# **Goldbach Conjecture Proved Remarkably**

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## Abstract

The Goldbach Conjecture states that every even integer greater than 4 can be expressed as the sum of two odd primes. In this paper, the proof of Goldbach conjecture is guided by the approach for finding Goldbach partitions. This approach leads directly to evidence that every even integer greater than 4 is the sum of two odd primes. The main principle for finding Goldbach partitions from a known partition is the application of the addition axiom to a Goldbach partition equation. It is shown that given an equation for a Goldbach partition, one can produce a Goldbach partition for any even integer greater than 4. Beginning with the partition equations, one obtained Goldbach partitions for over 180 consecutive even integers. A consequent generalized procedure also produced Goldbach partitions for the non-consecutive even integers, 100; 1000; 372,131,740; and 400,000,001,1000. An equation derived for the Goldbach partition shows that every even integer greater than 4 can be written as the sum of two odd prime integers.

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## Preliminaries Introduction

The following is from the first page of the author's high school practical physics note book: Science is the systematic observation of what happens in nature and the building up of body of laws and theories to describe the natural world. Scientific knowledge is being extended and applied to everyday life. The basis of this growing knowledge is experimental work. To prove Goldbach conjecture, one would be guided by the approach for finding Goldbach partitions.

## **Finding Goldbach Partitions**

For communication purposes, let  $E_n$  be a positive even integer, and let  $P_r$  and  $P_s$  be two odd prime integers, where the subscript n is an even integer and the subscripts r and s are odd prime integers.; and r + s = n. Also,  $E_n = P_r + P_s$ .

The main principle for finding a Goldbach partition for a consecutive even integer from a known partition is the application of the addition axiom which states that if equal quantities are added to equal quantities, the sums are equal. One will begin with the Goldbach partition, 6 = 3 + 3, and apply the addition axiom to this equation to obtain partitions for larger even integers. In obtaining partitions for consecutive even integers, one will add 2 to both sides of the equation. For the next consecutive even integer, one will add a 2 to the present even integer, and one will also add a 2 to the right side of the equation. For the addition of a 2 to the right side of the equation, there are a number of possibilities.

**Possibility 1** (desirable): The addition of a 2 to any of the terms results in two prime integers. **Possibility 2:** One will inspect the two terms,  $P_r$  and  $P_s$  to determine which term if not prime would become prime when 2 is added to it, and add to it accordingly.

**Possibility 3:** If on adding a 2, to say,  $P_r$  one obtains a composite integer, one may add another 2 or more 2's until one obtains a prime integer; but for compensation, one would have to subtract the extra 2 or the extra 2's (added) from the other term  $P_s$ , noting that one is adding a single 2 to the left side and a single 2 to the right side of the equation. For examples, if one repeats the addition of 2 once, one will subtract a single 2 from the other term. If one repeats the addition twice, one will subtract 4 from the other term. If one repeats the 2-addition a third time, one will subtract a 6 from the other term. With experience, one would be able to determine which term to add a 2 or 2;s to in order to avoid the extra 2-addition. For the difference in the subtraction, the resulting difference cannot be less than 3. The difference must be a prime number.

An important skill for finding Goldbach partitions is changing composite integer sums to prime integer sums. With respect to the addends in the following equations, change any composite integer to a prime integer without changing the sum of the addends.

**1.** 70 = 31 + 39; **2.** 68 = 5 + 63; **3.** 100 = 31 + 69

**Solution:** For #1: 31 is prime but 39 is composite, To make 39 prime add 2 to 39 to obtain 41 which is prime, and perform the opposite operation on 31, that is, subtract 2 from 31 to obtain 29 which is also prime.

#### Solutions

<b>Given</b> : 70 = 31 + 39	<b>Given</b> : 68 = 5 + 63	<b>Given:</b> 100 = 31 + 69
70 = (31 - 2) + (39 + 2)	68 = (5+2) + (63-2))	100 = (31 - 2) + (69 + 2)
70 = 29 + 41 ( <b>Note</b> : 29 and 41 are prime		100 = 29 + 71 <b>Note</b> : 29 and 71 are prime

## **Examples on Finding Goldbach Partitions**

Example 1a. Given : 3, 5, 7 Required: Show that each of the even integers, 6,8,10 is either the sum of two of the above prime numbers or is twice any of the above prime numbers Solution: $E_n = P_r + P_s$ , $r + s = n$ 1. $E_6 = P_3 + P_3$ ; $6 = 3 + 3$ 2. $E_8 = P_5 + P_3$ ; $8 = 5 + 3$ 3. $E_{10} = P_7 + P_3$ ; $10 = 7 + 3$	Details From 1 to 2: On both sides: add 2 to 6 to obtain 8; add 2 to the first 3 to obtain 5 which is a prime; and keep the other 3 unchanged From 2 to 3: On both sides, add 2 to 8 to obtain 10; and add 2 to 5 to obtain 7 which is a prime number and keep the 3 unchanged
Example 1b. Given: 3, 5, 7, <u>11, 13, 17, 19</u> . Added Required: Show that each of the	<b>Details</b> From 2 to 3: On the left side , add 2 to 14 to obtain 16, On the right side, add 2 to 11 to obtain 13,
even integers, 12,14,16.18,20 is either the sum of two of the above prime numbers or is twice any of the above prime numbers	which is prime and desirable; one keeps the 3 unchanged.
Solution: , 1. $E_{12} = P_7 + P_5$ ; $12 = 7 + 5$ 2. $E_{14} = P_{11} + P_3$ ; $14 = 11 + 3$ 3. $E_{16} = P_{13} + P_3$ ; $16 = 13 + 3$ 4. $E_{18} = P_{13} + P_5$ ; $18 = 13 + 5$ 5. $E_{20} = P_{17} + P_3$ ; $20 = 17 + 3 = 13 + 7$	From 3 to 4: On the left side, add 2 to 16 to obtain 18, On the right side, keep the 13 (which is prime) and add 2 to the 3 to obtain 5 which is prime. Note if one added 2 to the 13, one would obtain 15, which is not prime; one would have to add another 2 to obtain 17 which is prime; and one would have to subtract a 2 from the 3 to obtain 1 which is not prime.
Details for 1b From Ia to Ib: Add 2 to the 3 and keep the 7. From 1 to 2: On the left side , add 2 to 12 to obtain 14, On the right side if one adds 2 to 7, one obtains 9 which is not prime and one adds another 2 to obtain 11, which is prime; and to compensate for the extra 2, one subtracts 2 from the 5 on	From 4 to 5 Two options: Option 1: : On the left side , add 2 to 18 to obtain 20, On the right side if one adds 2 to 13, one obtains 15 which is not prime and one adds another 2 to obtain 17, which is prime; and to compensate for the extra 2, one subtracts 2 from the 5 on the right side to obtain 3.

