

The inherent derivations derived theoretically from one-dimensional Maxwell equations on the basis of exact differential equation

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The second in the sequel

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(to be continued to the third of sequel)

#### Abstract

This second paper of sequels submitted by Ohki in viXra, proposes solutions to free most people from well-known spells: massless of light for violation the Lorentz transformations, impossibility for light to travel in free space with no outer media, unable to derive the so-called longitudinal wave from the equations of Maxwell. The others are maladaptation for the conservation law at any given point in time for electromagnetic wave function like mechanical system with total energy summed kinetic plus potential energy, and substantial distinction between electromagnetic corpuscular system (ECS) and mechanical particle system (MPS).

To free from the spells, its solutions are: (1) inherent derivations theoretically from one-dimensional complex equations of Maxwell on theorem of the Noether, (2) the derivations of electromagnetic attitude of radiant octad beam carriers of electric momentum, magnetic momentum, mass, momentum, energy, force, power, and electromagnetic indeterminacy described as the wave form. (3) self-medium in continuity entity helped the radiant octad carriers travel on an axis in free vacuum space, (4) the indeterminacy of the radiant octad carriers with space interval or time interval disappeared only in observing. (5) maladaptation of time reversal symmetry in the ECS, (6) the self-medium in the continuity with permittivity and permeability in free space as the carrier, helped the carrier travel

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 Self-funding electric engineer researching novel ways to study specific derivations theoretically from Maxwell's complex equations on the basis of the Noether's theorem with a complex symmetry, which is constituted due to the imaginary part and the real part rotating out of phase by  $j\pi/2$ , under an orthogonal respective relationship between complex time axes and complex space axes in absolute complex spacetime with attributes of homogeneity, isotropy, linearity, differential continuity and electromagnetic invariant product of permittivity and permeability.

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(D-2) <https://www.academia.edu/s/b01cc1dfdc/version1-22-nov-2019-substructure-and-configuration-of-an-electron-on-the-orbit-in-hydrogen>.

in free space as the longitudinal wave moving in the same direction of travel on an axis through the movements backwards and forwards in the continuity, we can observe electromagnetic waves which electromagnetic distortion due to the movement generates. Moreover, the self-medium helps both electromagnetic longitudinal and transverse waves able to travel in vacuum space.

The above-mentioned context is derived theoretically from one-dimensional the equations of Maxwell on the basis of exact differential equation in free orthogonal space only with the self-medium under conditions postulated that the space has an attribute electromagnetic invariant product of permittivity and permeability. Besides, the electromagnetic wave in the ECS interchanges the real manifest regimen into the imaginary potential regimen each other to-and-fro for each carrier is described as complex wave function. Therefore, there exists of complex conservation laws able to apply respectively to the radiant octad carriers at any one point in time like total energy plus kinetic energy and potential energy in the MPS, in short word, the ECS has potential imaginary regimen like the potential energy in the MPS. A fundamental difference between the ECS and the MPS is that the ECS has an attribute of absolute spacetime, absolute regimen. In the indeterminacy with indeterminate space interval or time interval, the indeterminate factor disappears in observing. Moreover, beam energy is equal to product of beam mass times the speed of light squared only on the ECS side, that is,  $b(E) = Sq(c)b(m)$ , and beam energy is equal to product of beam indeterminacy times coherent frequency in the continuity with self-medium, that is,  $b(E) = fb(h)$  equation stands only on the ECS side.

Keyword: Maxwell's complex equations, the Noether's theorem, time reversal symmetry, the indeterminacy principle, radiant octad carriers, longitudinal and transverse wave duality, electromagnetic mechanical substructure, self-medium in continuity entity

Precaution statement specified in advance, disobedient to conventional sign and description, non-use of the Greek alphabet in this abstract.

Apart from well-known notation convention, to simplify and never to use superscript notation and subscript notation under no specifications to need to describe, to simplify, so this paper is described as below:

<Abbreviations>

(Ab-1) ECS: Electromagnetic corpuscular System

(Ab-2) MPS: Mechanical particle system

<Terms>

(a) Scalar notation for all terms under no need to specify.

(b) If need, using bold sign as respective unit vector:  $\mathbf{i}$  on an axis of  $x$ ,  $\mathbf{j}$  on an axis of  $y$ ,  $\mathbf{k}$  on an axis of  $z$

We can use them as scalar notation as example: radiant electric flux density  $D$ , radiant magnetic flux density  $B$  and electromagnetic velocity  $dz/dt$  are, respectively, function with independent variables  $z$ ,  $t$ , just on  $x$  axis, just on  $y$  axis and just on  $z$  axis in this paper discussed only in free space.

(c) To avoid using superscript notation and subscript notation and to simplify their notations, both permittivity  $\epsilon$  and permeability  $\mu$  have no suffix zero in this paper discussed only in free space.

(d) End notes are square brackets: [ ].

(e) For the same reason,  $Cub(x)$  means the third power of  $x$ ,  $Sq(x)$  means  $x$  squared and  $Sqrt(x)$  means the square root of  $x$ .

(f) For the same reason, radiant electric flux density  $D = D(x)$ :  $\partial(\partial D/\partial z)/\partial t$  means the second partial derivative of  $D$  with respect to independent variable  $x$ ,  $z$  in space and  $t$  in time, second partial  $D$  by second partial  $z$ .

(g) For the same reason, radiant magnetic flux density  $B = B(y)$ :  $\partial(\partial B/\partial z)/\partial z$  means the second partial derivative of  $B$  with respect to independent variable  $y$ ,  $z$  in space and  $t$  in time, second partial  $B$  by second partial  $z$ .

(h) Integral constant is able to be zero through choosing judiciously the point, so constant through the result of integrating will not be described for all terms integrating under no need to specify.

(i) All wave form stands for root mean square (afterward, if need, uses r.m.s) for getting mechanical energy equivalent to electromagnetic energy on common criterion, so electromagnetic corpuscular system keeps equivalent to the MPS on the basis of energy.

