short compared to the size of the wave packet and that this is short compared to variations in the curvature of space.

Furthermore, we assume that the rays follow null geodesics and therefore any deviations from flat space-time produce change in shape of the wave packet. In other words, since the scale length of deviations from flat space are large compared to the size of the wave packet they act as a very small perturbation to the propagation of the wave packet.

Consider a wave packet moving through a space of constant positive curvature. Because of geodesic deviation, the rays come closer together as the wave packet moves forward. They are focused. In particular the direction θ , of a ray (geodesic) with initial separation ξ after a distance r is (assuming small angles)

$$\theta = -\frac{r\xi}{R^2},$$

where R is the radius of curvature.

Since the central geodesic is the direction of energy flow, we can integrate the wave-energy-function times the component of θ normal to the trajectory, over the dimensions of the wave packet in order to calculate the amount of energy that is now traveling normal to the trajectory. The result is a finite energy that depends on

the average lateral extension of the wave packet, the local radius of curvature, and the original photon energy.

The actual value is not important but rather the fact that there is a finite fraction of the energy that is moving away from the trajectory of the original wave packet. This suggests a photon interaction in which the photon interacts with curved space-time with the hypothesis that the energy flow normal to the trajectory goes into the emission of secondary photons normal to its trajectory.

From a quantum-mechanical point of view, there is a strong argument that some interaction must take place. If the spin of the photon is directly related to the angular momentum of the wave packet about its trajectory then the computation of the angular momentum is a similar integral.

Then because of *focussing* the angular momentum clearly changes along the trajectory, which disagrees with the quantum requirement that the angular momentum, that is the spin, of the photon is constant. The Heisenberg uncertainty principle requires that an incorrect value of spin can only be tolerated for a small time before something happens to restore the correct value. We now investigate the consequences.

Consider motion on the surface of a three-dimensional sphere with radius r . As described above, two adjacent geodesics will move closer together due to focusing. Simple kinematics tells us that a body with velocity v associated with these geodesics has acceleration v^2/r , where r is the radius of curvature. This acceleration is directly experienced by the body.

The geometry of a three-dimensional "surface" with curvature in the fourth dimension is essentially the same as motion in three dimensions except that the focusing now applies to the cross-sectional area and not to the separation.

Since a wave packet that is subject to focusing has acceleration in an orthogonal dimension will also experience an acceleration of c^2/r normal to the surface of the sphere. Then a wave packet (and hence a photon) that has its cross-sectional area focused by curvature in the fourth dimension with radius R would have an energy loss rate proportional to this acceleration. The essence of the Curvature-redshift hypothesis is that the focusing causes the photon to interact and that the energy loss rate is proportional to c^2/R .

In general relativity the crucial equation for the focusing of a bundle of geodesics was derived by [Raychaudhuri \(1955\)](#), also see [Misner et al. \(1973\)](#) and [Ellis \(1984\)](#) and for the current context we can assume that the bundle has zero shear and zero vorticity. Since any change in geodesic deviation along the trajectory will not alter the direction of the geodesics, we need consider only the cross-sectional area A of the geodesic bundle to get the equation

$$\frac{1}{A} \frac{d^2 A}{dr^2} = -\mathbf{R}_{\alpha\beta} \mathbf{U}^\alpha \mathbf{U}^\beta = -\frac{1}{R^2}, \quad (1)$$

where \mathbf{R} is the Ricci tensor, \mathbf{U} is the 4-velocity of the reference geodesic and R is the local radius of curvature. This focusing can be interpreted as the second order rate of change of cross-sectional area of a geodesic bundle that is on the three-dimensional surface in four-dimensional

space. Then if we consider that a photon is a wave packet we find that the rate at which the photon loses energy is

$$\frac{1}{E} \frac{dE}{dr} = -\frac{1}{R}. \quad (2)$$

What is interesting about this equation is that, for the Schwarzschild (and Kerr) solutions for the external field for a mass, the Ricci tensor is zero; hence, there is no focusing and no energy loss. A geodesic bundle passing a mass such as the sun experiences a distortion but the wave packet has not changed in area. Hence, this model predicts that photons passing near the limb of the sun will not suffer any energy loss due to curvature-redshift.

The question is what happens to the photon when the change in momentum exceeds the Heisenberg uncertainty principle. A reasonable answer is that it decays into two very low energy photons and one large energy photon that keeps the remaining energy. By symmetry the two low energy photons have the same energy and are emitted at right angles to the trajectory in opposite directions. Thus the high energy photon retains the same trajectory.

For the primary photon the Heisenberg uncertainty principle is $\sigma_E \sigma_r \geq \hbar/2$ where σ_E is the uncertainty in energy and σ_r is the uncertainty in distance. Since Eq.2 shows a rigid relationship between distance and energy loss we get $\sigma_E = E\sigma_r/R$ hence

$$\sigma_r^2 = \frac{\hbar R}{2E} = \frac{R\lambda}{4\pi}, \quad (3)$$

where λ is the primary wavelength.

2.3. Derivation of Curvature-pressure.

The hypothesis of Curvature-pressure is that for moving particles there is a pressure generated that acts back on the matter that causes the curved space-time. In this case, Curvature-pressure acts on the matter (plasma) that is producing curved space-time in such a way as to try to decrease the curvature.

Consider a Newtonian model where all of the particles are constrained to lie on the surface of a sphere. From Gauss's law the gravitational acceleration at the radius r is normal to the surface, directed inward. From simple celestial mechanics, the particle velocity is $v^2 = GM/r$.

However, the basis of the Curvature-pressure model is that all particles are constrained to have the same radius regardless of their mass or velocity with the value of the radius set by the average radial acceleration. Thus for a high temperature plasma with a distribution of velocities we average over the squared velocities to get

$$\langle v^2 \rangle = \frac{GM}{r}. \quad (4)$$

The effect of this balancing of the accelerations against the gravitational potential is seen within the shell as a Curvature-pressure that is a direct consequence of the geometric constraint of confining the particles to a shell.

If the radius r decreases then there is an increase in this Curvature-pressure that attempts to increase the surface area by increasing the radius. For a small change in radius in a quasi-equilibrium process where the particle velocities do not change the work done by this Curvature-pressure with an incremental increase of area dA is $p_c dA$ and this must equal the gravitational force times the

change in distance to give

$$p_c dA = \frac{GM^2}{r^2} dr,$$

where $M = \sum m_i$ with the sum going over all the particles. Therefore, using Eq. 4 we can rewrite the previous equation in terms of the velocities as

$$p_c dA = \frac{M \langle v^2 \rangle}{r} dr.$$

$dA/dr = 2A/r$, hence the Curvature-pressure is

$$p_c = \frac{M \langle v^2 \rangle}{2A}.$$

This simple Newtonian model provides a guide as to what the Curvature-pressure would be in the full three-dimensional general relativistic model. We first change $dA/dr = 2A/r$ to $dV/dr = 3V/r$ (where V is the volume) and 3 is the number of degrees of freedom. The result is

$$p_c = \frac{\langle \beta^2 \rangle M c^2}{3V}. \quad (5)$$

Define the average density by $\rho = M/V$ and allowing for relativistic velocities, the cosmological Curvature-pressure is

$$p_c = -\frac{1}{3} \langle \gamma^2 - 1 \rangle \rho c^2 \quad (6)$$

where $\gamma = 1/\sqrt{1 + \beta^2}$ is the Lorentz factor.

My hypothesis is that the cosmological model must include this Curvature-pressure. In particular, it is proportional to an average over the squared velocities whereas the thermodynamic pressure is proportional to an average over the kinetic energies. Eq. 6 is the basic equation for Curvature-pressure.

2.4. The Curvature-cosmological model

Curvature-cosmology can now be derived by including Curvature-redshift and Curvature-pressure into the equations of general relativity. This is done by using a homogeneous isotropic plasma as a model for the real universe. The general theory of relativity enters through the Friedmann equations.

The first-order model considers the universe to be a gas with uniform density and complications such as density fluctuations, galaxies, and stars are ignored. In addition, we assume (to be verified later) that the gas is a high temperature plasma. Based on the Robertson-Walker metric, the Friedmann equations for the homogeneous isotropic model with constant density and pressure without the cosmological constant are (Longair 1991)

$$\begin{aligned} \dot{R}^2 &= \frac{8\pi G \rho}{3} R^2 - c^2 \\ \ddot{R} &= -\frac{4\pi G}{3} \left(\rho + \frac{3p}{c^2} \right) R, \end{aligned} \quad (7)$$

where R is the radius of curvature as used in Eq.2, ρ is the density, p is the pressure, G is the Newtonian gravitational constant and the superscript dots denote time derivatives.

The Curvature-pressure hypothesis is to use the pressure from Eq. 6 (note that the thermodynamic pressure is about 10^{-5} times the energy density and thus may be ignored) and then the modified Friedmann equations are

$$\begin{aligned}\dot{R}^2 &= \frac{8\pi G\rho}{3}R^2 - c^2 \\ \ddot{R} &= -\frac{4\pi G\rho}{3}[2 - \langle\gamma^2\rangle]R,\end{aligned}\quad (8)$$

Clearly, there is a static solution with $\ddot{R} = 0$ which means that $\gamma^2 = 2$.

The first Friedmann equation with $\dot{R} = 0$, provides the radius of the universe, R_0 , which is

$$\begin{aligned}R_0 &= \sqrt{\frac{3c^2}{8\pi G\rho_0}}, \\ &= 1.272 \times 10^{13}/\sqrt{\rho_0} \text{ m}, \\ &= 3.110 \times 10^{26}/\sqrt{N_H} \text{ m}, \\ &= 10.08/\sqrt{N_H} \text{ Gpc},\end{aligned}\quad (9)$$

where N_H is the number density measured in number of hydrogen atoms per m^3 . Later in section 4.1 the value for this free variable is shown to be $N_H = 1.93$. which means $R_0 = 7.255 \text{ Gpc}$ or $R_0 = 2.239 \times 10^{26} \text{ m}$.

Using the equation $E = ch/\lambda$ and since $1+z = \lambda/\lambda_0 = E_0/E$, then integrating Eq. 2 provides the first basic equation for Curvature-cosmology that is

$$r = R_0 \log(1+z). \quad (10)$$

Whereas most cosmologies have a strong emphasis on the redshift here the emphasis is on the distance r and the effects of the cosmic medium on the progress of photons. Thus the importance of Eq. 10 is that provides the relationship between r and redshift and is non-linear.

For example, the apparent redshift “velocity” is the rate of change of z and since by definition $dr/dt = c$, then

$$\frac{dz}{dt} = \frac{c(1+z)}{R_0}. \quad (11)$$

Since this equation is valid for any observation that is time dependent it means that the width of Type Ia supernova light curves, and similar observations, must have a $(1+z)$ width dependence on redshift. Thus a static universe can produce a redshift dependence that is identical to that from universal expansion.

The basic instability of the static Einstein model is well known (Tolman 1934; Ellis 1984). On the other hand, the effect of Curvature-pressure is opposite in effect to the normal pressure thus Curvature-cosmology is intrinsically stable.

Of interest is that the distance to the furthest point is $r = \pi R_0$ which has a redshift of $z = 22.141$. The light travel time to that point is 74.3 Myr. Note that in principle photons can keep on travelling around the universe.

Recently Naidu et al. (2022) has reported two high redshift galaxies that were observed by the James Web Space Telescope (JWST). One GLASS-z10 has a redshift of 10.4 and Glass-z12 has a redshift of 12.4. They are inconsistent with current models of galaxy number densities.

Using Eq. 10 the distance at $z = 12.4$ is $r = 18.8 \text{ Gpc}$. Of interest is that Glass-z12 is at 83% of the distance through the galaxy.

The total volume of the universe is $2\pi^2 R_0^3 = 2.24 \times 10^{80} \text{ m}^3$. Thus there are a total of 4.32×10^{80} hydrogen atoms with a mass of $7.18 \times 10^{53} \text{ kg}$.

2.5. Distance modulus.

The geometry of Curvature-cosmology is that of a three-dimensional “surface” of a four-dimensional hypersphere with radius R_0 . For this geometry the area is

$$A(r) = 4\pi[R_0 \sin(r/R_0)]^2. \quad (12)$$

Let a source have a luminosity $L(\nu)$ (W Hz^{-1}) at the emission frequency ν . Then if energy is conserved, the observed flux density, $F(\nu)$ ($\text{W m}^{-2} \text{ Hz}^{-1}$) at a distance parameter z is the luminosity divided by the area, which is

$$F(\nu)d\nu = \frac{L(\nu) d\nu}{4\pi[R \sin(r/R_0)]^2}.$$

However, because of Curvature-redshift there is an energy loss that is proportional to $(1+z)$. The total energy loss is equivalent to an integral of the incremental energy loss as a function of r . But what is required is the total energy loss as a function of z . Using Eq. 11 this will cancel the intrinsic energy loss to provide

$$F(\nu_0)d\nu_0 = \frac{L(\nu_0) d\nu_0}{4\pi[R_0 \sin(r/R_0)]^2}.$$

Since the absolute magnitude is the apparent magnitude when the object is at a distance of 10 pc then

$$F_{10}(\nu_0) d\nu_0 = \frac{1}{10pc/R_0},$$

where because 10 pc is negligible compared to R , approximations have been made. The flux density ratio is

$$F(\nu_0) = \left[\frac{10pc/R_0}{\sin(r/R_0)} \right]^2.$$

The apparent magnitude is defined as $m = -2.5 \log_{10}(S)$ where the constant 2.5 is exact and if M is the absolute magnitude we get the distance modulus, $\mu = m - M$ with $N_H = 1.93$ to be

$$\mu = 5 \log_{10}[\sin(r/R_0)] + 42.8. \quad (13)$$

Using Eq.10 an alternative version is

$$\mu = 5 \log_{10}[\sin(\log(1+z))] + 42.8. \quad (14)$$

Because the absolute magnitude is referenced to 10pc the free parameter, $N_H = 1.93$, only appears in the constant term. Thus the absolute magnitude is completely defined by the calibration of the flux density observations. There is no need for further calibration. Compared to current distance modulus equations these equations are remarkably simple.

2.6. Temperature of the cosmic plasma

One of the most remarkable results of Curvature cosmology is that it predicts the temperature of the cosmic plasma from fundamental constants.

For a stable solution to Eq. 8 we need that $\langle \gamma^2 \rangle = 2$, where the average is taken over the electron velocities. Since the total energy for a particle is γmc^2 the kinetic energy is $E = (\gamma - 1)mc^2$. Thus for electrons the average kinetic energy is $E = 0.414mc^2$. Assuming that the electrons have a black body spectrum their temperature is

$$T = 2.455 \times 10^9 \text{ K}. \quad (15)$$

In section 4.1 on the X-ray background radiation the observed temperature is measured to be $(2.62 \pm 0.13) \times 10^9 \text{ K}$, which assuming that the photon temperature is the same as the electron temperature, and shows excellent agreement with the predicted temperature.

2.7. Black holes and Jets

Consider a very small homogeneous mass with a radius R_1 . Its dynamics are described by the Friedmann equations Eq. 7, and if the acceleration $\dot{R}_1 = 0$ is zero then

$$\frac{8\pi G \rho_0 R_1^2}{3} = c^2,$$

and substituting for the density $\rho_0 = 3m/(4\pi R_1^3)$, the radius is

$$R_1 = \frac{2Gm}{c^2}, \quad (16)$$

which happens to be the Schwarzschild radius for a simple theoretical black hole.

