Living Room Model

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Abstract

By presenting the relevant, in relation to the climate problem, measured variables as exponential functions, truthfully representing the real values, surprising informative mutual relations show up. One of these relations led to the successful investigation of the possibility that the global temperature raise can not be caused by indirect heating, prescribed by the Green House model, but is caused by direct heating, prescribed by the here named Living Room Model. It is of fundamental importance to realize that sun, wind and earth energy that is transformed to energy, intended to be consumed by mankind, also directly heats the atmosphere. Besides that it has been proven that the Sea is heated by the geothermal heat flux. The final outcome therefore is that aiming for reduced CO$_2$ emissions will not result in any improvement of the climate. Only a drastically reduction of the consumed energy, of whichever kind, will help.
The importance of the enormous amount of increased heat energy in the oceans and seas, compared to that in the atmosphere, is emphasized in edition 3.
The amount of increased heat energy in the oceans and seas, created during the past centuries, is about 100 times as large as the amount of increased heat energy in the atmosphere.

Therefore, if humanity were to cease to exist overnight, it would most likely also take a few centuries to return to Earth’s original temperature.
Prologue

One of the original objections to the Greenhouse Model is the conflicting observation that it happened the last 200 years four times that the global temperature dropped while the CO₂ concentration in the atmosphere kept rising.

To support this opinion more scientifically, a special mathematical operation has been applied to the very noise-like graph of the global temperature, which filters out all that noise, but preserves the essence. The result was even a much more clear contradiction between global temperature and CO₂ concentration.

However the graph of the global temperature also shows a long-term increase, having a strong similarity with the CO₂ concentration in the atmosphere.

Eventually it has been made clearly visible that a nice sinusoidal (64-year period) change is the cause of what led originally to the conflicting observations. This yet incomprehensible periodical phenomenon has to be considered as a completely independent part of the long-term increasing global temperature.

As a result the aforementioned long-term similarity now strongly tempts the observer to consider the increasing CO₂ concentration in the atmosphere as the cause of its increasing temperature. However, a similarity/correlation does not necessarily mean a causation.

Studying the basic principle of the Greenhouse Model tells that the alleged difference between the incoming radiation from the Sun during the day and the outgoing radiation during the night has not been measured, but has only been made up in order to account for the actually measured increase of the heat energy in the Sea (all oceans and seas together).

Besides this misleading presentation it can be proven that the actually measured heat energy in the Sea, diminishing with depth, can not be caused by a top down heating as assumed in the Greenhouse Model. Such a result can only be achieved by a bottom up heating. This is emphasized by the fact that the amount of increased heat energy in the Sea is roughly 100 times as large as the increase of heat in the atmosphere.

The most obvious solution appears to be the millions of years old natural geothermal heat flow, caused by the extremely high temperature of Earth's core. This heat flow is nowadays ‘hindered’ by a temperature of the atmosphere that increased 1.5 ⁰C during the past 150 years. The heating process of the Sea by this geothermal heat flow behaves like a river flowing into a sea whose average level has clearly risen. In the estuary of the river its level has increased as much as in the sea, and then gradually decreases inland.

Based on the physical law, prescribing that all consumed energy, of whatever kind, is fully converted into heat, the idea arose that the increase of atmosphere’s temperature could, in principle, be caused by direct heating. Rather simple calculations, based the consumed energy by mankind, show that the word ‘principle’ has indeed to be changed into ‘reality’. This model got the name Living Room Model.

The theoretical research into the relationship between consumed energy and global warming, together with several fundamental objections to the Greenhouse Model, leads to the conclusion that the Greenhouse Model has to be rejected in favour of the Living Room Model.

With this model the so-called Hot Spots on Earth can perfectly be explained too.
Conclusions

1. The long-term trends of the variables: atmospheric CO₂ concentration, global temperature, world population and globally applied power by mankind, can all four truthfully be represented by the function: \( y_i = c_i + a_i \exp(t/b) \), with time constant \( b \) the same for all of them and equal to 61 years.

2. Superimposed on this trend the global temperature shows an almost perfect sinusoidal variation with a period of 64 years and an amplitude of \( 0.1 \) °C. This variation has frequently led to attempts to reject the Greenhouse Model, but it has nothing to do with global warming.

3. Having the same curvature, the mentioned variables can all simply be expressed as function of each other. For example: global temperature = \( 13.5 \) °C + \( 0.05 \cdot \) ‘globally applied power’. Such expressions may give rise to confusion as to cause and effect.

4. The just shown expression and the calculation of the heat capacity of the atmosphere has eventually lead to the evidence that the increase of atmosphere’s temperature is caused by the worldwide consumed energy, of whatever kind. The here called Living Room Model shows that the increased temperature of the atmosphere unavoidably leads to the heating of the Sea and of the land (with which the permafrost is affected) by means of the geothermal heat flux of Earth’s core.

5. The Greenhouse Model claims that the Sea is heated by the net difference between Sun’s heating radiation during day-time and Earth’s cooling radiation during night-time. But this claim has never been validated by means of measurements of these radiations. Its alleged enormous power density has been created in order to try to explain the heating of the Sea.

6. The measured increased heat energy in the Sea is roughly hundred times higher than the one in the atmosphere. Given conclusion 5, the Greenhouse Model therefore suggests that this enormous amount of energy is accumulated in the atmosphere during the day and that \( \sim 99\% \) of it will be transported to the Sea at night. Furthermore, this heat energy thus is believed to flow towards Earth’s hot centre rather than towards cold space. Completely contrary to its natural behaviour.

7. Once the above mentioned geothermal heat flux reaches the atmosphere, it will cause a rise in temperature in the upper layer of Earth’s crust, equal to the rise of the temperature of the atmosphere and obviously decrease with depth.

8. It has been proven, based on 3 different kinds of observations, that the atmosphere absorbs 10 ppm more CO₂ per °C rise of its temperature, here called the Reverse Greenhouse Effect. The existence of this phenomenon excludes the existence of the Greenhouse Effect, because the simultaneous existence would lead to an unlimited increase of both variables.

9. The so-called Vostok (Antarctica) Ice Core Records do not prove the validity of the Greenhouse Model, but of the Reverse Greenhouse Effect. The measured gradient \( \Delta CO_2/\Delta T \) is \( \sim 10 \) ppm/°C!

10. Another compelling argument against the Greenhouse Model is the creation of Hot Spots. The only way to explain this phenomenon is to apply the Living Room Model.

11. The enormous temperature difference at the surfaces of Mars and Venus doesn’t have anything to do with greenhouse effects, but is caused by the geothermal flux of these planets in combination with their mutual enormous difference in isolation to space of the respective atmospheres.

12. Given the conclusions 4 up to and including 11 the Greenhouse Model should be rejected in favour of the Living Room Model.

13. An exponential fit has been applied to the Global Mean Sea Level measurements. Extrapolation to the year 2100 shows a rise of \( \sim 30 \) cm relative to the present year, assumed that the global warming keeps rising with the same curvature, so up to an increase of \( 4 \) °C in the year 2100.
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I Mathematical expression for the CO$_2$

From here on, for simplicity’s sake, the variable “CO$_2$ concentration in the atmosphere” will be called: CO$_2$. The CO$_2$ measurements, as presented in reference [I], are called: Monthly Mean Concentrations at the Mauna Loa Observatory. For the purpose of this investigation their monthly registrations are transformed to yearly mean values. The measurements have been carried out since 1958. The units are in parts per million or ppm.

The graphs of these measurements show a very smooth tendency, hardly possessing random deviations and are therefore very suitable for applying the curve fitting $y = c + a \exp(t/b)$. See Appendix 1.2. The outcome, based on the measurements in the years 1958, 1986 and 2014, is:

$$\text{CO}_2(t) = 259.4 + 6.60 \cdot 10^{-13} \exp(t/61.06)$$

Taking $b = 61$, $c = 259$ and $a = 6.4 \cdot 10^{-13}$, learns that hardly any deviation can be found in the graph in fig. I.1. Therefore the mathematical expression for the concentration of the CO$_2$ is chosen as:

$$\text{CO}_2(t) = 259 + 6.4 \cdot 10^{-13} \exp(t/61) \text{ ppm}$$

(1)

In this function the variable $t$ is the actual year number, which explains the small value of the constant $a$. Based on the fact that the calculated curve shows an excellent fit with the measurements, it is considered justifiable to extrapolate the values back to 1850.

1850 is the year in which the recording of the global temperature, to be considered hereafter, was started.

**Figure I.1: Measured CO$_2$ since 1958 and fitted curve extrapolated back to 1850 and forward to 2050**
II  Mathematical expression for the global temperature

II.1  Definition of the global temperature

The global temperature is calculated as the average temperature, measured in a few thousand stations throughout the world. The measurements take place at a height of 1.5 to 2 meters above Earth's surface. The global temperature is therefore the temperature of the atmosphere at that height. For that reason, the heat capacity of the atmosphere is considered to be the most crucial parameter in the following assessments. From now on the variable ‘global temperature’ will be used to express the yearly mean value of the measurements.

II.2  Short-term-trend

The measurements of the global temperature had been downloaded around 2015 from a site called: National Aeronautics and Space Administration, Goddard Institute for Space Studies, showing measurements starting in 1850. However the link to that site has been removed. The new link (reference [II]) now shows measurements starting in 1880. The measurements since 1850 have been used for the fitting described below. The measurements have been fitted to an 8th and 9th order polynomial, shown in figure II.1. See Appendix 1.1 for the mathematical background. Considering the mutual rather divergent behaviour, between the 8th and 9th order curves, only during the last five years, the mean value of these two polynomials has been calculated and applied as the final high order polynomial fitting.

Over the past 10 years, the global temperature no longer significantly increased (0.03 °C), despite the ongoing increase of the CO₂ concentration, as presented above. This means that, assuming the Greenhouse theory is correct, seemingly other processes determine the global temperature too.

This conclusion is supported by the observation that during the periods 1945-1965, 1875-1905 and * - 1855 this temperature even decreased notwithstanding the always increasing CO₂ concentration. So it might even be that the Greenhouse theory is not correct, with the consequence that the CO₂ concentration in the atmosphere is not responsible for the increase of the global temperature. To investigate this in more detail a long-term-trend of the global temperature only has to be extracted.

* The question mark concerns data that started in 1834, but this data is not found at Internet anymore since about 2017.
II.3 Long-term-trend

In order to extract a pure long-term-trend of the global temperature, in first instance a 2nd order polynomial fitting has been carried out. See figure II.2. The result shows an unrealistic trend in the first four decades. To eliminate this, the curve fitting \( y = c + a \cdot \exp(t/b) \) has been applied to 3 places where the 2nd order polynomial equals the high order polynomial. That means the years 1892, 1958 and 2012.

At the same time it is investigated whether the curvature of the CO\(_2\), to read as the value of \( b \), can be used.

Figure II.2 shows the graph of the function:

\[
T_G(t) = 13.5 + 4.4 \cdot 10^{-15} \exp(t/61) \quad ^\circ C
\]  
(2)

No reason can be assigned to reject such a curvature, starting at 1890.

![Global temperature graph](image)

**Figure II.2: Global temperature, polynomial and curve fitted, as function of time**

II.3 Interesting spin-off

If in figure II.2 the (green) exponentially fitted long-term-trend curve is subtracted from the total (blue) curve, a surprising periodical curve results, except for the first period. See the blue curve in fig II.3.

If in figure II.2 the (red) second order polynomial fitted long-term-trend curve is subtracted from the total curve a more perfect sinusoidal function remains. See the red curve in fig II.3.