(j) Specified unit: Frequency [Nos/s], electric charge [As], magnetic charge [Vs], permittivity [As/Vm], permeability [Vs/Am], radiant electric flux density [As/Sq(m)], radiant magnetic flux density [Vs/Sq(m)], wavenumber [Nos/m], the others accord with SI base units [1].

- (k) Radiant electromagnetic indeterminacy product of electric charge and magnetic charge, which has a unit product of Joule and second, [Js].
- (l)  $\Delta t$ : observable time interval with nonzero, which is on a time axis for light to travel, which has a unit of [s],  
 $\Delta z$ : observable space interval with nonzero, space interval on a space axis for light to travel, which has a unit of [m], those observables disappear when we observe them.
- (m)  $\Delta f$ : observable frequency with nonzero for reciprocal time with nonzero, time number per unit time on a time axis for light to travel, which has a unit of [Nos/s],  $\Delta k$ : observable wave number with nonzero, wave number per unit length on a space axis for light to travel, which has a unit of [Nos/m].
- (n) Electromagnetic invariance is constant product of permittivity and permeability, which has a unit divided the second squared by the meter squared. [Sq(s/m)].
- (o) Self-medium in continuity entity contained permittivity and permeability duality in free space help the carrier travel at the speed of light, keeping a coherent frequency product of wave number times the speed of light.
- (p) Radiant octad carriers: (1) radiant electric flux density, (2) radiant magnetic flux density, (3) mass, (4) momentum, (5) energy, (6) force, (7) power, (8) electromagnetic indeterminacy, which are, respectively, able to travel concurrently at the speed of light invariable in free orthogonal space with the self-medium which light generates from any source and annihilates into any sink.
- (q) Longitudinal and traverse wave duality:  
 The self-medium help those carriers travel in free space as the longitudinal wave moving in the same direction of travel on an axis through the movements backwards and forwards in the continuous entity, we can observe electromagnetic waves made electromagnetic distortion generated due to compressing and expanding the movement, however, our observation of the longitudinal wave is very difficult to observe the longitudinal momentum. However, the self-medium can help both electromagnetic longitudinal and transverse waves able to travel in vacuum space with no media.

## 1. Introduction

This paper proposes lots of solutions freed most people from well-known spells: light's massless for violation the Lorentz

transformations [2] regarded as defective equation without the validity at the speed of light, impossibility to travel in free space with no field in no media, longitudinal wave unable to derive from Maxwell's equation, no existence of the conservation law at any given point in time and any time in every point in electromagnetic wave function like mechanical system with total energy summed kinetic plus potential energy.

We will be freed from those spells

(a) When we take root of the concept that there is no existence of medium in free space under facts that Michelson-Morley experiments denied existence of the medium in space, we believe light's continuity entity has a medium property with coherent frequency, permittivity and permeability.

(b) When we come to believe in a renaissance of longitudinal wave made coexistence of transverse wave to prevail through Maxwell's equations.

(c) When the concept of light with mass has been superseded all previous misunderstandings for the concept to violate the Lorentz transformations.

(d) When, in observing a continuity entity, we know it be natural that attribute of the indeterminate space length or gauge or time disappears.

To return to this paper's subject, according to the paper [3] submitted by Ohki Yasutsugu, many derivations is showed theoretically from Maxwell's equations [4], [5] on the basis of exact differential equation in an orthogonal relationship between time axis and each axis of free space with attributes of homogeneity, isotropy, linearity, differential continuity and invariant electromagnetic invariant product of constant permittivity and constant permeability in the space with light's generation from any source and annihilation into the sink.

Using the above-mentioned derivations and new derivation in this paper in detail, those spells are freed below.

## 2. Characteristics in the ECS different from mechanical system

The so-called MPS seems to be comprehensible to the ECS [3] on the surface, however, there is primordial difference between the ECS and the MPS, the difference details below.

In the MPS, we know that wave is quite different from particle with mass [6], so it is well-known they are different concept unacceptable each other. The MPS never allows the duality to be acceptable, on the other hand, this paper will help the ECS take acceptable positions in future. However, in the ECS, most

peoples have discussed with wave-particle duality [7] for a long time, irrespective of taking root of concept of light 's massless denied under the Lorentz transformations, and according to Ohki's paper [3], the duality is derived easily from Maxwell's equations.

Besides, a fundamental difference between the ECS and the MPS, which has an attribute of the self-medium independent from geometric coordinates in the ECS, in contrast, the MPS has a property of a relative spacetime in geometric coordinates.

In consequence, the MPS will be able easily to use the speed of light derived from the ECS only when they stand on a proper criterion.

## 2.1 Wave function in the ECS

### 2.1.1 Phase function in the ECS

Phase function in the ECS different from the MPS is described in detail below.

In general, using Euler formula in regard to complex exponential function [8], [9], in one-dimensional wave function, the phase function  $\theta$  is able to be described below.

$$\theta = ft - kz \quad (2.1.1-1)$$

where

$z$  is space variable [m], means the direction for the wave to travel on an axis, and either derivative of a point function in differentiable continuous function or a space interval as finite different value in finite difference function on the axis, which is positive with non-zero.

$t$  is time variable [s], and means either derivative of a time function in differentiable continuous function or a time interval as finite different value in finite difference function on the axis, which is positive with non-zero.

$f$  is time number per unit time in wave function in detail later: the so-called frequency in wave function [Nos/s]:

### 2.1.2 Time reversal symmetry in the phase function

A context that time reversal symmetry in the MPS cannot apply to the ECS is described in detail below.

As to the time reversal symmetry for the ECS, we discuss with the difference between the MPS and the ECS below. Under the conditions that each time and space interval means, respectively, an interval never to be negative, positive with non-zero, time reversal, we can discuss with mathematical operation of replacing the expression for time with its negative in the wave

function expressed above so that they describe an event in which time runs backward or all the motions are reversed below.

