Simulation of observable properties of a quantum object on a classical computer

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Abstract

Properties such as the energy and momentum of a quantum object can be calculated exactly in quantum theory, but they cannot be simulated on a classical computer. This is in part due to the fact that the physical nature of quantum objects is not yet understood (ontology problem). In this paper it is shown that it is possible to simulate observable properties of a quantum object on a classical computer. For this purpose, the wave describing the quantum object is considered as a physical element with a constant amplitude of a quarter of the Planck constant (Ψ_{max} =h/4=const.). As a result, the values of energy and momentum, as well as the de Broglie wavelength, can be simulated *without the aid of further parameters*.

This is expected to give new ideas to ontological issues.

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1 Introduction

Quantum theory comprises a well-proven mathematical set of rules. Their physical interpretation is still controversial today [1-5, 9]. Related to this is the unsolved problem of simulating observable properties of individual quantum objects on a classical computer [6].

In this paper, two simple assumptions about the nature of a quantum object are made and it is shown that properties such as energy, momentum and de Broglie wavelength of a single quantum object can be simulated with it.

2 Assumptions

In the major interpretations of quantum mechanics, such as the Copenhagen Interpretation and quantum Bayesianism, the wave representing the quantum object is considered to be a mathematical entity for which there is no equivalent in physical reality [7, 8].

For the purposes of simulation, the following assumptions are made in this paper:

- The function values of the wave have the unit of action (corresponds to the unit of angular momentum kg·m²/s).
- The amplitude of the wave is constant and has the value of a quarter of the Planck constant *h* (Figure 1):

$$|\Psi_{max}| = \frac{h}{4} = const. \approx 1,65 \cdot 10^{-34} \, kg \cdot m \cdot m/s$$
 (1)

 Ψ_{max} : Amplitude of the quantum wave

• The wave can be localized over a wide area of space. If the absolute amounts of the function values of a maximum (wave crest or wave trough) are added over all its locations (Figure 2), this always results in the constant value of h/4.

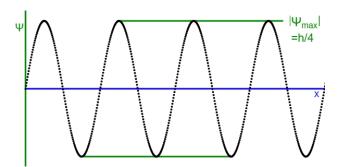


Figure 1: Schematic representation of a quantum wave with a constant amplitude of *h/4* in one spatial dimension.

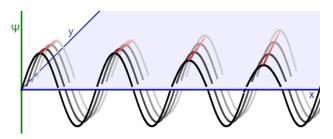


Figure 2: Schematic representation of a quantum wave in two spatial dimensions. The sum of the absolute values within the range of an amplitude (red lines) has a constant value of h/4.

Is it possible to reproduce observable properties of a quantum object by simulating it on a classical computer based on this assumption?

3 Simulations

3.1 Energy

In quantum mechanics, calculation of energy is done using the energy operator

$$\hat{E} = i\hbar \frac{\partial}{\partial t} \tag{2}$$

h: reduced Planck constant h = h/2πi: imaginary unit

acting on the wave function Ψ . In other words, it examines the development of Ψ over time.

In the context of this simulation, we consider the wave function Ψ describing the object not as an abstract mathematical construct, but as a wave with a constant amplitude of h/4 (equation 1). Based on equation 2, we simulate the change in the functional values of such a wave *over time*, to get the value of the energy:

$$\langle E \rangle = \left| \frac{\overline{\partial}}{\partial t} \Psi(t) \right| \tag{3}$$

Additional parameters are not required! The change in the wave over time provides the value of the energy *directly*.

As an example, we use a photon as a quantum object. The speed of propagation of this object thus corresponds to the speed of light. We simulate the change over time of the wave representing the photon for different wavelengths (Table 1). Only amounts are considered.

For comparison, the values calculated according to the equation E=hf are given in Table 1. Deviations from the simulated results are possible due to the limited number of simulation steps.

You can carry out the simulation for other wavelengths by yourself on the author's website:

https://www.quanten-krimi.de/pop/02/?ch0040?en

Conclusion: If a photon is described as a wave with a constant amplitude of h/4, the energy of the photon results directly from the mean time change of this wave.

3.2 Momentum

In quantum mechanics, calculation of momentum is done using the momentum operator

$$\hat{p}_x = -i\hbar \frac{\partial}{\partial x} \tag{4}$$

acting on the wave function Ψ . The development of Ψ over space is therefore considered. We limit ourselves to one spatial dimension x.

Based on equation 4, we simulate the *local* change in the functional values of a wave with constant amplitude of h/4 to get the value of the momentum:

$$\langle p_x \rangle = \left| \frac{\overline{\partial}}{\partial x} \Psi(x) \right| \tag{5}$$

The results of the simulations using a photon can also be found in table 1. In the last column, the values calculated using the equation $p=h/\lambda$ are given for comparison. You can test it by yourself:

https://www.quanten-krimi.de/pop/02/?ch0070?en

Conclusion: If a photon is described as a wave with a constant amplitude of h/4, the momentum of the photon results *directly* from the mean local change of this wave.