**Option 2:** On the right side, keep the 13 and add 2 to the 5 to obtain 7, which is prime and desirable.. Option 2 is faster.

the right side to obtain 3. Note above that one

could also add the 2 to the 5 to obtain 7 to

result in 14 = 7 + 7

Example 2	Example 3
<b>Given</b> : 3, 5, 7, 11, 13, 17, 19,	<b>Given</b> : 3, 5, 7, 11, 13, 17, 19,
23, 29	23, 29, 31, 37
added	added
<b>Required:</b> Show that each of the	<b>Required:</b> Show that each of the
even integers, 22, 24, 26, 28, 30. is either	even integers, 32, 34, 36, 38, 40. is either
the sum of two of the above prime numbers or is twice any of the above prime numbers	the sum of two of the above prime numbers or is twice any of the above prime numbers
or is twice any of the above prime numbers	
Solution:	Solution:
1. $E_{22} = P_{19} + P_3;  22 = 19 + 3$	1. $E_{32} = P_{29} + P_3; 32 = 29 + 3$
2. $E_{24} = P_{19} + P_5; 24 = 19 + 5$	2. $E_{34} = P_{31} + P_3;  34 = 31 + 3$
$3. E_{26} = P_{19} + P_7; 26 = 19 + 7$	3. $E_{36} = P_{31} + P_5;  36 = 31 + 5$
4. $E_{28} = P_{23} + P_5;  28 = 23 + 5$	4. $E_{38} = P_{31} + P_7;  38 = 31 + 7$
5. $E_{30} = P_{23} + P_7$ ; 30 = 23 + 7	5. $E_{40} = P_{37} + P_3;  40 = 37 + 3$
From Ib to 2: Add 2 to 20; add 2 the 17 to	From Ex 2 to Ex 3: Add 2 to the 30 to obtain
obtain 19 and keep the 3.	32; add 6 (why?) to 23 to obtain 29; subtract
From 1 to 2 Add 2 to 22,, keep the 19, and	the extra 4 added from 7 to obtain 3.
add 2 to 3 obtain 5.	<b>From 1 to 2</b> Add 2 to 32; add 2 to 29, keep the 3
<b>From 2 to 3:</b> Add 2 to 24 to obtain 26;,, keep	<b>From 2 to 3:</b> Add 2 to 34; keep the 31, and
the 19, and add 2 to 5 obtain 7. <b>From 3 to 4:</b> On the left side , add 2 to 26	add 2 to 3 obtain 5.
to obtain 28, On the right side, if one adds 2 to	From 3 to 4: Add 2 to 36; keep 31 & add 2 to 5.
19, one obtains 21 which is not prime; add	<b>From 4 to 5:</b> Add 2 to 38 to obtain 40. On the
another 2 to obtain 23, which is prime; to	right side, add 6 to 31 to obtain 37; to
compensate for the extra 2, one subtracts 2 from the 7 on the right side to obtain 5	compensate for the extra 4 added, subtract 4
From 4 to 5: Add 2 to 28 to obtain 30;,,	from the 7 on the right side to obtain 3., <b>Note</b> : One skipped the composites 33 and 35.
keep the 23, and add 2 to 5 obtain 7.	The skipped the composites 55 and 55.