When each time  $t$  and space  $z$  is interchangeable to plus or minus, excluded phase equation (2.1.1-1), we can fall the phase function into three cases:

Case 1: only time change;  $t \rightarrow -t, z \rightarrow z$ :

$$\theta = -(ft + kz) \quad (2.1.2-2)$$

Under conditions that only time changes negative in phase equation as mathematical operation, so that phase equation changes  $\theta = -(ft + kz)$ , that is, the wave function changes wave inversion form out of phase by  $\pi$  rad., so that the inversion does never occur under invariant boundary condition allowed the light to travel in free space with homogeneity and isotropy. Besides, this case has no existence to violate the condition of (c) in section 2.1

Case 2: only space change  $t \rightarrow t, z \rightarrow -z$ :

$$\theta = kz + ft \quad (2.1.2-3)$$

This case has no existence to violate the condition of (c) in section 2.1

Case 3: both change;  $t \rightarrow -t, z \rightarrow -z$ :

$$\theta = kz - ft \quad (2.1.2-4)$$

Under conditions that both space and time are negative, so that in wave function, observer's eye moving with wave changes observer's eye at rest position.

Under conditions that both time and space are negative as mathematical operation, the thought experiment will allow.

In consequence, there is no existence of the time reversal symmetry in the ECS, however, the MPS will be able to have mathematical operations.

### 2.1.3 Wave function expressed with root mean square form in complex exponential function of Euler formula

Wave function in the MPS is different from the function in the ECS to be described due to root mean square form on the basis of energy.

Using the phase  $a$  in phase equation (2.1.1-1), we can get wave function with rms factor of  $1/2$  and amplitude of  $\text{Exp}(j0 \pi/2)$  below.

$$\text{Exp}(4j\pi\theta)/2 \quad (2.1.3-1)$$

where

$j$  is  $\text{Exp}(j\pi/2)$

$1/2$  means root mean square (hereafter, abbreviated as r.m.s.), is factor equivalent to energy in the MPS

$\text{Exp}(ja)$  is a complex exponential function of Euler formula with phase  $a$  below.

Using the phase function and the Euler formula, most terms in the ECS is expressed as a wave function form in simple case of amplitude equal to  $\text{Exp}(j 0 \pi/2)$  below.

## 2.2 Two lights traveling parallel to each other out of phase by $\pi/2$ in both real and imaginary regimens

### 2.2.1 The speed of light in real regimen

Velocity of particle in the MPS is unattainable to the speed of light in free space only with the self-medium due to the Lorentz transformations, however, all the time, the speed is invariant. Note, however, it is well-known that Cherenkov radiation [10] is when a particle moves through a medium at a speed faster than speed of light for that medium.

In other word, a big different point is that any particle with mass in the MPS is unattainable to the speed of light for the particle subject to the Lorentz transformations, whereas, according to Ohki's paper [11], regardless of light with massless, the paper shows a linear continuous beam mass  $b(m)$  that travels at the speed of light in free orthogonal space with homogeneity and isotropy attributes in the ECS, with no generation and annihilation.

To return to this subject in this section, and to lead to the speed of light in an imaginary regimen in after sections, breaking free the spell of light's zero mass, well-known the speed of light is specified below.

According to Ohki's paper [1] derived from one-dimensional Maxwell's equations on basis of exact differential equation under invariant permittivity and permeability in the space, using the phase equation (2-3), the speed of light in the ECS is described below.

$$c = dz/dt = \Delta z / \Delta t > 0 \quad (2.2.1-1)$$

where

$\Delta$  means a finite difference that each space and time interval is, respectively, a finite difference in the first divided differences [12], so that we can regard the speed of light as the ratio of the interval to time interval for each term never to be zero.

The derivative of the space interval with respect to time in the phase equation (2-1) or the positive ratio infers below.

So this equation falls into three cases below.

- (a) When either is positive, the other is positive
- (b) When either is negative, the other is negative

(c) When either is positive/negative, in reverse, the other will never be negative/positive.

Furthermore, given a condition that the direction for light to travel on an axis is on  $z$  axis with unit vector  $\mathbf{k}$ , the speed of light  $c$  is on the  $z$  axis, so that space variable with vector sign for the direction for light to travel in the phase equation (2-1) shows below.

$$dz = c \mathbf{k} dt \quad (2.2.1-2)$$

In consequence, we can postulate that time has a scalar function for the speed of light is a vector function with direction of unit vector  $\mathbf{k}$ .

### 2.2.2 The speed of light in imaginary regimen

The MPS will be supposed to have no attribute of traveling independent parallel to each other in respective real and imaginary regimens with the speed of light like the ECS.

In section 2.1, we discuss with the speed of light, and this section shows the speed of light in imaginary regimen.

Given each space and time interval, respectively, multiplied by a factor of  $\exp(j\pi/2)$ , under condition that the speed of light is invariant as the real regimen, assumed a derivative space variable with respect to time variable or a ratio of imaginary space interval to imaginary time interval, so new postulate is that there exist of an imaginary ratio equation below.

$$c = j dz / j dt = j \Delta z / j \Delta t > 0 \quad (2.2.2-1)$$

This equation above (2-8) means electromagnetic carriers can travel at the speed of light in an imaginary spacetime, and the above-mentioned discussion, so that we assume the absolute complex spacetime do never allow time reversal symmetry [13], in mathematical operation in details below.

### 2.2.3 No rest point in the ECS

There is rest condition for particle with mass in the MPS, whereas, there is no rest condition in the ECS.

In addition, the MPS has a rest point and interval with respect to time and space, however, the ECS has no point of time and space but independent variable intervals with respect to time and space on an axis for light to travel under a postulate that the speed of light does never stop.

Whereas, in mechanical inertia system, there exists the particle in rest condition, however, in the ECS, there do not exist the beam in rest condition in any regimen.