	λ [nm]	Energ	gy [kg·m·m/s·s]	Mome	ntum [kg·m/s]
		simulated mean temporal change of the quantum wave	calculated E=h·f		calculated p=h/λ
Red light	700	2,838 · 10 ⁻¹⁹	2,838 · 10 ⁻¹⁹	9,466 · 10 ⁻²⁸	9,466 · 10 ⁻²⁸
Blue light	450	4,414 · 10 ⁻¹⁹	4,414 · 10 ⁻¹⁹	1,472 · 10 ⁻²⁷	1,472 · 10-27
UV	300	6,622 · 10 ⁻¹⁹	6,621 · 10 ⁻¹⁹	2,209 · 10 ⁻²⁷	2,209 · 10 ⁻²⁷

Table 1: Energy and momentum of photons of different wavelengths λ . The values simulated on the basis of a quantum wave of constant amplitude are highlighted in yellow. The calculated values are given for comparison.

3.3 De Broglie wavelength of an electron

As the next quantum object we consider an electron. To do this, we build on the model of a photon used for the simulation as a quantum wave with a constant amplitude of h/4.

An electron, together with a positron, can be created from a photon by pairing. We investigate whether observable properties of an electron can also be simulated within the framework of the assumption made in equation 1.

The simplified model used for the purpose of the simulation represents an electron as a superposition of a the back and forth light wave. The wavelength of these "inner" waves (the two upper waves in Figure 3) is $2.4 \cdot 10^{-12}$ m in

the case of an electron that is not moving (Compton wavelength of the electron). This corresponds to about twice the wavelength of the photon required for pair formation.

When this object moves relative to an observer, the optical Doppler effect occurs: The wavelength of the partial wave *in* the direction of movement decreases:

$$\lambda_F = \lambda_{01} \sqrt{\frac{1 - \frac{v}{c}}{1 + \frac{v}{c}}} \tag{6}$$

 λ_0 : Wavelength of the inner wave when the object is at rest

 λ_F : Wavelength of the inner wave in the direction of movement

v: Speed of the object

c: Speed of light

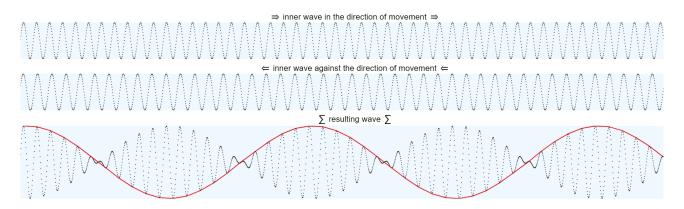


Figure 3: Superposition of two waves of different wavelengths and opposite directions of propagation. The enveloping wave (envelope) is shown in red.

speed of the electron [m/s]	Wavelength of the inner wave in the direction of movement [m]	wave opposite to the direc-	Wavelength of enveloping wave [m]	De Broglie wavelength of an electron according to λ=h/p [m]
10000	2,426229·10 ⁻¹²	2,426391·10 ⁻¹²	7.274·10 ⁻⁸	7.274·10 ⁻⁸
15000	2,426189·10 ⁻¹²	2,426432·10 ⁻¹²	4.849·10 ⁻⁸	4.849·10 ⁻⁸
80000	2,425663·10 ⁻¹²	2,426958·10 ⁻¹²	9.092·10 ⁻⁹	9.092·10 ⁻⁹

Table 2: De Broglie wavelength of an electron for different speeds. Values determined by superimposing two waves (yellow) and results calculated according to $\lambda=h/p$ (last column).

The wavelength of the partial wave *against* the direction of movement increases:

$$\lambda_b = \lambda_0 \sqrt{\frac{1 + \frac{v}{C}}{1 - \frac{v}{C}}} \tag{7}$$

 λ_b : Wavelength of the inner wave against the direction of movement

We obtain the frequencies f of the inner waves by means of the relationship $f=c/\lambda$ (c: speed of light).

As a result of the superposition of the partial waves, an enveloping wave forms ("envelope", Figure 3 below). Their frequency f_E results from:

$$f_E = \frac{f_F - f_B}{2} \tag{8}$$

Table 2 shows the wavelengths of the envelope obtained by simulation for some speeds. For comparison, you will find the values calculated using $\lambda = h/p$.

You can also carry out this simulation by yourself: https://www.quanten-krimi.de/pop/06/?ch0040?en

4 Motivation of some formulas

Now there are completely different options available to determine the energy and momentum of a quantum object:

- by calculation using the equations $E=h \cdot f$ and $p=h/\lambda$.
- by simulating the mean temporal or local change of a wave with a constant amplitude of h/4.

Is there any connection?

4.1 E=h·f

According to the simulation in chapter 3.1, the value of the energy of a quantum wave results from the mean change of the wave over time This statement should be formulated mathematically. We only consider amounts.