Since the acceleration is zero, it is an absolute minimum radius and smaller radii are inaccessible. This object has all the external properties of a black hole, such as accretion disks. Thus it looks like the theoretical black hole but is not a black hole.

Since the radii smaller than R_1 are inaccessible, there is no problem with the divergence of space-time at zero radius, that is there is no singularity, which may help the understanding of quantum gravity.

If the compact object is rotating there is the tantalizing idea that Curvature-pressure may produce the emission of material in two jets parallel to the spin axis. The limiting distance, R_1 , will be determined by the polar radius. Thus radii greater than this, such as equatorial radii will still be able to emit energy that can be seen. Thus the object will appear like a doughnut with very low radiation at the center and with a very broad jet parallel to the spin axis.

This could be the 'jet engine' that produces the astrophysical jets seen in stellar-like objects and in many huge galactic radio sources. More importantly it acts to recycle its mass to the cosmic plasma.

2.8. Inhibition of Curvature-redshift

From the discussion above it is clear that the process of Curvature-redshift requires a gradual focusing to a critical limit, followed by the emission of secondary photons. It is as if the photon gets slowly excited by the focusing until the probability of secondary emission becomes large enough for it to occur. Eq.3 shows that the typical interaction length is

$$\sigma_r = \sqrt{R\lambda/4\pi}. \quad (17)$$

For the cosmic plasma it is $\sigma_r = 4.22 \times 10^{12} \sqrt{\lambda} \text{ m}$. In this case the 21 cm hydrogen line has an average interaction distance of $1.93 \times 10^{12} \text{ m}$.

For other situations such as local cloud of hydrogen with a number density of N it is reasonable to assume that because the effects are local we can assume that the interaction distance is same as that for a universe with the same density. Thus we put

$$\sigma_r = 4.97 \times 10^{12} N^{-1/4} \lambda^{1/2} \text{ m}. \quad (18)$$

If there is any other interaction the excitation due to focusing will be nullified. That is, roughly speaking, Curvature-redshift interaction requires an undisturbed path length of at least σ_r for the interaction to occur. Thus a suitable criterion for inhibition to occur is that the competing interaction has an interaction length less than σ_r .

Although Compton or Thompson scattering are possible inhibitors, there is another interaction that has a much larger cross-section. This is the coherent multiple scattering that produces refractive index.

In classical electromagnetic theory, the refractive index of a medium is the ratio of the velocity of light in vacuum to the group velocity in the medium. However, in quantum mechanics photons always travel at the velocity of light in vacuum. In a medium, a group of photons appears to have a slower velocity because the individual photons interact with the electrons in the medium and each interaction produces a time delay.

Because the interaction of a photon is with many electrons spread over a finite volume, the only possible result of an interaction is the emission of another photon with the same energy and momentum. Now consider the absorption of a wave. In order to cancel the incoming wave a new wave with the same frequency and amplitude but with opposite phase must be produced. Thus, the outgoing wave will be delayed by half a period with respect to the incoming wave.

This simple observation enables us to compute the interaction length for refractive index μ . If L is this interaction length then it is

$$L = \frac{\lambda}{2|\mu - 1|}, \quad (19)$$

where the modulus allows for plasma and other materials where the refractive index is less than zero.

Note that L is closely related to the extinction length derived by Ewald and Oseen (see (Jackson 1975) or Born & Wolf (1999)) which is a measure of the distance needed for an incident electromagnetic wave with velocity c to be replaced by a new wave.

For plasmas the refractive index is $\mu = \sqrt{1 - (\nu_p/\nu)^2}$ where ν_p is the plasma frequency and where for propagation we must have that ν is greater than ν_p . Thus $\mu \cong 1 - (1/2)(\nu_p/\nu)^2$. The plasma frequency is $\nu_p = \sqrt{e^2 N_e / \pi m_e}$ where N_e is the electron density, and the refractive index is

$$\mu \cong 1 - \sqrt{\frac{e^2 N_e}{2\pi m_e \nu^2}}$$

Then from Eq. 19 and putting $\nu = c/\lambda$, we get

$$L = \sqrt{\frac{2\pi m_e c^2}{e^2 \lambda N_e}} \cong 1.49 \times 10^{12} / \sqrt{\lambda N_e}. \quad (20)$$

Thus, we would expect the energy loss to be inhibited if the average Curvature-redshift interaction distance is greater than that for refractive-index interactions. Therefore, we can compute the ratio

$$\sigma_r/L = 3.33 N_H^{3/4} \lambda^{-1/2}, \quad (21)$$

where N_e is set equal to N_H . This result shows that Curvature-redshift will be inhibited if this ratio is greater than one. For example, Curvature-redshift for the 21 cm hydrogen line will be inhibited if the electron number density is greater than about 14 m^{-3} . Thus in many parts of the galaxy the effects of Curvature-cosmology will be inhibited at long wavelength radio transmission.

2.9. Possible laboratory tests.

It is apparent from the above analysis that to observe the redshift in the laboratory we need to have sufficient density of gas (or plasma) to achieve a measurable effect but not enough for there to be inhibition by the refractive index.

The obvious experiment is to use as a model is the Mössbauer effect for γ -rays that enable very precise measurement of their frequency. Simply put, the rays are emitted by nuclei in solids where there is minimal recoil or thermal broadening of the emitted ray.

Since the recoil momentum of the nucleus is large compared to the atomic thermal energies and since the nucleus is locked into the solid so that the recoil momentum is precisely defined, then the γ -ray energy is also precisely defined. The absorption process is similar and has a very narrow line width.

Such an experiment has already been done by Pound & Snider (1965). They measured gravitational effects on 14.4 keV γ -rays from ^{57}Fe being sent up and down a vertical path of 22.5m in helium near room pressure. They found agreement to about 1% with the predicted fractional redshift of 7.5×10^{-15} , whereas fractional Curvature-redshift predicted by Eq. 2 for this density is 7.5×10^{-13} . Clearly, this is much larger.

The experimental method would use a horizontal (to eliminate gravitational redshifts) tube filled with helium and with accurately controlled temperature. Then we would measure the redshift as a function of pressure. The above theory predicts that if it is free of inhibition then the redshift should be proportional to the square root of the pressure.

Alternatively, it may be possible to detect the secondary photons. For helium with a pressure of 1 mm Hg the expected frequency of the secondary radiation from ^{57}Fe is about 100 kHz. The expected power from a 1 Cu source is about 5×10^{-22} W. Unfortunately, the secondary radiation could be spread over a fairly wide frequency band which makes its detection somewhat difficult but it may be possible to detect the radiation with modulation tech

3. PART B: TYPE IA SUPERNOVA

3.1. Introduction

This part describes a new analysis method for Type Ia supernova that is simple and can replace the standard SALT2 method. A major difference from SALT2 is that it explicitly estimates and uses intrinsic flux densities that are a function of the intrinsic wavelength.

Although the intrinsic magnitude is the same as the absolute magnitude, a different name is used because the measurement method is different. The intrinsic magnitude can only be used when there are many bands and relies on the fact that each band must have the same distance modulus. Whereas by using a distance modulus, the absolute magnitude can be determined for a single observation.

3.2. Analysis of Type Ia supernova

From Wikipedia: “Type Ia Supernova is believed to result from mass accretion to a carbon-oxygen white dwarf in a close binary system. When the white dwarf mass exceeds the Chandrasekhar limit, the degenerate electron pressure can no longer support the accumulated mass and the star collapses in a thermonuclear explosion producing a supernova. The peak luminosity of supernova Ia is set by the radioactive decay chain, and the observed photometric correlation between the peak luminosity and the time-scale over which the light curve decays from its maximum is understood physically as having both the luminosity and opacity being set by the mass of Nickel-56 synthesized in the explosion.

The major observational evidence for Type Ia supernova is a lack of hydrogen lines and a singly ionized silicon (Si II) absorption feature at $0.615 \mu\text{m}$ near peak brightness.”

An example of the light curve for typical supernova, PSc071032, is shown in Figure 1.

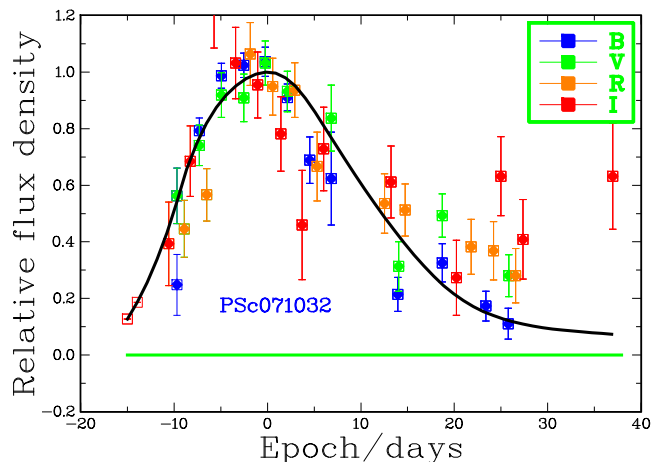


FIG. 1.— A plot of the Type Ia supernova PSc071032 light curve. The plotted flux densities are relative to a fitted peak flux density for each band. All the plotted epochs are relative to a common peak epoch. Note that the longest wavelength (the *I* band) shows evidence of a second maximum. This supernova has a redshift $z = 0.46$ and has a light curve width of 1.28 ± 0.12 .

A critical requirement in measuring the light curve width of Type Ia supernova light curves is to have a reference light curve. The observed light curve must have the same shape independent of redshift. Only its width and

height will vary with redshift. Consequently this property is assumed in this analysis. In order to remove any possible bias, a standard independent template, the B band Parab-18 from Table 2 in Goldhaber et al. (2001) which has the first half-peak width at -10.1 days and the second half-peak width at 22.3 days is used. Consequently all widths are relative to this light curve.

3.3. The observations.

The Type Ia supernova data used here comes from the Supernova Legacy Survey (SNLS), the Sloan Digital Survey (SDSS), (all sourced from the SNANA website Kessler et al. (2009b)), and the Panoramic Survey Telescope and Rapid Response System, (Pan-STARRS), supernova survey Kaiser et al. (2010); Jones et al. (2018); Scolnic et al. (2018) and those observed by the Hubble Space Telescope (HST) Riess et al. (2007); Jones et al. (2013).

The observations of Type Ia supernova from Pan-STARRS, (PS1), were accessed from the site <https://archive.stsci.edu/prepds/ps1cosmo/jones> and the file datatable.html. In 2018 Pan-STARRS consisted of two 1.8-m Ritchey-Chrétien telescopes located at Haleakala in Hawaii and could record almost 1.4 billion pixels per image. It is designed to detect moving or variable objects on a continual basis. An image with a 30 to 60 second duration can record down to an apparent magnitude of 22 mag. The whole visible sky will be surveyed four times a month.

Although theoretically, the Type Ia supernova model has a fixed absolute magnitude, its measurement is subject to the usual noise effects. This is why they can be observed at redshifts beyond the nominal limit of the telescope and are subject to Malmquist bias. However many of the observations come from the PS1 survey which is essentially providing a continuous record of the sky so that the simple Malmquist bias is not applicable. However for the LOWZ, SDSS, and SNLS supernova a Malmquist bias of $-1.382\sigma^2$ mag, where σ is the observed flux density uncertainty has been applied.

The purpose of the light-curve analysis is to obtain estimates of the peak flux density for each band, the width (common to all bands) of the light-curve relative to the template and the epoch offset of the light curve. This offset is a nuisance parameter that allows for the unknown epoch of the peak flux density and is defined to be the epoch difference between the fitted light curve relative to the observed epochs.

An initial problem is to determine this initial epoch offset q . The solution used was to use the average of the epochs of the maximum flux density for each band. The analysis starts with the observed flux density, f_i for the epoch index i , and its uncertainty σ_i . Then for each supernova and each band the maximum likelihood method is used to determine the fitted maximum flux density, F and its epoch.

Let the reference supernova light curve be $C((p_i - q)/w)$ where p_i is the epoch, w is the computed width, and q is the epoch offset of the maximum of the fitted light curve. Then, assuming a Gaussian flux density noise distribution, the modified log-likelihood function is

$$\mathcal{L} = \sum_{k=1}^K \sum_{i=1}^{N_k} \left[\left(\frac{f_i - F_k \times C((p_i - q)/w)}{\sigma_i} \right)^2 \right], \quad (22)$$

TABLE 1
NUMBER OF REJECTED OBSERVATIONS

Catalogue	Total	Rejected
LOWZ	11,971	6,905
SDSS	25,288	3,694
SNLS	8,012	1,502
PS1	34,198	2,050
HST	111	9

where i is the observation index within each band with epoch p_i , and N_k is the number of observations in the band and k is the band index. A constant term that depends only on the measurement uncertainties is omitted. Additionally the omission of the factor $-1/2$ means that \mathcal{L} is a χ^2 variate. Thus the maximization of the likelihood is identical to the minimization of \mathcal{L} .

Although the peak flux density, F_k , is determined by an analytic fit, the values for the epoch offset and width are easily found by numerical minimization. Fortunately, the flux density and width are almost orthogonal so that a sequence of alternate fits rapidly converges.

Note that in Eq 22 each flux density and each peak flux density is divided by its uncertainty which means that the fitted width is independent of individual band calibrations and all bands can be included in the same expression.

One problem with the fitting is that there many observations that are clearly anomalous. These were determined by computing the goodness of fit

$$\psi = \left| \frac{f_i - F_k \times C((p_i - q)/w)}{\sigma_i} \right|, \quad (23)$$

for each observation and rejecting that observation if was greater than chosen limit. Since there were many iterations this limit started very high and was slowly reduced so that for acceptance $\psi \leq 5$. For the Type Ia supernova used, the total number of individual observations and the number of rejected ones are shown in Table 1.

The first step of the analysis was to set the width to $(1+z)$ and iterate until all the anomalies were rejected and the estimated peak epoch was stable. Next iterations were done for both the width and the peak flux densities. The supernova was rejected if it had three or fewer observations of if its width estimate was greater than 4.5. From the original 2,317 supernova, 2,272 were accepted.

It must be noted that the fitting procedure is completely independent of the redshift and is also independent of the band type. Although each band had its own estimate of its peak flux density, the width is the result of a common fit to all observations for each supernova. Thus the computed parameters for each supernova are its light curve width, and the estimated peak flux density for each band, which is the flux density for that band at the maximum epoch of the common fitted light curve. Finally the width is only accepted if it is less than 3.5 and greater than 0.3. The number of accepted supernova are shown Table 2.

3.4. Results for the light curve width

The important result of this width analysis is a regression of $w_{obs}(z)$ as a function of $(1+z)$ for all the 2,250

TABLE 2
ACCEPTED NUMBER OF SUPERNOVA FOR EACH BAND

Band	λ/μ	N
B	0.445	189
V	0.551	183
R	0.658	112
I	0.806	117
g	0.481	1791
r	0.617	2052
i	0.752	2077
z	0.866	1777
F775W	0.767	5
F850LP	0.806	14
F125W	1.438	2

accepted observations which is

$$w_{obs} = 0.067 \pm 0.005 + (1.053 \pm 0.027) \times (1 + z). \quad (24)$$

Although the ordinate is statistically different from zero, it is this ordinate that is most sensitive to calibration and systematic errors such as having minor errors in the reference light curve. However the coordinate shows an excellent agreement with expected value of one. Note that this width measurement is independent any cosmological model.

The widths for the 2,250 supernova are shown in Figure 1. It is clear that the slope (Eq.3.4) is completely consistent with the expected dependence of $w(z) = (1 + z)$.