### 3. Wave function derived from one-dimensional Maxwell's Complex equations on basis of the Noether's theorem

In one-dimensional wave equation, stretched string movable longitudinally [14] in the MPS and a linear electromagnetic wave to travel on an axis in the ECS have the same wave form with unit of velocity squared, so the string wave in the MPS interchanges the manifest energy into the potential energy in the stretched wire as the strain energy each other to-and-fro, whereas, the electromagnetic wave in the ECS interchanges the real manifest regimen into the imaginary potential regimen each other to-and-fro in a self-complex medium.

In consequence, the MPS with velocity less than the speed of light is quite different from the ECS with the speed of light under the conditions according to conservation law with respect to the energy at any one point in time.

#### 3.1 Rederivations from one-dimensional Maxwell's equations on the basis of exact differential equation<sup>1</sup>

Using examples from well-known that one-dimensional Maxwell's equations [15], under conditions that permittivity and permeability are invariant respectively, one-dimensional Maxwell's equations in the ECS is expressed below.

$$\partial D/\partial z = -\partial \epsilon B/\partial t \quad (3.1-1)$$

$$\partial B/\partial z = -\partial \mu D/\partial t \quad (3.1-2)$$

According to exact differential equation text [16], given the total differential of function of  $g(z,t)$  with respect to each of independent variable,  $z, t$ , we can get the function described as follows.

$$dg(z,t) = (\partial g(z,t)/\partial t) dt + (\partial g(z,t)/\partial z) dz = 0 \quad (3.1-3)$$

$$\partial(\partial g(z,t)/\partial z)/\partial t = \partial(\partial g(z,t)/\partial t)/\partial z \quad (3.1-4)$$

From exact differential equation (3.1-3), divided both hands in the equation by  $dt$ , arranging them, using  $c = dz/dt$ , we can get equation below.

$$(\partial g(z,t)/\partial t) = -c(\partial g(z,t)/\partial z) \quad (3.1-5)$$

where

$(dz/dt)$  is the speed of light  $c$

Substituting radiant electric flux density  $D$  for  $g(z, t)$  and radiant magnetic flux density  $B$  in equation (3.1-5), we can get respective equation below.

$$(\partial D/\partial z) = -(1/c)(\partial D/\partial t) \quad (3.1-6)$$

$$(\partial B/\partial z) = -(1/c)(\partial B/\partial t) \quad (3.1-7)$$

Comparing respective left hands in equation (3.1-6) and (3.1-7), and respective left hands in equation (3.1-6) and (3.17), each

hand equal each other, arranging them respectively, we can get equation below.

$$(\partial D/\partial z) = -(1/c)(\partial D/\partial t) = -\epsilon \partial B/\partial t \quad (3.1-8)$$

$$(\partial B/\partial z) = -(1/c)(\partial B/\partial t) = -\mu \partial D/\partial t \quad (3.1-9)$$

Integral constant is able to be zero through choosing judiciously the point, we can get equations below.

$$D = \epsilon c B \quad (3.1-10)$$

$$B = \mu c D \quad (3.1-11)$$

Multiplying respective left hands in the equation (3.1-10) and (3.1-11) and right hands, both hands equal them, we can get equation below.

$$Sq(1/c) = \epsilon \mu \quad (3.1-12)$$

Substituting radiant electric flux density  $D$  and radiant magnetic flux density  $B$  for  $g(z, t)$  in the equation (3.1-4) respectively, using the equation (3.1-1) and (3.1-2), arranging them, we can get respective one-dimensional wave equation below.

$$\partial(\partial D/\partial z)/\partial z = Sq(1/c) \partial(\partial D/\partial t)/\partial t \quad (3.1-13)$$

$$\partial(\partial B/\partial z)/\partial z = Sq(1/c) \partial(\partial B/\partial t)/\partial t \quad (3.1-14)$$

#### 3.2 Maxwell's complex equations on Noether's theorem in Cartesian complex coordinate system with octad axes

##### 3.2.1 Maxwell's complex equations

Given one function of the octad carriers as  $g(z, t)$ , we can describe below.

$$\partial(\partial g(z, t)/\partial z)/\partial z = Sq(1/c) \partial(\partial g(z, t)/\partial t)/\partial t \quad (3.2.1-1)$$

When substituting complex  $jz$  and  $jt$  for  $z$  and  $t$  in the equation above, each equation keeps the same form through dividing both hands in each equation by imaginary operator  $\text{Exp}(j\pi/2)$ ,  $\text{Exp}(j\pi)$ , respectively.

Therefore, we can define Maxwell's complex equation in an imaginary regimen, representative function  $g(z, t)$  are able to replace any one carrier, respectively, so we can be described as the same wave function in both real and imaginary regimens below.

Therefore, we can sum up each wave function in a real regimen and in an imaginary regimen respectively, so the total complex wave function  $g(T: z, t)$  is described as below.

$$g(T: z, t) = g(R: z, t) + jg(I: z, t) \quad (3.2.1-2)$$

where

$g(R: z, t)$  denotes wave function in a real regimen

$$g(R: z, t) = A(g) \text{Exp}(4j\pi\theta) \quad (3.2.1-3)$$

$g(I: z, t)$  denotes wave function in an imaginary regimen

$$g(I: z, t) = A(g) \text{Exp}(4j\pi\theta + j\pi/2) \quad (3.2.1-4)$$

Furthermore, using equation (3.2.1-4) above, we can get total complex wave function  $g(T: z,t)$  below.

$$g(T: z,t) = g(R: z,t) + j g(I: z,t) \\ = g(R: z, t) (1 + \text{Exp}(j\pi)) = 0 \quad (3.2.1-5)$$

From the equation above, total complex wave function  $g(T: z,t)$  is zero at any point in time and at any time in point, so we can get equation below .

$$g(R: z, t) = g(I: z, t) \text{Exp}(-j\pi/2) \quad (3.2.1-6)$$

### 3.2.2 Conservation law in the ECS

The equation (3-19) implies that all of terms are preserved at any one given point in time and at any time in point, coming and go to the real regimen and the imaginary regimen, in short word, those terms have complex regimen.