Both curves in figure II.3 show 2.5 periods in 160 years, resulting in 64 years per period.

The curves prove that the actual amplitude of this periodic function is most likely rather precise 0.1 \(^\circ C\).
N.B. The remarkable upwards trend during the first period of the blue curve in figure II.3 might be the reason for withdrawing the data of 1850–1880 from Internet. This data has been available until roughly 2016.

Both periodic functions in figure II.3 have been extrapolated from the year 2012 until 2100 by applying the function: $-A \sin\{\omega(t - 2012)\}$, with $\omega = \frac{2\pi}{64}$, and $A = 0.1 \, ^\circ$C.

Doing so, the global temperature increase can be predicted precisely for a long time, shown in figure II.4.
III Mathematical expression for the world population

There are several sources at the Internet informing about this subject. The world population as shown in reference [III] has been taken as the first approximation. “As a first approximation”, because the graph has such an unnatural character that it is impossible to qualify it as correct:

- an artificial nod in 1925 as well as in 1950,
- in between the two nods and from 1800 to 1925 a straight line.

In order to obtain a more credible curve, which means: as belonging to a natural process, the exponential curve \( y = c + a \exp(t/b) \) is chosen. The value of \( b \) is, in advance, taken 61.

The two artificial nods have been eliminated by using the inputs belonging to 2014 and 1914. The result is:

\[
W_p(t) = 0.47 + 3.2 \cdot 10^{14 - 14 \exp(t/61)} \text{ [billion]} \tag{3}
\]

Figure III.1 proves that this is most likely an entirely acceptable representation of reality.

![Figure III.1: The world population as function of time: the original and the most likely curve](image)

Formula (3) expresses that such a growth will lead to a world population of 29 billion in 2100!
IV Mathematical expression for the worldwide energy consumption

Global administrations of the consumption of fossil fuels has led to the graph of the annual energy consumption in the past 200 years, shown in figure IV.1. The figure has been copied from reference [IV].

![Figure IV.1 World Energy Consumption by Source, Based on Vaclav Smil estimates from Energy Transitions](image)

The graph shows “humps” and “dents” conflicting with the streamlined graph of the measured and backwards extrapolated CO₂ concentration in the atmosphere, shown in chapter I. For this reason this graph has also been streamlined by means of exponential curve-fitting.

The data has first been converted to a stylized graph and at the same time to TeraWatt (TW), applying the relation: 1 Exajoule/year = $10^{18}/(3600\cdot24\cdot365)$ W = 0.0317 TW. See the blue curve in figure IV.2.

The years 2010 and 1810 have been taken as references for the curve fitting. The time constant (b) is, in advance, taken 61 year. The result is: $P_G(t) = -0.06 + 8.4\cdot10^{-14}\cdot\exp(t/61)$. The value -0.06 is not realistic, but small enough to be ignored. So the globally applied power, expressed in TW, will be written as:

$$P_G(t) = 8.4\cdot10^{-14}\cdot\exp(t/61) \ \text{TW} \quad (4)$$

Figure IV.2 shows the related graphs and also that, without compromising credibility, the curvature of the applied power graph may be chosen as 61. The legitimate question namely is how reliable these registrations were until the discovery of the climate problem!

![Figure IV.2. Worldwide power usage from 1810 to 2050](image)
V Consideration of cause and effect

It has been shown in the previous chapters that the four variables: CO₂ concentration, global temperature, world population and globally applied power, can all reasonably be expressed as function of time by an exponential function with time constant 61 years:

\[
\text{CO}_2 \text{ concentration (ppm)} \quad \text{CO}_2(t) = 259 + 6.4\times10^{13}\exp(t/61) \quad (1)
\]

\[
\text{Global temperature (°C)} \quad T_G(t) = 13.5 + 4.4\times10^{15}\exp(t/61) \quad (2)
\]

\[
\text{World population (billion)} \quad W_p(t) = 0.5 + 3.2\times10^{14}\exp(t/61) \quad (3)
\]

\[
\text{Globally applied power (TW)} \quad P_G(t) = 8.4\times10^{14}\exp(t/61) \quad (4)
\]

The mutual relations between these variables can be deduced as shown below by means of the example, showing the Greenhouse model.

\[
\text{CO}_2(t) - 259 = 6.4\times10^{13}\exp(t/61)
\]

\[
T_G(t) - 13.5 = 4.4\times10^{15}\exp(t/61)
\]

so

\[
\{T_G(t) - 13.5\} / \{\text{CO}_2(t) - 259\} = 4.4\times10^{15} / 6.4\times10^{13} = 7\times10^{-3} \text{ resulting in:}
\]

\[
\text{global temperature} = 13.5 + 0.007\times(\text{CO}_2 - 259)
\]

This expression written inversely shows:

\[
\text{CO}_2 = 259 + 145\times(\text{global temperature} - 13.5)
\]

In the first expression the CO₂ is meant as the cause and the temperature as the effect, while the second one suggests the opposite. So the interpretation of such relationships requires a careful consideration.

For example, might it be that the world population is directly responsible for the global warming, given the relation

\[
\text{global temperature} = 13.5 + 0.14\times(\text{population} - 0.5)
\]

Or is that population indirectly responsible, via its energy consumption:

\[
\text{global temperature} = 13.5 + 0.05\times\text{Globally applied power}
\]

In chapter VII it will be shown that and why the Greenhouse Model is untenable. One of the reasons is that this model assumes a top down heating until great depth of the Sea. The word “Sea” is used to express all the oceans and seas together. In order to explain that such a process is physically impossible, it is firstly necessary to investigate this heating. See the next chapter.

After having proven that the Greenhouse Model is untenable it will be proven in chapter VIII that the global warming is the result of the globally applied power by mankind, referred to with the name Living Room Model. Its density, in terms of Watt/m², is much lower than the alleged density of the Greenhouse Model. That is to say: this alleged density has never been measured but adapted to the density necessary to heat the Sea top down. It will be shown that an unexpected source is responsible for the heating of the Sea, bottom up.

Finally: the so-called phenomenon Hot Spot can not be explained by the Greenhouse Model. In the last section of chapter VIII it will be shown that the Living Room Model perfectly explains this phenomenon.
VI Investigation of the increased Sea heat energy

Two sources have been investigated in order to find reliable information about the amount of the increased heat energy in the Sea (all oceans and seas together). Figure VI.1 is a copy of figure 6 from reference [VI.1]. Figure VI.2 is a copy of page 10 from reference [VI.2].

![Graph showing energy content from 1960 to 2015](image)

*Figure VI.1 “Improved estimates of Sea heat content from 1960 to 2015”*

![Graph showing rate of heat storage](image)

*Figure VI.2 “Rate of heat storage has increased, with significant storage in deep ocean”*

The two figures show a remarkable discrepancy. In figure VI.1 hardly any increase has been measured in the year 1960, where figure VI.2 presents a significant increase. Given the fact that the global warming started about 150 years ago, figure VI.2 gives a more reliable impression. However it only shows relative numbers.

Given the fact that all relevant variables in the global warming process up to this moment can be well represented as exponential functions, all with the same time constant of 61 years, such a curve has been chosen to fit the increased heat energy between 1870 and 2015, assuming that the absolute value in 2015 in figure VI.1 is correct. The result in first instance is: $\Delta E_S(t) = 1.6 \times 10^9 \cdot \exp(t/61)$ Joule.
In order to check this assumption Table VI.1 has been calculated. This table shows the results for each layer in the year 2015, deduced from figure VI.1. The applied variables per layer are defined as follows:
\[
\Delta \text{temp} \quad : \text{measured energy} \cdot \text{volume} \cdot \Delta C_{\text{heat}} \\
C_{\text{heat}} \quad : \text{specific heat capacity of water, put on } 4 \cdot 10^6 \\
\Delta V \quad : \text{volume only caused by the expansion of the water: } \Delta \text{temp} \cdot \text{volume} \cdot c_e \\
c_e \quad : \text{volume expansion coefficient of water, put on } 0.00021 \\
\Delta \text{height} \quad : \text{Sea level rise only due to the expansion} \ 100 \cdot \frac{\Delta V}{S_e} \\
S_e \quad : \text{total Sea surface, put on } 3.6 \cdot 10^{14} \\
\]

The total of \(\Delta \text{temp}\) is the temperature increase at the surface of the Sea in mK.

<table>
<thead>
<tr>
<th>layer (m)</th>
<th>thickness (m)</th>
<th>volume (m(^3))</th>
<th>(\Delta)energy (J)</th>
<th>(\Delta)temp. (mK)</th>
<th>(\Delta V) (m(^3))</th>
<th>(\Delta)height (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0-300</td>
<td>300</td>
<td>(1.1 \cdot 10^{17})</td>
<td>(1.3 \cdot 10^{23})</td>
<td>303</td>
<td>(6.8 \cdot 10^{12})</td>
<td>1,9</td>
</tr>
<tr>
<td>300-700</td>
<td>400</td>
<td>(1.4 \cdot 10^{17})</td>
<td>(7.0 \cdot 10^{22})</td>
<td>123</td>
<td>(3.7 \cdot 10^{12})</td>
<td>1,0</td>
</tr>
<tr>
<td>700-2000</td>
<td>1300</td>
<td>(4.6 \cdot 10^{17})</td>
<td>(1.0 \cdot 10^{23})</td>
<td>54</td>
<td>(5.3 \cdot 10^{12})</td>
<td>1,5</td>
</tr>
<tr>
<td>2000-3700</td>
<td>1700</td>
<td>(6.1 \cdot 10^{17})</td>
<td>(2.0 \cdot 10^{22})</td>
<td>8</td>
<td>(1.1 \cdot 10^{12})</td>
<td>0,3</td>
</tr>
<tr>
<td><strong>totals</strong></td>
<td><strong>3700</strong></td>
<td><strong>(1.3 \cdot 10^{18})</strong></td>
<td><strong>(3.2 \cdot 10^{23})</strong></td>
<td><strong>488</strong></td>
<td><strong>(1.7 \cdot 10^{13})</strong></td>
<td><strong>4,7</strong></td>
</tr>
</tbody>
</table>

Table VI.1 deduced from figure VI.1 for the year 2015

The remarkable result is that the temperature increase of 488 mK is half the measured temperature increase of the atmosphere in the year 2015. This observation has to lead to the conclusion that the measured energy increase in all the layers is a factor 2 too low. The final result regarding the mathematical expression for \(\Delta E_{\text{at}}(t)\) after 1870 thus is:

\[
\Delta E_{\text{at}}(t) = 3.2 \cdot 10^9 \cdot \exp(t/61) \quad \text{J} \tag{5}
\]

The heat content of the Sea is measured by measuring the temperature in various places in the Sea as function of depth. The crucial question thus is how reliable these measurements have been carried out. Measuring the temperature at great depths requires very special and very accurately calibrated equipment. This consideration also shows that the smaller the temperature rise, not only as a function of depth, but especially in earlier years, the worse the relative accuracy must have been.

The calculation of the temperature increase in Table VI.1 is a rather rough one, given the fact that in reality most likely this temperature change, as function of depth, will much more look like an exponential function, with a yet unknown depth-constant \(c_d\), like: \(\Delta T(d) = \Delta T_{\text{atm}} \cdot \exp(-d/c_d)\), with \(\Delta T_{\text{atm}}\) the increase of the temperature of the atmosphere.