Example 4	Example 5
<b>Given</b> : 3, 5, 7, 11, 13, 17, 19,	<b>Given</b> : 3, 5, 7, 11, 13, 17, 19,
23, 29, 31, 37, 41, 43, 47	23, 29, 31, 37, 41, 43, 47,
added 25, 25, 51, 57, 11, 15, 17	53, 59
<b>Required:</b> Show that each of the	added
even integers 42, 44, 46, 48, 50. is either	<b>Required:</b> Show that each of the
the sum of two of the above prime numbers or	even integers 52, 54, 56, 58, 60. is either the
is twice any of the above prime numbers	sum of two of the above prime numbers or is
Solution:	twice any of the above prime numbers
	Solution:
1. $E_{42} = P_{37} + P_5;  42 = 37 + 5$	1. $E_{52} = P_{47} + P_5;  52 = 47 + 5$
2. $E_{44} = P_{41} + P_3;  44 = 41 + 3$	2. $E_{54} = P_{47} + P_7$ ; 54 = 47 + 7
3. $E_{46} = P_{43} + P_3;  46 = 43 + 3$	3. $E_{56} = P_{53} + P_3;  56 = 53 + 3$
4. $E_{48} = P_{43} + P_5;  48 = 43 + 5$	4. $E_{58} = P_{53} + P_5; 58 = 53 + 5$
5. $E_{50} = P_{47} + P_3;  50 = 47 + 3$	5. $E_{60} = P_{53} + P_7;  60 = 53 + 7$
Example 6	Example 7
<b>Example 6</b> <b>Given</b> : 3, 5, 7, 11, 13, 17, 19,	<b>Example 7</b> <b>Given</b> : 3, 5, 7, 11, 13, 17, 19,
· ·	-
<b>Given</b> : 3, 5, 7, 11, 13, 17, 19,	Given: 3, 5, 7, 11, 13, 17, 19,
<b>Given</b> : 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, <u>61, 67</u> added	<b>Given</b> : 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, <u>71, 73, 79</u> added
<b>Given</b> : 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67 added <b>Required:</b> Show that each of the	<b>Given</b> : 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79 added <b>Required:</b> Show that each of the
<b>Given</b> : 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, <u>61, 67</u> added <b>Required:</b> Show that each of the even integers 62, 64, 66, 68, 70.is either	<b>Given</b> : 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79 added <b>Required:</b> Show that each of the even integers 72, 74, 76, 78, 80.is either
<b>Given</b> : 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, $\underbrace{61, 67}_{added}$ <b>Required:</b> Show that each of the even integers 62, 64, 66, 68, 70. is either the sum of two of the above prime numbers or	<b>Given</b> : 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79 added <b>Required:</b> Show that each of the even integers 72, 74, 76, 78, 80.is either the sum of two of the above prime numbers or
<b>Given</b> : 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, $61, 67$ added <b>Required:</b> Show that each of the even integers 62, 64, 66, 68, 70.is either the sum of two of the above prime numbers or is twice any of the above prime numbers	<b>Given</b> : 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, $71, 73, 79$ added <b>Required:</b> Show that each of the even integers 72, 74, 76, 78, 80.is either the sum of two of the above prime numbers or is twice any of the above prime numbers
Given: 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67 added Required: Show that each of the even integers 62, 64, 66, 68, 70. is either the sum of two of the above prime numbers or is twice any of the above prime numbers Solution:	Given: 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, $71, 73, 79$ added Required: Show that each of the even integers 72, 74, 76, 78, 80.is either the sum of two of the above prime numbers or is twice any of the above prime numbers Solution:
<b>Given</b> : 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, <u>61, 67</u> added <b>Required:</b> Show that each of the even integers 62, 64, 66, 68, 70. is either the sum of two of the above prime numbers or is twice any of the above prime numbers <b>Solution:</b> $1 \cdot E_{62} = P_{59} + P_3; 62 = 59 + 3$	<b>Given</b> : 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, $71, 73, 79$ added <b>Required:</b> Show that each of the even integers 72, 74, 76, 78, 80.is either the sum of two of the above prime numbers or is twice any of the above prime numbers <b>Solution:</b> 1. $E_{72} = P_{67} + P_5$ ; 72 = 67 + 5
<b>Given</b> : 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, <u>61, 67</u> added <b>Required:</b> Show that each of the even integers 62, 64, 66, 68, 70.is either the sum of two of the above prime numbers or is twice any of the above prime numbers <b>Solution:</b> $1 \cdot E_{62} = P_{59} + P_3; 62 = 59 + 3$ $2 \cdot E_{64} = P_{61} + P_3; 64 = 61 + 3$	<b>Given</b> : 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79 added <b>Required:</b> Show that each of the even integers 72, 74, 76, 78, 80.is either the sum of two of the above prime numbers or is twice any of the above prime numbers <b>Solution:</b> 1. $E_{72} = P_{67} + P_5$ ; 72 = 67 + 5 2. $E_{74} = P_{71} + P_3$ ; 74 = 71 + 3
Given: 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, $61, 67$ added Required: Show that each of the even integers 62, 64, 66, 68, 70.is either the sum of two of the above prime numbers or is twice any of the above prime numbers Solution: $1. E_{62} = P_{59} + P_3; 62 = 59 + 3$ $2. E_{64} = P_{61} + P_3; 64 = 61 + 3$ $3. E_{66} = P_{61} + P_5; 66 = 61 + 5$	Given: 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, $71, 73, 79$ added Required: Show that each of the even integers 72, 74, 76, 78, 80.is either the sum of two of the above prime numbers or is twice any of the above prime numbers Solution: 1. $E_{72} = P_{67} + P_5$ ; 72 = 67 + 5 2. $E_{74} = P_{71} + P_3$ ; 74 = 71 + 3 3. $E_{76} = P_{73} + P_3$ ; 76 = 73 + 3
Given: 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, $\underbrace{61, 67}_{added}$ Required: Show that each of the even integers 62, 64, 66, 68, 70. is either the sum of two of the above prime numbers or is twice any of the above prime numbers Solution: 1. $E_{62} = P_{59} + P_3$ ; $62 = 59 + 3$ 2. $E_{64} = P_{61} + P_3$ ; $64 = 61 + 3$ 3. $E_{66} = P_{61} + P_5$ ; $66 = 61 + 5$ 4. $E_{68} = P_{61} + P_7$ ; $68 = 61 + 7$	Given: 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79 added Required: Show that each of the even integers 72, 74, 76, 78, 80.is either the sum of two of the above prime numbers or is twice any of the above prime numbers Solution: 1. $E_{72} = P_{67} + P_5$ ; 72 = 67 + 5 2. $E_{74} = P_{71} + P_3$ ; 74 = 71 + 3 3. $E_{76} = P_{73} + P_3$ ; 76 = 73 + 3 4. $E_{78} = P_{73} + P_5$ ; 78 = 73 + 5
Given: 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, $61, 67$ added Required: Show that each of the even integers 62, 64, 66, 68, 70.is either the sum of two of the above prime numbers or is twice any of the above prime numbers Solution: $1. E_{62} = P_{59} + P_3; 62 = 59 + 3$ $2. E_{64} = P_{61} + P_3; 64 = 61 + 3$ $3. E_{66} = P_{61} + P_5; 66 = 61 + 5$	Given: 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, $71, 73, 79$ added Required: Show that each of the even integers 72, 74, 76, 78, 80.is either the sum of two of the above prime numbers or is twice any of the above prime numbers Solution: 1. $E_{72} = P_{67} + P_5$ ; 72 = 67 + 5 2. $E_{74} = P_{71} + P_3$ ; 74 = 71 + 3 3. $E_{76} = P_{73} + P_3$ ; 76 = 73 + 3

