# Energy conditions in advanced SRT of fourth order 

Holger Döring<br>IQ-Berlin<br>Germany<br>e-mail:haw-doering@t-online.de


#### Abstract

Discussed is the role of rest-mass and possible negative restenergy in SRT of fourth-order. Given is an action, and a Lagrangian for this case. Also the term of advanced kinetic energy and its possibility of negative form is mentioned resp. the corresponding Hamilton-function. key-words: rest-mass-changing; SRT of fourth order;Lagrangian of fourth-order; negative kinetic energy; Hamiltonian of fourth-order; negative rest-energy


## I. Changing of restenergy in SRT-theory of fourth order with analogy of damped, enforced oscillation

## 1. Introduction:

In the previous papers [2.],[8.],[9.],[10.], on advanced SRT of fourth order in analogy of damped oscillation-model the role of rest mass resp. restenergy or kinetic energy either in the advanced SRT was not really discussed. In detail, it seemed before, that restmass resp. rest-energy would be unchanged by the damping velocity factor a. But restenergy is changed either, not alone kinetic energy, it would be depend on velocity factor a of outer enforcing system what can be seen now below.
Since energy relations play an important role in many areas of physics [1.],[3.],[5.],[6.],[7.] terms of restenergy and kinetic energy of a moving particle in SRT of fourth order are developed in this paper.

## 2.Calculation:

If a linelement of local tangent Minkowski-spacetime is considered as of fourth order:

$$
\begin{equation*}
d s^{4}=\left(c d t^{2}-d x^{2}\right)^{2}+d x^{2} R^{2} \quad, \quad \text { and } \quad d s^{4}=c d t^{4} \tag{1.}
\end{equation*}
$$

R taken as a constant length, maybe Planck-length,
then there is

$$
\begin{equation*}
\mathrm{dt}^{‘}=\frac{d s}{c}=\frac{1}{c} \cdot \sqrt[4]{\left(1-\frac{v^{2}}{c^{2}}\right)^{2}+\frac{n a^{2} v^{2}}{c^{4}}} . \tag{2.}
\end{equation*}
$$

Also there is the action as:
$\mathrm{S}=-\alpha \int_{a}^{b} d s$ and with $d s=\frac{-L}{\alpha} d t$ and the Lagrangian as

$$
\begin{equation*}
\Rightarrow L=-\alpha c \cdot \sqrt[4]{\left(1-\frac{v^{2}}{c^{2}}\right)^{2}+\frac{n a^{2} v^{2}}{c^{4}}}, \tag{3.}
\end{equation*}
$$

thererefore then results for the action:

$$
\begin{equation*}
S=\int_{t_{1}}^{t} L d t \quad \Rightarrow S=-\alpha \cdot c \int_{t_{1}}^{t_{2}} \sqrt[4]{\left(1-\frac{v^{2}}{c^{2}}\right)^{2}+\frac{n a^{2} v^{2}}{c^{4}}} d t \tag{4.}
\end{equation*}
$$

$$
\begin{equation*}
\Rightarrow L=-\alpha c \cdot \sqrt[4]{\left(1-\frac{v^{2}}{c^{2}}\right)^{2}+\frac{n a^{2} v^{2}}{c^{4}}} \tag{5.}
\end{equation*}
$$

The Lagrangian of advanced lorentz-factor with damping-term-analogy is developed into a series in first order:

$$
\begin{equation*}
L=-\alpha \cdot c \cdot \sqrt[-4]{\left(1-\frac{v^{2}}{c^{2}}\right)^{2}+\frac{n a^{2} v^{2}}{c^{4}}}=-\alpha c \cdot\left(1+\frac{1}{4} \cdot\left(\frac{2 v^{2}}{c^{2}}-\frac{v^{4}}{c^{4}}-\frac{n a^{2} v^{2}}{c^{4}}\right)\right)+O(n) \tag{6a.}
\end{equation*}
$$

Then there is:

$$
\begin{equation*}
L=-\alpha \cdot c-\frac{1}{2} \cdot \frac{v^{2} \cdot \alpha}{c} \cdot\left(1-\frac{n a^{2}}{2 c^{2}}\right) \quad \text { in first order. } \tag{6b.}
\end{equation*}
$$

With valid classical term for kinetic energy $\quad E_{\text {kin }}=\frac{1}{2} \cdot m \cdot v^{2}$ there is

$$
\begin{equation*}
\alpha=\frac{-m_{0} \cdot c}{\left(1-\frac{n a^{2}}{2 c^{2}}\right)} \tag{7.}
\end{equation*}
$$