The expression: \(\Delta E_{\text{total}} = C_{\text{heat}} \cdot S_e \cdot \int_0^\infty \Delta T(d)\Delta d\) represents the total increase of heat energy in the Sea. The boundary \(\infty\) has to be read as the bottom of the Sea. The product \(S_e \cdot \Delta d\) is the value of the volume of the layer of water with thickness \(\Delta d\). So \(\Delta E_{\text{total}} = \Delta T_{\text{atm}} \cdot 4 \cdot 10^6 \cdot 3.6 \cdot 10^{14} \cdot c_d\) J.

For \(\Delta E_{\text{total}} = 6.4 \cdot 10^{23}\) J and \(\Delta T_{\text{atm}} = 1\) K, \(c_d = 444\) m.

This result now also offers the possibility to calculate the expansion of the Sea, in terms of its level rise, more accurately by: \(\Delta h = c_e \cdot \int_0^\infty \Delta T(d)\Delta d = 1 \cdot c_e \cdot c_d = 9.3 \text{ cm in the year 2015}\).

Given the value of the total \(\Delta h\) in Table VI.1 and the applied correction by a factor 2 to the measured heat energy in the Sea in the references [VI.1] and [VI.2], the outcome \(\Delta h = 9.3\) cm creates confidence in the just applied philosophy and calculations.

This outcome will be used in chapter X: “Global Mean Sea Level until 2100”.
VII Why the Greenhouse Model is untenable

VII.1 Introduction

In this chapter it will be proven in 6 sections why the Greenhouse Model is untenable. These sections are:

VII.2 Principle of the GHM
VII.3 A closer look at spectra
VII.4 A closer look at the heat fluxes of the GHM
VII.5 The heating of the Sea in the GHM
VII.6 The GHM applied on Mars and Venus
VII.7 The Reverse Greenhouse Effect

The Reverse Greenhouse Effect expresses that the higher the temperature of the atmosphere the more it absorbs CO$_2$ at the cost of the absorption by Earth’s surface, given a certain amount of emission. If the Reverse and the normal Greenhouse Effect would exist together, a positive feedback loop would have been created, leading to an unlimited increasing global temperature.

VII.2 Principle of the GHM

It is beyond dispute that half of the Earth is heated during the day and that, at the same time, the other half gives off the previously absorbed heat during the night. That release is eventually done to the universe through radiation. According to the GHM, cooling is more impeded by the atmosphere the more it contains greenhouse gases. The defence that these greenhouse gases should therefore hinder the much stronger incoming solar radiation too and thus cool the Earth is refuted by the following alleged reasoning put forward by the GHM supporters.

The incoming radiation has a shorter wavelength than the cooling one. According to the GHM, this short-wave radiation is not blocked by the greenhouse gases, while the long-wave radiation is. The spectrum of the solar radiation is maximum at a wavelength of \(~ 600 \text{ nm}\). According to the GHM, the spectrum of the cooling radiation lies at a wavelength of \(~ 20000 \text{ nm}\).

N.B. It is not mentioned that the cooling starts primarily with convection through the atmosphere, to eventually be completed as radiation from the exosphere.

VII.3 A closer look at spectra

Originally the idea, based on the above-described principle of the GHM, was that a thorough theoretical investigation of the spectrum of the radiation during cooling is essential. After this investigation was completed, it appeared to play no role. The result of the investigation is considered noteworthy. In brief:

The cooling hemisphere of the Earth will be regarded as a black radiator, with a temperature at the surface of 525 K (250 °C). The note on that surface is that the associated so-called exosphere is so thin that it borders on vacuum. By definition vacuum has no temperature. But only 1 molecule in any volume does! The temperature of that exosphere is very high indeed. The maximum of the spectrum of its radiation is, at a temperature of 250 °C, at a wavelength of \(~ 10000 \text{ nm}\). So not at the 20000 nm, as alleged by the GHM. The temperature of a black radiator with the maximum at a wavelength of 20000 nm is -20 °C!

VII.4 A closer look at the heat fluxes of the GHM

“Heat flux” stands for: “heat power per surface unit” and is therefore expressed in W/m$^2$.

The GHM focuses on heat fluxes, mainly in the form of radiation, which are intended to indicate the heating and cooling of the Earth. All this is done by means of figure VII.1, copied from reference [VII.1], intended to provide insight. The yellow fluxes represent the heating and the red, upward, the cooling. The downward directed red ones, referred to as radiation from greenhouse gases, are thought to determine the heating of both the atmosphere and the Sea. The “net absorbed” flux is claimed to be 0.6 W/m$^2$ in 2010.
However, in no way whatsoever it can be found that this alleged net absorbed flux should be 0.6 W/m$^2$. Further study of reference [VII.1] also offers no guidance. It is therefore unbelievable that this small difference could have been derived from the much larger fluxes, with an accuracy that also suggests to be significant smaller than 0.1 W/m$^2$.

Reference [VII.1] reports under the chapter “Climate Forcings and Global Warming”:

“The absorption of outgoing thermal infrared by carbon dioxide means that the Earth is still absorbing about 70 percent of the incoming solar energy, but an equivalent amount of heat is not emitted again. The exact amount of energy imbalance is very difficult to measure, but turns out to be slightly more than 0.8 watts per square meter. The imbalance is derived from a combination of measurements, including… observations of sea level rise and warming.”

In the next section it is made plausible that the last sentence should almost certainly have read: The imbalance is only deduced from the measured increased temperature of the Sea, transformed to warmth.

Reference [VII.2] is also particularly unconvincing given the fact that measurements of “thermal infrared radiation emitted to space” cannot distinguish between radiation as a result of the alleged greenhouse effect and radiation from heat generated by human energy consumption.

VII.5 The heating of the Sea in the GHM

According to the GHM the Sea is heated top down to great depth, gradually decreasing to zero, while simultaneously the atmosphere is heated too. In the previous section it is shown that the alleged related “net absorbed” heat flux/power density is presented as 0.6 W/m$^2$ in 2010, “based on the average values over the past 10 years”. Such a calculation cannot lead to a power density in just the year 2010. It would result in the mean value of the power densities over these 10 years and thus nothing tell about the temperature increase of the Sea in 2010.
Given the investigations in chapter VI such a power density can be calculated by firstly differentiating equation (5) : \( \Delta E_S(t) = 3.2 \cdot 10^9 \cdot \exp(t/61) \), leading to \( P_S(t) = 3.2 \cdot 10^9 / 61 \cdot \exp(t/61) \) J/year, resulting in 1.65 \( \cdot \exp(t/61) \) Watt after dividing it by the number of seconds per year (3.15\( \times \)10\(^7\)). This power can be converted to power density through dividing by the Sea surface of 3.6\( \times \)10\(^{14}\) m\(^2\). The final result is found to be: \( PD_S(t) = 4.6 \cdot 10^{-15} \cdot \exp(t/61) \) W/m\(^2\), being 0.9 W/m\(^2\) in the year 2010.

It thus has to be concluded that the following two mistakes have been made in the presentation of the power density in 2010 in figure VII.1. In the first place not the increased heat energy in this year has been taken, but the mean value over the past 10 years. In the second place it has not been shown which information about increased energy levels in the Sea has been used. And if the values of figure VI.1 would have been used, the outcome would have been, right at the start already, a factor 2 too low, as has been proven in chapter VI.

But the most remarkable and fundamental argument against the validity of the GHM is the observation that the total heat energy absorbed by the Sea until 2015 is roughly 100 times larger than the energy absorbed by the atmosphere in that period: 6.4\( \times \)10\(^{23}\) J versus 5\( \times \)10\(^{21}\) J. The last-mentioned energy follows from the heat capacity of the atmosphere, calculated in Appendix 2, multiplied by 1 K, measured in 2015.

If the GHM would be the correct model for the heating of the atmosphere as well as of the Sea then half of Earth’s atmosphere would, each day, be heated by an enormous amount of energy. This would lead to an increase in temperature, in first instance, by at least 5 mK/day. For comparison: the actual increase is nowadays 0.04 mK/day. In addition to this striking big discrepancy this heat is, according to the GHM, supposed to flow, opposite to its natural direction, towards the high temperature in Earth’s centre instead of towards the low temperature in space. The GHM namely assumes that the transport of this enormous heat towards space is for \(~\)99% blocked by a very low concentration of CO\(_2\) in the atmosphere: < 0.4 \%.

The argument in favour of the GHM, put forward by Ocean Specialists, is that the Sea does not stand still, meaning that it has a three dimensional circulation that takes heat from the surface into the subsurface layers, for example caused by: storms mixing the upper 100 m, large-scale winds that drive Sea currents filling Sea basins to depths greater than 1000 m, equatorial waters flowing in the direction of the poles and tidal currents. This phenomenon has got the name “thermohaline circulation”.

But still the net stream would be opposite to its natural direction and should therefore be rejected as cause of the heating of the Sea, top down!

It will be shown in section VIII.5 that most likely the so-called geothermal heat flux, instead of the alleged heat flux resulting from the GHM, is responsible for the heating of the Sea, bottom up!

Because this warming starts at great depths and the water thus heated wants to rise, it might be that the thermohaline circulation is caused by this heat flow in combination with the tide movements.

**VII.6 The GHM applied on Mars and Venus**

The surface temperature on Mars is -63 °C, its atmosphere has a pressure of 0.01 atm. These values at Venus are 500 °C, respectively 100 atm. The atmosphere of both planets consists of 96% CO\(_2\). It is generally believed that, due to the CO\(_2\) in the atmosphere, Earth’s temperature increase is expressed by \( \Delta T_E = 0.007 \cdot \Delta CO_2 \) (ppm). See Chapter V. To convert this expression to the situation on Mars the gradient 0.007 must first be reduced by 2.3 due to the larger distance from the Sun. Secondly be multiplied by 100, due to the fact that the heat capacity of Mars’ atmosphere is 100 times smaller.

At a CO\(_2\) concentration of almost 1 million ppm, a temperature increase of 300 thousand °C should thus be observed on Mars. Applying this method to Venus results in a temperature increase of 135°C. The result for Mars is absurd enough to reject such a transformation, or to reject the Greenhouse Model.

What has been overlooked is the role of the geothermal flux on the planets, which originates in their core. As on Earth, these cores radiate their energy into space through the atmosphere, which on Mars means that this radiation is hardly hindered by its atmosphere, while on Venus the isolation of this layer is about 10 thousand times higher. This phenomenon simply explains the observed large temperature difference at the surfaces of these planets and makes the just mentioned choice easy: the GHM has to be rejected.
VII.7 The Reverse Greenhouse Effect

A detailed study of the CO$_2$ concentration in the atmosphere as a result of the CO$_2$ emission eventually learns that the CO$_2$ concentration increases with the temperature of the atmosphere. This phenomenon has been given the name Reverse Greenhouse Effect. This effect would have a disastrous effect on the global warming, because together with the Greenhouse effect it would create a process with a positive feedback, leading to an unlimited increase of the temperature of the atmosphere.

VII.7.1 CO$_2$ emission factor in terms of Gigaton/consumed energy

CO$_2$ emissions, as a result of the combustion of fossil fuels, are for example expressed in terms of the number of tons of CO$_2$ per released amount of energy in Terajoule. This emission factor depends on the type of fossil fuel. Reference [VII.3] shows the following CO$_2$ emission factors, together with the here added transformation factor: ‘Gigaton CO$_2$/TWyear’.