Example 8	Example 9
<b>Given</b> : 3, 5, 7, 11, 13, 17, 19,	<b>Given</b> : 3, 5, 7, 11, 13, 17, 19,
23, 29, 31, 37, 41, 43, 47,	23, 29, 31, 37, 41, 43, 47,
53, 59, 61, 67, 71, 73, 79	53, 59,61,67,71,73,79, 83,
83, 89	89, 97
added <b>Required:</b> Show that each of the even integers 82, 84, 86, 88, 90. is either the sum of two of the above prime numbers or is twice any of the above prime numbers	added <b>Required:</b> Show that each of the even integers 92, 94, 96, 98, 100.is either the sum of two of the above prime numbers or is twice any of the above prime numbers
Solution:	Solution:
1. $E_{82} = P_{79} + P_3;  82 = 79 + 3$	<b>1.</b> $E_{92} = P_{89} + P_3;  92 = 89 + 3$
2. $E_{84}^{62} = P_{79} + P_5; 84 = 79 + 5$	2. $E_{94} = P_{89} + P_5;  94 = 89 + 5$
3. $E_{86} = P_{83} + P_3; 86 = 83 + 3$	3. $E_{96} = P_{89} + P_7;  96 = 89 + 7$
4. $E_{88} = P_{83} + P_5; 88 = 83 + 5$	4. $E_{98} = P_{79} + P_{19};  98 = 79 + 19$
5. $E_{90} = P_{83} + P_7;  90 = 83 + 7$	5. $E_{100} = P_{97} + P_3;  100 = 97 + 3$
Example 10	Example 11
<b>Given</b> : 3, 5, 7, 11, 13, 17, 19,	<b>Given</b> : 3, 5, 7, 11, 13, 17, 19,
23, 29, 31, 37, 41, 43, 47,	23, 29, 31, 37, 41, 43, 47,
53, 59,61,67,71,73,79, 83,	53, 59, 61, 67, 71, 73, 79, 83,
89, 97, 101, 103, 107, 109	89, 97, 101, 103, 107, 109, 113
added	added
<b>Required:</b> Show that each of the	<b>Required:</b> Show that each of the
even integers 102,104,106,108,110.is	even integers 112,114,116,118,120.is either the sum of two of the above prime numbers or
either the sum of two of the above prime numbers or is twice any of the above prime	is twice any of the above prime numbers
numbers	Colution
Solution:	Solution: 1 = P + P + 112 = 100 + 3
<b>Solution:</b> <b>1.</b> $E_{102} = P_{97} + P_5;  102 = 97 + 5$	<b>1.</b> $E_{112} = P_{109} + P_3;  112 = 109 + 3$
1. $E_{102} = P_{97} + P_5$ , $102 = 97 + 3$ 2. $E_{104} = P_{101} + P_3$ ; $104 = 101 + 3$	2. $E_{114} = P_{109} + P_5;  114 = 109 + 5$ 2. $E_{114} = P_{109} + P_5;  116 = 112 + 2$
2. $E_{104} = P_{101} + P_3$ ; $104 = 101 + 3$ 3. $E_{106} = P_{103} + P_3$ ; $106 = 103 + 3$	3. $E_{116} = P_{113} + P_3$ ; 116 = 113 + 3
	4. $E_{118} = P_{113} + P_5; 118 = 113 + 5$
4. $E_{108} = P_{103} + P_5;  108 = 103 + 5$ 5. $E = P_{103} + P_{103} + P_{103} + 7$	5. $E_{120} = P_{113} + P_7;  120 = 113 + 7$
5. $E_{110} = P_{103} + P_7$ ; 110 = 103 + 7	

Example 12	Example 13
<b>Example 12</b> <b>Given</b> : 3, 5, 7, 11, 13, 17, 19,	<b>Example 13</b> <b>Given</b> : 3, 5, 7, 11, 13, 17, 19,
23, 29, 31, 37, 41, 43, 47,	23, 29, 31, 37, 41, 43, 47,
	, , , , , , , , ,
53, 59, 61, 67,71,73,79, 83,	53, 59, 61, 67,71,73,79, 83,
89, 97, 101, 103, 107, 109,	89, 97, 101, 103, 107, 109,
113, <u>127</u> added	113, 127, 131, 137, 139
<b>Required:</b> Show that each of the	added <b>Required:</b> Show that each of the
even integers 122,124,126,128,130.is	even integers 132,134,136,138,140.
either the sum of two of the above prime	is either the sum of two of the above prime
numbers or is twice any of the above prime numbers	numbers or is twice any of the above
	prime numbers
Solution:	Solution:
<b>1.</b> $E_{122} = P_{109} + P_{13};  122 = 109 + 13$	<b>1.</b> $E_{132} = P_{127} + P_5;  132 = 127 + 5$
2. $E_{124} = P_{113} + P_{11};  124 = 113 + 11$	2. $E_{134} = P_{131} + P_3;  134 = 131 + 3$
3. $E_{126} = P_{113} + P_{13};  126 = 113 + 13$	3. $E_{136} = P_{131} + P_5$ ; 136 = 131 + 5
4. $E_{128} = P_{109} + P_{19};$ 128 = 109 + 19	4. $E_{138} = P_{131} + P_7$ ; 138 = 131 + 7
5. $E_{130} = P_{127} + P_3;$ 130 = 127 + 3	5. $E_{140} = P_{137} + P_3$ ; 140 = 137 + 3
Example 14	Example 15
<b>Given</b> : 3, 5, 7, 11, 13, 17, 19,	<b>Given</b> : 3, 5, 7, 11, 13, 17, 19,
23, 29, 31, 37, 41, 43, 47,	23, 29, 31, 37, 41, 43, 47,
53, 59, 61, 67,71,73,79, 83,	53, 59, 61, 67,71,73,79, 83,
89, 97, 101, 103, 107, 109,	89, 97, 101, 103, 107, 109,
113, 127, 131, 137, 139, 149	113, 127, 131, 137, 139, 149,
added	151, 157
<b>Required:</b> Show that each of the even integers 142, 144, 146, 148, 150. is	added
either the sum of two of the above prime	<b>Required:</b> Show that each of the
numbers or is twice any of the above prime	even integers 152, 154, 156, 158, 160.is either the sum of two of the above prime
numbers	numbers or is twice any of the above prime
Solution:	numbers
<b>1.</b> $E_{142} = P_{139} + P_3;  142 = 139 + 3$	Solution:
2. $E_{144} = P_{139} + P_5$ ; 144 = 139 + 5	<b>1.</b> $E_{152} = P_{149} + P_3$ ; 152 = 149 + 3
3. $E_{146} = P_{139} + P_7$ ; 146 = 139 + 7	<b>2.</b> $E_{154} = P_{151} + P_3$ ; 154 = 151 + 3
4. $E_{148} = P_{137} + P_{11};$ 148 = 137 + 11	<b>3.</b> $E_{156} = P_{151} + P_5$ ; 156 = 151 + 5
5. $E_{150} = P_{139} + P_{11};$ 150 = 139 + 11	<b>4.</b> $E_{158} = P_{151} + P_7$ ; 158 = 151 + 7
	<b>5.</b> $E_{160} = P_{157} + P_3$ ; 160 = 157 + 3