In consequence, we are able to be postulated that complete conservation law for those terms come into effect in the ECS, comparable to the conservation law in the MPS.

### 3.2.3 Noether's theorem

Reviewing equation (3.2.1-6), we can know that any carrier function in the real regimen is equivalent to any carrier function in the imaginary regimen under conditions of rotating angle of  $\text{Exp}(-j\pi/2)$ , respectively, their relationships are symmetric each other, so we will be able to see fitting the Maxwell's complex equations into Noether's theorem.

Therefore, we can postulate that the ECS has an inherent complex coordinates with orthogonal octad axes: both real axes with space three dimensions and time which coexists alongside imaginary axes with the same dimensions.

In consequence, the ECS is essentially different from the MPS.

In addition, through the equation above, given space and time defined as complex term like the four quadrants of a Cartesian coordinate system [17] with totally real and imaginary regimens, so that there exists of one-dimensional real system with the four quadrants in real regimen parallel to one-dimensional imaginary system with the four quadrants in imaginary regimen. To simplify, when we focus only directional axes for light to travel in real and imaginary regimens, the double two quadrants constitute of time axis, imaginary time axis out of phase by  $\pi/2$  on a circle rotating in anticlockwise of time, space axis and imaginary space axis out of phase by  $\pi/2$  on a circle rotating in anticlockwise of space, each time and space is independent variable each other.

Moreover, the absolute spacetime [18] proposed by Newton is applied absolutely to the MPS, however, the Newtonian's spacetime is quite different from the absolute spacetime in the ECS, which the absolute complex spacetime with each real and imaginary regimen have a respective attribute of the speed of light parallel to each other. For the speed of light in both regimens is positive in the phase equation (2.1-1) and (2.1-3), besides, the speed of light in real regimen is equivalent to the speed of light in imaginary under condition rotating out of phase by  $j\pi/2$ , so they are symmetric to each other.

### 3.2.4 Cartesian complex coordinate system

In consequence, in the ECS, Cartesian complex coordinate system has eight dimensions: a time dimension, a time imaginary dimension, three spatial dimensions, and three spatial imaginary dimensions.

Furthermore, we will be able to define complex Maxwell's equations on Noether's theorem on Cartesian complex coordinate system.

In consequence, under an orthogonal respective relationship between complex time axes and complex space axes in absolute complex spacetime with attributes of homogeneity, isotropy, linearity, differential continuity and electromagnetic invariant product of permittivity and permeability, we can use the Maxwell's complex equation on the Noether's theorem.

## 3.3. Octad carriers

### 3.3.1 Wave functions for octad density carriers

It is well-known that electromagnetic energy density  $\rho(w)$  is described below.

$$\rho(w) = 0.5(\text{Sq}(D)/\epsilon + \text{Sq}(B)/\mu) \quad [\text{J/Cub}(m)] \quad (3.3.1-1)$$

where to simplify, suffix zero is left out as:

$\epsilon$  is invariant permittivity in free space

$\mu$  is invariant permeability in free space

product of  $\epsilon$  and  $\mu$  is defined as  $\text{Sq}(1/c)$

$c$  is the speed of light

$D$ : electric flux density

$B$ : magnetic flux density

$\text{Sq}()$ : squared function

$\text{Cub}()$ : cubed function

$m$ : meter

Besides, the energy density expressed with wave function form is described below.

$$\partial(\partial\rho(w)/\partial z)/\partial z = \epsilon\mu\partial(\rho(w)/\partial t)/\partial t \quad (3.3.1-2)$$



Multiplying the both hands in the equation above by  $\epsilon\mu$ , under conditions that  $\epsilon\mu$  is invariant, we can insert  $\epsilon\mu$  into both hands in the partial differential equation, so the wave equation is below.

$$\partial(\partial\epsilon\mu\rho(w)/\partial z)/\partial z = \epsilon\mu\partial(\epsilon\mu\rho(w)/\partial t)/\partial t \quad (3.3.1-3)$$

So that,  $\rho(m)$  is defined as  $\epsilon\mu\rho(E)$ , we can get equation below.

$$\rho(m) = \epsilon\mu\rho(w) [\text{kg/Cub}(m)] \quad (3.3.1-4)$$

This  $\rho(m)$  means electromagnetic mass density.

$$\partial(\partial\rho(m)/\partial t)/\partial t = \text{Sq}(c)\partial(\partial\rho(m)/\partial z)/\partial z \quad (3.3.1-5)$$

Multiplying the equation above by the speed of light  $c$  invariant, electromagnetic momentum is defined as below.

$$\rho(p) = c\rho(m) [\text{kgm/s/Cub}(m)] \quad (3.3.1-6)$$

Besides, inserting  $\rho(p)$  into the wave function, arranging them, we can get equations below.

$$\partial(\partial(c\rho(m)/\partial t)/\partial t) = \text{Sq}(c)\partial(\partial(c\rho(m)/\partial z)/\partial z) \quad (3.3.1-7)$$

$$\partial(\partial\rho(p)/\partial t)/\partial t = \text{Sq}(c)\partial(\partial\rho(p)/\partial z)/\partial z \quad (3.3.1-8)$$

In consequence, we can get electromagnetic wave function of the octad carriers below.

$$\partial(\partial\rho(w)/\partial t)/\partial t = \text{Sq}(c)\partial(\partial\rho(E)/\partial z)/\partial z \quad (3.3.1-9)$$

$$\partial(\partial\rho(m)/\partial t)/\partial t = \text{Sq}(c)\partial(\partial\rho(m)/\partial z)/\partial z \quad (3.3.1-10)$$

$$\partial(\partial\rho(p)/\partial t)/\partial t = \text{Sq}(c)\partial(\partial\rho(p)/\partial z)/\partial z \quad (3.3.1-11)$$