<table>
<thead>
<tr>
<th></th>
<th>ton CO$_2$/TeraJ</th>
<th>Gt CO$_2$/TWyear</th>
</tr>
</thead>
<tbody>
<tr>
<td>gas</td>
<td>55</td>
<td>1.7</td>
</tr>
<tr>
<td>oil</td>
<td>74</td>
<td>2.3</td>
</tr>
<tr>
<td>coal</td>
<td>100</td>
<td>3.2</td>
</tr>
</tbody>
</table>

*Table VII.1*

The relative distribution of the consumed energy in the years 2010, 1910 and 1810 of these fuels is shown in table VII.2 on the left side. The emission factor of biofuel/biomass is taken the same as of coal. The contributions of Nuclear and Hydro-elect energies (both 5%) to the CO$_2$ emissions are left away. The column in the middle shows the related emission factor from Table VII.1. The right side of Table VII.2 shows the left side, after multiplication with the middle column.

<table>
<thead>
<tr>
<th></th>
<th>2010</th>
<th>1910</th>
<th>1810</th>
<th>X</th>
<th>2010</th>
<th>1910</th>
<th>1810</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gas</td>
<td>0.2</td>
<td>0</td>
<td>0</td>
<td>1.7</td>
<td>0.4</td>
<td>0.0</td>
<td>0.0</td>
</tr>
<tr>
<td>Oil</td>
<td>0.31</td>
<td>0.3</td>
<td>0</td>
<td>2.3</td>
<td>0.7</td>
<td>0.0</td>
<td>0.0</td>
</tr>
<tr>
<td>Coal+ Biomass</td>
<td>0.39</td>
<td>1</td>
<td>1</td>
<td>3.2</td>
<td>3.2</td>
<td>3.2</td>
<td>3.2</td>
</tr>
<tr>
<td>sum</td>
<td>2.3</td>
<td>3.2</td>
<td>2.3</td>
<td>3.2</td>
<td>2.3</td>
<td>2.3</td>
<td>2.3</td>
</tr>
</tbody>
</table>

*Table VII.2*

In the next section this ‘sum’, being the weighed average emission factor, will be applied in the years 1850 – 2050 in steps of 20 year. The values for the years since 1910 are found by linear interpolation between the values at 1910 and 2010. The values for 2030 and 2050 are taken the same as for 2010 is.

<table>
<thead>
<tr>
<th></th>
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<th></th>
<th></th>
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<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>emission factor</td>
<td>3.2</td>
<td>3.2</td>
<td>3.2</td>
<td>3.2</td>
<td>3.0</td>
<td>2.8</td>
<td>2.7</td>
<td>2.5</td>
<td>2.3</td>
<td>2.3</td>
<td>2.3</td>
</tr>
</tbody>
</table>

*Table VII.3 Emission factor in Gt/TWyear*

VII.7.2 CO$_2$ concentration expressed in Gigaton

The CO$_2$ concentration in the atmosphere is normally expressed in ppm, that is to say, the amount of CO$_2$ in relation to the amount of molecules in the atmosphere, both expressed in mol.

The total mass of air in the atmosphere is 5.3·10$^{18}$ kg. Given the definition of ppm, this mass has to be converted to the unit mol, defined as the mass of N$_A$ atoms/molecules of that substance. N$_A$ is the number/constant of Avogadro (6·10$^{23}$ mol$^{-1}$). The mean molar mass of air is 29 kg/kmol, so the amount of ‘mean’ air molecules in the atmosphere is 5.3·10$^{18}$/29 = 1.8·10$^{17}$ kmol.
The worldwide mean concentration of 400 ppm CO₂ in the atmosphere in the year 2018 thus represents 400·10^6 · 1.8·10^{17} = 7.3·10^{13} kmol CO₂. The molar mass of CO₂ is 44 kg/kmol, so the mass of 400 ppm CO₂ in the atmosphere is 44·7.3·10^{13} = 3.2·10^{13} kg = 3200 Gigaton (Gt).

The conversion from ppm CO₂ to absorbed Gt CO₂ in the atmosphere thus is 3200/400 = 8 Gt/ppm.

This factor has been used calculating ΔCO₂/CO₂e from ΔCO₂R/CO₂e in table VII.4

<table>
<thead>
<tr>
<th>year</th>
<th>CO₂ (ppm)</th>
<th>ΔCO₂R (ppm/year)</th>
<th>ΔCO₂R (Gt/year)</th>
<th>Power (TW)</th>
<th>E factor (Gt/TW/year)</th>
<th>CO₂e (Gt/year)</th>
<th>ΔCO₂R/ΔCO₂e (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1850</td>
<td>269</td>
<td>0,15</td>
<td>1,2</td>
<td>1,2</td>
<td>3,2</td>
<td>4,0</td>
<td>2,7</td>
</tr>
<tr>
<td>1870</td>
<td>273</td>
<td>0,22</td>
<td>1,7</td>
<td>1,7</td>
<td>3,2</td>
<td>5,5</td>
<td>3,8</td>
</tr>
<tr>
<td>1890</td>
<td>278</td>
<td>0,30</td>
<td>2,4</td>
<td>2,4</td>
<td>3,2</td>
<td>7,7</td>
<td>5,3</td>
</tr>
<tr>
<td>1910</td>
<td>285</td>
<td>0,4</td>
<td>3,3</td>
<td>3,3</td>
<td>3,2</td>
<td>10,6</td>
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<tr>
<td>1930</td>
<td>295</td>
<td>0,6</td>
<td>4,6</td>
<td>4,6</td>
<td>3,0</td>
<td>13,9</td>
<td>9,3</td>
</tr>
<tr>
<td>1950</td>
<td>308</td>
<td>0,8</td>
<td>6,4</td>
<td>6,4</td>
<td>2,8</td>
<td>18,2</td>
<td>12</td>
</tr>
<tr>
<td>1970</td>
<td>327</td>
<td>1,1</td>
<td>8,9</td>
<td>8,9</td>
<td>2,7</td>
<td>23,7</td>
<td>15</td>
</tr>
<tr>
<td>1990</td>
<td>353</td>
<td>1,5</td>
<td>12</td>
<td>12</td>
<td>2,5</td>
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<td>390</td>
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<td>17</td>
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<td>39</td>
<td>22</td>
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<td>2030</td>
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<td>3,0</td>
<td>24</td>
<td>24</td>
<td>2,3</td>
<td>55</td>
<td>31</td>
</tr>
<tr>
<td>2050</td>
<td>510</td>
<td>4,1</td>
<td>33</td>
<td>33</td>
<td>2,3</td>
<td>76</td>
<td>43</td>
</tr>
</tbody>
</table>

*Check of the column ‘ΔCO₂A’.

Digital integration of the column ‘ΔCO₂A’ by taking 20 times the value of each year, up to and including the year 1990, plus 8 times the value of 2010 in order to find the result for the period 1850 - 2018, shows 953 Gigaton. This result has to be compared with the difference between the CO₂ concentration in 2018 (400 ppm) and in 1850, multiplied by 8 Gt/ppm. That outcome is 1048 Gigaton. The 10% difference is caused by the large integration step of 20 years.

†Remark:
In first instance the columns ‘ΔCO₂A’ and ‘Power’ show surprisingly exactly the same numbers. The background is as follows. ‘ΔCO₂A’ is calculated as the derivative of CO₂(t) = 259 + 6.4·10^{13}·exp(t/61), shown as equation (1) in chapter I, times 8 Gt/ppm, resulting in: 8.4·10^{14}·exp(t/61) ppm/year.

The variable ‘Power’ is fitted by P(t) = 8.4·10^{14}·exp(t/61) TW, shown as equation (4) in chapter IV.

The importance of the variable ‘ΔCO₂A/CO₂e’ will be considered in the next section.
VII.7.3 Short term evidence for the existence of the Reverse Greenhouse effect

Table VII.4 in the previous section shows that most of the CO₂ emission is absorbed by Earth’s surface. It also shows that the absorption increases with time from roughly a 30–70 to a 40–60% distribution. During that same period the temperature of the atmosphere increased 1°C.

Given this phenomenon the following hypothesis is posited: the measured increase of the CO₂ concentration in the atmosphere is only caused by the increase of its temperature. A Reverse Greenhouse Effect.

If this hypothesis would be valid then the gradient of the growth of the CO₂ concentration in the atmosphere, as function of atmosphere’s temperature, would be 145 ppm/°C, as shown in chapter V.

In chapter II it has been found that the temperature of the atmosphere changes, on top of the long-term-trend, with \(-0.1\sin\{\omega(t – 2012)\}\) (°C), in which \(\omega\) represents a period of 64 years. Chapter I shows the CO₂ measurements during the period 1958-2018. These 60 years form a just long enough period to investigate the relation between atmosphere’s CO₂ concentration and temperature in more detail.

Figure VII.2 shows the measured CO₂ minus the exponential fitted curve +0.5, indicated as “measured”. The “+0.5” is applied in order to make the curve symmetrical around zero, just like the, to investigate, sinusoidal CO₂ curve is. This curve has been drawn with two amplitudes, indicated as “theoretical CO₂ 1.5 ppm” resp. as “theoretical CO₂ 1.0 ppm”. Comparison with the measured curves leads to the conclusion that the hypothesis has to be rejected, because the amplitude should have been 0.1 times 145, say 15 ppm. But still it clearly shows an influence of atmosphere’s temperature on its CO₂ concentration.

A partially Reversed Greenhouse Effect has been demonstrated, with a gradient of 10 to 15 ppm/°C.

The word ‘partially’ has to be understood as: only about 10% of the total increase of the atmospheric CO₂ concentration is caused by the atmospheric temperature increase. The other 90% is caused by emission.

Another way of presenting the correlation between “measured CO₂” and “theoretical CO₂” is to fit a high order polynomial curve to the differences between the measured CO₂ data and the exponential fitting of this data, as shown in chapter I. Taking a 8th order fitting of these deviations the result is as shown in figure VII.3. The resemblance is fundamentally the same as shown in figure VII.2.
Figure VII.3 shows that there is in the same period of 60 years a rather high resemblance between the patterns of the random \( \text{CO}_2 \) and random temperature deviations. To investigate this, the derivative in each year has been calculated for both variables. The quotient of these derivatives has been calculated in case they are both positive and in case they are both negative. This turned out to happen in 32 of the 55 years. Such a result is from a statistical point of view not convincing. But their mean value is \( \sim 10 \text{ ppm/}^{\circ}\text{C} \), showing a remarkable good agreement with the range 10 - 15 ppm/\( ^{\circ}\text{C} \), found in the sinusoidal curve.

Figure VII.4 Yearly random deviations of global temperature and atmospheric \( \text{CO}_2 \) concentration
VII.7.4 Long term evidence for the existence of the Reverse Greenhouse effect

Figure VII.5 shows very long term historical relations between CO$_2$ and global temperature. This figure has been deduced from the original article, ref. [VII.4]. The abstract sounds:

“The recent completion of drilling at Vostok station in East Antarctica has allowed the extension of the ice record of atmospheric composition and climate to the past four glacial–interglacial cycles. The succession of changes through each climate cycle and termination was similar, and atmospheric and climate properties oscillated between stable bounds. Interglacial periods differed in temporal evolution and duration. Atmospheric concentrations of carbon dioxide and methane correlate well with Antarctic air temperature throughout the record. Present-day atmospheric burdens of these two important greenhouse gases seem to have been unprecedented during the past 420,000 years.”

Figure VII.5 420000 years of global temperature and atmospheric CO$_2$ concentration

From the point of view of the Reverse Greenhouse Effect it is interesting to deduce, just like it is done in figure VII.4, the ratio: $\Delta$CO$_2$(t)/$\Delta$T(t). Given the uniformity between the two curves in Figure VII.5, only one sample is already representative for the whole period. This sample is taken at the steep change in the middle of the graph, where $\Delta$CO$_2$/$\Delta$T $\sim$ 80/8 = 10 ppm/$^\circ$C, being in remarkable good agreement with the gradient 10-15 ppm/$^\circ$C of the Reverse Greenhouse Effect and thus not at all in agreement with the greenhouse effect. So the temperature variations over the past 420000 years have not been caused by CO$_2$ variations, but vice versa. What has been proven with the Vostok study is the validity of the Reverse Greenhouse Effect (RGHE), instead of the Greenhouse Effect.

