Weak equivalence principle violations for stars gravitation – the hint from visual binaries data preliminary analysis. Implications to dark matter search.

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Abstract.

The way the stars in Galaxy are weighted relies heavily on the weak equivalence principle (Third Kepler Law). This law was verified in Solar System for baryonic matter – the planets and satellites rotating around the Sun. No deviations from this law was found (assuming the GR corrections). However, the Sun has a lot of non-baryonic matter inside (the photons are trapped inside for millions of years, slowly progressing toward the surface). The gravitation properties of such non-baryonic matter were never carefully investigated: unfortunately the Sun is not a binary star and gravitational attraction of two stars in the solar system was never checked. Observations of visual binaries may help to check the validity of the third Kepler law for stars motion. Re-analysis of the old data (1972) on binaries gives a hint that the slope of the mass-luminosity relation (the best way to measure the distant star) depends upon the choice of stars. This unusual observation may hint onto the violation of third Kepler Law for stars dynamic. If confirmed on large databases, this observation may resolve the dark matter problems: the stars are heavier than expected and gravitationally much heavier than expected and it may lead to re-evaluation of the mass of galaxies and as a consequence to elimination of the dark matter hypothesis for galaxies rotation.
Stars are special objects in the sense of the possible gravitational deviations: they have both baryonic and non-baryonic matter (like trapped and slowly advancing to the surface light) inside. While for baryonic matter the weak equivalence principle was established by Kepler (planets orbiting around stars) it was never checked for stars.

The good example are binaries. There are many binary stars which are visible as double stars with resolved period and axis and ratio of inertial masses (through measurements of the velocities of stars). Many parameters of such stars are published in [1]

The usual formula applied to the stars from the third Kepler Law:

\[ T^2 = \frac{4\pi^2 a^3}{G(m_1 + m_2)} \]  (1)

Here \( T \) is the period of rotation of one star around the second one, \( a \) is semi-axis, \( m_1 \) and \( m_2 \) are masses of the stars (assuming gravitational mass is equal to inertial mass) and \( G \) is gravitational constant.

However, the light theoretically may have much higher gravitational pull compare to the inertial mass from \( E=mc^2 \) relation (it is assumed that the inertial mass of light being emitted and reabsorbed inside star is still according to \( E=mc^2 \), as it was proved by Einstein himself) [2]. The presence of slow light may modify the gravitational pull, making it much stronger for the star which has more trapped light (and other non-baryonic matter). While the exact amount of trapped light is difficult to calculate (not much is known about the light content of the interior of fully ionized plasma), it is obvious that this amount is correlated with luminosity of the star - the higher the luminosity, the higher the amount of trapped light and the higher the additional gravitational pull on the star (the higher the deviation between the gravitational and inertial mass).

In the derivation of the formula (1) the gravitational masses are always comes as a product [3]:

\[ F = G * M_1 * M_2 / r^2 \]

Here \( M_1 \) and \( M_2 \) are gravitational masses. Assuming the added pull is proportional to luminosity which is proportional to mass (whether gravitational or inertial) [1], it is possible to assume:

\[ F = G * K_1 * K_2 * m_1 * m_2 / r^2 \]

Here \( K_1 \) and \( K_2 \) are multiplicity coefficients, the value of \( K \) may be especially high to ultra-bright star. It is important that both coefficients for binaries are always a product.

The modified third Kepler Law:

\[ T^2 = \frac{4\pi^2 a^3}{G * K_1 * K_2 * (m_1 + m_2)} \]
Here \( m_1 \) and \( m_2 \) are inertial masses. When \( K_1 = K_2 = 1 \), the third Kepler Law for baryonic matter is obtained.

To determine the masses from the observation of binaries we need: \( T \), \( a \), and ratio of masses \( m_1/m_2 = n \). Since the ratio of masses is determined through the Doppler shift of spectra of stars, it is a ratio of inertial masses. We have two equations for masses \( m_1 \), \( m_2 \):

\[
G K_1 K_2 (m_1 + m_2) = 4\pi^2 a^3 / T^2
\]

\[
m_1/m_2 = n
\]

Then:

\[
m_2 = 4\pi^2 a^3 / [G T^2 K_1 K_2 (n+1)]
\]

\[
m_1 = 4\pi^2 a^3 n / [G T^2 K_1 K_2 (n+1)]
\]

Suppose we decided to determine the inertial masses from the visual binaries with two distinct masses \( m_1 >> m_2 \). How it would influence the mass-luminosity correlation (like in [1])?