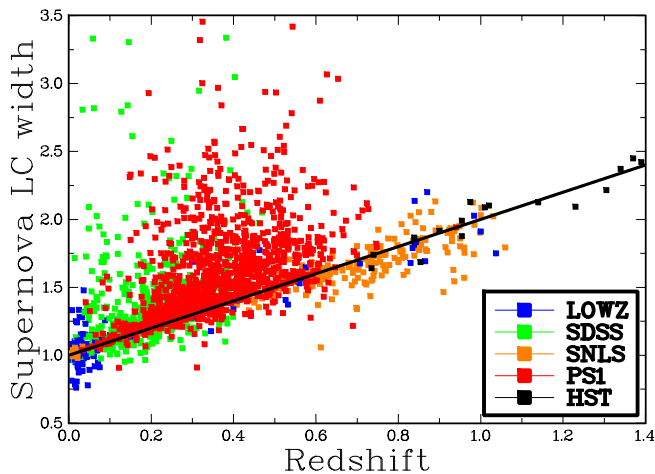


FIG. 2.— A plot of the observed Type Ia supernova light curve widths. The colours show the supernova’s survey. The black line shows a $(1 + z)$ dependence.

3.5. Supernova intrinsic magnitudes

All computed apparent magnitudes were calculated by $m_k = 27.5 - 2.5 \log_{10}(F_k)$ where F_k is the peak flux density and k is the band index.

Since each supernova has a peak magnitude for each observed band, they can be combined to provide an intrinsic magnitude for each band and an average magnitude for the supernova. The problem is to determine these magnitudes from the observed redshifts for each band. Traditionally the method has been to choose a reference band (eg. *B*) and to use the other bands to provide ad hoc colour adjustments.

An alternative approach is to note that each band has an intrinsic wavelength ($\lambda/(1 + z)$) and to determine a

common distribution of magnitude as a function of intrinsic wavelength and then use these magnitudes to correct the magnitudes for the different bands. Thus the difference between the observed magnitude for each band and the average magnitude for that supernova provides an intrinsic magnitude for each band.

The trick in the analysis is to assume that all the supernova have the same intrinsic magnitude distribution. This process is easily iterated until the distribution of intrinsic magnitudes is stable. The common intrinsic distribution was the average in 30 boxes that cover the $\lambda/(1 + z)$ range.

The individual intrinsic peak magnitude data points for the supernova are shown in Figure 3. The black line shows the average for each box. The short wavelengths of the intrinsic distribution show a rapid decrease in average luminosity as the wavelength decreases. This unexpected result is discussed in the following section 3.9, on quasars.

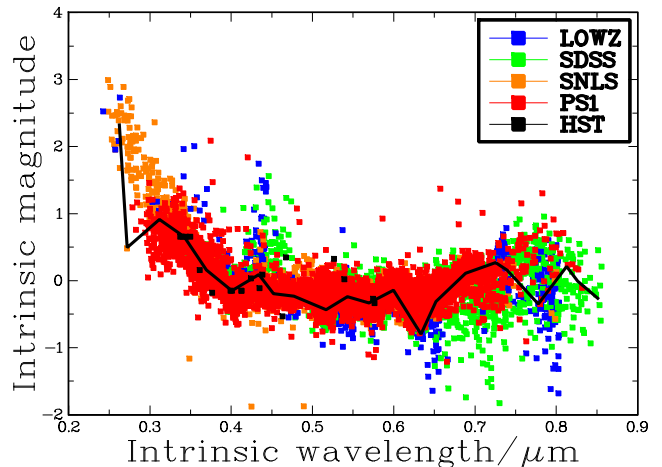


FIG. 3.— The intrinsic magnitude of Type Ia supernova as a function of intrinsic wavelength, $\lambda/(1 + z)$. The black curve shows the average intrinsic magnitude as a function of intrinsic wavelength. The colours show the survey for each supernova.

3.6. Absolute magnitudes

The apparent magnitude for each supernova was computed using Eq. 22 with the assumption that the widths were exactly $(1 + z)$. The apparent magnitude is the same for all bands of the supernova and is a result of the fitting for intrinsic magnitudes. Figure 4 shows the apparent magnitude for the 2,272 Type Ia supernova. The black line shows the distance modulus (Eq. 13) as a function of redshift for Curvature-cosmology.

$$M_0 = -22.535 \pm 0.012 - (0.075 \pm 0.054) \times (1 + z), \quad (25)$$

which shows excellent agreement with a constant value. Thus the simple analysis described above provides excellent estimates of the dependence of Type Ia supernova light widths on redshift and also for their absolute magnitudes. Furthermore the estimation for absolute magnitude does not have any free parameters. These results show very strong support for Curvature-cosmology.

For an overall check Table 3 shows the number of supernova and relative absolute magnitude for each catalogue.

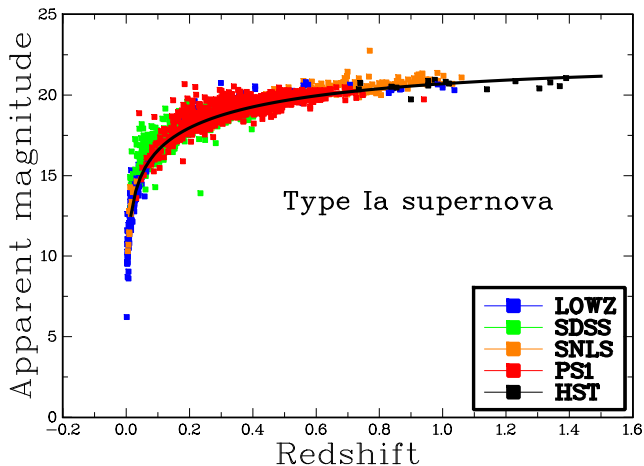


FIG. 4.— This is the plot of 2,272 Type Ia supernova apparent magnitudes as a function of redshift. For each supernova the magnitude is the average magnitude for all the observed bands using the method described in section 3.5. The black line shows the distance modulus Eq. 13.

TABLE 3
RELATIVE ABSOLUTE MAGNITUDE FOR EACH CATALOGUE

Catalogue	N	$M - M_0$
LOWZ	223	0.024 ± 0.046
SDDS	622	0.036 ± 0.027
SNLS	249	0.123 ± 0.024
PS1	1,161	-0.028 ± 0.013
HST	17	-0.198 ± 0.089

TABLE 4
ABSOLUTE MAGNITUDE REGRESSIONS VERSES REDSHIFT

Model	Regression
BB	$-(21.108 \pm 0.007) - (0.178 \pm 0.053) \times z$
BB ^a	$-(21.057 \pm 0.008) + (0.051 \pm 0.059) \times z$
CC	$-(22.634 \pm 0.012) - (0.009 \pm 0.092) \times z$

^a The α term is not included.

Scolnic et al. (2017) suggests several distance moduli that have a good fit to the PS1 Medium Deep Survey that were analyzed with the SALT2 method. The simplest is the Λ CDM model. The PS1 set (Jones et al. (2018) table (1)) has a list of results from the Pan-STARRS supernova survey and other catalogues. There are 1,015 of these Type Ia supernova that used the SALT2 model and Λ CDM cosmology that are common with the current set. They make an excellent set of supernova for comparing Curvature-cosmology (CC) with the SALT2 plus Λ CDM (BB:Big Bang) cosmology.

The regression equations for the absolute magnitudes for both cosmologies are provided in Table 4 and all show good agreement with no redshift dependence.

Since the Curvature-cosmology is radically different from the BB model and both have acceptable agreement with the observations how can we judge which is the better cosmology. Note that the difference in actual value of the absolute magnitude ordinate is probably due to calibration differences and is not relevant to the choice

of cosmologies. The next section has a brief summary of the SALT2 model and the consequences of BB models that shows that they are susceptible to regular errors.

3.7. SALT2

The current analysis of Type Ia supernova uses the SALT2 procedure to get apparent magnitudes followed by one of the Λ CDM models to provide the distance modulus to order to get absolute magnitudes.

To quote Guy et al. (2007, 2010) the aim of SALT2 is to model a spectral energy distribution (SED) of the Type Ia supernova and its variation with a few dominant components. Including a color variation with epoch. It is important to note that SALT2 is modelling the light curves with minimum restrictions on their shape or redshift dependence. This explains the complexity of the process. The functional form is

$$F(p, \lambda) = x_0 \times [M_0(p, \lambda) + x_1 M_1(p, \lambda) + \dots] \times e^{[cCL(\lambda)]},$$

where p is the epoch since B-band maximum luminosity, and λ is the band wavelength, $M_0(p, \lambda)$ is the average spectral sequence and $M_k(p, \lambda)$ for $k > 0$, are additional components that describe the main variability of the supernova. The color c is $c = (B - V)_{MAX} - < B - V >$, and $CL(\lambda)$ represents the average color correction law. The components $M_i(p, \lambda)$ are two-dimensional templates with one dimension being the epoch and the other being the flux density of the light curve with a total of 103,310 elements per component. The brilliance of SALT2 is that has the minimal assumptions about the nature of supernova light curves. It does not require that use of a specified reference light curve that Curvature-cosmology does.

Thus the absolute magnitude, M , Scolnic et al. (2018) is provided by

$$M = m_B - \mu(z) + \alpha x_1 - \beta c, \quad (26)$$

where x_1 is the light-curve shape parameter, c is the color at maximum brightness magnitude. The first parameter, α , is the coefficient of the relationship between luminosity and stretch (which is the width divided by $(1 + z)$). The second parameter, β , is the coefficient between color and flux density.

The strength of the SALT2 method is that uses previous observations to train the internal parameters. In other words, SALT2 is a sophisticated interpolation procedure that uses the calibrated flux densities of previous supernova to determine its internal parameters and then the light curve width and apparent flux density of a new supernova from the observed data. Hence its results only show self-consistency and do not provide validation of the flux densities. Moreover if there is a systematic error in the previous supernova measurements, it will be transmitted to new observations. Hence these results only show self-consistency and do not provide validation of the flux densities. Over all the SALT2 procedure is obscure and ad hoc with a large number of internal parameters.

Finally the apparent magnitudes are converted to absolute magnitudes using one of the Λ CDM cosmologies.

3.8. Cosmology comparison

The major support for the BB model is that it describes the general relativistic model of an unstable expanding universe. This is similar to assuming that a

falling feather should have the same acceleration as a falling stone, whereas we know that the difference is due to air resistance and is not due to a deficiency in the gravitational model. Maybe cosmology needs something like air resistance such as Curvature-cosmology,

One possible source of error in the SALT2 analysis is the α parameter. The α parameter is based Phillips relation 4.20 that showed that there was a good correlation between the peak magnitude and the width of the light curve for Type Ia supernova. If it is intrinsic to the supernova then the final width must be product of it and the cosmological redshift factor. But as shown in the following section 3.8, on quasars, The observed intrinsic wavelength distribution is due to cosmological effects and section 4.20 argues that it does not exist. The second row in Table 4 shows that the regression for the BB analysis with the α term omitted has a better fit than the first row that includes the α term.

Crucially the Λ CDM requires the determination of several the density parameters, which depend on assumptions of inflation, dark matter and dark energy. Since none of these properties are substantiated by other independent observations, they do not provide any support for this cosmology. Thus minor errors in the SALT2 method can be compensated by these estimates. Moreover they are ad hoc models largely determined by supernova observations. In other words, there are no observations other than those for Type Ia supernova that show strong confirmation of the SALT2 analysis and the Λ CDM model. The major criticism of SALT2 and Λ CDM is that they a large number of ad hoc parameters.

In contrast Curvature-cosmology is simple and transparent in its application. It is different from SALT2 in that assumes a common reference light curve whereas SALT2 lets it be produced as part of the analysis by using many supernova. The excellent width fit shown in Eq. 24 and the absolute magnitude fit shown in Eq. 25 and Table 4 all with no free parameters implies that the assumption of a common light curve and the accuracy of the analysis means that Curvature-cosmology provides a valid description of these observation.

On the basis of simplicity, minimal parameters and no dependence on multiple ad hoc cosmological models, Curvature-cosmology is the clearly the better cosmological model.

3.9. Quasars

The investigation of the intrinsic magnitude distribution shown in Figure 3 is helped by considering the distribution of quasar magnitudes.

From Wikipedia: “A quasar also known as a quasi-stellar object is an extremely luminous active galactic nucleus (AGN), powered by a supermassive black hole, with mass ranging from millions to tens of billions times the mass of the Sun, surrounded by a gaseous accretion disc. Gas in the disc falling towards the black hole heats up because of friction and releases energy in the form of electromagnetic radiation. The radiant energy of quasars is enormous; the most powerful quasars have luminosities thousands of times greater than a galaxy such as the Milky Way. Usually, quasars are categorized as a subclass of the more general category of AGN. The redshifts

of quasars are of cosmological origin.”

All quasar data used here is taken from the Sloan Digital Sky Survey Quasar Catalog: Sixteenth Data Release (DR16Q) Lyke et al. (2020).

The majority of these quasars have been discovered by a flux density limited survey without knowledge of the redshift and the observed magnitudes have a very limited dependence on their observed redshift. Thus the observation model is that the selection of each quasar is determined by the cut-off flux density and the overall telescope noise and it is assumed that these values are the same for all the quasars. The selection of quasars is that each magnitude uncertainty had to be less or equal to 1.5.

Thus for each quasar discovered its apparent magnitude must lie in the range of magnitudes that are accepted by the telescope and it is completely independent of the intrinsic magnitude of the quasar. Clearly they are subject to Malmquist bias and $-1.382\sigma^2$, where σ is the magnitude uncertainty, is added to each magnitude. Since all the observed bands for a quasar must have the same distance modulus we can use the identical analysis used for the supernova to determine the average intrinsic magnitude distribution for quasars. Their advantage is that the quasars cover a redshift range up to $z = 7$. Figure 5 shows the average intrinsic magnitude distribution for these quasars.

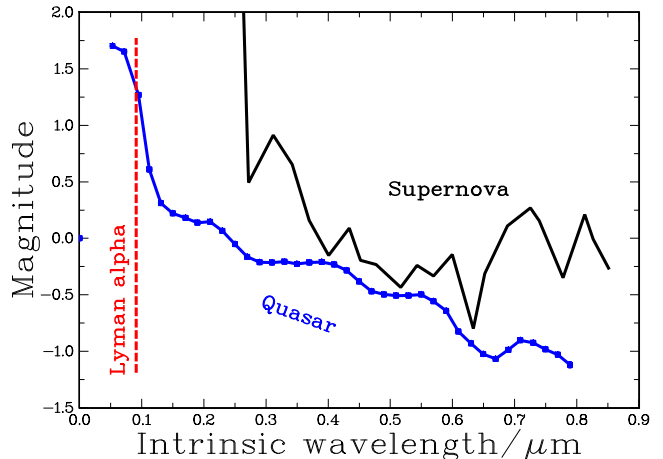


FIG. 5.— The blue shows the average intrinsic magnitude of SDSS quasars as a function of intrinsic wavelength, $\lambda/(1+z)$. The position of the wavelength for the full ionization is shown in red. The black line shows the intrinsic magnitude distribution of supernova from Figure 3.

Clearly, the intrinsic magnitude shows a strong decrease in luminosity as the wavelength decreases towards that for full ionization. Although this does not rule out an intrinsic dependence on the observed object, it is strong evidence that the cause is due to propagation in the cosmic plasma that has a major hydrogen component. It appears that the presence of atomic hydrogen can, by photo-ionisation, remove most of the very high energy photons. Further investigation into this distribution is outside the scope of this paper.