Around the year 0 (present time) a very long and steep curve upwards of the CO$_2$ concentration is drawn, in conformity with reality, however without a clearly visible increase of the temperature. That confirms the presentation of the present process, indeed being very different from the historical processes.

The consequence of the existence of the RGHE is that the Greenhouse Model must be declared non-existent, because if they would exist together, an increase in atmospheric temperature would cause an increase in the atmospheric CO$_2$ concentration, which in turn would lead to an increase in atmospheric temperature. Definitely an unstable process, in this situation not disastrous, because the gradient of the RGHE is 10 times smaller than the reciprocal value of the Greenhouse gradient (145 ppm/$^\circ$C).

*The figure exactly as shown here seems not to be available anymore on Internet after about 5 years!
VIII Living Room Model

VIII.1 Introduction

Imagine a living room occupied by a lot of people being very busy with whatever. The more people and/or the more hustle and bustle, the higher the temperature in that living room rises, assuming no external influences. This situation perfectly resembles the Earth's atmosphere in which many people consume a lot of energy of any kind.

The thermodynamic law of conservation of energy forces us to conclude that all energy consumed worldwide, of whatever nature, such as solar, wind and nuclear energy, is eventually converted into heat. Also when basic energy is converted into kinetic energy, such as with propulsion. This kinetic energy is inevitably converted into heat by friction with the medium in and on which the propulsion takes place, and by the friction in the machine itself. If the propulsion also results in an increase in the potential energy of the vehicle, as in the case of an airplane, or a car driving up a mountain, this potential energy is still converted into heat as soon as the vehicle returns to its original height.

By converting solar energy into electrical energy, that part is eventually transformed into thermal energy in the atmosphere, fully equivalent to, for example, the heat generated by fossil combustion. It could be argued that if this part had not been converted into electrical energy, it would still have heated the Earth’s surface and the atmosphere. But history has proven for thousands of years that solar heating did not raise the temperature of the atmosphere higher than the level it was 200 years ago. It must therefore be seriously taken into account that generating electrical energy from solar energy will not contribute to the reduction of the warming of the atmosphere.

VIII.2 Heat balance of the atmosphere

Apparently there has been a balance between absorbed and released heat by the atmosphere for many centuries, but this balance has been severely disrupted for about 200 years, as shown in figure VIII.1. This disturbance has an increase in the global temperature with a time-dependent gradient as shown in Table VIII.1. These values can be calculated by taking the derivative to time of (2) in chapter II.

![Figure VIII.1: Global temperature since the year -20000](image)

<table>
<thead>
<tr>
<th>year</th>
<th>mk/year</th>
</tr>
</thead>
<tbody>
<tr>
<td>1850</td>
<td>1,1</td>
</tr>
<tr>
<td>1875</td>
<td>1,6</td>
</tr>
<tr>
<td>1900</td>
<td>2,4</td>
</tr>
<tr>
<td>1925</td>
<td>3,7</td>
</tr>
<tr>
<td>1950</td>
<td>5,5</td>
</tr>
<tr>
<td>1975</td>
<td>8,3</td>
</tr>
<tr>
<td>2000</td>
<td>12,5</td>
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<tr>
<td>2005</td>
<td>13,6</td>
</tr>
<tr>
<td>2010</td>
<td>14,7</td>
</tr>
<tr>
<td>2020</td>
<td>17,4</td>
</tr>
<tr>
<td>2100</td>
<td>64,5</td>
</tr>
</tbody>
</table>

Table VIII.1 Gradient global temperature
VIII.3 The heating of the atmosphere in the LRM

In order to calculate the temperature increase of the atmosphere by direct heating, it is necessary to know its heat capacity. The heat capacity of the atmosphere, expressed in J/K, determines how much the atmosphere rises in temperature, given the net heat supplied to it. Here "net" is defined as the difference between the supplied and released heat. In Appendix 2 it has been calculated by two methods that this heat capacity is \(5 \times 10^{21} \text{ J/K}\).

In as well the GHM as the LRM the (alleged) supplied heat is well defined. It is not known which part of it is released, in order to calculate the net supplied heat. But the actually measured temperature rise as function of time is known and can be expressed mathematically by equation (2).

The following equation applies in both models:

\[
\text{"Atmospheric heat capacity [J/K]" times "atmospheric temperature increase during a year [K/year]" = 
\text{"net heat energy absorbed by the atmosphere during that year [J/year]".}
\]

The dimension \([\text{J/year}]\) is equivalent to the dimension \([\text{W}]\), so the last mentioned variable in the equation above can also be presented as: “net average heat power applied during that year”, expressed in W. The atmospheric heat capacity can also be written in the dimension \(\text{W/(K/s)}\). Table VIII.1 shows that the atmospheric temperature gradient in 2010 was \(14.7 \text{ mK/year} = 0.0147/3.1536 \times 10^{-7} = 4.7 \times 10^{-10} \text{ K/s}\). So in the year 2010 a net heat power of: ‘Atmospheric heat capacity’ times ‘atmospheric temperature gradient’, being: \(5 \times 10^{21} (\text{J/K}) \times 4.7 \times 10^{-10} (\text{K/s}) = 2.4 \text{ TW}\) is sufficient to achieve that gradient in 2010.

Equation (4) shows that the globally applied power in 2010 is \(8.4 \times 10^{-14} \cdot \exp(2010/61) = 17.2 \text{ TW}\). The required net power, to heat the atmosphere as has been measured, thus is only 14% of this globally generated power. In other words and in terms of energy: by far the largest part (86%) of the gross heat energy, generated by the LRM in 2010, is radiated to space. The remaining part is sufficient to increase the temperature of the atmosphere as has been measured during that year.

The generated gross power of the LRM can be expressed in terms of (mean) global gross power density, by dividing this power by Earth’s surface \(5.1 \times 10^{14} \text{ m}^2\), resulting in \(0.034 \text{ W/m}^2\). This value compared to the value of the GHM \(0.6 \text{ W/m}^2\), to be corrected to 0.9 \text{ W/m}^2\) shows an extremely large difference of almost a factor 30. The cause is that the GHM-value, in terms of radiation, is created instead of actually measured in order to explain the heating of the Sea.

VIII.4 LRM heating since 1810

The derivative of the actually measured temperature gradient equals the derivative of equation (2), being: 
\(7.2 \times 10^{-14} \cdot \exp(t/61) \text{ mK/year}\).

Taking 14% of the globally applied power, equation (4) results in: \(0.14 \times 8.4 \times 10^{-14} \cdot \exp(t/61) \text{ TW}\).

This result in Watt, divided by the heat capacity of the atmosphere and multiplied by the ratio “sec/year”, results in \(7.4 \times 10^{-14} \cdot \exp(t/61)\). The small deviation from the measured \(7.2 \times 10^{-14} \cdot \exp(t/61)\) mK/year is eliminated when the heat capacity of the atmosphere is taken \(5.1 \times 10^{21}\) instead of \(5.0 \times 10^{21} \text{ J/K}\)!

Qualifying this expression as the calculated temperature gradient as function of the world wide applied power, it has been proven that this calculated yearly increase of the global temperature during the past 200 years, perfectly matches the measured yearly increase of the global temperature. And thus can be predicted too on this basis!
VIII.5 The heating of the Sea in the LRM

In view of the findings in section VII.5 “The heating of the Sea in the GHM”, such a heating can only take place bottom up and by means of convection.

The application of a heat pump with a so-called horizontal ground exchanger (at a depth of 2 meters) teaches that a continuous heat flux of 50 W/m² can be generated. But then the temperature at that depth drops from +10 °C to -5 °C. At such a place heat is extracted from Earth in a forced way. Incidentally, that temperature will return to its original value within a few hours after the heat abduction has been stopped. So most likely the natural geothermal heat flux is at least an order of magnitude lower than this forced heat flux of 50 W/m².

In section VII.5 it has been shown that the power density, forcing the increase of the heat content of the Sea, can be expressed by $P_D(t) = 4.6 \times 10^{13} \cdot \exp(t/61)$ W/m². This heat flux varies from 0.1 to 1 W/m² during the period 1870-2020, and is much lower then the mentioned forced geothermal heat flux of 50 W/m², so fully acceptable as possible source of the heating of the Sea. The unknown natural geothermal heat flux most likely has been constant during the past several thousands of years. The exponentially increasing heat flux, responsible for the heating of the Sea, has to be considered as that part of the natural geothermal heat flux that heats the Sea, while its remaining part is radiated into space. Just as it did until 1870 without adding heat energy to the Sea, because the temperature of the atmosphere hadn't risen yet. Check: $\int_{1870}^{2015} P_D(t) \cdot dt \cdot \text{seconds/year} (3.15 \times 10^7) \cdot \text{surface Sea} (3.6 \times 10^{14} \text{m}^2) = 6.4 \times 10^{23}$ Joule QED.

In order to understand the influence of that geothermal heat flux on the temperature of the Sea, we consider a basically comparable situation: a river flowing into a sea. Mind the difference between sea and Sea! The level of that sea varies with the tide. The level of the river water in the estuary rises and falls without delay with the level of the sea. The further inland, the less remains in the river of that varying level in the estuary.

If we replace, in this reality, the height of that sea by the temperature of the atmosphere, then the temperature difference at the transition of the atmosphere and the Sea's surface is always zero, given the slow change in temperature of the atmosphere. Thus, as the long-term temperature of the atmosphere increases, the long-term temperature of the Sea at its surface increases by the same amount, through the supply of thermal energy in the form of geothermal heat flux. And for this reality also applies: the deeper into the Sea, the less remains of that increase in temperature at the surface.

The total amount of heat in the Sea is $15 \times 10^{26}$ Joule, as follows from the parameters below:

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Specific heat capacity per m³</td>
<td>4.0 \times 10⁶ J/K/m³</td>
</tr>
<tr>
<td>Volume</td>
<td>1.3 \times 10¹⁸ m³</td>
</tr>
<tr>
<td>Mean temperature</td>
<td>280 K</td>
</tr>
</tbody>
</table>

The increased amount of heat in the Sea over the past 150 years has been corrected to $6.4 \times 10^{23}$ Joule. In comparison to the total amount this is only about 0.4 %!

Summarized: The geothermal heat flux, that has existed for millions of years, once brought at some moment the Sea and the atmosphere to certain temperatures, equal to each other at the transition of both media. As mankind has raised the temperature of the atmosphere by 1 °C, the geothermal heat flux does adjust the temperature at the surface of the Sea to this increase, gradually decreasing to 0 at the bottom.

N.B. Permafrost is in the same way heated by the geothermal heat as the Sea is heated by this phenomenon. In addition to the mathematical and physical substantiation of the heating of the Sea and Earth's crust, as presented above, it is also intuitively very likely that Earth's core is responsible for the heating of the outer shell of, say, 3 km. After all, on a scale of 120 mm for the diameter of Earth, this 3 km is only 0.06 mm!
VIII.6 Hot Spots on Earth

Hot Spots are columns in the atmosphere where the temperature is significantly higher than the mean temperature of the atmosphere. The explanation for these thermal columns cannot be given by the GHM. After all, a column of increased CO$_2$ concentration would be spread over the rest of the atmosphere before that gas would be able to cause an increase in temperature exactly above the considered surface. Only a continuous heat flow, significantly higher than the globally mean value, can maintain such a local higher temperature.