### 3.3.2 Wave functions for octad carriers

#### 3.3.2.1 Wave function form

According to wave function from equation (2.1-9) to equation (2.1-11), the electromagnetic energy density  $\rho(E)$ , momentum  $\rho(p)$  and mass  $\rho(m)$  are, respectively, included electric flux density squared and magnetic flux density squared, able to be described with  $4\pi$  factor in the phase on the r.m.s. base as follows.

$$\rho(w) = A(w) \text{Exp}(j4\pi\theta)/2 \quad (3.3.2.1-1)$$

$$\rho(p) = A(p) \text{Exp}(j4\pi\theta)/2 \quad (3.3.2.1-2)$$

$$\rho(m) = A(m) \text{Exp}(j4\pi\theta)/2 \quad (3.3.2.1-3)$$

where

$A(w)$ : Amplitude in electromagnetic energy density wave [J/Cub(m)]

$A(p)$ : Amplitude in electromagnetic momentum density wave [kgm/s/Cub(m)]

$A(m)$ : Amplitude in electromagnetic mass density wave [kg/Cub(m)]

$j$  is  $\text{Exp}(j\pi/2)$

$\theta$ : electromagnetic wave phase

$$\theta = ft - kz \quad (3.3.2.1-4)$$

$z$  is space variable [m], means the direction for the wave to travel on an axis, and either derivative of a point function in

differentiable continuous function or a space interval as finite different value in finite difference function on the axis, which is positive with non-zero.

$t$  is time variable [s], and means either derivative of a time function in differentiable continuous function or a time interval as finite different value in finite difference function on the axis, which is positive with non-zero.

$f$  is time number per unit time in wave function in detail later: the so-called frequency in wave function [Nos/s]

Furthermore, inserting equation (2.2.1-1), (2.2.1-2) and (2.2.1-3) into (2.1-9), (2.1-10) and (2.1-11) respectively, arranging them, we get equation below.

$$\text{Sq}(f) = \text{Sq}(c)\text{Sq}(k) \quad (3.3.2.1-5)$$

Under conditions that the speed of light is positive and the others are, respectively, positive, so we can get equation below.

$$f = ck \quad (3.3.2.1-6)$$

Given a coherent frequency  $f$  in the entity with self-medium, we can know that if frequency  $f$  is invariant, so when the speed of light varies, wave number  $k$  must change.

We can postulate that frequency  $f$  or product of wave number and the speed of light is invariant under the entity with a coherent frequency is invariant below.

$$df = 0 \quad (3.3.2.1-7)$$

If  $c$  varies, wave number  $k$  must vary for the coherent frequency conserves in a continuous self-medium as below.

$$d(kc) = 0 \quad (3.3.2.1-8)$$

Furthermore, under the coherent frequency  $f$ , we can postulate that equation (3.3.2.1-6) is described in the finite difference form [19],

$$\Delta f = c\Delta k \quad (3.3.2.1-9)$$

#### 3.3.2.2 A momentum carrier

According to Ohki's paper, relationship between electric flux density and magnetic flux density is described as vector form and scalar form

$$\mathbf{D}_i = \mathbf{B}_j \times \epsilon \mathbf{c}_k \quad (3.3.2.2-1)$$

$$\mathbf{B}_j = \mu \mathbf{c}_k \times \mathbf{D}_i \quad (3.3.2.2-2)$$

$$D = \epsilon c B \quad (3.3.2.2-3)$$

$$B = \mu c D \quad (3.3.2.2-4)$$

Multiplying both hands in equation (2.2-3) and equation (2.2-4), dividing them by  $DB$ , we can get equation below.

$$\mu \epsilon \text{Sq}(c) = 1 \quad (3.3.2.2-5)$$

$$\mu \epsilon = \text{Sq}(1/c) \quad (3.3.2.2-6)$$



In addition, electromagnetic volumetric momentum density  $\rho(p)$  in the ECS is defined as follows.

$$\rho(p)\mathbf{k} = \mathbf{D}\mathbf{i} \times \mathbf{B}\mathbf{j} = \mathbf{D}\mathbf{B}\mathbf{k} \quad (3.3.2.2-7)$$

$$\rho(p) = \mathbf{D}\mathbf{B} \text{ [kgm/s/Cub(m)} = \text{Ns/Cub(m)}] \quad (3.3.2.2-8)$$

where

$\rho(p)$  is a scalar of momentum density in the ECS

$\mathbf{D}$  is radiant electric flux density on an axis of  $x$  with  $\mathbf{i}$  unit vector.

$\mathbf{B}$  is radiant magnetic flux density on an axis of  $y$  with  $\mathbf{j}$  unit vector.

$\mathbf{k}$  is unit vector on an axis of  $z$  for radiant momentum density.

$\times$  means vector product.

Electromagnetic momentum string density in the ECS is defined as below.