An important cosmological property is that all redshifts have a redshift dependence of $(1+z)$ that amounts to an addition of $2.5(1+z)$ to the observed magnitude.

TABLE 5
AVERAGE QUASAR COEFFICIENT FOR EACH BAND.

Band	Number	Coefficient
u'	746,922	1.154 ± 0.004
g'	746,922	0.779 ± 0.004
r'	746,922	0.710 ± 0.003
i'	746,922	0.669 ± 0.003
z'	746,922	0.790 ± 0.003

Table 3.9 shows the results of a regression of the raw observations for each band versus the photon redshift. The coefficient is the multiplier of $2.5(1+z)$ which has an expected value of one. The average value of the coefficient is 0.799. Since the quasar flux density distribution has a strong Malmquist bias to smaller values, there is a bias in the selection towards fainter quasars. The observed flux density is the product of the actual flux density and the $2.5(1+z)$ term. Thus the observed flux density term will include the distribution bias to smaller values. Although the results are biased, they show strong support for the presence of this redshift term in the quasar data.

There is another property of these quasars that warrants investigation in a static universe, that is their absolute magnitude distribution. Since each quasar is seen at its maximum redshift its expected density is proportional the reciprocal of the volume of the universe at that redshift. The volume is proportional to this area times the “vertical” distance. Since $dz/dr = (1+z)$ this distance is proportional to $(1+z)$, thus the density for a quasar is inversely proportional to $4\pi(1+z) \times (R_0 \sin(r/R_0))^2$ where $R_0 = 7.26$ Gpc. The density shown by the redline has

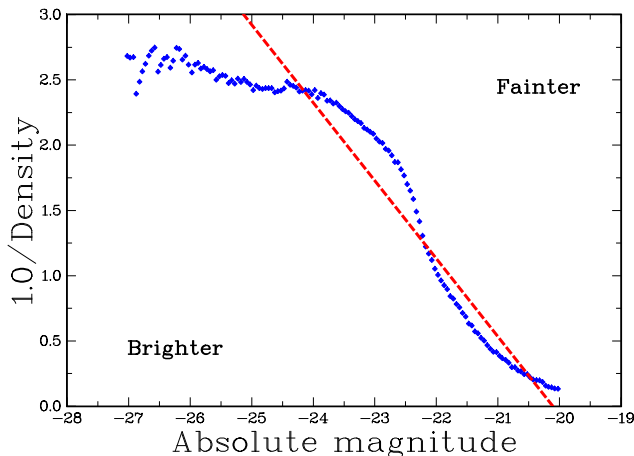


FIG. 6.— Shows the reciprocal of the spatial density of quasars as a function of the absolute magnitude. The red line is a linear fit to the reciprocal density versus absolute magnitude.

the equation $1/\text{density} = (-12.00 \pm 0.02) - (0.60 \pm 0.02) \times M$, where M is the absolute magnitude. The reciprocal was chosen in order to make the distribution clearer.

To convert the densities displayed in Figure 6 to actual values multiply them by $4\pi R_0^3$.

4. PART C: OBSERVATIONS

4.1. X-ray background radiation

Since Giacconi et al. (1962) observed the X-ray background there have been many suggestions made to explain its characteristics. Although much of the unresolved X-ray emission comes from active galaxies, there is a part of the spectrum between about 10 keV and 1 MeV that is not adequately explained by emission from discrete sources.

In Λ CDM cosmology for the intermediate X-ray range of about 10–300 keV, the production of X-rays in hot cosmic plasma through the process of bremsstrahlung has been suggested by Hoyle (1962); Gould & Burbidge (1963); Field & Henry (1964); Cowsik & Kobetich (1972).

In a review of the spectrum of the X-ray background radiation Holt (1992) concluded that the measured spectra of discrete sources are not consistent with the observations in the intermediate energy range but there is a remarkable fit to a 40 keV (4.6×10^8 K) bremsstrahlung spectrum from a diffuse hot gas.

However, in an expanding universe most of the X-rays are produced at redshifts of $z \approx 3$ where the density is large enough to scatter the CMBR. This scattering known as the Sunyaev–Zel’dovich effect (see Section 4.11), which makes a distinct change in the spectrum of the CMBR. This predicted change in the spectrum has not been observed and this is the major reason why the bremsstrahlung model in Λ CDM is rejected.

In Curvature-cosmology, the basic component of the universe is plasma with a very high temperature, and with low enough density to avoid the Sunyaev–Zel’dovich effect.

The background X-ray emission is produced in this plasma by the process of free-free emission (bremsstrahlung). The observations of the background X-ray emission are analyzed in order to measure the density and temperature of the plasma. In Curvature-cosmology, this density is the only free parameter and it determines the size of the universe.

The first step is to calculate the expected X-ray emission from high temperature plasma in thermal equilibrium. Here the dominant mechanism is bremsstrahlung radiation from electron-ion and electron-electron collisions. With a temperature T and emission into the frequency range ν to $\nu + d\nu$ the volume emissivity per steradian can be written as

$$j_\nu(\nu)d\nu = \left(\frac{16}{3}\right) \left(\frac{\pi}{6}\right)^{1/2} r_0^3 m_e c^2 \left(\frac{m_e c^2}{kT}\right)^{1/2} g(\nu, T) \exp\left(-\frac{h\nu}{kT}\right) N_H \sum Z_i^2 N_i d\nu, \quad (27)$$

where $g(\nu, T)$ is the Gaunt factor, N_H is the electron number density, N_i is the ion number density and r_0 is the classical electron radius and the other symbols have their usual significance (Nozawa, Itoh, & Kohyama 1998). The intensity, $j_\nu(\nu)$, has the units of $\text{W m}^{-3} \text{Hz}^{-1}$.

As it stands this equation does not include the electron-electron contribution. Nozawa et al. (1998) and Itoh et al. (2000) have done accurate calculations for many light elements. Based on their calculations Professor Naoki Itoh (<http://www.ph.sophia.ac.jp/>) provides a subroutine to calculate the Gaunt factor that is accurate for temperatures greater than 3×10^8 K. It is used here.

Because of the very high temperature, we can assume that all atoms are completely ionized. Thus, Eq. 27 including the Gaunt factor provides the production rate of X-ray photons as a function of the plasma temperature and density.

The next step is to compute the expected intensity at an X-ray detector. Consider an X-ray photon that is produced at a distance r from the detector. During its travel to the detector, it will have many Curvature-redshift interactions. Although the photon is destroyed in each interaction, there is a secondary photon produced that has the same direction but with a slightly reduced energy.

It is convenient to consider this sequence of photons as a single particle and to refer to it as a primary photon. The important result is that the number of these primary photons is conserved. Therefore, we need the production distribution of the number of photons per unit energy interval. The number of photons emitted per unit volume per unit time in the energy interval ε to $\varepsilon + d\varepsilon$ is given by

$$j_n(\varepsilon) d\varepsilon = \frac{j_\nu(\nu)}{\varepsilon} h d\nu, \quad (28)$$

where $\varepsilon = h\nu$, h is Plank's constant and $j_\nu(\nu)$ is the energy distribution per unit frequency interval.

Now consider the contribution to the number of X-rays observed by a detector with unit area. Because the universe is static, the area at a distance r from the source is the same as the area at a distance r from the detector. Since there is conservation of these photons, the number coming from a shell at radius r per unit time and per steradian within the energy interval ε to $\varepsilon + d\varepsilon$ is

$$\frac{dn(r)}{dt} d\varepsilon = j_n(\varepsilon) d\varepsilon r d\chi.$$

Next, we integrate the photon rate per unit area and per steradian from each shell where the emission energy is ε and the received energy is ε_0 to get

$$I_n(\varepsilon_0) d\varepsilon_0 = r \int_0^{\chi_m} j_n(\varepsilon) d\varepsilon d\chi,$$

where $\varepsilon = (1+z)\varepsilon_0$ and it is assumed that the flux is uniform over the 4π steradian. Furthermore, it is useful to change the independent coordinate to the redshift parameter z .

Then using Eq. 28 we get

$$I_\nu(\nu_0) d\nu_0 = \frac{c}{H} \int_0^{z_m} \frac{j_\nu(\nu)}{1+z} dz d\nu_0,$$

where H is the Hubble constant and the change in bandwidth factor $d\nu/d\nu_0$, cancels the $(1+z)$ factor that comes from the change in variable from $d\chi$ to dz but there is another divisor of $(1+z)$ that accounts for the energy lost by each photon.

Thus the energy flux per unit area, per unit energy interval, per unit frequency and per solid angle is given by Eq. 29 where Plank's constant is included to change the differential from frequency to energy. The z_m limit of 8.2 comes from the limit of $\chi \leq \pi$.

$$I_\nu = \left(\frac{16}{3}\right) \left(\frac{\pi}{6}\right)^{1/2} \frac{r_0^3 m_e c^3}{h} (8\pi GM_H)^{-1/2} \left(\frac{mc^2}{kT}\right)^{1/2}$$

TABLE 6
LIST OF BACKGROUND X-RAY DATA USED.

Name	Instrument	Reference
Gruber	HEAO 1 A-4	Gruber et al. (1999)
Kinzer	HEAO 1 MED	Kinzer et al. (1997)
Dennis	OSO-5	Dennis et al. (1973)
Mazets	Kosmos 541	Mazets et al. (1975)
Mandrou	Balloon	Mandrou et al. (1979)
Trombka	Apollo 16, 17	Trombka et al. (1977)
Santangelo	Rocket	Santangelo et al. (1973)
Fukada	Rocket	Fukada et al. (1975)

TABLE 7
BACKGROUND X-RAY DATA: REJECTED POINTS.

Source	Energy keV	Flux density keV/(keV cm ² sr)	χ^2 (1 DoF)
Gruber	98.8	0.230±0.012	108.6
Gruber	119.6	0.216±0.022	65.2
Fukada	110.5	0.219±0.011	66.6
Gruber	152.6	0.140±0.022	50.9
Fukada	179.8	0.110±0.005	41.5
Gruber	63.9	0.484±0.034	25.1

$$\begin{aligned} &= n_e n_i N_H^{3/2} \int_0^{z_m} \frac{g((1+z)\nu_0, T)}{(1+z)} \exp\left(-\frac{h(1+z)\nu_0}{kT}\right) dz \\ &= \frac{1.9094 \times 10^3 \text{ keV}}{\text{keV m}^2 \text{ sr}} \left(\frac{mc^2}{kT}\right)^{1/2} n_e n_i N_H^{3/2} \\ &\quad \varepsilon_0 \int_0^{z_m} \frac{g((1+z)\nu_0, T)}{(1+z)} \exp\left(-\frac{h(1+z)\nu_0}{kT}\right) dz, \quad (29) \end{aligned}$$

where I_ν is a function of ν_0 .

The density N_H is obtained by fitting Eq. 29 to the observed data as a function of the temperature T , and then extracting N_H from the normalization constant.

The X-ray data used is tabulated in Table 6. It consists of the background X-ray data cited in the literature and assessed as being the latest or more accurate results. Preliminary analysis showed that there were some discrepant data points that are listed in Table 7 in order of exclusion.

Very hard X-rays cannot be produced even by this hot plasma and are presumably due to discrete sources (Holt 1992).

The results of the fit of the data to this model of pure hydrogen is a temperature of

$$(2.62 \pm 0.13) \times 10^9 \text{ K}, \quad (30)$$

which is good agreement with the predicted temperature of 2.456×10^9 K in section 2.6. The measured density is

$$1.93 \pm 0.13 \text{ H atoms per m}^3, \quad (31)$$

which is the only free parameter in Curvature-cosmology.

Most of the X-ray flux below 10 keV and part of the flux just above 10 keV is emission from discrete sources. The deviation from the curve at energies above about 300 keV arises from X-rays coming from discrete sources.

In the intermediate region where bremsstrahlung should dominate, there are clear signs of some minor

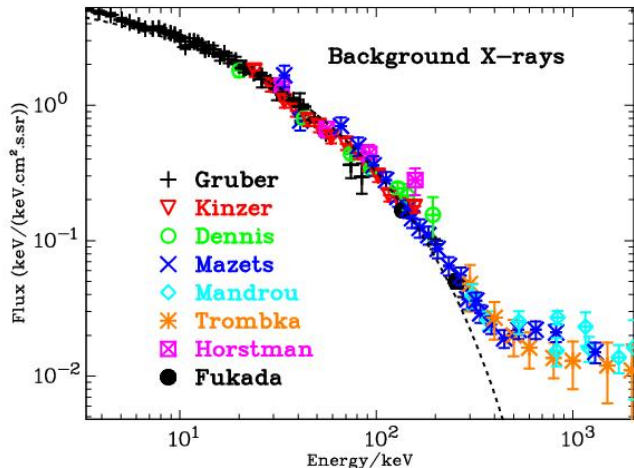


FIG. 7.— Background X-ray spectrum. See Table 6 for list of observations. The dashed (black) line is best fit from 10 keV to 300 keV for the pure hydrogen model.

systematic errors. In addition, there appears to be some variation between the data sets. It is not clear whether the discrepancy between the observed points and the predicted flux densities is due to an inadequate theory, inadequate X-ray emission model, or systematic errors in the observations. After all the measurements are very difficult and come from a wide range of rocket, balloon and satellite experiments. In particular, the recent HEAO results Kinzer et al. (1997) differ from earlier results reported by Marshall et al. (1980).

4.2. Cosmic microwave background radiation.

The cosmic microwave background radiation (CMBR) is one of the major success stories for the standard model. The observed radiation has a spectrum that is extremely close to a black body spectrum which means that it can be described by a single parameter, its temperature.

Observations of the CMBR spectrum were obtained from the FIRAS instrument on the *Cobe* satellite by Mather et al. (1990). They measured the temperature of the CMBR to be 2.725 K. This temperature is in agreement with the observations of Roth & Meyer (1995) who measured a temperature of $2.729(+0.023, -0.031)$ K using cyanogen excitation in diffuse interstellar clouds. More recently Fixsen (2009) using data from the Wilkinson Microwave Anisotropy Probe (WMAP) and many earlier results provides a temperature of 2.72548 ± 0.00057 K.

Since electrons and nucleons have wave properties they are subject to Curvature-redshift where the energy loss is to low energy photons. In this case the energy loss from the high energy protons in the cosmic plasma due to Curvature-cosmology is the source of CMBR.

The basic energy loss is $\Delta E = E_0 r/R$, where E_0 is the particle energy and r is the distance traveled. With a velocity of βc the distance traveled is $r = \beta ct$ and the rate of energy loss is

$$\frac{\Delta E}{dt} = \frac{E_0 \beta c}{R_0}. \quad (32)$$

The distribution of relativistic particles in equilibrium is the Maxwell-Jüttner distribution. With $\gamma = 1/\sqrt{1-\beta^2}$

it is

$$f(\gamma) = \frac{\gamma^2 \beta}{\theta K_2(1/\theta)} \exp(-\gamma/\theta), \quad (33)$$

where $\theta = kT/mc^2$ and K_2 is the modified Bessel function of the second kind.