The force of that flow/flux is proportional to the applied power on the related area, divided by the surface of that area. No data has been found on the Internet about the amount of energy consumed per country per year. There are data of the Gross Domestic Product (GDP), expressed in US $, per country per year. It is assumed that the higher the GDP of a country, the more energy is consumed. In order to transform ‘GDP’ to ‘Watt’ the globally GDP (GWP), i.e. the sum of the GDPs of all countries, has been divided by the globally applied power, as shown by (4): $P_G(t)=8.4\cdot10^{14}\text{exp}(t/61)$. According to reference [VIII.1], the GWP for the year 2015 is about 75000 billion (75$\cdot10^{12}$) $. In that year the applied power was 19 TW. The requested conversion factor thus is 0.25 W/$. Ref. [VIII.2] and [VIII.3] show, by country, their GDP in 2015, respectively their surface. These values have been converted to $ resp. m$.

The power density per country can now be calculated from: GDP($) / surface (m$^2$) $\cdot$ 0.25 W/$ in W/m$^2$. The results of the 10 countries with the highest resp. lowest values are shown in Table VIII.2 resp. VIII.3. The warming of the Netherlands is measured as twice as high as the rise of the global mean value. See reference [VIII.4]. Due to the influence of the surrounding atmosphere a factor 2 higher than the global mean value in 2015: 19 TW/5.1$\cdot10^{14} = 0.037$ W/m$^2$ would not be enough of course. But still the value 4.5 is surprisingly high. Multiplying the power densities with the related surfaces and adding these results shows a worldwide applied power of 18$\cdot10^{12}$ W. The difference with the number 19$\cdot10^{12}$ W is caused by the fact that about 20 of the 200 countries are not found in as well reference [VIII.2] as in [VIII.3].

<table>
<thead>
<tr>
<th>Country</th>
<th>W/m$^2$</th>
<th>Country</th>
<th>W/m$^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Singapore</td>
<td>101</td>
<td>Guyana</td>
<td>0.0037</td>
</tr>
<tr>
<td>Bahrain</td>
<td>9,9</td>
<td>Namibia</td>
<td>0.0035</td>
</tr>
<tr>
<td>Malta</td>
<td>7,6</td>
<td>Mali</td>
<td>0.0026</td>
</tr>
<tr>
<td>San Marino</td>
<td>6,5</td>
<td>Chad</td>
<td>0.0021</td>
</tr>
<tr>
<td>Luxembourg</td>
<td>5,5</td>
<td>Mongolia</td>
<td>0.0019</td>
</tr>
<tr>
<td>Netherlands</td>
<td>4,5</td>
<td>Niger</td>
<td>0.0014</td>
</tr>
<tr>
<td>Switzerland</td>
<td>4,0</td>
<td>Mauritania</td>
<td>0.0012</td>
</tr>
<tr>
<td>Belgium</td>
<td>3,7</td>
<td>Zimbabwe</td>
<td>0.0009</td>
</tr>
<tr>
<td>Qatar</td>
<td>3,6</td>
<td>Kyrgyz Republic</td>
<td>0.0008</td>
</tr>
<tr>
<td>Korea</td>
<td>3,4</td>
<td>Suriname</td>
<td>0.0008</td>
</tr>
<tr>
<td>Israel</td>
<td>3,4</td>
<td>Central African Rep.</td>
<td>0.0006</td>
</tr>
</tbody>
</table>

Table VIII.2 Highest ranked countries

Table VIII.3 Lowest ranked countries

If only Earth’s land (30% of the total surface) is chosen as the reference surface, as is effectively done in the above calculations, the related mean power density in 2015 would be 0.12 W/m$^2$.

The five countries: Nigeria, Estonia, Equatorial Guinea, Indonesia and Bulgaria show roughly this value. These countries are ranked around the position 70 in the list of 180.

The total power of the 17 countries below, in descending order, includes 80% of the worldwide applied power. The related mean power density is 0.2 W/m$^2$ and the total surface 0.4 times Earth’s land surface.

These 17 countries are: United States, China, Japan, Germany, United Kingdom, France, India, Italy, Brazil, Canada, Korea, Russia, Australia, Spain, Mexico, Indonesia, Netherlands.
IX  Monthly global temperature and CO$_2$ anomalies

Monthly averaged records of the global temperature and of the CO$_2$ concentration in the atmosphere show both a surprisingly yearly periodic anomaly.

IX.1  Monthly temperature anomalies

Figure IX.1, copied from reference [IX.1], shows a graph of the monthly temperature deviations per year relative to the worldwide mean global temperature for that year since 1880. The separation of the curves has been realized by adding the related *long-term* increase of the worldwide mean global temperature during that year. As a result the curve for the year 2017 is drawn about 1 °C higher than the curve for 1880. See note 1 regarding the original source: reference [IX.2].

Possible background for the presented anomalies.

Reference [IX.3] presents that during the summer the rise in temperature around the North pole (between $60^\circ$ and $82.5^\circ$ latitude) is significantly higher than the fall in temperature around the South pole in the same months. A similar phenomenon occurs between $32.5^\circ$ and $50^\circ$ latitude. The graphs of these anomalies are shown in the figures IX.2 and IX.3. The blue line shows the mean value during the period 1980–1989 and the red line during the period 2000–2009. The curves prove that this phenomenon is perfectly consistent.

*Reference [IX.2] should have shown such anomalies, but doesn’t anymore. The person who is responsible for this data has been sent an email for clarification. It has been admitted that this data has been removed, but a clarification is not given, not even after two other attempts.*
Figure IX.2: Temperature measurements between 60° and 82.5° latitude

Figure IX.3: Temperature measurements between 32.5° and 50° latitude
These graphs have been converted into data shown in Table IX.1 in the columns marked with NH and SH. Although the differences between the red and blue lines are very small, the mean value is presented.

<table>
<thead>
<tr>
<th>month</th>
<th>latitudes (60° to 82.5°)</th>
<th>latitudes (32.5° to 50°)</th>
<th>latitudes</th>
<th>dev. latitudes</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>NH temp</td>
<td>SH temp</td>
<td>NH temp</td>
<td>SH temp</td>
</tr>
<tr>
<td>1</td>
<td>243.4</td>
<td>249.5</td>
<td>255.0</td>
<td>273.1</td>
</tr>
<tr>
<td>2</td>
<td>245.6</td>
<td>249.2</td>
<td>254.0</td>
<td>274.8</td>
</tr>
<tr>
<td>3</td>
<td>244.6</td>
<td>245.4</td>
<td>255.0</td>
<td>273.5</td>
</tr>
<tr>
<td>4</td>
<td>246.0</td>
<td>241.6</td>
<td>258.6</td>
<td>272.1</td>
</tr>
<tr>
<td>5</td>
<td>251.5</td>
<td>242.6</td>
<td>263.3</td>
<td>269.4</td>
</tr>
<tr>
<td>6</td>
<td>257.1</td>
<td>243.0</td>
<td>267.1</td>
<td>268.0</td>
</tr>
<tr>
<td>7</td>
<td>263.6</td>
<td>240.7</td>
<td>269.5</td>
<td>266.9</td>
</tr>
<tr>
<td>8</td>
<td>264.0</td>
<td>239.1</td>
<td>271.9</td>
<td>266.7</td>
</tr>
<tr>
<td>9</td>
<td>258.9</td>
<td>238.1</td>
<td>270.6</td>
<td>267.8</td>
</tr>
<tr>
<td>10</td>
<td>255.6</td>
<td>240.9</td>
<td>266.9</td>
<td>269.2</td>
</tr>
<tr>
<td>11</td>
<td>252.0</td>
<td>242.3</td>
<td>262.0</td>
<td>271.0</td>
</tr>
<tr>
<td>12</td>
<td>248.5</td>
<td>246.1</td>
<td>258.0</td>
<td>272.8</td>
</tr>
</tbody>
</table>

**Table IX.1**

The variable “Latitudes mean” shows the mean values of all the 4 temperatures on its left side in °C. The green value on top is the mean value of these mean values, used to calculate “dev. latitudes mean”. The top-top value of this variable is 5 to 6 °C, so significantly higher than the top-top values of 4 °C in figure IX.1. That is logical, because the variable “Latitudes mean” is a very poor representative of the **globally** mean temperature. The last one is the mean value of thousands of stations on the global surface. But their respective maximum and minimum value are in the same months (Jul-Aug resp. Dec-Jan).

This investigation thus learns that the monthly global temperature anomalies, as shown in figure IX.1, are strongly related to the orientation of the Earth’s rotation axis relative to the Sun. However, it doesn’t explain yet in more detail what happens on Earth during summer and winter, in NH, resp. SH, that causes these mutual significant differences. More details will be presented in the next section.

The map in figure IX.4 shows perfectly the seasonal temperature differences between NH and SH.

![Seasonal Temperature Range](image)

**Figure IX.4:** “Using the Berkeley Earth Surface Air Temperature (SAT) dataset the seasonal temperature range was calculated over the entire land surface of the globe. For the purposes of this map the seasonal range was defined as the difference between the warmest month and the coolest month. The difference ranges from a low of 0 degrees C in equatorial regions to a high of 60 degrees C in north eastern Russia. While not as dramatic as the ranges found in Siberia, the seasonal range in northern Canada is also large.”

This phenomenon is also known as Polar amplification, reference [IX.4]. Given the large difference between North and South Pole the phenomenon has been split into Arctic and Antarctic amplification. The explanation is based on the Greenhouse Model, without giving an explanation for the large difference between Arctic and Antarctic amplification: “Polar amplification is the phenomenon that any change in the net radiation balance (for example greenhouse intensification) tends to produce a larger change in temperature near the poles than the planetary average.”
IX.2 Monthly CO₂ anomalies

Reference [1] shows the monthly records of the CO₂-concentration in the atmosphere in ppm since 1958. It has been used to make a graph of this anomaly averaged over the total period of measurements. Figure IX.5 shows this graph as well as the monthly temperature anomalies, also as averaged values over the whole period of measurements*. The curves have been made symmetrical around zero by subtracting the yearly mean value over the respective periods.

![Seasonal anomaly of temperature and CO₂ averaged over 1880 - 2017 resp. over 1958 - 2017](image)

* The curve in figure IX.5 is based on data that was available at the original site until the end of 2017!

Figure IX.5 shows that during the summer of the NH (around July) the globally averaged CO₂ concentration starts to become lower than the yearly mean value. This can possibly understood as follows. A property of plants is that they grow more during warm periods than during cold periods and that they thus absorb more CO₂ during a growing period. During the summer of the NH it is winter on the SH. However the SH has by far less area where plants grow and at all these areas it never becomes cold, because they are all located closer to the equator. So the plants at the SH will not create a significant anomaly in the absorption of CO₂ during a year. As a result the globally mean value is season dependent, without any relation with the long-term trend of this variable.

The question remains what the fundamental cause of the monthly temperature anomaly might be.

The generally accepted idea is that the Sea absorbs more heat than land does. Given the fact that the SH contains by far more water than the NH, the temperature of the atmosphere at SH increases less during summer at SH (Oct-Feb) than this temperature does at NH during summer at NH (Apr-Aug).

Given these argumentations the conclusion must be that the seasonal anomalies don’t have any relation with the long-term increase of the yearly averaged global atmospheric temperature, neither of the yearly averaged CO₂ concentration in the atmosphere.
X Global Mean Sea Level until 2100

X.1 Introduction

Global Mean Sea Level is a hot topic nowadays, because maybe we will eventually drown in the oceans. The most intricate models for its increase in the future have been created and will be created, some of them leading to the most worst thinkable scenario in 2100. See for example reference [X.1]. Several organisations realize data sets for the GMSL. They have all been asked in 2018 for numerical data. The only one that did react fast as well as with appropriate data was CSIRO, indirectly shown in [X.2].