Example 16 Example 17 Given: 3, 5, 7, 11, 13, 17, 19, Given: 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97, 101, 103, 107, 109, 89, 97, 101, 103, 107, 109, 113, 127, 131, 137, 139, 149, 151, 157 113, 127, 131, 137, 139, 149, 151, 163, 167 157, 163, 167, 173, 179 added added **Required:** Show that each of the **Required:** Show that each of the even integers 172, 174, 176, 178,180. is even integers 162, 164, 166, 168, 170. either the sum of two of the above prime is either the sum of two of the above prime numbers or is twice any of the above prime numbers or is twice any of the above prime numbers numbers Solution: Solution: **1.**  $E_{172} = P_{167} + P_5$ ; 172 = 167 + 5 **1.**  $E_{162} = P_{157} + P_5$ ; 162 = 157 + 5 2.  $E_{174} = P_{167} + P_7$ ; 174 = 167 + 7 2.  $E_{164} = P_{157} + P_7$ ; 164 = 157 + 7 3.  $E_{176} = P_{173} + P_3$ ; 176 = 173 + 3 3.  $E_{166} = P_{163} + P_3$ ; 166 = 163 + 3 4.  $E_{178} = P_{173} + P_5$ ; 178 = 173 + 5 4.  $E_{168} = P_{163} + P_5$ ; 168 = 163 + 5 5.  $E_{180} = P_{173} + P_7$ ; 180 = 173 + 7 5.  $E_{170} = P_{167} + P_3$ ; 170 = 167 + 3

Example 18 Example Extra 1:T 1,000 Here, one will skip the even integers Given: 3, 5, 7, 11, 13, 17, 19, 192-940, and jump to the even integers 23, 29, 31, 37, 41, 43, 47, 992, 994, 996, 998, 1000. 53, 59, 61, 67, 71, 73, 79, 83, Given: 3, 5, 7, 11, 13, 17, 19, 89, 97, 101, 103, 107, 109, 23, 29, 31, 37, 41, 43, 47, 113, 127, 131, 137, 139, 149, 151, 53, 59, 61, 67, 71, 73, 79, 83, 157, 163, 167, 173, 179, 181 89, 97, 101, 103, 107, 109, added 113, 127, 131, 137, 139, 149, 151, **Required:** Show that each of the 157, 163, 167, 173, 179, 181..... even integers 182, 184, 186, 188, 190. 977, 983, 991, 997 is either the sum of two of the above prime numbers added or is twice any of the above prime numbers **Required:** Show that each of the even integers 992, 994, 996, 998, 1000. Solution: is either the sum of two of the above prime **1.**  $E_{182} = P_{179} + P_3$ ; 182 = 179 + 3 numbers or is twice any of the above prime 2.  $E_{184} = P_{181} + P_3$ ; 184 = 181 + 3 numbers Solution: 3.  $E_{186} = P_{181} + P_5$ ; 186 = 181 + 5 **1.**  $E_{992} = P_{919} + P_{73}; 992 = 919 + 73$ 4.  $E_{188} = P_{181} + P_7$ ; 188 = 181 + 7 **2.**  $E_{994} = P_{991} + P_3$ ; 994 = 991 + 3 5.  $E_{190} = P_{179} + P_{11}$ ; 190 = 179 + 11 **3.**  $E_{996} = P_{991} + P_5$ ; 996 = 991 + 5 **4.**  $E_{998} = P_{991} + P_7$ ; 998 = 991 + 7 5.  $E_{1000} = P_{997} + P_3$ ; 1000 = 997 + 3 Observe also that we used the first odd prime number to change 997 to 1000,

#### Example Extra 2: To 1,000,000

Here, one will skip the even integers 1,002-999990, and jump to the even integers 999992, 999994, 999996, 999998,1,000,000.

Given: 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67,71,73,79, 83, 89, 97, 101, 103, 107, 109, 113, 127, 131, 137, 139, 149, 151, 157, 163, 167, 173, 179,181... 977, 983, 991,997... 999931 999953, 999959, 999961,999983

added **Required:** Show that each of the even integers 999992, 999994, 999996, 999998,1,000,000.,is either the sum of two of the above prime numbers or is twice any of the above prime numbers **Solution:**.

- 1.  $E_{999,992} = P_{999,979} + P_{13}; 999,992 = 999,979 + 13$
- 2.  $E_{999,994} = P_{999,983} + P_{11}; 999,994 = 999,983 + 11$
- 3.  $E_{999,996} = P_{999,983} + P_{13}$ ; 999,996 = 999,983 + 13
- 4.  $E_{999,998} = P_{999,979} + P_{19}; 999,998 = 999,979 + 19$
- 5.  $E_{1,000,000} = P_{999,983} + P_{17}$ ; 1,000,000 = 999,983 + 17

Observe that we used the sixth odd prime number, 17, to change 999,983 to 1000,000.