Therefore the result for rest-energy is:

$$
\begin{equation*}
E_{0}=-\alpha \cdot c=\frac{m_{0} \cdot c^{2}}{1-\frac{n a^{2}}{2 c^{2}}} \tag{8a.}
\end{equation*}
$$

This can be written also as:

$$
\begin{equation*}
E_{0}=\frac{2 m_{0} \cdot c^{4}}{2 c^{2}-n a^{2}} \tag{8b.}
\end{equation*}
$$

So, what ever the damping-factor velocity a is interpreted as, it holds the relation:

$$
\begin{equation*}
a \neq c \cdot \sqrt{\frac{2}{n}} \tag{9.}
\end{equation*}
$$

So, the advanced SRT-theory has no restriction of a singularity at $\quad v=c$ but in the dampingfactor of outer velocity a of the enforcing system.

## 3.Result:

a) For $a \equiv 0 \Rightarrow E_{0}=m_{0} \cdot c^{2}$; classical SRT
b) for $a>\sqrt{\frac{2}{n}} \cdot c$ there is $E_{0}<0$
c) for $a<\sqrt{\frac{2}{n}} \cdot c$ there is $E_{0}>0$

## 4. Conclusions:

There are the action and the Lagrangian for SRT-theory of fourth-order (damping analogy) for a free particle:

$$
\begin{equation*}
S=\frac{-m_{0} \cdot c}{1-\frac{n a^{2}}{2 c^{2}}} \cdot \int_{a}^{b} d s=\frac{-2 m_{0} \cdot c^{3}}{2 c^{2}-n a^{2}} \int_{a}^{b} d s \tag{11.}
\end{equation*}
$$

For $a \equiv 0$ this leads to classical action of a free particle in SRT:

$$
\begin{equation*}
S=-m_{0} \cdot c \int_{a}^{b} d s \tag{11a.}
\end{equation*}
$$

The Lagrange-function results to:

$$
\begin{equation*}
L=\frac{m_{0} \cdot c^{2}}{1-\frac{n a^{2}}{2 c^{2}}} \cdot \sqrt[4]{\left(1-\frac{v^{2}}{c^{2}}\right)+\frac{n v^{2} a^{2}}{c^{4}}} \tag{12.}
\end{equation*}
$$

Always $n=1$ chosen but $n \in \mathbb{N}$ possible. More evidently, $n=4$ probable (see [8.],[10.]).

For $a \equiv 0$ this leads again to classical SRT-Lagrangian for a free particle of:

$$
\begin{equation*}
L=m_{0} \cdot c^{2} \cdot \sqrt{1-\frac{v^{2}}{c^{2}}} \tag{13.}
\end{equation*}
$$

(and including inverse Feinberg-term for possible FTL-movement of classical tachyons)[4.].

## 5. Summary:

An Action and a Lagrangian can be constructed for a free particle in advanced SRT of fourth order with damping analogies of oscillation but there are restrictions in damping factor a.So the system has no singularity in v at $\quad v=c$ but in a with $a \neq \sqrt{\frac{2}{n}} \cdot c$.

## 6. Numerical data for possible experimental measurement of rest-energy:

For $c=1$; $m_{0}=1 \mathrm{~kg}$; $n=1$ there is with

$$
\begin{equation*}
E_{0}=\frac{2 \cdot m_{0} \cdot c^{4}}{2 \cdot c^{2}-a^{2}}=\frac{2 \cdot c^{2}}{2 \cdot c^{2}-a^{2}} \cdot m_{0} \cdot c^{2} \tag{8a./8b}
\end{equation*}
$$

for

$$
\begin{aligned}
& E_{0}\left(a=10^{-4}\right)=1,000000005 \cdot E_{0, S R T} \\
& E_{0}\left(a=10^{-3}\right)=1,0000005 \cdot E_{0, S R T}
\end{aligned}
$$

A term of $a=10^{-4}$ means, if a is interpreted as a rotation velocity in terms of c there has to be a rotation velocity of $\quad a=30.000 \frac{\mathrm{~m}}{\mathrm{~s}}$ to get a sigificant measurement, that is with $r=1 \mathrm{~m}$, $N=4777 \frac{1}{s}$.Other data is possible, if experimental equipment will fulfill the requirement.