X.2 Mathematical expression for CSIRO measurements

The CSIRO data, presented as monthly mean values in mm, have been transformed to yearly mean values in cm. After that the values have been corrected with a constant value in order to start at 0 cm in 1880. Figure X.1 shows the measured Sea level rise, as well as the corresponding fitted exponential function:

\[
SL(t) = -10.8 + 1.7 \times 10^4 \times \exp(t/120) \quad \text{cm}
\]  

(6)

The figure proves that this function fits the measured values perfectly. The standard deviation of the measured values with respect to this curve has been calculated as 0.65 cm.

In November 2021 satellite data for the period 1993 – 2019 has been added, using the graph in ref. [X.3]. The calculations carried out in chapter VI show that the GMSL rise, only as a result of the expansion of the water during the past 150 years, is 9.3 cm. The measured increase is about 22.5 cm. The remaining 13 cm must be the result of the melting of the snow on the mountains on the mainland and of the snow on both poles. Not of the melting of the ice on and around the poles, because when ice melts, its volume decreases by 10%. On the basis of the currently measured GMSL rise, it is therefore grossly exaggerated to predict that we have to take meters of increase into account. Figure X.1 shows that even if the prevailing increasing trend of global warming is maintained over the next 100 years, the GMSL will rise only 30 cm from the current level.

![Global Mean Sea Level measurements and fitting up to 2019](image)

*Figure X.1 All satellite data is corrected with +0.9 cm w.r.t. the fitted CSIRO value in 1993*

The observation that by far the largest part of the GMSL rise must have been caused by snowmelt, forces us to consider more closely its possible influence on Sea’s temperature increase. The snowmelt at the poles results in water of the same temperature as the water of the sea around the poles. The snow melting on the mainland is heated during the time it flows to the Sea. It is heated until roughly the temperature of the atmosphere. However the amount of Seawater on Earth is much larger than the amount sweet water. Its temperature, roughly equal to atmosphere’s temperature, can therefore not have significant influence on Sea’s temperature. All Sea’s heat energy increase must have been accomplished by the geothermal flux.
Appendix 1  Mathematical background of the polynomial and exponential curve fitting

1.1  Polynomial curve fitting

Polynomial fitting means the fitting of the measured data \( y_n \) as function of the variable \( x_n \) to a polynomial \( y \) of order \( k \): \( y = \sum a_i x_i \), in such a way that the sum \( R \) (residuals) of the quadratic deviations between the measurements \( y_n \) and \( y \) is minimal. The variable \( x \) is an arbitrary value inside as well as outside the original range of \( x_n \), just like \( y \) is in relation to \( y_n \).

\[
R = \sum (y_i - y)^2 = \sum (a_0 + a_1 x_i + \ldots + a_k x_i^k)^2
\]

N.B. The symbol \( \Sigma \) is exclusively assigned to \( i \).

For minimization the following relations have to be fulfilled:

\[
\frac{\partial R}{\partial a_0} = -2 \sum a_i (y_i - (a_0 + a_1 x_i + \ldots + a_k x_i^k)) = 0
\]

\[
\frac{\partial R}{\partial a_1} = -2 \sum a_i x_i (y_i - (a_0 + a_1 x_i + \ldots + a_k x_i^k)) = 0
\]

\[
\frac{\partial R}{\partial a_2} = -2 \sum a_i x_i^2 (y_i - (a_0 + a_1 x_i + \ldots + a_k x_i^k)) = 0
\]

\[
\vdots
\]

\[
\frac{\partial R}{\partial a_k} = -2 \sum a_i x_i^k (y_i - (a_0 + a_1 x_i + \ldots + a_k x_i^k)) = 0
\]

These relations can be written as:

\[
a_0 \Sigma x_i + a_1 \Sigma x_i x_i + \ldots + a_k \Sigma x_i x_i^k = \Sigma y_i
\]

\[
a_0 \Sigma x_i^2 + a_1 \Sigma x_i x_i^2 + \ldots + a_k \Sigma x_i x_i^{k+1} = \Sigma x_i y_i
\]

\[
\vdots
\]

\[
a_0 \Sigma x_i^k + a_1 \Sigma x_i x_i^k + \ldots + a_k \Sigma x_i x_i^{2k} = \Sigma x_i y_i
\]

In matrix format:

\[
\begin{bmatrix}
\Sigma x_i & \Sigma x_i x_i & \ldots & \Sigma x_i x_i^k & a_0 \\
\Sigma x_i x_i & \Sigma x_i x_i^2 & \ldots & \Sigma x_i x_i^{k+1} & a_1 \\
\vdots & \vdots & \ddots & \vdots & \vdots \\
\Sigma x_i^k & \Sigma x_i x_i^k & \ldots & \Sigma x_i x_i^{2k} & a_k
\end{bmatrix}
\begin{bmatrix}
a_0 \\
a_1 \\
\vdots \\
a_k
\end{bmatrix}
= 
\begin{bmatrix}
\Sigma y_i \\
\Sigma x_i y_i \\
\vdots \\
\Sigma x_i^k y_i
\end{bmatrix}
\]

Shortly written as: \( M_s \cdot \tilde{a} = M_y \cdot \tilde{y} \), with \( \tilde{a} \) and \( \tilde{y} \) to be read as a column vectors.

The matrix \( M_s \) can be composed by the product of the 2 matrices: \( M^T \cdot M \), with \( M^T \) the transpose of \( M \) and \( M \) and \( M^T \) as shown below.

\[
M (k x n) = M^T (n x k)
\]

\[
\begin{array}{cccccc}
1 & x_1 & \ldots & x_1^k & 1 & 1 & \ldots & 1 \\
1 & x_2 & \ldots & x_2^k & x_1 & x_2 & \ldots & x_0 \\
\vdots & \vdots & \ddots & \vdots & \vdots & \vdots & \ddots & \vdots \\
1 & x_n & \ldots & x_n^k & x_1^k & x_2^k & \ldots & x_0^k
\end{array}
\]

It turns out that \( M^T \cdot \tilde{y} = M_y \cdot \tilde{y} \), as defined above, so \( M_s = M^T \). As a result: \( M^T \cdot M \cdot \tilde{a} = M^T \cdot \tilde{y} \)

Both sides ‘left side multiplied’ by \( (M^T \cdot M)^{-1} \) results in: \( (M^T \cdot M)^{-1} \cdot M^T \cdot M \cdot \tilde{a} = (M^T \cdot M)^{-1} \cdot M^T \cdot \tilde{y} \).

Given: \( (M^T \cdot M)^{-1} \cdot M^T \cdot M = I \), it follows that \( \tilde{a} = (M^T \cdot M)^{-1} \cdot M^T \cdot \tilde{y} \), showing the requested coefficients \( a \).

Note:
Calculating the check \( (M^T \cdot M)^{-1} \cdot M^T \cdot M = I \), the result strongly departs from that unity matrix \( I \) for orders greater than 6, due to the restricted number length of Excel. However the 8th and 9th order polynomials still seem to be calculated good enough in the current investigations, given their strong similarity.
1.2 Exponential curve fitting

Exponential curve fitting is here meant to be the use of 3 points of measurement out of a collection of measurement data (here as function of time), in which a clear tendency is visible. The 3 measurements are used for the solution of the 3 variables a, b and c in the function \( y = c + a \exp(t/b) \). The variable \( t \) will represent the year under consideration. As a result the dimension of \( b \) is also “year”.

Given the measuring points: \((t_1, y_1)\), \((t_2, y_2)\) en \((t_3, y_3)\) the solution of the constant \( c \) is as follows:

\[
\begin{align*}
y_1-c &= a \exp(t_1/b) \\
\ln(y_1 - c) &= \ln(a) + t_1/b \\
\ln(y_2 - c) - \ln(y_1 - c) &= (t_1 - t_2)/b \\
b &= (t_1 - t_2)/\{\ln(y_1 - c) - \ln(y_2 - c)\}
\end{align*}
\]

\( c \) can only be solved numerically by means of an iteration process, applied to the function:

\[
(t_1 - t_2)/\{\ln(y_1 - c) - \ln(y_2 - c)\} - (t_1 - t_3)/\{\ln(y_1 - c) - \ln(y_3 - c)\} = 0
\]

\[
b = (t_1 - t_3)/\{\ln(y_1 - c) - \ln(y_3 - c)\} \\
a = (y_2-c)/\exp(t_2/b)
\]

In this report an essential approach is that several times the fitting to other measured variables is started with the same \( b \) as found for the \( \text{CO}_2 \) concentration. In such a situation the solving of \( a \) and \( c \) is as follows:

\[
\begin{align*}
B_i &= \exp(t_i/b) \\
y_1 &= c + a \cdot B_1 \\
y_3 &= c + a \cdot B_3 \\
y_1 - y_3 &= a \cdot (B_1 - B_3)
\end{align*}
\]

\[
a = (y_1 - y_3)/(B_1 - B_3) \\
c = y_1 - a \cdot B_1
\]
Appendix 2

Calculation of the heat capacity of the atmosphere

2.1 Temperature constant as function of height

The specific heat capacity of air at 0 °C and 1 bar is 1000 J/kg/K. The specific weight of such air (sw₀) is 1.3 kg/m³. Multiplication of these quantities leads to its specific volumetric heat capacity as 1300 J/m³/K.

Quote from: https://en.wikipedia.org/wiki/Atmospheric_pressure

"Altitude variation
Pressure on Earth varies with the altitude of the surface;...............

\[ p(h) \approx p_0 e^{-M g h / R T} \]

with:

- \( p_0 \): Sea level standard atmospheric pressure = 101325 Pa
- \( h \): Altitude in m
- \( M \): Molar mass of dry air = 0.029 kg/mol
- \( g \): Earth-surface gravitational acceleration = 9.8 m/s²
- \( R \): Universal gas constant = 8.31 J/(mol·K)
- \( T \): Sea level standard temperature = 288.15 K

In stead of \( p(h) \) the variable \( sw(h) \) can be chosen. Replacing the \( e^{-Ch} \) function into \( e^{-C h} \), with the boundary condition that \( e^{-C h} = 1 \) for \( h = r \) (r the radius of the Earth), this function becomes \( e^{-Ch} \).

The total mass of air in the atmosphere can now be calculated as:

\[ sw_0 \int_{r}^{\infty} e^{-Ch} \cdot \text{O(h)} \, dh, \]

with \( \text{O(h)} = 4 \pi h^2 \).

After applying twice partial integration to \( \int_{r}^{\infty} e^{-Ch} \cdot h^2 \, dh \) the result is \( -C^{-1} e^{-Ch} \cdot (h^2 + 2C^{-1}h - 2C^{-2}) \mid_{r}^{\infty} \)

A few calculations of \( e^{Ch} \cdot h^2 \) learn that the value of this integrand is zero for \( h = \infty \).

The result for the total mass of the atmosphere thus is:

\[ 4\pi sw_0 e^{-C} \cdot C^{-1} \cdot e^{-C} \cdot (r^2 + 2C^{-1}r - 2C^{-2}) = 4\pi \cdot 1.3 \cdot C^{-1} \cdot (r^2 + 2C^{-1}r - 2C^{-2}) \]

The constant \( C^{-1} = RT/Mg \) equals: 8.31·288/(0.029·9.8) = 8420 m.