The wave function for a harmonic wave that only depends on time *t* is:

$$\Psi(t) = \Psi_{max} \cdot \sin(2\pi \cdot \frac{t}{T}) \tag{9}$$

 Ψ_{max} = Maximum value (amplitude) of Ψ , T = period duration

The 1st derivative with respect to the time *t* gives:

$$\Psi(t)' = \Psi_{max} \cdot \frac{2\pi}{T} \cdot \cos(2\pi \cdot \frac{t}{T})$$
 (10)

In order to determine the energy, we require the mean value $\overline{\Psi(t)}'$ of this function. The mean value of a unidirectional cosine function can be determined from its maximum value:

$$\overline{\Psi'} = \frac{2}{\pi} \cdot \Psi'_{max} \tag{11}$$

For the sake of clarity, we omit the amount symbols. We require the maximum value Ψ'_{max} . In equation 10, Ψ' is greatest when the cosine has its maximum possible value of 1:

$$\Psi(t)'_{max} = \Psi_{max} \cdot \frac{2\pi}{T} \cdot 1 \tag{12}$$

$$\Psi(t)'_{max} = \Psi_{max} \cdot \frac{2\pi}{T}$$
 (13)

Inserting equation 13 into equation 11, we have:

$$\overline{\Psi(t)'} = \frac{2}{\pi} \cdot \Psi_{max} \cdot \frac{2\pi}{T}$$
 (14)

$$\overline{\Psi(t)'} = \Psi_{max} \cdot \frac{4}{T} \tag{15}$$

The period T corresponds to the reciprocal of the frequency:

$$T = \frac{1}{f} \tag{16}$$

With this we replace T in equation 15:

$$\overline{\Psi(t)'} = \Psi_{max} \cdot 4 \cdot f \tag{17}$$

According to the assumption in equation 1, the amplitude of a quantum wave corresponds to a quarter of the Planck constant h. With this we replace Ψ_{max} in equation (17):

$$\overline{\Psi(t)'} = \frac{h}{4} \cdot 4 \cdot f \tag{18}$$

$$\overline{\Psi(t)'} = h \cdot f \tag{19}$$

The mean time change of a quantum wave can therefore be calculated from the product $h \cdot f$. According to the simulation in chapter 3.1, this change over time corresponds to the energy E of a quantum wave:

$$\overline{\Psi(t)'} = h \cdot f = E \tag{20}$$

Conclusion: The equation E=h: f results from the assumption that a quantum object is described as a wave with a constant amplitude of h/4. The energy of the quantum object corresponds directly to the mean temporal change of the wave.

4.2 p=h/λ

According to the simulation in chapter 3.2, the momentum of a quantum wave results from the mean local change of the wave. This statement should also be formulated mathematically.

The wave function for a harmonic wave that only depends on one spatial dimension x is:

$$\Psi(x) = \Psi_{max} \cdot \sin(2\pi \cdot \frac{x}{\lambda})$$
 (21)

 $\Psi_{max} = Maximum \ value \ (amplitude) \ of \ \Psi, \ \lambda = wavelength$

The 1st derivative of equation 22 with respect to the location *x* results in:

$$\Psi(x)' = \Psi_{max} \cdot \frac{2\pi}{\lambda} \cdot \cos(2\pi \cdot \frac{x}{\lambda})$$
 (22)

In order to determine the momentum, we require the mean value $\overline{\Psi(x)'}$ of this function (equation 11). For this, we have to determine the maximum value of the 1st derivative Ψ'_{max} . In equation 22, Ψ' is greatest when the cosine has its maximum possible value of I:

$$\Psi(x)'_{max} = \Psi_{max} \cdot \frac{2\pi}{\lambda} \cdot 1 \tag{23}$$

$$\Psi(x)'_{max} = \Psi_{max} \cdot \frac{2\pi}{\lambda}$$
 (24)

We insert equation 24 into equation 11:

$$\overline{\Psi(x)'} = \frac{2}{\pi} \cdot \Psi_{max} \cdot \frac{2\pi}{\lambda}$$
 (25)

$$\overline{\Psi(x)'} = \Psi_{max} \cdot \frac{4}{\lambda} \tag{26}$$

According to the assumption in equation 1, the amplitude of a quantum wave corresponds to a quarter of the Planck constant h. With this we replace Ψ_{max} in equation 26:

$$\overline{\Psi(x)'} = \frac{h}{4} \cdot \frac{4}{\lambda} \tag{27}$$

$$\overline{\Psi(x)'} = \frac{h}{\lambda} \tag{28}$$

The mean local change of a quantum wave can therefore be calculated from the quotient h/λ . According to the simulation in chapter 3.2, this local change corresponds to the momentum p of a quantum wave:

$$\overline{\Psi(x)'} = p = \frac{h}{\lambda} \tag{29}$$

Conclusion: The equation $p=h/\lambda$ results from the assumption that a quantum object is considered to be a wave with a constant amplitude of h/4. The momentum of the quantum object corresponds directly to the mean local change of the wave.

5 Summary

In order to simulate observable properties of a quantum object on a classical computer, the assumption was made that a quantum object can be described as a wave with a constant amplitude of h/4 (h = Planck constant). The energy of the quantum object then results directly from the mean temporal change of the wave, the momentum from its mean local change. If a model in the form of opposing light waves is used for quantum objects with a rest mass, the speed-dependent wavelength of the enveloping wave corresponds to the de Broglie wavelength observed.

The assumptions made here could allow a deeper understanding of what quantum objects actually are.

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