Here its application requires that θ is a constant value, $\theta = \sqrt{2}$, then the integral over the range of γ is

$$\frac{\Delta E}{dt} = \frac{\gamma^2 \beta^2 c(\gamma - 1) m_p c^2}{R_0} \exp(-\gamma/\theta)/A, \quad (34)$$

where A is the normalization constant and it is

$$A = \int_1^\infty \gamma^2 \beta(\exp(-\gamma/\theta)) d\gamma. \quad (35)$$

As explained earlier this lost energy consists of a pair of identical photons whose usual interaction with the electrons and photons bring them into thermal equilibrium. Since the total energy must be conserved, the energy lost by Curvature-redshift must be radiated by the emittance of these photons. Then allowing for the proton number density $N_H = 1.93 \pm 0.13 m^{-3}$, section 4.1, their equilibrium temperature is 2.736 ± 0.092 K. This radiation is the cosmic microwave background radiation and is within 0.4% of the WMAP value. Considering that the theory has only one free parameter, the agreement is exceptionally good.

Clearly, the same analysis can be applied to the free electrons. In this case the radiation has a temperature of 0.419K with a typical wavelength of 34.4mm.

4.3. Tolman surface density.

This test, suggested by Tolman (1934), relies on the observation that the surface brightness (SB) of objects does not depend on the geometry of the universe. Although it is obviously true for Euclidean geometry, it is also true for most non-Euclidean geometries. For a uniform source, the quantity of light received per unit angular area is independent of distance. However, the quantity of light is also sensitive to non-geometric effects, which make it an excellent test to distinguish between cosmologies. For expanding universe cosmologies the surface brightness is predicted to vary as $(1+z)^{-4}$, where one factor of $(1+z)$ comes from the decrease in energy of each photon due to the redshift, another factor comes from the decrease in the rate of their arrival and two factors come from the apparent decrease in area due to aberration. This aberration is simply the rate of change of area for a fixed solid angle with redshift. In a static, tired light, cosmology (such as Curvature-cosmology) only the first factor is present. Thus an appropriate test for Tolman surface brightness is the value of this exponent.

The obvious candidates for surface brightness tests are elliptical and S0 galaxies which have minimal projection effects compared to spiral galaxies. The major problem is that surface brightness measurements are intrinsically difficult due to the strong intensity gradients across their images. In a series of papers Sandage & Lubin (2001); Lubin & Sandage (2001a,b,c) (hereafter SL01) have investigated the Tolman surface brightness test for elliptical and S0 galaxies. More recently Sandage (2010) has done a more comprehensive analysis but since he came to the same conclusion as the earlier papers and since the

TABLE 8
GALACTIC PROPERTIES FOR PETROSIAN RADIUS $\eta = 2.0$

Cluster	N	$\log(S_{BB})$	$\overline{m_{BB}}$	$\overline{M_{BB}}$
Nearby	74	4.69±0.28	22.56±0.84	-23.84±0.66
1324+3011	11	3.99±0.21	22.87±0.75	-23.28±0.65
1604+4304	6	4.05±0.17	22.34±0.60	-23.51±0.68
1604+4321	13	4.00±0.15	22.35±0.78	-23.33±0.64

earlier papers are better known this analysis will concentrate on them.

The observational difficulties are thoroughly discussed by Sandage & Lubin (2001) with the conclusion that the use of Petrosian metric radii helps solve many of the problems. Petrosian (1976); Djorgovski & Spinrad (1981); Sandage & Perelmuter (1990) showed that if the ratio of the average surface brightness within a radius is equal to η times the surface brightness at that radius then that defines the Petrosian metric radius, η . The procedure is to examine an image and to vary the angular radius until the specified Petrosian radius is achieved.

Thus, the aim is to measure the mean surface brightness for each galaxy at the same value of η . The choice of Petrosian radii greatly diminishes the differences in surface brightness due to the luminosity distribution across the galaxies. However, there still is a dependence of the surface brightness on the size of the galaxy which is the Kormendy relationship (Kormendy 1977).

The purpose of the preliminary analysis done by SL01 is not only to determine the low redshift absolute luminosity but also to determine the surface brightness versus linear size relationship that can be used to correct for effects of size variation in distant galaxies. The data on the nearby galaxies used by SL01 was taken from Postman & Lauer (1995) and consists of extensive data on the brightest cluster galaxies (BCG) from 119 nearby Abell clusters. All magnitudes for these galaxies are in the R_c (Cape/Landolt) system.

Since the results for different Petrosian radii are highly correlated the analysis repeated here using similar procedures will use only the Petrosian $\eta = 2$ radius. Although the actual value used for the Hubble constant does not alter any significant results here, it is set to $h=50 \text{ km s}^{-1} \text{ Mpc}^{-1}$ for numerical consistency. A minor difference is that the angular radius used here is provided by Curvature-cosmology whereas SL01 used the older Mattig equation.

The higher z data comes from SL01. They made Hubble Space Telescope observations of galaxies in three clusters and measured their surface brightness and radii. The names and redshifts of these clusters are given in Table 8 which also shows the number of galaxies in each cluster, N , the logarithm of the average metric radius in kpc, $\log(S_B)$, and the average apparent magnitude and the absolute magnitude. In order to avoid confusion in BB denotes a measurement made using the standard Λ CDM cosmology. Note that the original magnitudes for Cl 1324+3011 and Cl 1604+4304 were observed in the I band.

In order to get a reference surface brightness at $z = 0$ all the surface brightness values, SB , of the nearby galaxies were reduced to absolute surface brightness by using Eq. 36. Since all the redshifts are small, this reduction is

TABLE 9
FITTED EXPONENTS FOR DISTANT CLUSTERS ($\eta = 2.0$)

Cluster	Col	\bar{z}	n_{BB}	n_{SL01}
1324+3011	I	0.757	1.98±0.19	1.99±0.15
1604+4304	I	0.897	2.22±0.22	2.29±0.21
1604+4321	R	0.924	2.24±0.18	2.48±0.25

essentially identical for all cosmological models. However the calculation of the metric radii for the distant galaxies is very dependent on the cosmological model.

This procedure of using the same cosmology in analyzing a test of that cosmology is discussed in SL01. Their conclusion is that it reduces the significance of a positive result from being *strongly supportive* to being *consistent with the model*. Of interest is that Table 8 shows that on average the distant galaxies are fainter than the nearby galaxies.

Then a linear least squares fit of the absolute surface brightness as a function of $\log(S_{BB})$, the Kormendy relationship, for the nearby galaxies results in the equation

$$SB = 9.29 \pm 0.50 + (2.83 \pm 0.11) \log(S_{BB}), \quad (36)$$

whereas SL01 found the slightly different equation

$$SB = 8.69 \pm 0.06 + (2.97 \pm 0.05) \log(S_{BB}). \quad (37)$$

Although a small part of the discrepancy is due to slightly different procedures, the main reason for the discrepancy is unknown. Of the 74 galaxies used, there were 19 that had extrapolated estimates for either the radius or the surface brightness or both. In addition there were only three galaxies that differed from the straight line by more than 2σ . They were A147 (2.9σ), A1016 (2.0σ) and A3565 (-2.4σ). Omission of all or some of these galaxies did not improve the agreement. The importance of this preliminary analysis is that Eq. 36 contains all the information that is needed from the nearby galaxies in order to calibrate the distant cluster galaxies.

Next we use the galaxies' radius and Eq. 36 to correct the apparent surface brightness of the distant galaxies for the Kormendy relation and then do least squares fit to the difference between the corrected surface brightness and its absolute surface brightness as a function of $2.5 \log(1+z)$ to estimate the exponent, n , where $SB \propto (1+z)^n$. If needed the non-linear corrections given by Sandage (2010) were applied to the nearby surface brightness values. For the I band galaxies, the absolute surface brightness included the color correction $< R - I > = 0.62$ Lubin & Sandage (2001c).

The results for the exponent, n , for each cluster are shown in Table 9 together with the values from SL01 (column 5) where the second column is the band (color) in which the cluster was observed.

Because the definition of magnitude contains a negative sign the expected value for n_{BB} in standard cosmology is four. Nearly all of the difference between these results and those from SL01 arise from the use of a different Kormendy relationship. If the Kormendy relationship used by SL01 Eq. 37 is used instead of Eq. 36) the agreement is excellent. If it is assumed that there is no evolutionary or other differences between the three clusters and all the data are combined the resulting exponent is $n_{BB} = 2.16 \pm 0.13$.

Clearly, there is a highly significant disagreement between the observed exponents and the expected exponent of four. Both SL01 and Sandage (2010) claim that the difference is due to the effects of luminosity evolution. Based on a range of theoretical models SL01 show that the amount of luminosity evolution expressed as the exponent, $p = 4 - n_B$, varies between $p = 0.85 - 2.36$ in the R band and $p = 0.76 - 2.07$ in the I band. In conclusion, to their analysis, they assert that *they have either (1) detected the evolutionary brightening directly from the SB observations on the assumption that the Tolman effect exists or (2) confirmed that the Tolman test for the reality of the expansion is positive, provided that the theoretical luminosity correction for evolution is real.*

SL01 also claims that their results are completely inconsistent with a tired light cosmology. Although this is explored for Curvature-cosmology in the next subsection, it is interesting to consider a very simple model. The essential property of a tired light model is that it does not include the time dilation factor of $(1+z)$ in its angular radius equation. Thus assuming B but without the $(1+z)$ term all values of $\log(S_{BB})$ will be increased by $\log(1+z)$. Hence the predicted absolute surface brightness will be (numerically) increased by $(2.83/2.5)\log(1+z)$. For example, the exponent for all clusters will be changed to

$$n_{\text{tired_light}} = 2.16 \pm 0.16 - \frac{2.83}{2.5} = 1.03 \pm 0.16.$$

This is clearly close to the expected value of unity predicted by a tired-light cosmology and thus disagrees with the conclusion of SL01 that the data are incompatible with a tired light cosmology.

There are two major criticisms of this work. The first is that relying on theoretical models to cover a large gap between the expected index and the measured index makes the argument very weak. Although SL01 indirectly consider the effects of relatively common galaxy interactions and mergers in the very wide estimates they provide for the evolution, the fact that there is such a wide spread makes the argument that Tolman surface brightness for this data is consistent with Λ CDM possible but weak.

Ideally, there would be an independent estimate of p based on other observations. The second criticism is that the nearby galaxies are not the same as the distant cluster galaxies. The nearby galaxies are all brightest cluster galaxies (BCG) whereas the distant cluster galaxies are normal cluster galaxies. It is well known that BCG (Blanton & Moustakas 2009) are in general much brighter and larger than would be expected for the largest member of a normal cluster of galaxies. Whether or not this amounts to a significant variation is unknown but it does violate the basic rule that like should be compared with like.

Unsurprisingly it is found that using Curvature-cosmology the relationship between absolute surface brightness and radius is identical to that shown in Table 8. What is different is the average radius, the absolute magnitudes and the observed exponent n . These are shown in Table 10.

The result for all clusters is $n = 1.38 \pm 0.13$ which is in agreement with unity. Note that the critical difference from the standard analysis is in the size of the radii. They are not only much closer to the nearby galaxy radii but because they are larger they do not require the non-

TABLE 10
RADI AND FITTED EXPONENTS FOR DISTANT CLUSTERS ($\eta = 2.0$)

Cluster	N	$\log(S)$	\bar{M}	n
nearby	74	4.70 ± 0.28	-23.78 ± 0.66	
1324+3011	11	4.18 ± 0.21	-22.41 ± 0.66	1.19 ± 0.19
1604+4304	6	4.27 ± 0.17	-22.54 ± 0.65	1.45 ± 0.21
1604+4321	13	4.23 ± 0.15	-22.33 ± 0.68	1.48 ± 0.17

linear corrections for the Kormendy relation. As before we note that the nearby galaxies are BCG which may have a brighter SB than the normal field galaxies. If this is true, it would bias the exponent to a larger value. If we assume that Curvature-cosmology is correct then this data shows that on average the BCG galaxies are -0.64 ± 0.08 mag (which is a factor of 1.8 in luminosity) brighter than the general cluster galaxies.

The SL01 data for the surface brightness of elliptical galaxies is consistent with Λ CDM but only if a large unknown effect of luminosity evolution is included. The data do not support expansion and are in complete agreement with Curvature-cosmology.

4.4. Dark matter and Coma cluster

All observational evidence for dark matter comes from the application of Newtonian gravitational physics to either clusters of objects or the rotation of galaxies. Galaxy rotation will be dealt with in Section 4.18. The original concept for dark matter comes from applying the virial theorem to the Coma cluster of galaxies (Zwicky 1937). The virial theorem is a statistical theorem that states that for an inverse square law the average kinetic energy of a bound system is equal to half the potential energy (i.e. $2T + V = 0$).

Then with knowing the linear size of the cluster and measuring the mean square spread of velocities we can estimate the total mass of the cluster. There is no doubt that applying the virial theorem to the Coma and other clusters of galaxies provides mass estimates that can be several hundred times the mass expected from the total luminosity. Even the mass of intergalactic gas is not enough to overcome this imbalance. In Λ CDM cosmology dark matter has been introduced to make up for the shortfall of mass.

However if Curvature-cosmology is valid then it is possible that the observed redshifts are not due to kinematic velocities but are Curvature-redshifts produced by the intra-cluster gas. The purpose of this section is to show that Curvature-redshift can explain the galactic velocities without requiring dark matter.

For simplicity, we will use the Coma cluster as a test bed. Not only is it very well studied, but it also has a high degree of symmetry and the presence of an intergalactic gas cloud is known from X-ray observations.

Watt et al. (1992) and Hughes (1989) have fitted the density of the gas cloud to an isothermal model with the form

$$\rho = \rho_0 \left(1 + \left(\frac{r}{r_e} \right) \right)^{-\alpha}. \quad (38)$$

The central density is obtained from the X-ray luminosity and has a strong dependence on the distance. Watt et al. (1992) assumed a Hubble constant of $h=50$ $\text{km s}^{-1} \text{Mpc}^{-1}$. With a mean velocity of $6,853$ km s^{-1}

TABLE 11
COMA VELOCITY DISPERSIONS FOR SOME DISTANCES.

Distance/Mpc	50	87	100	150
Dispersion /km s ⁻¹	318	554	636	955

(Colless & Dunn 1996) and with this Hubble constant, the distance to the Coma cluster is 137 Mpc. Recently Rood (1988) using the Tully–Fisher relation to measure the distance modulus to the galaxies in the Coma cluster, to observe a value of 34.4 ± 0.2 mag whereas Liu & Graham (2001) using infrared surface brightness fluctuations get 34.99 ± 0.21 mag. The average is 34.7 mag that corresponds to a distance of 87.1 Mpc. This is consistent with the distance of 85.6 Mpc given by Freedman et al. (2001).

The galactic velocity data are taken from Beijersbergen (2003) who provide information for 583 galaxies. They find that early-type galaxies (E+S0+E/S0) have a mean velocity of $9,926 \text{ km s}^{-1}$ and a rms (root-mean-square) velocity, of 893 km s^{-1} . Let us assume that all the galactic velocities are due to Curvature-redshift. That is we assume that the actual velocities, the peculiar velocities, are negligible. Then the redshifts for the galaxies are calculated (in velocity units) by

$$v = v_0 + \int_0^Z 51.691 \sqrt{N(Z)} dZ \text{ km s}^{-1}, \quad (39)$$

where Z is the distance from the central plane of the Coma cluster to the galaxy measured in Mpc, $N(Z)$ is the density of the intergalactic gas cloud and v_0 is the average velocity of the galaxies in the cluster. The problem here is that we do not know Z distances. Nevertheless, we can still get a good estimate by assuming that the distribution in Z is statistically identical to that in X and in Y . In a Monte Carlo simulation, each galaxy was given a Z distance that was the same as the X (or Y) distance of one of the other galaxies in the sample chosen at random. For 50 trials, the computed dispersion was 554 km s^{-1} which can be compared with the measured dispersion of 893 km s^{-1} . Curvature-cosmology has predicted the observed dispersion of galactic velocities in the Coma cluster to within a factor of two.