It is possible to show, that contrary to the case of valid third Kepler Law the slope of the dependence will be depended upon the ratio of masses!

Let’s consider three cases:

1. Binary \( m_1 \) and \( m_1 \)
2. Binary \( m_2 \) and \( m_2 \)
3. Binary \( m_1 \) and \( m_2 \)

In the first case the value of \( m_1 \) is (because \( n = 1 \))

\[
m_1 = m_1(\text{old}) / [K_1 K_1], \text{ here } m_1(\text{old}) = 4\pi^2 a^3 / [G T^2 K_2]
\]

Here \( m_1(\text{old}) \) is real inertial mass. \( K_1 \) is large and the value of \( m_1 \) is shifted strongly toward smaller mass compare to real inertial mass.

In the second case the value of \( m_2 \) (\( n \) is equal to 1)

\[
m_2 = m_2(\text{old}) / [K_2 K_2]
\]

If \( K_2 \) is smaller than 1 (supposedly Sun has the value of \( K \) exactly one) the mass of smaller star will shifted strongly toward larger mass.

In the third case the value of \( m_1 \) is
$$m_1 = \frac{m_1\text{old}}{K_1 K_2}, \quad m_1\text{old} = 4\pi^2 a^3 n/[G T^2 (n+1)]$$

Since both coefficients $K_1$ and $K_2$ are here, one is small and one is big, the shift compare to the real inertial mass is smaller compare to the case of the equal masses

$$m_2 = \frac{m_2\text{old}}{K_1 K_2}$$

This idea may be immediately checked. If the mass-luminosity curve is plotted using first only stars with close masses, it will be compressed toward y-axis because of $K_1 K_1$ and $K_2 K_2$ coefficients along the x-axis (the slope will be larger). If the same curve is plotted using the stars with different masses (preferably with large difference, but I used what we have in [1]) the slope will be smaller. I manually chose approximately half of visual binaries (17 binaries or 34 stars) from Table 1A from [1] with close masses and obtained the relation between the luminosity and mass:

Absolute luminosity = $-3.2119 \ln(m) + 5.1264$

![Graph](image_url)

Fig 1. The mass-luminosity relation for close in mass stars (from visual binaries data, Table 1A from [1])

And for the rest of the binaries (21 binaries, 42 stars) - masses are different:

Absolute luminosity = $-2.495 \ln(m) + 5.4042$
The white dwarfs were excluded, like in [1].

The scattering in the second case is much larger (as expected, because the product of coefficients $K1$ and $K2$ is highly unpredictable), but they must give much smoother curve if the coefficients are the same - the shift is larger, but it is more predictable - obviously it is some smooth function of luminosity and can not jump from star to star).

Indeed as predicted the slope is larger beyond any error for the subset of close in masses stars compare to the far in masses stars.

Since the deviation from Newton law for the baryonic matter of such large scale would be noticed long ago in our Solar system (some small deviation due to GR are not considered), the only possible explanation is that the weak equivalence principle does not hold for gravitation of stars (mixture of baryonic and non-baryonic matter), possibly due to mechanism outlined in [2].

The implications for dark matter are as follows: since for the same luminosity the masses of stars are higher (and gravitational masses are much higher), it may be enough to eliminate the need for dark matter hypothesis to explain the rotation of galaxies. Implications of this idea (if valid) to the overall Universe total mass are also inevitable.
Fig. 3 The approximate sketch for the shift in mass-luminosity ratio after analysis.

Unfortunately the used dataset of visual binaries is rather limited and the publication is old (1972). Careful analysis of the large databases on binaries is necessary before any final conclusion. This analysis is just a hint for the future investigation of this matter by professional astrophysicists (especially in binary stars and dark matter).

Additional evidence for the outlined general idea [2] may be found for the triple stars and stars associations [4]. The accurate application of the proposed enhanced gravitation of trapped light may explain some abnormalities in triple stars behavior (where the central star is of huge luminosity, like Algol [5]) and explain why clusters of young stars are super-viral [4].

Conclusions.

The outlined results may lead to the necessity of careful re-evaluation of modern approach for mass evaluation of distant stars using mass-luminosity curve. Dark matter composition of the Universe may be different if the results are indeed correct.

References.


2. D.S. Tipikin, publication on blog

https://tipikin.blogspot.com/2019/10/stars-are-full-of-trapped-light-may.html