The derivative of string flux  $s(p)$  with respect to  $z$  is defined below.

$$ds(p)/dz = \rho(p) \quad (3.3.2.2-9)$$

Integrating antiderivative of  $\rho(p)$ ,

$$\int \rho(p) dz \text{ (from zero to } \Delta z)$$

$$= \int ds(p) \text{ (from zero to } \Delta z) = s(p) \Delta z \quad (3.3.2.2-10)$$

$\Delta A$  is cross-section area element product of an infinitesimal length  $dx$  on an axis of  $x$  and an infinitesimal length  $dy$  on an axis of  $y$ ,

$$\Delta A = \Delta x \Delta y \quad (3.3.2.2-11)$$

The derivative of  $b(p)$  with respect to variable area element  $A$  product of infinitesimal variable  $dx$  and  $dy$  is defined below.

$$db(p)/dA = s(p) \quad (3.3.2.2-12)$$

Integrating antiderivative of  $s(p)$ ,

$$\int s(p) dz \text{ (from zero to } \Delta A = \Delta x \Delta y)$$

$$= \int db(p) \text{ (from zero to } \Delta A) = b(p) \Delta x \Delta y \quad (3.3.2.2-13)$$

Furthermore, given double integrating  $\rho(p)$  with respect to variable  $z$  and variable cross-section area  $A$ , we can get equation defined as electromagnetic beam indeterminacy  $b(h)$  defined as below.

$$b(h) = \iiint \rho(p) dA dz dz / (\Delta x \Delta y \Delta z)$$

$$= b(p) \Delta z \text{ [Js]} \quad (3.3.2.2-14)$$

Using  $\Delta z = c\Delta t$  in equation (2-6), the beam indeterminacy  $b(h)$  is below.

$$b(h) = c b(p) \Delta t \quad (3.3.2.2-15)$$

This equation (2.2.2-14) and (2.2.2-15) mean the indeterminacy principle in the ECS like the uncertainty principle in the MPS.

### 3.3.3 Octad carriers

The same process above, we can get the other carriers below.

For the speed of light is invariant, using electromagnetic octad carriers defined below, respectively.

Beam energy defined as below.

$$b(w) = f b(h) = ck b(h) = cb(p) = Sq(c)b(m) \text{ [J]} \quad (3.3.3-1)$$

Beam momentum defined as below.

$$b(p) = cb(m) = kb(h) \text{ [kgm/s]} \quad (3.3.3-2)$$

Beam mass defined as below.

$$b(m) \text{ [kg]} \quad (3.3.3-3)$$

Under conditions of invariant frequency  $f$  in (2.2.1-7) and invariant wave number  $k$  in equation (2.2.1-8), we can get equation of beam force through  $k$  times  $b(w)$  and  $f$  times  $b(p)$ , respectively, so beam force is defined below.

Beam force defined as below.

$$b(N) = k b(w) = f b(p) \text{ [kgm/Sq(s)]} \quad (3.3.3-4)$$

Using equation (2.2.3-4) multiplying the speed of light  $c$ , we can get equation of power below.

Beam power defined as below.

$$b(P) = cb(N) = ckb(w) \text{ [Nm/s]} \quad (3.3.3-5)$$

Beam indeterminacy  $b(h)$  in equation (2.2.2-14) is expressed below.

$$b(h) = \Delta z b(p) = \Delta t b(w) \text{ [Js]} \quad (3.3.3-6)$$

where

$\Delta z$  is indeterminate space interval in finite difference.

$\Delta t$  is indeterminate time interval in finite difference.

$\Delta$  means difference sign in finite difference

Beam electric momentum defined as below.

$$b(\epsilon B) \text{ [kgm/s]} \quad (3.3.3-7)$$

Beam magnetic momentum defined as below.

$$b(\mu D) \text{ [kgm/s]} \quad (3.3.3-8)$$

Moreover, we know that electric flux density is described as wave function form in electromagnetic text [20].

$$\partial(\partial(D/\partial t)/\partial t) = Sq(c)\partial(\partial D/\partial z)/\partial z \text{ [As/Cub(m)]} \quad (3.3.3-9)$$

Multiplying the equation above by invariant  $\mu$ , we can get equation below.

$$\partial(\partial(\mu D/\partial t)/\partial t) = Sq(c)\partial(\partial \mu D/\partial z)/\partial z \text{ [J]} \quad (3.3.3-10)$$

So, we know that magnetic flux density is described as wave function form in electromagnetic text [21].

$$\partial(\partial(B/\partial t)/\partial t) = Sq(c)\partial(\partial B/\partial z)/\partial z \text{ [Vs/Cub(m)]} \quad (3.3.3-11)$$

Multiplying the equation above by invariant  $\epsilon$ , we can get equation below.

$$\partial(\partial(\epsilon B/\partial t)/\partial t) = Sq(c)\partial(\partial \epsilon B/\partial z)/\partial z \text{ [J]} \quad (3.3.3-12)$$

In consequence, we can get each electromagnetic wave function with respect to all of the octad carriers below.

(1) electric beam momentum

$$\partial(\partial(\mu D/\partial t)/\partial t) = Sq(c)\partial(\partial(\mu D/\partial z)/\partial z) \text{ [kgm/s]} \quad (3.3.3-\mu D)$$

(2) magnetic beam momentum

$$\partial(\partial(\varepsilon B/\partial t)/\partial t) = Sq(c)\partial(\partial(\varepsilon B/\partial z)/\partial z) \text{ [kgm/s]} \quad (3.3.3-\varepsilon B)$$

(3) electromagnetic beam energy

$$\partial(\partial(b(E)/\partial t)/\partial t) = Sq(c)\partial(\partial(b(E)/\partial z)/\partial z) \text{ [J]} \quad (3.3.3-e)$$

(4) electromagnetic beam momentum

$$\partial(\partial(b(p)/\partial t)/\partial t) = Sq(c)\partial(\partial(b(p)/\partial z)/\partial z) \text{ [kgm/s]} \quad (3.3.3-p)$$

(5) electromagnetic beam mass

$$\partial(\partial(b(m)/\partial t)/\partial t) = Sq(c)\partial(\partial(b(m)/\partial z)/\partial z) \text{ [kg]} \quad (3.3.3-m)$$

(6) electromagnetic beam power

$$\partial(\partial(b(P)/\partial t)/\partial t) = Sq(c)\partial(\partial(b(P)/\partial z)/\partial z) \text{ [Nm/s]} \quad (3.3.3-P)$$

(7) electromagnetic beam force

$$\partial(\partial(b(N)/\partial t)/\partial t) = Sq(c)\partial(\partial(b(N)/\partial z)/\partial z) \text{ [N]} \quad (3.3.3-N)$$

(8) electromagnetic beam indeterminacy

$$\partial(\partial(b(h)/\partial t)/\partial t) = Sq(c)\partial(\partial(b(h)/\partial z)/\partial z) \text{ [Js]} \quad (3.3.3-I)$$

All of octad carriers can travel concurrently at the speed of light in a continuity entity with self-beam-media played as the localized beam in free space like a flow of bullet discharged continuously.