Considering that this is a prediction of the cosmological model without fitting any parameters and ignoring all the complications of the structure both in the gas and galactic distributions the agreement is remarkable.

Since the distance to the Coma cluster is an important variable, the computed velocity dispersion from the Monte Carlo simulation for some different distances (all the other parameters are the same) is shown in Table 11. Thus, the redshift dispersion (in velocity units) is approximately a linear function of the Coma distance. This is not surprising since in this context the distance is mainly a scale factor.

Beijersbergen (2003) note that a better fit to the velocity distribution is provided by the sum of two Gaussian curves. Their best fit parameters for these two Gaussians are $v_1 = 7,501 \pm 187 \text{ km s}^{-1}$, with $\sigma_1 = 650 \pm 216 \text{ km s}^{-1}$ and $v_2 = 6641 \pm 470 \text{ km s}^{-1}$, with $\sigma_2 = 1,004 \pm 120 \text{ km s}^{-1}$. This double structure is supported by Colless & Dunn (1996) who argue for an ongoing merger between two sub clusters centered in pro-

jection on the dominant galaxies NGC 4874 and NGC 4889.

In addition, Briel, Henry, & Boehringer (1992) found evidence for substructure in the X-ray emission and Finoguenov et al. (2004) and White, Briel, & Henry (1993) have measured the X-ray luminosity of individual galaxies in the Coma cluster showing that the model for the gas used above is too simple. The net effect of this substructure is that the observed velocity dispersion would be different from that predicted by a simple symmetric model. Thus, it appears that substructure makes it very difficult to achieve a more accurate test of Curvature-cosmology using the Coma cluster.

There is an important difference between Curvature-redshift and models that assume that the redshifts of the galaxies within a cluster are due to their velocities. Since the laws of celestial mechanics are symmetric in time, any galaxy could equally likely be going in the opposite direction. Thus a galaxy with a high relative (Z) velocity could be in the near side of the cluster or equally likely on the far side of the cluster. However, if the redshifts are determined by Curvature-redshift then there will be a strong correlation in that the higher redshifts will come from galaxies on the far side of the cluster.

A possible test is to see if the apparent magnitudes are a function of relative redshift. With a distance of 87.1 Mpc the required change in magnitude is about $0.025 \text{ mag Mpc}^{-1}$. A simple regression between magnitude of Coma galaxies (each relative to its type average) and velocity did not show any significant dependence.

Although this was disappointing, several factors can explain the null result. The first is the presence of the substructure; the second is that the magnitudes for a given galactic type have a standard deviation of about one magnitude, which in itself is sufficient to wash out the predicted effect; and thirdly mistyping will produce erroneous magnitudes due to the different average velocities of different types. In support of the second factor, we note that for 335 galaxies with known types and magnitudes, the standard deviation of the magnitude is 1.08 mag and if we assume that the variance of the Z distribution is equal to the average of the variances for the X and Y distributions then the expected standard deviation of the slope is $0.076 \text{ mag Mpc}^{-1}$. Clearly, this is such larger than the expected result of $0.025 \text{ mag Mpc}^{-1}$. It is expected that better measurements or new techniques of measuring differential distances will in the future make this a very important cosmological test.

In Λ CDM observations of the velocity dispersion of clusters of galaxies cannot be explained without invoking an ad hoc premise such as dark matter. However Curvature-cosmology not only explains the observations but also makes a good prediction, without any free parameters, of its numerical value.

4.5. Angular size

Closely related to surface brightness is relationship between the observed angular size of a distant object and its actual linear transverse size.

The major distinction in angular size is that Curvature-cosmology, like all tired-light cosmologies, does not include the $(1+z)$ aberration factor. Its relationship between the observed angular size and the linear size is very close (for small redshifts) to the Euclidean equation.

Gurvits, Kellermann, & Frey (1999) provide a comprehensive history of studies for a wide range of objects that generally show a $1/z$ or Euclidean dependence. Most observers suggest that the probable cause is some form of size evolution. Recently López-Corredoira (2010) used 393 galaxies with redshift range of $0.2 < z < 3.2$ in order to test many cosmologies.

Briefly, his conclusions are

- : *The average angular size of galaxies is approximately proportional to $z^{-\alpha}$ with α between 0.7 and 1.2.*
- : *Any model of an expanding universe without evolution is totally unable to fit the angular size data ...*
- : *Static Euclidean models with a linear Hubble law or simple tired-light fit the shape of the angular size vs z dependence very well: there is a difference in amplitude of 20%–30%, which is within the possible systematic errors.*
- : *It is also remarkable that the explanation of the test results with an expanding model requires four coincidences:*
 1. *The combination of expansion and (very strong evolution) size evolution gives nearly the same result as a static Euclidean universe with a linear Hubble law: $\theta \propto z^{-1}$.*
 2. *This hypothetical evolution in size for galaxies is the same in normal galaxies as in quasars, as in radio galaxies, as in first-ranked cluster galaxies, as the separation among bright galaxies in cluster*
 3. *The concordance model gives approximately the same (differences of less than 0.2 mag within $z < 4.5$) distance modulus in a Hubble diagram as the static Euclidean universe with a linear law.*
 4. *The combination of expansion, (very strong) size evolution, and dark matter ratio variation gives the same result for the velocity dispersion in elliptical galaxies (the result is that it is nearly constant with z) as for a simple static model with no evolution in size and no dark matter ratio variation.*

With a redshift range of $z < 3$ the value of S is approximately proportional to $z^{0.68}$ which shows that it is consistent with these results. A full analysis requires a fairly complicated procedure to correct the observed sizes for variations in the absolute luminosity.

A simple example of the angular size test can be done using double-lobed quasars. Using quasar catalogues, Buchalter et al. (1998) carefully selected 103 edge-brightened, double-lobed sources from the VLA FIRST survey and measured their angular sizes directly from the FIRST radio maps.

Since Buchalter et al. (1998) claim that three different Friedmann Λ CDM models fit the data well but that a Euclidean model had a relatively poor fit a reanalysis is warranted.

Their angular sizes were converted to linear sizes for each cosmology and were divided into six bins so that

there were 17 quasars in each bin. Because these double-lobed sources are essentially one-dimensional a major part of their variation in size is due to projection effects.

For the moment assume that in each bin they have the same size, \hat{S} , and the only variation is due to projection then the observed size is $\hat{S} \sin(\theta)$ where θ is the projection angle. Clearly, we do not know the projection angle but we can assume that all angles are equally likely so that if the N sources, in each bin, are sorted into increasing size the i 'th source in this list should have, on average, an angle $\theta_i = \pi(2i - 1)/4N$. Thus the maximum likelihood estimate of \hat{S} is

$$\hat{S}_{\text{est}} = \frac{\sum_{i=1}^N \sin(\theta_i) S_i}{\sum_{i=1}^N \sin^2(\theta_i)}.$$

Note that the sum in the denominator is a constant and that the common procedure of using median values is the same as using only the central term in the sum.

Next a regression was done between logarithm of the estimated linear size in each bin and $\log(1 + z)$ where z is the mean redshift. Then the significance of the test was how close was the exponent, b , to zero. For Λ CDM the exponent was $b = -0.79 \pm 0.44$ and for Curvature-cosmology, it was $b = 0.16 \pm 0.44$. Although the large uncertainties show that this is not a decisive discrimination between the two cosmologies the slope for the Curvature-cosmology suggests that no expansion is more likely.

For angular size the conclusion is in favor of Curvature-cosmology.

4.6. Galaxy distribution

Recently, large telescopes with wide fields and the use of many filters have enabled a new type of galactic survey. The light-collecting capability of the large telescopes enables deep surveys to apparent magnitudes of 24 mag or better and the wide field provides a fast survey over large areas.

A major innovation is the use of many filters whose response can be used to classify the objects with great accuracy. Thus, galaxies can be separated from quasars without needing morphological analysis. This photometric method of analysis works because photometric templates are available for a wide range of types of galaxies and other types of objects. In addition, accurate redshifts are obtained from fitting the templates without the tedious procedure of measuring the spectrum of each object.

A typical example of this photometric method is the COMBO-17 survey (Classifying Objects by Medium-Band Observations in 17 filters) provided by Wolf et al. (2004). The goal of this survey was to provide a sample of 50,000 galaxies and 1000 quasars with rather precise photometric redshifts based on 17 colors.

In practice, such a filter set provides a redshift accuracy of 0.03 for galaxies and 0.1 for quasars. The central wavelength of the 17 filters varied from 364 nm to 914 nm and consisted of 5 broadband filters (U, B, V, R, I) and 12 narrower-band filters. Wolf et al. (2003) have analyzed this data and claim that there is strong evolution for $0.2 < z < 1.2$.

Instead of using generic K-corrections, the intrinsic (rest frame) luminosity of all galaxies are individually

TABLE 12
 M_C^* FOR SED TYPE 1 GALAXY LUMINOSITY DISTRIBUTIONS.

z	$\Delta\mu$	$M_r^{*\alpha}$	M_{BB}^*	M_{280}^*
0.3	0.426	-20.49	-19.06	-17.38
0.5	0.642	-20.49	-19.15	-17.84
0.7	0.822	-20.77	-19.37	-17.62
0.9	0.975	-20.54	-19.09	-17.79
1.1	1.107	-20.87	-19.23	-18.23
χ^2		3.70	2.32	12.81

^aAbsolute magnitude for the SDSS r -band

measured from their 17-filter spectrum. For each galaxy, three rest-frame pass bands are considered, (i) the SDSS r -band, (ii) the Johnston B -band and (iii) a synthetic UV continuum band centered at $\lambda_{\text{rest}} = 280$ nm with 40 nm FWHM and rectangular transmission function.

A spectral energy distribution, SED, was determined for each galaxy by template matching. For the evolution analysis, they were assigned to one of four types. The only type that showed a well-defined peak in their luminosity distribution was Type 1 which covers the E-S_a galactic types. The characteristics of the luminosity distribution were obtained by fitting a Schechter function which is

$$\phi(L)dL\phi^*(L/L^*)^\alpha e^{L/L^*} dL,$$

where the luminosity L^* (and its magnitude M^*) is a measure of location and α is a measure of shape.

They found that a fixed value for α works quite well for the luminosity functions of individual SED types. Examination of their estimate of M^* for Type 1 galaxies showed that if they were converted to Curvature-cosmology magnitudes they were independent of redshift. This is shown in Table 12 where the data are taken from the appendix to Wolf et al. (2003). The second column is the difference, $\Delta\mu = \mu_C - \mu_{BB}$, between C, (Curvature-cosmology) and B (standard), distance moduli. The remaining columns show the Curvature-cosmology absolute magnitudes for the three rest-frame bands.

The last row shows the χ^2 for the five magnitudes relative to their mean using the given uncertainties (all in the range 0.14-0.23).

With four degrees of freedom, the first two bands show excellent agreement with a constant value. The values for M_{280}^* have less than a 2.5% chance of being constant. However since most of the discrepancy comes from the $z = 0.3$ value of -17.38 mag and most of this band at small redshifts is outside the range of the 17 filters this discrepancy can be ignored.

If this value is ignored, the χ^2 is reduced from 12.81 to 6.12 (with 3 Dof) which is consistent with being constant. Since α is independent of redshift, the result is that if the data had been analyzed using Curvature-cosmology the magnitude for these Type 1 galaxies does not vary with redshift.

Thus we have the surprising result that using Λ CDM a class of galaxies has a well-defined luminosity evolution that can be explained by Curvature-cosmology. In other words, there is no expansion.

4.7. Quasar variability in time

One of the major differences between a tired-light cosmology and an expanding universe cosmology is that any expanding universe cosmology predicts that time varia-

tions and clocks have the same dependence on redshift as does the frequency of the radiation.

Hawkins (2010, 2003) has analyzed the variability of 800 quasars covering epoch scales from 50 days to 28 years. His data permitted the straightforward use of Fourier analysis to measure the time scale of the variability. He showed that there was no significant change in the time scale of the variability with increasing redshift. He considered and rejected various explanations including that the time scales of variations were shorter in bluer pass bands or that the variations were not intrinsic but were due to intervening processes such as gravitational micro-lensing. His conclusion was either that the quasars are not at cosmological distances or that the expanding universe cosmologies are incorrect in this prediction.

Curvature-cosmology predicts the observed quasar epoch variability of zero.

4.8. The Butcher-Oemler effect

If there were evidence of significant change in the universe as a function of redshift, it would be a detrimental to any static cosmology. Probably the most important evidence for this cosmic evolution that appears to be independent of any cosmological model is the Butcher & Oemler (1978) effect. Although the effect has been discussed in earlier papers, the definitive paper is Butcher & Oemler (1984).

They observed that the fraction of blue galaxies in galactic clusters appears to increase with redshift. Clusters allow the study of large numbers of galaxies at a common distance and out to large redshifts, which makes them ideal for studies in evolution. The core regions in a cluster are dominated by early-type (elliptical and lenticular) galaxies, which have a tight correlation between their colors and magnitudes.

We can calculate R_{30} , the projected cluster-centric radius that contains 30% of the total galaxy population. The blue fraction, f_B , is defined to be the fraction of galaxies within R_{30} which are bluer than the color-magnitude relationship for that cluster.

At first sight, this may appear to be a simple test that could be done with apparent magnitudes. However to compare the ratio for distant clusters with that for nearby ones the colors must be measured in the rest frame of each cluster, hence the need to use K-corrections.

The major advantage of the Butcher-Oemler effect is that it is independent of the luminosity-distance relationship that is used. Therefore, to be more precise f_B is the fraction that has an absolute magnitude M_V , whose rest frame (B-V) color is at least 0.2 magnitudes bluer than expected. A review by Pimblet (2003) summaries the important observations.

In its original form the Butcher-Oemler effect is dependent on the apparent magnitude cut-off limits. It is essential that selection effects are the same in the rest frame for each cluster. There are further complications in that the percentage of blue galaxies may or may not depend on the richness of the cluster and the effect of contamination from background galaxies.

Although Pimblet (2003) concluded there was a definite effect, his Fig. 1 shows that this conclusion is open to debate. Since then there have been several attempts to measure an unambiguous effect. Even though

they attempted to duplicate the original methodology of Butcher & Oemler, Hawkins (2003) found essentially no effect for K-selected galaxies.

Andreon, Lobo, & Iovino (2004) examined three clusters around $z=0.7$ and did not find clear-cut evidence for the effect. To quote one of their conclusions: *Twenty years after the original intuition by Butcher & Oemler, we are still in the process of ascertaining the reality of the Butcher–Oemler effect.*

The Butcher-Oemler effect remains uncertain, and therefore does not provide evidence to refute a static cosmology.

4.9. Fluctuations in the CMBR

In the model proposed for Curvature-cosmology these fluctuations will also occur but in this case they are due to variations in the density of the cosmic plasma. The CMBR seen through the denser gas within a galactic cluster will have lower than average temperature. Cabré et al. (2006) show some support for this model in that they have correlated data from the Wilkinson Microwave Anisotropy Probe (WMAP) with galaxy samples from the SDSS DR4 galaxy survey and found a significant correlation for the intensity fluctuations with galaxy density.