Because the temperature is expressed in Kelvin, the sensitivity of that parameter is low.

The radius \( r \) of the Earth is 6371000 m. With \( 2C^{-1}r - 2C^{-2} \ll r^2 \), the result of the integral is \( 4\pi \cdot 1.3 \cdot C^{-1} \cdot r^2 \).

So the total mass of the atmosphere is \( 5.6 \cdot 10^{18} \) kg.

This calculation forms the essential basis for the calculation of the total heat capacity of the atmosphere. The mass calculated in this way is also a check on the method used. This check is that the total mass can easily be calculated too as follows:

The atmospheric pressure on the Earth's surface is 101325 Pa = 1.013·10⁵ N/m² or kg m⁻¹ s⁻².

The surface of the Earth is \( 5.1 \cdot 10^{14} \) m². The total mass of air in the atmosphere is therefore \( 1.013 \cdot 10^{15} \cdot 5.1 \cdot 10^{14} \) /g. With \( g = 9.8 \) ms⁻² resulting in \( 5.3 \cdot 10^{18} \) kg.

The atmospheric heat capacity thus is \( (5.3 \div 5.6) \cdot 10^{18} \) kg · 1000 J/kg/K = \( (5.3 \div 5.6) \cdot 10^{21} \) J/K, neglecting the influence of its temperature as function of height.

This has been checked in the next section.
2.2 Temperature height dependant

The figure below shows how T depends on the height in the atmosphere.

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![Figure Appendix 2](image)

**Figure Appendix 2**

In order to check the influence of this variation the integral $4\pi \cdot sh_0 \cdot \int e^{C(h) \cdot h^2} \cdot dh$, as used in the previous section, has now to be written as $4\pi \cdot sh_0 \cdot \int e^{C(h) \cdot (r-h)^2} \cdot dh$, with $C(h) = Mg/RT(h)$.

This integral has been calculated numerically in Excel in steps of 1000 m and with $sh_0 = 1300 \text{ J/m}^3/\text{K}$.

The calculation is checked by taking T height independent and 288 K and for a maximum height of 120 km, in accordance with the maximum height shown in the figure above. The outcome is 5.6$\cdot 10^{21}$ J/K, so sufficiently in agreement with the analytical outcome.

Replacing the temperature in a height dependent one in accordance with the information shown in the figure above, the result is 4.6$\cdot 10^{21}$ J/K.

This outcome, together with the two outcomes in the previous section, presents a good reason to take as a rounded value for the heat capacity of the atmosphere the value 5$\cdot 10^{21}$ J/K.

The same program shows also that the total heat energy of the atmosphere equals 1.5$\cdot 10^{24}$ Joule.
Appendix 3  Impact of sustainable energy

3.1  Sun energy

The net electrical power generated by means of sun cells is 15 W/m$^2$. Experience learns that a mean household of 3 persons in the prosperous part of the world can generate its own need for electrical purposes by means of 20 m$^2$ of sun cells. The heating of the house excluded. Including the heating would result in about 50 m$^2$. So heating the houses with their own sun energy is impossible. The need for electrical energy of the meant household is, exclusive the heating, 100 W per person. The prosperous part of the world population is roughly living in the 17 countries, mentioned at the end of section VIII.6, occupied by 5 billion persons. These prosperous 5 billion persons as a result need 0.5 TW power, exclusive the heating. Such a power is a negligible fraction of the worldwide required power of 20 TW. Nature would worldwide be destroyed, if such a power would have to be generated by sun cells.

3.2  Wind energy

The drawing in figure Appendix 3, copied from ref. [A], shows the power of the worldwide generated wind energy. It presents in 2014 a growth of 51 GW, so 0.05 TW/year, in terms of capacity!

![Wind Power Global Capacity, 2004–2014](image)

Figure Appendix 3

The expression “Wind Power Global Capacity” is misleading. It should have been presented as Globally Installed Wind Power. The generally accepted net power is 20% of its installed power, so the presently net wind power is < 0.1 TW. Completely negligible w.r.t the global need of about 20 TW at this moment.

The derivative of (4) in chapter V shows a prevailing annual growth in applied power of 0.3 TW/year. The annual growth of net wind power is 0.01 TW/year, so also completely negligible w.r.t. the applied one.

3.3  Earth heat energy

Suppose the worldwide mean family consists of 3 persons and suppose each family needs a power of 500 W to heat its house. As soon as the world population would consists of 3 billion of such families, the required total power to heat all the houses on the world would be 1.5 TW. That is a negligible fraction of the total need at that time: 23 TW. So even in the most extreme, and at the same time most unrealistic, situation that each house on the world would be heated by means of Earth heat energy, only a negligible part of the worldwide required power would be generated by such a kind of sustainable energy.

But to top it all of: As presented in the Living Room Model, whatever kind of energy is applied it is all converted into heat. So applying sustainable energy will not solve the problem of the increasing global temperature at all.
Appendix 4  The World Population in the Past and in the Future

4.1 Introduction

Given the proven validity of the Living Room Model, it has to be concluded that the global heating problem is a symptom of a much more fundamental problem: the worldwide overpopulation. The world population is known through censuses, but up to 1950 only by approximation. The more accurate the past is known, the better the future can be predicted therefrom. The approximations, together with the more precise-looking counts after 1950, are processed into a natural looking curve for the period 1800 up to now in chapter III. Using the mathematical expression for this curve, predictions can be calculated for the future. In addition a simple model has been realized in this appendix for the growth of a population. Mutual comparison of the two curves results in interesting conclusions, of which the most important one is that the solution of the climate problem must be sought in the reduction of the world population.

4.2 Applied growth model of a population

Given the fact that a large number of statistical variables permit to work with (only) averages, the following simple model of the growth of a population is established, based on the following assumptions:

1. The world population is made up of N humans.
2. There are N/2 male and N/2 female humans.
3. Each human dies at age L, where L is the average age of the N humans.
4. The age of humans is distributed evenly, so there are N/L humans by age.
5. Each couple gets at a certain age x children, of which S survive to procreate. The variable S thus is the net result of the birth and of the death among youth.

From this model it follows directly that if S = 2 the population is not growing nor declining. Indeed, every year N/L humans die and every year S*(N/2)/L humans procreate. At a constant population, these two expressions are equal.

This model is realized in an Excel program in which the increase and decrease of the population in each year is calculated from the previous year. By adding this net result of the population growth to the population in the previous year the population of the present year is obtained. In symbolic form:

<table>
<thead>
<tr>
<th>Year</th>
<th>decrease</th>
<th>increase</th>
<th>population</th>
</tr>
</thead>
<tbody>
<tr>
<td>Y-1</td>
<td></td>
<td></td>
<td>N_{Y-1}</td>
</tr>
<tr>
<td>Y</td>
<td>S*(N_{Y-1}/2)/L</td>
<td>N_{Y-1}/L</td>
<td>N_{Y-1} + S*(N_{Y-1}/2)/L - N_{Y-1}/L (=N_{Y})</td>
</tr>
</tbody>
</table>

In order to verify that this model fits somewhat with actual counts/estimates (henceforth the sake of brevity from now on referred to as observations) the graph from reference [1] is taken as the reference. This graph is based on a curve fitting of the available observations. This curve fitting is based on the model \( y = c + a\exp(t/b) \), with the symbol t representing the year and y the number of humans. With the aid of this expression the number of humans outside the period of observation can be calculated too for each year. The period 1800-2100 is chosen here.

The variables L and S are, by trial and error, adjusted in such a way that the populations in 2100 in both models are equal. The initial value \( N_{1800} \) of the growth model is of course selected equal to the initial value of the observations. Figure Appendix 4.1 shows this result for \( L = 60 \) and \( S = 3.5 \).
Subsequently, the growth model is adjusted by making both variables L and S as a function of time. L in the year 1800 is, of course, chosen to be smaller than in the year 2100. In-between it increases linearly with time. For S basically the same is done.

These variables are now labelled: \( L_{1800} \) and \( L_{2100} \), respectively \( S_{1800} \) and \( S_{2100} \).

Figure Appendix 4.2 shows the well-fitting result for: \( L_{1800} = 60, L_{2100} = 75, S_{1800} = 3 \) and \( S_{2100} = 4.4 \)

For information: the values \( L_{1800} = 60, L_{2100} = 70, S_{1800} = 3 \) and \( S_{2100} = 4.27 \) result in an equally perfect fit!

Based on this well-fitting growth model with the observations, this model is frozen for the period 1800-2017 in order to investigate what will be the development of the population in the future, varying only the variable S, so only \( S_{2100} \). The reason for this is that variable L is found to be much less sensitive. It turns out that in 2017 the variable S equals 4.008. Starting from this value, S decreases linearly down to \( S_{2100} \) in the year 2100. Figure Appendix 4.3 shows the results for \( S_{2100} = 2, 1 \) and 0.
Figure Appendix 4.3, with 3 possible growth scenarios in relation to the current growth

Resume

1. With the described simple growth model it is possible to reproduce perfectly the observed world population from the year 1800 to the present year.

2. The applied parameter values for the average age $L$ and the average number $S$ of people per pair that procreates again, all the way look realistic: $L_{1800} = 60$ and $L_{2017} = 71$ years, resp. $S_{1800} = 3$ and $S_{2017} = 4$. The increase of the latter parameter is representative of the global average increased human health.

3. The three possible future growth scenarios all show that the current one rises so steeply that only a drastic reduction of the variable $S$, translated into a drastic decrease of the global birth rate, can save nature on Earth and as a result mankind.
Epilogue

The total amount of heat energy in the atmosphere has been $15 \times 10^{23} \text{ J}$ for at least thousands of years.

The amount of increased heat energy in the atmosphere in 2015 is $5 \times 10^{21} \text{ J}$.

Relatively thus an increase of only 3 promille.

The total amount of heat energy in the Sea has been $15 \times 10^{26} \text{ J}$ for at least thousands of years.

The amount of increased heat energy in the Sea in 2015 is $6.4 \times 10^{23} \text{ J}$.

Relatively thus an increase of only 0.4 promille.

The crucial question is: is such a heating of the atmosphere and the Sea really disastrous for Earth’s nature and for mankind?

It seems that the disastrous consequences only occur during extreme weather conditions, such as heavy rainfall and extremely dry periods in random places around the world. Most likely ultimately caused by hot spots.

But should mankind in the first place not concentrate on reduction of the destruction and the pollution of nature?
References

[I] ftp://aftp.cmdl.noaa.gov/products/trends/co2/co2_mm_mlo.txt
[V1] https://advances.sciencemag.org/content/3/3/e1601545
[V1.1] http://assets.climatecentral.org/pdfs/March2016_HeatContentSeaLevel_WMO.pdf
[VII.1] https://Earthobservatory.nasa.gov/features/EnergyBalance
[VII.4] Climate and Atmospheric History of the Past 420,000 Years from the Vostok Ice Core, Antarctica
[VIII.3] https://www.indexmundi.com/facts/indicators/AG.SRF.TOTL.K2/rankings
[VIII.4] The Netherlands is warming more than twice as fast as the global average temperature
[IX.1] https://data.giss.nasa.gov/gistemp/grahps/graph_data/GISTEMP_Seasonal_Cycle_since_1880/graph.pdf
[IX.2] https://data.giss.nasa.gov/gistemp/tabledata_v3/GLB.Ts+dSST.txt
[IX.3] Satellite Global and Hemispheric Lower Tropospheric Temperature Annual Temperature Cycle
[X.1] https://www.researchgate.net/publication/314295190_A_high-end_sea_level_rise_probabilistic_projection_including_rapid_Antarctic_ice_sheet_mass_loss