Besides, the self-beam-medium constitutes of permittivity and permeability in the continuity entity, so there is absolute need of both electric flux density and magnetic flux density as fundamental term in the ECS.

#### 4. Conclusions

Conclusions fall into three parts:

(A) Indispensable premises as each postulate

(B) Reviewing respective equations derived from Maxwell's equations on Noether's theorem

(C) Respective interpretation for those equations

If one of the above-mentioned postulates breaks, the postulate will need to be remedied and equations concerning the postulates will need change, so derivative of the postulate draw a wrong conclusion.

However, I hope that some conclusions carry through under boiling reviews to free from the great spells.

(A) Indispensable postulates

(a-1) There coexists of absolute orthogonal real coordinates and imaginary coordinates in free complex spacetime only in the ECS

(a-2) In the complex spacetime, there exist of one-dimensional Maxwell's complex equation applicable to the Noether's theorem

(a-3) There exists of the space with self-media in continuity entity with coherent frequency and with invariant permeability and permeability applicable to both the real and the imaginary regimen.

(B) Assumptions derived from the above-mentioned postulates  
(b-1) Self-media allowed self-field in the continuity entity

In wave function form, all of radiant octad carriers with each coherent frequency can travel concurrently at the speed of light in a free orthogonal space, using the self-media allowed self-field in the continuity entity with permittivity and permeability terms.

(b-2) Mechanical substructure of light

Given divisible infinitesimal light element under conditions that characteristics of light do never lose at all even when sliced up a linear continuous entity on an axis, if the element allows a beam mass element with its center to be treated as a mass element sliced ultimately up the entity of light, we will be able to define the beam mass element with length and gauge, however, when we observe the beam mass, the length and the gauge will disappear and we can get only value of energy, so we can get the beam mass divided the beam energy by  $Sq(c)$ , the beam momentum divided the beam energy by  $c$ , the force multiplying the beam energy by the coherent frequency, etc.

In consequence, we will be supposed the substructure of light less value so that the substructure depends on the interaction to observe it.

(b-3) Longitudinal and transverse wave duality

However, in spite of the less value, from equation (3.3.2.2-9) to equation (3.3.2.2-15) and from equation (3.3.3-1) to equation (3.3.3-12), we are able to suppose the substructure of light has an infinitesimal bead element, an string connected lots of beads and a group beam bundled lots of the strings. Given the substructure and regarding particle as the bead element on self-medium, through an analogy to mechanical longitudinal wave mechanism [22] with moving particle with mass in-lined in a string stretched, we able to postulate that electromagnetic wave is the longitudinal wave more than the well-known transverse wave [23]. The group of light holds together by the self-internal-directional-force between beads, which is fastened bead element by self-longitudinal-back-forth-force as action through the self-medium.

So that in free space, radiant octad carriers in electromagnetic wave form can travel concurrently at the speed of light via the self-medium.

Moreover, our observation of the electromagnetic wave will be assumed to cause electromagnetically due to continuous distortions generated inside the continuity in making progressive process in the longitudinal wave.

In consequence, we will be able to observe both the waves. However, it is exceedingly difficult for us to observe its wave so that we have to observe the longitudinal momentum. So that, we have come to believe only the transverse wave to easily observe it.

(b-4) The indeterminacy principle and respective observation value in the octad

Reviewing both equation (3.3.3-5) and equation (3.3.3-6), light has the beam indeterminacy with size interval or time interval, we can it natural that, when observing the continuity entity, the indeterminacy disappears, after we can observe one value in octad carriers, we can calculate each value through multiplying frequency, the speed of light or the squared.

(b-5) Relationship between beam mass and beam energy, relationship between beam energy and beam indeterminacy

The Planck-Einstein-Schrodinger formula [24] is equivalent to equation (3.3.3-1) below

$$b(w) = f b(h) = ck b(h) = cb(p) = Sq(c)b(m) \quad (3.3.3-1)$$

This equation stands only on the ECS side, shows an equivalent equation between the beam energy and the beam mass.

Therefore, Albert Einstein's famous formula [25] is energy E equal to mass times the speed of light squared, this equation seem to be able to apply to either ECS or MPS, however, so it is

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difficult for us to take the mass-energy relationship in the MPS from the relationship in the equation (3-43) in the ECS.

(C) Interpretations

(c-1) An absolute spacetime applied only in ECS contradistinguished from theory of relativity in MPS

If anyone deals with the speed of light as the highest priority in solving relative motions for objects, most of the people will need to the theory of relativity. However, if we believe that there exist of an absolute spacetime, we will not need the theory of relativity for point of viewing via observer's eyes on board traveling at the speed of light.

In this paper, we know the chicken-or-the-egg problem, this paper builds it on a foundation that there exists of space with attribute of invariant permittivity and permeability in free geometric orthogonal space as the highest priority, on the other hand, most people believe that there exists of the speed of light as the highest priority and need to the theory of relativity.

(c-2) Reduction proportional to distance for all the octad carriers In case of beam energy b(E), substituting b(E) for g(z,t) in the equation (3-5),

$$(\partial b(E)/\partial t) = -c (\partial b(E)/\partial z) \quad (c-2-1)$$

So we can get equation defined as beam mass.

$$b(m) = Sq(1/c) (\partial b(E)/\partial t) = -(1/c) (\partial b(E)/\partial z) \quad (c-2-2)$$

The equation above implies that the farther, the less beam energy per unit length and the less beam mass per unit length, all carriers reduces being proportional to distance.

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