4.10. Pioneer 10 acceleration.

Precise tracking of the *Pioneer 10/11*, *Galileo* and *Ulysses* spacecraft (Anderson et al. 2002) have shown an anomalous constant acceleration for *Pioneer 10* with a magnitude $(8.74 \pm 1.55) \times 10^{-10} \text{ m s}^{-2}$ directed towards the sun.

The only method for monitoring *Pioneer 10* is to measure the frequency shift of the signal returned by an active phase-locked transponder. These frequency measurements are then processed using celestial mechanics in order to get the spacecraft trajectory.

The simplicity of this acceleration and its magnitude suggests that *Pioneer 10* could be a suitable candidate for investigating the effects of Curvature-redshift. There is a major problem in that the direction of the acceleration corresponds to a blue shift whereas Curvature-redshift predicts a redshift.

Nevertheless, we will proceed, guided by the counter-intuitive observation that a drag force on a satellite actually causes it to speed up. This is because the decrease in total energy makes the satellite change orbit with a redistribution of kinetic and potential energy.

The crucial point of this analysis is that the only information available that can be used to get the *Pioneer 10* trajectory is Doppler shift radar. There is no direct measurement of distance.

Thus the trajectory is obtained by applying celestial mechanics and requiring that the velocity matches the observed frequency shift. Since the sun produces the dominant acceleration, we can consider that all the other planetary perturbations and know drag effects have been applied to the observations and the required celestial mechanics is to be simple two-body motion.

If the observed velocity (away from the sun) is increased by an additional apparent velocity due to Curvature-redshift the orbit determination program will compensate by assuming that the spacecraft is closer to the sun than its true distance. It will be shown that this

distance discrepancy produces an extra apparent acceleration that is directed towards the sun. The test of this model is whether the densities required by Curvature-redshift agree with the observed densities.

Let the actual velocity of *Pioneer 10* at a distance r , be denoted by $v(r)$, then since the effect of Curvature-redshift is seen as an additional velocity, $\Delta v(r)$ where from Eq. 2

$$\Delta v(r) = 2\sqrt{8\pi G} \int_0^r \sqrt{\rho(r)} dr, \quad (40)$$

where the factor of 2 allows for the two-way trip and the density at the distance r from the sun is $\rho(r)$. Since *Pioneer 10* has a velocity away from the sun, this redshift shows an increase in the magnitude of its velocity.

We will assume that all the perturbations and any other accelerations that may influence the *Pioneer 10* velocity have been removed as corrections to the observed velocity and the remaining velocity, $v(r)$, is due to the gravitational attraction of the sun. In this case the energy equation is

$$v(r)^2 = v_\infty^2 + \frac{2\mu}{r}, \quad (41)$$

where $\mu = GM$ is the gravitational constant times the mass of the sun ($\mu = 1.327 \times 10^{20} \text{ m}^3 \text{ s}^{-2}$) and v_∞ is the velocity at infinity.

The essence of this argument is that the tracking program is written to keep energy conserved so that an anomalous change in velocity, $\Delta v(r)$, will be interpreted as a change in radial distance which is

$$\Delta r = -\sqrt{\frac{2r^3}{\mu}} \Delta v(r).$$

Thus an increase in magnitude of the velocity will be treated as a decrease in radial distance which, in order to keep the total energy constant, implies an increase in the magnitude of the acceleration. Either by using Newton's gravitational equation or by differentiating Eq. 41 the acceleration $a(r)$ is given by

$$a(r) = -\frac{\mu}{r^2}. \quad (42)$$

Hence with $v_\infty = 0$ and therefore $v(r) = \sqrt{2\mu}/r$ we get

$$\Delta a(r) = \frac{2\mu}{r^3} \Delta r = \sqrt{\frac{8\mu}{r^3}} \Delta r,$$

and then to the first order an increase in velocity of $\Delta v(r)$ will produce an apparent decrease in acceleration of $\Delta a(r)$, and

$$\begin{aligned} \Delta a &= 8\sqrt{\pi\mu G} r^{-3/2} \int_0^r \sqrt{\rho(r)} dr \\ &= 16\sqrt{\pi\mu G} r^{-1/2} < \sqrt{\rho(r)} > \\ &= 6.90R^{-1/2} < \sqrt{\rho(r)} >, \end{aligned}$$

where for the last equations we measure the distance in AU so that $r = 1.496 \times 10^{11} R$ and the angle brackets show an average value.

Now fig. 7 from (Anderson et al. 2002) shows that after about 20 AU the anomalous acceleration is essentially

constant. The first step is to get an estimate of the required density and see if is feasible.

Using the observed acceleration of $a_P = 8.74 \times 10^{-10} \text{ m s}^{-2}$ the required average density for the two-way path is $1.60 \times 10^{-20} R \text{ kg m}^{-3}$ and for $R=20$ it is $3.21 \times 10^{-19} \text{ kg m}^{-3}$.

The only constituent of the interplanetary medium that approaches this density is dust. One estimate by [Le Sergeant D'Hendecourt & Lamy \(1980\)](#) of the interplanetary dust density at 1 AU is $1.3 \times 10^{-19} \text{ kg m}^{-3}$ and more recently, [Grün et al. \(1999\)](#) suggests a value of $10^{-19} \text{ kg m}^{-3}$ which is consistent with their earlier estimate of $9.6 \times 10^{-20} \text{ kg m}^{-3}$ ([Grün, Zook, Fechtig, & Giese 1985](#)).

Although the authors do not provide uncertainties, it is clear that their densities could be in error by a factor of two or more. The main difficulties are the paucity of information and that the observations do not span the complete range of grain sizes.

The meteoroid experiment on board *Pioneer 10* measures the flux of grains with masses larger than 10^{-10} g . The results show that after it left the influence of Jupiter the flux ([Anderson et al. 2002](#)) was essentially constant (in fact there may be a slight rise) out to a distance of 18 AU.

It is thought that most of the grains are being continuously produced in the Kuiper belt. As the dust orbits evolve inwards due to Poynting-Robertson drag and planetary perturbations, they achieve a roughly constant spatial density. The conclusion is that interplanetary dust could provide the required density to explain the anomalous acceleration by a frequency shift due to Curvature-redshift.

Overall, this analysis has shown that it is possible to explain the acceleration anomaly of *Pioneer 10* but that a more definitive result requires Curvature-redshift to be included in the fitting program and more accurate estimates of the dust density are certainly needed. Subject to the caveat about the dust density, Curvature-redshift could explain the anomaly in the acceleration of *Pioneer 10* (and by inference other spacecraft).

Not only can Curvature-cosmology explain the anomalous *Pioneer 10* acceleration, it has a feasible prediction of its value.

4.11. The Sunyaev-Zel'dovich effect

The Sunyaev-Zel'dovich effect ([Sunyaev & Zeldovich 1970](#); [Peebles 1993](#)) is the effect of Thomson scattering of background radiation by free electrons in the intervening medium. The technique depends on knowing the spectrum of the background source and then measuring the changes in the spectrum due to the intervening plasma. For optical wavelengths the Thomson scattering wavelength is $6.65 \times 10^{-27} \text{ m}^2$. Thus for an electron density of 1.93 m^{-3} the interaction length is $1.79 \times 10^{25} \text{ m}$.

In particular, it is the scattering in both angle and frequency of the cosmic microwave background radiation (CMBR) by electrons in the cosmic plasma. Because of the rapidly changing density (like $(1+z)^3$) with redshift this is an important effect in Λ CDM cosmology. The effect is often characterized by the dimensionless y -parameter, which for a distance x through non-relativistic thermal plasma with an electron density of

N_H has the value

$$y = \frac{kT_e}{m_e c^2} \sigma_T N_H x = 3.46 \times 10^{-16} N_H T_e x \text{ Mpc}, \quad (43)$$

where σ_T is the Thomson cross-section. An object at redshift z is at the distance $x = R\chi = 5.80 \times 10^3 N_H^{1/2} \log(1+z) \text{ Mpc}$. Hence, using $T_e = 2.62 \times 10^9 \text{ K}$, $N_H = 1.93 \text{ m}^{-3}$ we get $y = 1.35 \times 10^{-5} \log(1+z)$.

Using the CMBR as a source the Sunyaev-Zel'dovich effect has been observed and [Mather et al. \(1990\)](#) report an observed upper limit of $y = 0.001$, and more recently [Fixsen et al. \(1996\)](#) report $y = 1.5 \times 10^{-5}$. Using this limit with Eq. 43 shows that there is no effect in Curvature-cosmology if $z < 2$. ([Longair 1991](#); [Sunyaev & Zeldovich 1980](#)). [Bielby & Shanks \(2007\)](#) extend the results of [Lieu, Mittaz, & Zhang \(2006\)](#) to show that not only was the Sunyaev-Zel'dovich effect less than what was expected but that it tended to disappear as the redshift went from 0.1 to 0.3. The conclusion is that Curvature-cosmology is completely consistent with the experimental observations of the Sunyaev-Zel'dovich effect on the CMBR. Thus the Sunyaev-Zel'dovich effect may be important in standard cosmology but it is not important in Curvature-cosmology.

4.12. Gravitational lensing.

There are many gravitational lens where a quasar or distant galaxy has one or more images produced by a nearer lensing galaxy or cluster of galaxies. A set of these lensing systems has been examined in the context of Curvature-cosmology to see if it offers a consistent and possibly simpler explanation. The two important measures are the prediction of the mass of the lensing galaxy and the determination of the Hubble constant from the time delays between variations in the luminosity of different images. Since the delay measurement is easily done, all that is needed is to measure the different path lengths. This path difference involves both geometric and general relativistic corrections.

One of the remarkable properties of gravitational lenses is that the geometry is completely determined by a two-dimensional lensing potential which can be expressed in terms of a surface density at the position of the lensing galaxy. For thin lenses, any two systems with the same surface density distribution have the same lens effect. Now the usual way to determine the surface density is to measure the widths of spectral lines, assume that the width is due to velocity and then use the virial theorem to obtain the surface density.

However in Curvature-cosmology the widths of spectral lines are likely to have a large component due to the effects of Curvature-redshift from dust and gas in the lensing object. Thus the widths are not a reliable measure of area density and this method cannot be used.

4.13. Lyman-alpha forest

The Lyman- α ($\text{Ly}\alpha$) forest is the large number of absorption lines seen in the spectra of quasars. Most of the lines are due to absorption by clouds of neutral hydrogen in the line of sight to the quasar. Some of the lines are due to other elements or due to Lyman- β absorption.

Because of the redshift between the absorbing cloud and us, the lines are spread out over a range of wavelengths. Usually the analysis is confined to lines between the Ly α (at a wavelength of 121.6 nm) and Ly β (at 102.5 nm). Thus, each quasar provides a relatively narrow spectrum of Ly- α lines at a redshift just less than that for the quasar. Since the advent of spacecraft telescopes, in which can observe the ultraviolet lines, and by using many quasars the complete redshift range up to the most distant quasar has been covered. The large redshift range makes the Lyman α spectra potentially a powerful cosmological tool.

The obvious cosmological observation is the density of lines as a function of redshift but as discussed by Rauch (1998) in an excellent review, there are many important observational problems.

The first, which has now been overcome, is that the spectra must have sufficient resolution to resolve every line. The second is that most lines are very weak and the number of resolved lines can depend greatly on the signal-to-noise ratio. This is accentuated because the steep spectrum for the density of lines as a function of their strength means that a small decrease in the acceptance level can drastically increase the number of observed lines. The third problem is that each quasar only provides a set of lines in a narrow range of redshift and there are considerable difficulties in getting uniform cross-calibrations.

In addition to these problems, it will be shown that Curvature-redshift can have a profound effect on the interpretation of the line widths and column densities.

Since in Curvature-cosmology, the distribution of clouds is independent of time or distance the expected density of lines as a function of redshift is

$$\frac{dn}{dz} = \frac{AcN_H}{H(1+z)}, \quad (44)$$

where N_c is the volume density and A is the average area of a cloud. Most observers have fitted a power law with the form $(1+z)^\gamma$ to the observed line densities with a wide range of results. They vary from $\gamma = 1.89$ to $\gamma = 5.5$ (Rauch 1998). All of which are inconsistent with the Curvature-cosmology prediction of $\gamma = -1$.

In Curvature-cosmology, there is the additional effect that much of the line broadening may be due to Curvature-redshift. Curvature-redshift will be operating within the clouds so that the observed line width will be a combination of the usual Voigt profile and the change in the effective central frequency as the photons pass through the cloud. If the cloud has a density $\rho(x)$ at the point x , measured along the photon trajectory then the change in frequency from the entering frequency due to Curvature-redshift is

$$\frac{\Delta\nu}{\nu} = \frac{1}{c} \int \sqrt{8\pi G\rho(x)} dx.$$

In units of $N(x) = \rho(x)/m_H$ this is (with N in m^{-3} and dx in kpc)

$$\frac{\Delta\nu}{\nu} = -\frac{\Delta\lambda}{\lambda} = \int 1.724 \times 10^{-7} \sqrt{N(x)} dx.$$

Then the final profile will be the combination of the natural line width, the Doppler width due to tempera-

ture, any width due to bulk motions and the Curvature-redshift width. Now assuming pure hydrogen, the hydrogen column density is given by $N_H = \int N(x) dx$.

Although it is unlikely that the line of sight goes through the center of the cloud, it is reasonable to expect a roughly symmetric distribution of gas with a shape similar to a Gaussian. We can define an effective density width by

$$x_w^2 = \int (x - \bar{x})^2 N(x) dx / \int N(x) dx.$$

Also define $N_c = N_H/x_w$ and an effective velocity width $\Delta v = 51.68\eta x_w \sqrt{N_c}$ and where η is a small numeric constant that depends on the exact shape of the density distribution. Eliminating the central density, we get (with x_w in kpc)

$$\Delta v^2 = 8.656 \times 10^{-17} \eta^2 N_H x_w. \quad (45)$$

For values $N_H = 10^{19} \text{m}^{-2}$, $x_w = 1 \text{kpc}$ and with $\eta = 1$ we get $\Delta v = 29 \text{km s}^{-1}$.

Since there is a wide variation in column densities and the effective widths are poorly known, it is clear that Curvature-redshift could completely dominate many of the Lyman- α line widths and the others would require a convolution of the Doppler profile with the Curvature-redshift density effect. What is also apparent is that the very broad absorption lines may be due to Curvature-redshift acting in very dense clouds.

Although there is uncertainty about the observed relationship between the line width and the column density, we note that for a fixed effective density width, Eq. 45 predicts a square relationship that may be compared with the exponent of 2.1 ± 0.3 found by Pettini et al. (1990). Clearly, there needs to be a complete re-evaluation of profile shapes, column densities, and cloud statistics that allows for the effects of Curvature-cosmology. We must await this analysis to see whether the Lyman- α forest can provide a critical test of Curvature-cosmology.

4.14. Nuclear abundances

One of the successes of Λ CDM cosmology is in its explanation of the primordial abundances of the light elements. Since the proposed Curvature-cosmology is static, there must be another method of getting the 'primordial' abundances of light elements. In Curvature-cosmology, the primordial abundance refers to the abundance in the cosmic gas from which the galaxies are formed and the cosmic gas is pure hydrogen.

The first point to note is that in Curvature-cosmology the predicted temperature of the cosmic plasma is $2.465 \times 10^9 \text{K}$ at which temperature nuclear reactions can proceed.

It is postulated that in Curvature-cosmology there is a continuous recycling of material from the cosmic plasma to galaxies and stars and then back to the plasma. Because of the high temperature, nuclear reactions will take place whereby the more complex nuclei are broken down to hydrogen.