#### Example Extra 3a :To 399,999,842

Here, one will skip the even integers.....and jump to the even integers 399,999,834; 399,999,834; 399,999,838; 399,999,840; 399,999,842

Given: 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67,71,73,79, 83, 89, 97, 101, 103, 107, 109, 113, 127, 131, 137, 139, 149, 151, 157, 163, 167, 173, 179,181... 977, 983, 991,997...999931 999953, 999959, 999961,999983, 399,999,781; 399,999,823; 399,999,827; 399,999,829,399,999,839

added

**Required:** Show that each of the

even integers 399,999,834; 399,999,836; 399,999,838; 399,999,840; 399,999,842 is either the sum of two of the above prime numbers or is twice any of the above prime numbers **Solution:** 

- 1.  $E_{399,999,834} = P_{399,999,829} + P_5$ ; 399,999,834 = 399,999,829 + 5
- 2.  $E_{399,999,836} = P_{399,999,829} + P_7$ ; 399,999,836 = 399,999,829 + 7
- 3.  $E_{399,999,838} = P_{399,999,827} + P_{11};$  399,999,838 = 399,999,827 + 11

4.  $E_{399,999,840} = P_{399,999,829} + P_{11}; 399,999,840 = 399,999,829 + 11$ 

5.  $E_{399,999,842} = P_{399,999,839} + P_3$ ; 399,999,842 = 399,999,839 + 3

Observe that we used the first odd prime number, 3, to change 399,999,839 to 399,999,842

#### Extra 3b

- 1.  $E_{3,399,999,834} = P_{3,399,999,797} + P_{37}; 3,399,999,834 = 399,999,797 + 37$
- 2.  $E_{3,399,999,836} = P_{3,399,999,763} + P_{73}; 3,399,999,836 = 3,399,999,763 + 73$
- 3.  $E_{3,399,999,838} = P_{3,399,999,797} + P_{41};$  3,399,999,838 = 3,399,999,797 + 41
- 4.  $E_{3,399,999,840} = P_{3,399,999,797} + P_{43}; 3,399,999,840 = 3,399,999,797 + 43$
- 5.  $E_{3,399,999,842} = P_{399,999,763} + P_{79}; 3,399,999,842 = 3,399,999,763 + 79$
- 6.  $E_{500,000,000,246} = P_{500,000,000,243} + P_3$ ; 500,000,000,246 = 500,000,000,243 + 3
- 7.  $E_{400,000,001,000} = P_{400,000,000,997} + P_3;$  400,000,001,000 = 400,000,000,997 + 3
- 8.  $E_{372,131,740} = P_{372,131,737} + P_3; 372,131,740 = 372,131,737 + 3$

### Condensed Goldbach Partition Production Consecutive Descendants

The following table condenses the processes involved in examples on page 4-12, and will show that every even integer greater than 4 can be expressed as the sum of two odd primes, because the process will not terminate and can continue indefinitely. Review the instructions on page 3, and review the examples on page 4-12. One will begin with the partition equation 6 = 3 + 3, and apply the addition of 2 to both sides of the equation to produce the partition for the next even number, 8. From the partition equation, 8 = 5 + 3, one will repeat the 2-addition process to obtain the partition for the next even integer, 10. From the partition for 10, the process will continue indefinitely and every even integer would be partitioned as the sum of two odd primes.

**•** 1

<b>Basis:</b> $n = 2k = 6$ ,	
1. 6 = 3 + 3	<b>26.</b> 56 = 53 + 3 = 37 + 19
<b>2.</b> 8 = 5 + 3	<b>27.</b> 58 = 53 + 5 = 41 + 17
<b>3</b> . 10 = 7 + 3	<b>28.</b> 60 = 53 + 7 = 43 + 17 = 41 + 19
<b>4</b> . 12 = 7 + 5	<b>29.</b> 62 = 59 + 3 = 43 + 19
<b>5</b> . 14 = 7 + 7 = 11 + 3	<b>30.</b> 64 = 59 + 5 = 47 + 17
<b>6.</b> 16 = 11 + 5 = 13 + 3	<b>31.</b> 66 = 59 + 7 = 47 + 19
<b>7.</b> 18 = 13 + 5	<b>32.</b> 68 = 61 + 7
8.20 = 13 + 7	<b>33.</b> 70 = 67 + 3 = 59 + 11
<b>9.</b> $22 = 17 + 5 = 11 + 11$	<b>34.</b> 72 = 67 + 5 = 59 + 13
<b>10.</b> $24 = 19 + 5 = 13 + 11$	<b>35.</b> 74 = 71 + 3 = 61 + 13 = 67 + 7
<b>11.</b> 26 = 19 + 7 = 23 + 3 = 13 + 13	<b>36.</b> 76 = 71 + 5 = 59 + 17
<b>12.</b> $28 = 23 + 5 = 17 + 11$	<b>37.</b> 78 = 71 + 7 = 61 + 17
<b>13.</b> 30 = 23 + 7 = 17 + 13	<b>38.</b> 80 = 73 + 7 = 61 + 19 =
<b>14.</b> 32 = 29 + 3 = 21 + 11	<b>39.</b> 82 = 79 + 3 = 59 + 23
<b>15.</b> 34 = 31 + 3 = 29 + 5	<b>40.</b> 84 = 79 + 5 = 61 + 23
<b>16.</b> 36 = 31 + 5 = 29 + 7	<b>41.</b> 86 = 79 + 7
<b>17.</b> 38 = 31 + 7	<b>42.</b> 88 = 83 + 5
<b>18.</b> 40 = 37 + 3 = 29 + 11	<b>43.</b> 90 = 83 + 7
<b>19.</b> 42 = 37 + 5 = 29 + 13	<b>44.</b> 92 = 89 + 3
<b>20.</b> 44 = 37 + 7 = 31 + 13	<b>45.</b> 94 = 89 + 5
<b>21.</b> 46 = 41 + 5 = 29 + 17	<b>46.</b> 96 = 89 + 7
<b>22.</b> 48 = 43 + 5 = 29 + 19	<b>47.</b> 98 = 79 + 19
<b>23.</b> 50 = 43 + 7 = 31 + 19	<b>48.</b> 100 = 83 + 17
<b>24.</b> 52 = 47 + 5 = 29 + 23	<b>49.</b> 102 = 83 + 19
<b>25.</b> 54 = 47 + 7 = 31 + 23	<b>50.</b> 104 = 97 + 7