Seen is in Graph 1: this effect lest restenergy increase in contrary against the proposed result of decreasing in [2.]:


Graph 1: Terms of restenergy $E_{0}$ over outer enforced velocity a for classical SRT ( green constant graph) with $a=0$ and blue curves for advanced SRT of fourth order, when $n=1$ and singularity at $a=\sqrt{2} \cdot c$ for $a \neq 0$

## II. Changing of kinetic energy in SRT-theory of fourth order with analogy of damped, enforced oscillation

## 7. Discussion of kinetic energy-term:

There is the advanced term of kinetic energy in analogy to theory of classical special relativity:

$$
\begin{equation*}
E_{k i n}=\frac{2 c^{4} m_{0}}{2 c^{2}-n a^{2}} \cdot\left(\frac{1}{\sqrt[4]{\left(1-\frac{v^{2}}{c^{2}}\right)^{2}+\frac{n a^{2} v^{2}}{c^{4}}}}-1\right) \tag{14a.}
\end{equation*}
$$

For $a \equiv 0$ the formula (14a.) goes into classical SRT-term for kinetic energy of a free particle of

$$
\begin{equation*}
E_{k i n}=m_{0} \cdot c^{2} \cdot\left(\frac{1}{\sqrt{1-\frac{v^{2}}{c^{2}}}}-1\right) \tag{14b.}
\end{equation*}
$$

The question now is:
When is this new term of kinetic energy (14 a.) positive?

Set $\quad A:=\frac{2 c^{4} m_{0}}{2 c^{2}-n a^{2}}$ and

$$
\begin{equation*}
B:=\frac{1}{\sqrt[4]{\left(1-\frac{v^{2}}{c^{2}}\right)^{2}+\frac{n a^{2} v^{2}}{c^{4}}}}-1 \tag{14c.}
\end{equation*}
$$



Graph 2: kinetic energy-term over v in classical SRT (blue curve) with $a \equiv 0$ and in advanced SRT of fourth order (red curve) for special, qualitative, elected value of $a \neq 0$ .Indeed $a=0.3$ elected.

The blue curve fit for open velocity- intervall of $v \in(-1 ; 1)$. It is plotted without the tachyon case for $v>c$ [4.].The red curve fits for every value of $v$ depending on outer velocity a of enforcing, damping system.

Then this problem is solved for conditions of:

$$
\begin{equation*}
(A>0 \wedge B>0) \vee(A<0 \wedge B<0) . \tag{15.}
\end{equation*}
$$

Below is a table (7.1.) with all solutions to this question:

### 7.1.Solutions for Conditions of positive kinetic energy in advanced SRT of fourth order:

| $A>0$ | $\begin{equation*} \frac{2 c^{4} \cdot m_{0}}{2 c^{2}-n a^{2}}>0 \tag{16а.} \end{equation*}$ <br> Since $2 c^{4} m_{0}>0$ obvious, it occurs. that $A>0$ for $a<\sqrt{\frac{2}{n}} \cdot c$ or $a>-\sqrt{\frac{2}{n}} \cdot c$. |
| :---: | :---: |
| $B>0$ | This term is solved as a result for : <br> a) $v^{2}<0 \wedge v^{2}>2 c^{2}-n a^{2}$. <br> This term fails because of $v^{2}<0$,this does mean that $v \notin \mathbb{R}$. (16 c.) <br> b) $\quad v^{2}>0 \wedge v^{2}<2 c^{2}-n a^{2}$.Herefore there are four solutions in $v$, two of them trivial, two of them restricted: <br> I $v>0$ <br> II $\quad v<0$ both trivial <br> and <br> III $v \in\left(0 ; \sqrt{2 c^{2}-n a^{2}}\right)$ <br> IV $v \in\left(-\sqrt{2 c^{2}-a^{2}} ; 0\right)$ <br> The roman third and fourth terms are open intervalls and restricted solutions for conditions of positive kinetic energy. |


| A<0 | This term is solved for $a>c \cdot \sqrt{\frac{2}{n}}$ or $a<-c \cdot \sqrt{\frac{2}{n}} \quad$ (16 e.) |
| :---: | :---: |
| $B<0$ | This term is solved as a result for : <br> a) $v^{2}<0 \wedge v^{2}<2 c^{2}-n a^{2}$. <br> This term fails because of $v^{2}<0$,this does mean that $v \notin \mathbb{R}$. <br> b) $v^{2}>0 \wedge v^{2}>2 c^{2}-n a^{2}$.Herefore there are four solutions in $v$, two of them trivial, two of them restricted: <br> I $v>0$ <br> II $v<0$ both trivial <br> and <br> III $v>\sqrt{2 c^{2}-n a^{2}}$ <br> IV $v<-\sqrt{2 c^{2} . n a^{2}}$ <br> I and III gets: $\quad v \in\left(\sqrt{2 c^{2}-n a^{2}} ; \infty\right)$ <br> II and IV gets: $\quad v \in\left(-\infty ; \sqrt{2 c^{2}-n a}\right)$ <br> I and IV not solvable in $\mathfrak{R}$ <br> II and III not solvable in $\mathfrak{R}$ <br> The roman third and fourth terms are open intervalls and restricted solutions for condition of positive kinetic energy. |

The possible measuring of this hypothetical postulated effect may be difficult because there may an overlapping by other, stronger, rotation-effects which has to be filtered out experimentally.