4.15. Galactic rotation curves

One of the most puzzling questions in astronomy is: why the observed velocity of rotation in spiral galaxies

does not go to zero towards the edge of the galaxy. Simple Keplerian mechanics suggest that there should be a rapid rise to a maximum and then a decrease in velocity that is inversely proportional to the square root of the radius once nearly all the mass has been passed. Although the details vary between galaxies, the observations typically show a rapid rise and then an essentially constant tangential velocity as a function of radius out to distances where the velocity cannot be measured due to lack of material.

In Curvature-cosmology there is a Curvature pressure, Eq.6, that acts to reduce any gravitational attraction. In general the temperature of the galactic halo with increase in the outer layers to eventually reach that of the cosmic plasma, and the Curvature pressure has a strong dependence on temperature its effect on the velocity of the gas components in the galaxy is to decrease the effects of gravitational attraction and the gross velocities of the galactic gas. A simple consequence is that the rotation of the galaxy will look more like that of a rigid body.

4.16. Redshifts in our Galaxy

In our Galaxy, the Milky Way, there is an interesting prediction. The density of the interstellar ionized gas can be high enough to inhibit Curvature-redshift for radio frequencies.

From Eq. 21 it was shown that for radio wavelengths the effect of refractive index in fully ionized plasma will inhibit Curvature-redshift. Thus for sight lines close to the Galactic plane we can assume a similar inhibition with the result that the observed radio redshifts can be correctly interpreted as genuine velocities. Thus, there is little change needed to the current picture of galactic structure and rotation derived from 21 cm redshifts. However, there may be some Curvature-redshift present in sight lines away from the plane and especially in the Galactic halo.

Since optical redshifts have the full effects of Curvature-redshift, it should be possible to find objects with discrepant redshifts where the optical redshift is greater than the radio redshift. The difficulty is that the two types of radiation are produced in radically different environments: the optical in compact high temperature objects, such as stars, and the radio in very low-density cold clouds. In addition, there is the complication that within the galactic plane, optical extinction due to dust limits the optical range to about 1 kpc.

Curvature-redshift may help to explain an old stellar mystery. There is a long history provided by Arp (1992) of observations of anomalous redshifts in bright hot stars, which is called the K-term or K-effect.

Allen (1976) states that B₀ stars typically show an excess redshift of 5.1 ms⁻¹, A₀ have 1.4 kms⁻¹ and F₀ have 0.3 kms⁻¹. This can be explained if these stars have a large corona that produces Curvature-redshift.

It is probably no coincidence that such stars have large stellar winds and mass outflows. In order to see if it is feasible let us consider a simple model for the outflow in which the material has a constant velocity v_0 , and conservation of matter (Gauss's Law) then requires that the density has inverse square law dependence. Although this is incorrect at small stellar radii, it is a reasonable approximation further from the star.

TABLE 13
VELOCITY AT, AND AVERAGE VELOCITY WITHIN VARIOUS
PROJECTED RADII IN THE COMA CLUSTER (DISTANCE = 87.1 Mpc).

Radius ^a /Mpc	Velocity /km s ⁻¹	Mean velocity /km s ⁻¹
0.0	2327.7	2327.7
0.5	1477.7	1764.8
1.0	1033.4	1342.5
1.5	803.3	1096.9
2.0	658.6	933.2
2.5	557.0	814.4
3.0	481.0	723.3
3.5	421.7	650.7
4.0	374.0	541.2
4.5	334.8	541.2
5.0	302.0	498.7

Then if ρ_1 is the density at some inner radius r_1 , then out to a radius r_2 , the expected redshift in velocity units is

$$v = \sqrt{\frac{2G\dot{M}}{v_0}} \log\left(\frac{r_2}{r_1}\right),$$

where \dot{M} is the observed stellar mass-loss-rate. Then with \dot{M} in solar masses per year, with v and v_0 in km s⁻¹, the redshift is

$$v = 91.7 \sqrt{\frac{\dot{M}}{v_0}} \log\left(\frac{r_2}{r_1}\right) \text{ km s}^{-1},$$

With $\dot{M} = 10^{-5} M_{\odot} \text{ yr}^{-1}$ Cassinelli (1979), $v_0 = 1 \text{ km s}^{-1}$ and $r_2/r_1 = 10^3$ the predicted redshift (in velocity units) is 2 km s⁻¹ which is in reasonable agreement with the observed K-effects mentioned above.

4.17. Voids

If Curvature-cosmology is valid then the redshift of the galaxies in the Coma cluster (Section 4.4) will have been increased, on average, by the additional redshift due to the intergalactic gas. Thus, they will have, on average, a larger redshift than an isolated galaxy at the same distance.

Table 13 shows the predicted (effective) velocity for a galaxy in the center plane of the Coma cluster as a function of the projected radius. The second column is the velocity at that exact radius and the third column shows the average velocity of galaxies (uniformly spread in area) within that radius. This simulation also showed that the average velocity offset for the galaxies in the Coma cluster is 1206 kms⁻¹ which means that the redshift of the center of the Coma cluster is 6926-1206=5720 kms⁻¹. This offset is important for calculating the Hubble constant which from these figures is 5270/87.1=65.7 kms⁻¹ Mpc⁻¹.

In addition, the redshift of objects seen through a cluster will be increased by Curvature-redshift from the intergalactic gas.

Karoji, Nottale, & Vigier (1976) claim to have seen this effect. They examined radio galaxies and classified them into region A if their light does not pass through a cluster and region B if their light passes through a cluster. They found no significant differences in magnitudes between the two regions but they did find a significant

difference in the average redshift that was consistent over the complete range.

Their result is that radio galaxies seen through a cluster had an average extra redshift (in velocity units) of $2412 \pm 1327 \text{ km s}^{-1}$. Overall the difference in the distance modulus was $\mu = 0.16 \pm 0.04$, which is just significant.

Since the density and distribution of the gas in the clusters is unknown and the limiting radius of the cluster is not stated, it is impossible to get an accurate prediction.

Nevertheless, we note that for the Coma cluster with a radius of 2 Mpc the average extra redshift (from Table 13 with a factor of two) corresponds to 1866 km s^{-1} showing that Curvature-cosmology could explain the effect.

In a different study, Nottale (1976) and Nottale & Vigier (1977) compared the magnitude of the brightest galaxy in a cluster with that in another cluster with similar redshift. They found that there was no significant difference in magnitudes between clusters but that the clusters with the largest number of galaxies had the higher redshift difference between the pairs.

On average the redshift difference (in velocity units) was $292 \pm 85 \text{ km s}^{-1}$. This can be explained by the expected correlation between the number of galaxies and size and density of the intergalactic gas. However it should be noted that these observations have been disputed by Rood & Struble (1982).

In his review of voids in the distribution of galaxies, Rood (1988) quotes Mayall (1960) who observed a large void in the distribution of galaxies in front of the Coma cluster. This void has a magnitude of about 3000 km s^{-1} , which although somewhat larger, is not inconsistent with the expected value of about 1200 km s^{-1} .

In other words, the Coma cluster galaxies have an extra Curvature-redshift due to the intergalactic gas. However, the galaxies just outside the cluster nearer to us do not have this extra redshift and would appear to be closer to us. Hence, we see an apparent void in the redshift distribution in front of the Coma cluster.

A consequence of gas clouds and Curvature-redshift is that the distribution of redshifts is similar to but not identical to the distribution of z distances. Galaxies that are behind a cloud will have a higher redshift than would be expected from a simple redshift distance relationship.

Thus, we would expect to see anomalous voids and enhancements in the redshift distribution. This will be accentuated if the gas clouds have a higher than average density of galaxies.

de Lapparent et al. (1986) show a redshift plot for a region of the sky that includes the Coma cluster. Their data are from the Center for Astrophysics redshift survey and their plot clearly shows several voids. They suggest that the galaxies are distributed on the surfaces of shells. However, this distribution could also arise from the effects of Curvature-redshift in clouds of gas.

4.18. Entropy

Consider a stellar cluster or an isolated cloud of gas in which collisions are negligible or elastic. In either case the virial theorem states that the average kinetic energy K , is related to the average potential energy V , by the equation $V = V_0 - 2K$ where V_0 is the potential energy when there is zero kinetic energy. Let U be the total energy then $U = K + V = V_0 - K$. Thus, we get the

somewhat paradoxical situation that since V_0 is constant; an increase in total energy can cause a decrease in kinetic energy. This happens because the average potential energy has increased by approximately twice as much as the loss in kinetic energy. Since the temperature is proportional to (or at the least a monotonic increasing function of) the average kinetic energy, it is apparent that an increase in total energy leads to a decrease in temperature. This explains the often-quoted remark that a self-gravitationally bound gas cloud has a negative specific heat capacity. Thus, when gravity is involved the whole construct of thermodynamics and entropy needs to be reconsidered.

One of the common statements of the second law of thermodynamics is that (Longair 1991): *The energy of the universe is Constant: the entropy of the Universe tends to a maximum*, (Feynman 1965): *the entropy of the universe is always increasing* or from Wikipedia *the second law of thermodynamics is an expression of the universal law of increasing entropy, stating that the entropy of an isolated system which is not in equilibrium will tend to increase over time, approaching a maximum value at equilibrium*.

Now the normal proof of the second law considers the operation of reversible and non-reversible heat engines working between two or more heat reservoirs. If we use a self-gravitating gas cloud as a heat reservoir then we will get quite different results since the extraction of energy from it will lead to an increase in its temperature. Thus if the universe is dominated by gravity the second law of thermodynamics needs reconsideration. In addition, it should be noted that we cannot have a shield that hides gravity. To put it another way there is no adiabatic container that is beyond the influence of external gravitational fields. Thus we cannot have an isolated system.

This discussion shows that in a static finite universe dominated by gravity simple discussions of the second law of thermodynamics can be misleading. The presence of gravity means that it is impossible to have an isolated system. To be convincing any proof of the second law of thermodynamics should include the universe and its gravitational interactions in the proof.

4.19. Olber's Paradox

For Curvature-cosmology, Olber's Paradox is not a problem. Curvature-redshift is sufficient to move distant starlight out of the visible band. Visible light from distant galaxies is shifted into the infrared where it is no longer seen. Of course, with a finite universe, there is the problem of conservation of energy and why we are not saturated with very low frequency radiation produced by Curvature-redshift. These low-energy photons are eventually absorbed by the cosmic plasma. Everything is recycled. The plasma radiates energy into the microwave background radiation and into X-rays. The galaxies develop from the cosmic plasma and pass through their normal evolution. Eventually all their material is returned to the cosmic plasma.

4.20. Philips relation

Phillips (1993) Showed that there was a good correlation between the peak magnitude and the width of the

light curve for Type Ia supernova. For the Phillips relation to be meaningful, it must be between the absolute magnitude and the width corrected for its $(1+z)$ dependence. If it is intrinsic to the supernova then the final width must be product of it and the cosmological redshift factor. But as shown earlier the observed redshift can be completely explained by the cosmology. Furthermore if it intrinsic to the supernova it should be evident as a function of intrinsic wavelengths of the bands. But as shown in section 3.8, on quasars, The observed intrinsic wavelength distribution is due to cosmological effects.

The slope of the regression of the absolute magnitudes (using the Λ CDM model and the intrinsic analysis) of Type Ia supernova for all the supernova versus the widths divided by $(1+z)$ is (-0.009 ± 0.091) . Which shows that for these observations of Type I a supernova there is no significant Phillips relation.

5. PART D: CONCLUSIONS

The major numerical results for Curvature -cosmology are provided in Table 14.

Curvature-cosmology is a static tired-light cosmology which is a static solution to the equation of general relativity that is described by the Friedmann equations with an additional term that stabilizes the solution. This term called Curvature-pressure is a reaction of high-speed particles back on the material producing the curved space-time. This sense of this reaction is to try and reduce the curvature.

The basic cosmological model is one in which the cosmic plasma dominates the mass distribution and hence the curvature of space-time. In this first-order model, the gravitational effects of stars and galaxies are neglected. The geometry is that of a three-dimensional "surface" of a four-dimensional hyper-sphere, which is common to most cosmologies. Its main strengths are that it does not have ad hoc additions to the model and it has exceptionally good agreement with cosmological observations.

The only free parameter is the density of the cosmic plasma which is defined by Eq. 31, repeated here as

$$1.93 \pm 0.13 \text{ H atoms per m}^3. \quad (46)$$

The major equation is the relationship between the distance, r and the redshift z , which is defined by Eq. 10, repeated here as

$$r = R_0 \log(1+z),$$

where $R_0 = 1.008 \times 10^4 / \sqrt{N_H} = 7.256 \text{ Gpc}$.

The second equation is that for the distance modulus which is defined by Eq. 13, repeated here as

$$\mu = 5 \log_{10}[\sin(\log(1+z))] + 42.8$$

Finally the restriction that the maximum density is restricted by the Schwarzschild radius for a simple theoretical black hole in that the radius of a very compact object must be greater than $2Gm/c^2$.

A brief summary of the quantitative observations that are relevant to the Curvature-cosmology model are:

Curvature-cosmology does not need dark matter to explain the velocity dispersion in clusters of galaxies or the shape of galactic rotation curves.

For angular size the conclusion is in favor of Curvature-cosmology.

An analysis of many galaxies that have multiple observed bands show no evidence of evolution.

Curvature-cosmology predicts the observed quasar epoch variability of zero.

The Butcher-Oemler effect not valid.

Not only can Curvature-cosmology explain the anomalous Pioneer 10 acceleration, it has a feasible prediction of its value.

Fluctuations in the CMBR can be explained a density fluctuations in the cosmic plasma.

Overall for Curvature-cosmology there is remarkable agreement between its predictions and observations, without any serious problems.

AUTHOR BIOGRAPHY

David F. Crawford was born at Griffith, NSW, Australia in 1937. He graduated BSc and PhD from School of Physics, University of Sydney. Half of his PhD thesis was on designing and building a Geiger counter array to study cosmic ray air-showers and the second half on programming a three-dimensional Monte Carlo simulation on the computer Silliac to calculate the energy and structure of electron-photon cascades. The results published in a 1,512-page book "Electron-photon Shower Distribution Function" by H. Messel and D.F. Crawford, Pergamon Press, 1970.

He worked for two years from 1966 at Cornell University learning about radar Astronomy. From 1969 to his retirement in 2003, He provided computer analysis of observations from the Molonglo Radio Telescope. He is a member of the Australian Astronomical Society. He has been an author in 33 papers published in refereed journals. Since he wrote his first program in 1959, He has had a major interest in computers and programming especially in the use of computers to analyze observations and apply them to astrophysical theories. He also have a long-time interest in the foundations of cosmology.

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TABLE 14
PREDICTED AND OBSERVED RESULTS FOR CURVATURE-COSMOLOGY.

Cosmological measurement	Ref.	Predicted	Observed
Quasar energy loss	3.8	$(1+z)$	$0.80 \times (1+z)$
Cosmic temperature	2.6	2.456×10^9 K	$(2.62 \pm 0.13) \times 10^9$ K
Supernova light curve width	3.4	$1+z$	$(1.053 \pm 0.027) \times (1+z)$
Supernova absolute mag.	3.8	M	$(-22.535 \pm 0.012) - (0.075 \pm 0.054) \times z$
CMBR temperature	4.2	2.736 ± 0.092 K	(2.7255 ± 0.0006) K
Tolman surface density exponent	4.3	1	(1.38 ± 0.13)

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