Above, beginning with the partition equation , 6 = 3 + 3, the partition equations #2 to #50 were produced. Also, knowing partition #5, above, one can also obtain partition #39 and vice versa. In the table, there are fifty Goldbach partitions. As shown below, if one skips partitions for 8–82, above, one can also obtain partitions for 84, 100 as well as partitions for 1000, 372,131,740, and 400,000,001,000,

Finding partitions for 84, 100, 1000, 372,131,740, and 400,000,001,000 and others

1. From 6 to 84 6 = 3 + 3 6 + (84 - 6) = 3 + (3 + 84 - 6) 6 + (78) = 3 + (3 + 78) 84 = 3 + 81 (Note : 81 is not prime) 84 = (3 + 2) + (81 - 2)

84 = 5 + 79 or 79 + 5. Note: 79 is prime (...Note above that if one adds 2 to 81, one obtains 83 which is prime, but on subtracting 2 from 3, one would get 1, which is not prime)

2. From 6 to 100 6 = 3 + 3 6 + (100 - 6) = 3 + (3 + 100 - 6) 6 + (94) = 3 + (3 + 94)100 = 3 + 97 Note: 97 is prime.

**3a**. From 6 to 1000 6 = 3 + 36 + (1000 - 6) = 3 + (3 + (1000 - 6))6 + 994 = 3 + (3 + 994)1000 = 3 + (3 + 994)1000 = 3 + 997 Note: 997 is prime **3b** From 84 to 6 84 = 5 + 7984 + (6 - 84) = 5 + (79 + (6 - 84))84 - 78 = 5 + 1 Note : 1 is not prime 6 = 3 + 3 (Add 2 to 1 and subtract 2 from 5) **3c** From 92 to 6 92 = 3 + 8992 + (6 - 92) = 3 + (89 + 6 - 92)92 - 86 = 3 + 89 - 866 = 3 + 3

#### **4.** From 6 to 372,131,740

4.

Three hundred seventy-two million, one hundred thirty-one thousand, seven hundred, forty 6 + (372,131,740 - 6) = 3 + (3 + (372,131,740 - 6))6 + (372,131,734) = 3 + (3 + (372,131,734))372,131,740 = 3 + 372,131,737

Note: 372,131,737 is prime

#### 5. From 6 to 400,000,001,000

5. Four hundred billion, one thousand 6 = 3 + 3
6 + (400,000,001,000 - 6) = 3 + (3 + 400,000,001,000 - 6)
6 + (400,000,000,994) = 3 + (3 + (400,000,000,994)
400,000,001,000 = 3 + 400,000,000,997
Note : 400,000,000,997 is prime

The repetition in the above partition processes is similar to compound interest calculations, except in the operations involved. For example, to find the amount at the end of 20 years in a compound interest calculation, one can find the interest for the first year, add the interest to the principal, followed by finding the interest on the new amount, and repeat the process 20 times., However, since there is a formula for determining the amount after 20 years, one does not have to use a repetitive process. Similarly, in Goldbach calculations, if one can find a formula which can be used to find a Goldbach partition for every even integer, one would not have to perform the consecutive calculations from p, 3-14. Therefore, on the next page, one will derive a formula for finding a Goldbach partition for every even integer, and such derivation will show that every even integer greater than 4 can be expressed as the sum of two odd primes.

## **Goldbach Conjecture Proved Remarkably**

**Given**: 1. A known Goldbach partition of the even integer  $E_1 = P_1 + P_2$ , where  $P_1$  and  $P_2$  are prime odd integers. 2. The even integer,  $E_n$ , (n > 4) whose partition is to be determined...

**Required:** To show that the even integer  $E_n$  has a Goldbach partition,

**Plan:** Let  $E_n = P_r + P_s$ , where  $P_r$  and  $P_s$  are prime odd integers. The proof would be complete after finding a general formula for  $E_n$  for a Goldbach partition equation.

#### Proof

#### Statements

- **1**. $E_1$  is an even integer
- **2**.  $P_1$  and  $P_2$  are prime odd integers

**3.** 
$$E_1 = P_1 + P_2$$

**4.** 
$$E_1 + (E_n - E_1) = P_1 + (P_2 + (E_n - E_1))$$

**5.**  $E_n = P_1 + (P_2 + E_n - E_1)$ 

**6.** In statement 5, above,  $P_1$  is an odd prime integer

7. Case A:  $(P_2 + E_n - E_1)$  is prime (desirable),  $P_r = P_1$  and  $P_s = (P_2 + E_n - E_1)$   $\boxed{E_n = P_r + P_s = P_1 + (P_2 + E_n - E_1)}$ ; and the proof is complete.

**Case B:**  $(P_2 + E_n - E_1)$  is **not** prime. The addition or subtraction of a 2 or 2 's would make  $(P_2 + E_n - E_1)$  become prime, However, the 2 or 2's added or subtracted must be subtracted from or added to  $P_1$ .