### 7.2.When is $E_{k i n}=0$ ?

a) For $\quad v \equiv 0 \quad$; that is obvious like in classical mechanics and in classical SRT.But there is a second zeroterm for kinetic energy in this theory-description of fourth-order here:
b) For $\quad v(a)= \pm \sqrt{2 c^{2}-n a^{2}}$ kinetic energy is zero. Restriction of defintion: $a \neq \sqrt{\frac{2}{n}} \cdot c$. With $\mathrm{a}=4$ this leads to condition of $a \neq \sqrt{\frac{1}{2}} \cdot c$.
Conclusion:
So there are two zeropoints of kinetic-energy-term. One trivial at velocity being zero but the other as a variable function of $v(a)$ where v depends on the damping velocity a of outer enforcing system.

## 8.The Hamilton-function:

It results from velocity dependent partial derivation of Lagrangian to momentum:

$$
\begin{equation*}
\frac{\partial L}{\partial v}=p \tag{17.}
\end{equation*}
$$

and

$$
\begin{equation*}
E_{G e s}^{2}-(p \cdot c)^{2}=H^{2} \tag{18.}
\end{equation*}
$$

There follows from

$$
\begin{equation*}
E_{G e s}=\frac{m_{0} \cdot c^{2}}{1-\frac{n \cdot a^{2}}{2 \cdot c^{2}} \cdot \frac{1}{\gamma}} \tag{19.}
\end{equation*}
$$

and

$$
\begin{equation*}
\mathrm{L}=\frac{m_{0} \cdot c^{2}}{1-\frac{n \cdot a^{2}}{2 c^{2}}} \cdot \gamma \quad \text { with } \quad \gamma=\sqrt[4]{\left(1-\frac{v^{2}}{c^{2}}\right)^{2}+\frac{n \cdot a^{2} \cdot v^{2}}{c 4}} \tag{20.a.b.}
\end{equation*}
$$

the momentum p to:

Therefore follows the correct Hamilton-function for the equation of movement to:

$$
\begin{equation*}
\mathrm{H}=\sqrt{\left.(p \cdot c)^{2}+\frac{m_{0}{ }^{2} \cdot c^{4}}{1-\frac{n \cdot a^{2}}{2 \cdot c^{2}} \cdot \frac{1}{\gamma} 2 \cdot\left[1-\frac{v^{2}}{c^{2}} \cdot \frac{1}{\gamma^{4}} \cdot\left[\left(1-\frac{v^{2}}{c^{2}}\right)+\frac{n \cdot a^{2}}{2 c^{2}}\right]^{2}\right]}\right]} \tag{22a.}
\end{equation*}
$$

which can be written shortened, in analogy to classical SRT-Hamiltonian if special variables are defined and established like:

$$
\begin{equation*}
\frac{1}{1-\frac{n \cdot a^{2}}{2 \cdot c^{2}}} \cdot \frac{1}{\gamma} \cdot\left[1-\frac{v^{2}}{c^{2}} \cdot \frac{1}{\gamma^{4}} \cdot\left[\left(1-\frac{v^{2}}{c^{2}}\right)+\frac{n \cdot a^{2}}{2 c^{2}}\right]^{2}\right]=k \tag{22b}
\end{equation*}
$$

Then the result is:

$$
\begin{equation*}
H=\sqrt{(p \cdot c)^{2}+k \cdot m_{0}^{2} \cdot c^{4}} \tag{22c.}
\end{equation*}
$$

For $a \equiv 0$ there is the classical limited Hamilton-function of Special Relativity Theory (SRT) with

$$
\begin{equation*}
H=\sqrt{(p \cdot c)^{2}+m_{0}^{2} \cdot c^{4}} \tag{23a.}
\end{equation*}
$$

and $k=1$.

## 9. Summary:

A Lagrange-function and a Hamilton-function can be constructed for advanced SRT of fourth order with any velocities $v$ in local inertial system of Minkowski-tangent-space as a model of damped oscillation with enforced system. The problem of negativism occurs both for rest-energy and kinetic-energy under special conditions and circumstances, depending from outer velocity a of enforcing system.

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