**Case B1**:  $P_1 = 3$ ;  $p_s = (P_2 + E_n - E_1) - 2t$ ;  $p_r = 3 + 2t$ , where t is the number of times 2 is subtracted before primality occurs.  $E_n = P_r + P_s = \boxed{(3 + 2t) + \boxed{(P_2 + E_n - E_1) - 2t}}$  **Case B2**:  $P_1 > 3$ ;  $P_s = (P_2 + E_n - E_1) \pm 2t$  and  $P_r = P_1 \mp 2t$ . After the inevitable successful changes in  $P_1$  and  $(P_2 + E_n - E_1)$ ,  $E_n = P_r + P_s = \boxed{(P_1 \pm 2t) + \boxed{(P_2 + E_n - E_1) \mp 2t}}$ , As  $n \rightarrow \infty$ , the general Goldbach partition equation for  $E_n$ . would still be given by  $E_n = P_1 + (P_2 + E_n - E_1)$ , which will always be defined and never zero; and where  $E_1$ ,  $P_1$ ,  $P_2$ , are from any known Goldbach partition equation. Therefore, every even integer,  $E_n$ can be expressed as the sum of two odd primes; and the proof is complete.

#### Reasons

1. Given

2. Given

**3.** .Given

- **4.** Addition axiom (Equals added to equals) E = E = difference between even integers
- $E_n E_1$  = difference between even integers.
- 5. Simplifying the left-side

**6**. Given

7. There are infinitely many primes and the addition or subtraction would ultimately make  $(P_2 + E_n - E_1)$  become prime. Note:  $E_1, E_n, P_1, P_2, P_r$  and  $P_s$  are all positive integers.  $(P_2 + E_n - E_1)$  is also a positive integer.

### Discussion

From above, generally,  $E_n = P_1 + (P_2 + E_n - E_1)$ , where  $E_1$ ,  $P_1$ ,  $P_2$ , are from any known Goldbach partition  $E_1 = P_1 + P_2$ . If  $(P_2 + E_n - E_1)$  is prime, there is no more work to be done, and one would have found a Goldbach partition for the even number,  $E_n$ ; However, if it is not prime, one has to apply cases B1 and B2, above. For example, in the table for Condensed Goldbach Partition Production (p.13), one can obtain Goldbach partition # 36 from partition #48 and vice versa. Thus by applying the derived formula, one can obtain a Goldbach partition for any even integer greater than 4.

For examples on Case A of the proof, see Example 2, 3a, 4 and 5 on page 14. For Case B1, see Example 1, p.14. For Case B2, see Example 3, page 5 ("From 4 to 5"). For more examples on the above cases, see pages 3-12

Interestingly, one can also obtain the partition equation 6 = 3 + 3 from any other partition equation, as in examples 3b and 3c, p.14. Such a result is very convincing that every even integer can be written as the sum of two odd primes. Thus, given a Goldbach partition of an even integer, by hand, one can find, without exception, a Goldbach partition for any other even integer, within minutes.

# Conclusion

It has been shown in this paper that every even integer greater than 4 can be expressed as the sum of two odd primes. The proof was guided by the approach the author used in finding Goldbach partitions. The approach for finding the partitions led directly to evidence that every even integer greater than 4 is the sum of two odd primes. The main principle for finding Goldbach partitions from a known partition is the application of the addition axiom to a Goldbach partition equation. It was shown that given an equation for a Goldbach partition, one can produce a Goldbach partition for any even integer greater than 4. Beginning with the partition equation, 6 = 3 + 3, and applying the addition of a 2 to both sides of this equation sequentially and repeatedly, one obtained Goldbach partitions for over 180 consecutive even integers. Also, a derived formula was used successfully to find partitions for the nonconsecutive even integers, 100; 1000; 372,131,740; and 400,000,001,1000. It is concluded that, knowing a single Goldbach partition equation for an even integer, one can by hand, find a Goldbach partition quickly for any other even integer.

#### References

- **1.** The approach used in covering Goldbach conjecture in this paper is similar to the approach the author used in proving Beal Conjecture (vixra: 2001.0694).
- **2.** In covering the Goldbach conjecture, one must have quick access to the list of the prime numbers, Some places on the web for the lists of prime numbers are at: 1.www.mathsfun.com; 2. CalculatorSoup.com.

## Extra Conjecture Humor

## **Conversation Between the Even Integers 6 and 84**

**Mr. 84 speaks:** Mr. 6. I can see that you have a Goldbach partition. Can you help me get my own Goldbach partition?

Mr. 6 answers: Yes, I can help you using my own Goldbach partition as in box A below:

A 6 = 3 + 3 6 + (84 - 6) = 3 + (3 + 84 - 6) 6 + (78) = 3 + (3 + 78) 84 = 3 + 81 (Note : 81 is not prime) 84 = (3 + 2) + (81 - 2)84 = 5 + 79 or 79 + 5. Note: 79 is prime

**B** 84 = 5 + 79 84 + (6 - 84) = 5 + (79 + (6 - 84)) 84 - 78 = 5 + 1 Note: 1 is not prime **6** = **3** + **3** (Add 2 to 1 and subtract 2 from 5)

Mr. 84 speaks: Thank you Mr. 6.

A week later, Mr. 84 meets Mr. 6 and Mr. 6 has no Goldbach partition.

Mr. 84 speaks: Mr. 6, where is your Goldbach partition?

Mr. 6 answers I lost my partition.

**Mr. 84 speaks** without hesitation: Mr. 6, I can help you get your Goldbach partition back as in box **B** above.

Mr. 6 speaks: Thank you very much, Mr. 84. I got my Goldbach partition back.

Mr. 84 speaks: Don't mention. You were kind to me, the first time we met.

Mr. 84 speaks: Here, comes my neighbor, Mr. 86, without a Goldbach partition. From my partition, I can easily get Mr. 86 a partition as in box C below

> C 84 = 5 + 79 84 + 2 = (5 + 2) + 79**86 = 7 + 79** (Add 2 to 84 and add 2 to 5)

Mr. 86 speaks: Thank you Mr. 84. I have a Goldbach partition for the first time.

Mr. 6 speaks to Mr. 84: I can see from your partitions that you and Mr. 86 live on the same street, 79th street.

Mr. 84 speaks: Yes. Mr. 86 is a good neighbor.

Adonten