Relativistic Newtonian Gravity Makes Dark Energy Superfluous

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Abstract

This paper shows that a simple and relativistic extension of Newtonian gravity leads to predictions that fits supernova observations of magnitude versus redshift very well without having to rely on the hypothesis of dark energy. In order to test the concept, we look at 580 supernova data points from the Union2 database.

Some relativistic extensions of Newtonian gravity have been investigated in the past, but we have reason to believe the efforts were rejected prematurely, before their full potential was investigated. Our model suggests that mass, as related to gravity, is also affected by standard relativistic velocity effects, something that is not the case in standard gravity theory, and this adjustment gives supernova predictions that fit the observations. Our findings are reflected in several recent research papers that follow the same approach; that work will also be discussed in this paper.

Key Words: Supernovas, redshift, dark energy, relativistic Newton modification.

1 Relativistic Newton Extension

Somewhat ad-hoc relativistic extensions of Newtonian gravity have been suggested in the past. In the 1980s, Bagge [1] and Phillips [2], for example, both suggested the following relativistic extension of Newtonian gravity

\[ F = \frac{M}{R^2} \left( \frac{m}{\sqrt{1 - \frac{v^2}{c^2}}} \right) \]

This idea was in line with Einstein’s [3] special relativity theory, where a moving mass can be seen as a relativistic mass of the form \( \frac{m}{\sqrt{1 - \frac{v^2}{c^2}}} \). The idea must be that the small mass is moving relative to the larger gravitational mass and therefore appears to be relativistic from the perspective of the larger gravitational mass.

Phillips initially claimed that his relativistic Newton extension led to a prediction of the perihelion precession of Mercury that was equal to the predictions from Einstein’s [4] general relativity, which has been confirmed by experiments. In 1986, Peters [5] claimed that Phillips had made a mistake in his calculations and in reality, the Phillips extension only predicted half of the needed perihelion precession of Mercury. Shortly after that revelation, Phillips [6] acknowledged the mistake, but claimed that the approach was still interesting and should be investigated further. The Phillips and Bagge model was, for similar reasons, also criticized by Ghosal [7] and Chow [8].

However, we will claim that an additional mistake appears in the relativistic logic here. Looking at the astronomical system, it is mainly the Sun that acts on Mercury and naturally both the Sun and the Mercury are moving relative to the Earth. In this case, Haug [9, 10] has therefore suggested that the relativistic model should be extended as follows

\[ F = \frac{M}{\sqrt{1 - \frac{v^2}{c^2}}} \left( \frac{m}{\sqrt{1 - \frac{v^2}{c^2}}} \right) \]

That is, we are simply using standard logic from special relativity. We are standing in a third reference frame, Earth, and are observing two masses moving relative to us, namely the Sun and Mercury. Clearly, both masses must be relativistic, not only one of them. Further, \( R \) must represent the center to center distance between Mercury and the Sun and this length, as seen by an observer outside this system (the Earth), will undergo length contraction. This simply follows relativistic logic. Previous researchers may have missed the point that, in the case of the Sun’s effect on Mercury, we are outside observers. Haug [10] has recently shown that this more logical relativistic extension of Newtonian gravity seems to give the correct precession of Mercury. As with the Phillips prediction, the work should be checked by several independent researchers before any final conclusion is made.

A central issue in such investigations is that relativistic extensions to Newtonian gravity must follow logic in a realistic manner. If we are standing on Earth, for example, and are completing gravitational predictions about the Moon then the large mass is the Earth, and we are at rest with respect to the Earth. The Moon is a relativistic mass relative to Earth, and the radius, center to center,
from Earth to the Moon is observed from the rest frame, that is from Earth. This means that the relativistic effects will only be present for the small mass, and in this case we should have the Bagge and Philips formula:

\[ F = \frac{M \frac{m}{\sqrt{1 - \frac{v^2}{c^2}}}}{R^2} \] (3)

Another case to consider would address a different phenomenon - observing the red-shift of a supernova as viewed from Earth, for example. In this case, the large mass \( M \) is the supernova, and the lab frame is the small mass and the relativistic Newton formula must actually be

\[ F = \frac{M \frac{m}{\sqrt{1 - \frac{v^2}{c^2}}}}{R^2} \] (4)

In this case, the large gravity mass is the supernova that is moving relative to Earth. Further, the distance \( R \) runs from the center of the supernova to the Earth, and this distance is not undergoing length contraction, because the distance between the Earth and the supernova itself is not moving, even though it is expanding due to the supernova moving relative to us. It seems we must have three versions of the relativistic Newton formula depending on the situation. These three situations are illustrated in Figure 1. In the upper panel, the Earth is the laboratory frame and at the same time it is the mass \( M \), and the moon is the mass \( m \). Here the small mass is relativistic relative to the lab frame. In the middle panel, we are studying the Sun’s gravitational effect on Mercury from the Earth. That is, both the Sun and Mercury must be moving relative to the observer-frame (the Earth). Here both of the masses in the Newton formula must be relativistic. In the lower panel, we are observing the gravity effect on light sent out from a supernova from our base on Earth. That is, the large mass \( M \) is the supernova, and the supernova is moving relative to the Earth. These all follow from the most logical steps in relativity theory as applied to Newtonian gravity. To our surprise, even after an extensive “library” search, only the formula in the upper panel has been discussed in the physics literature, and it was, in our view, incorrectly applied to the situation in the second panel. This led to an incorrect prediction and may have caused researchers to abandon further investigation of relativistic Newton extensions prematurely.

Using the correct relativistic extension based on special relativistic logic combined with Newtonian gravity even fits supernova redshift data very well using baryonic matter only. We will look at this in the next sections and show a striking result - that no dark energy is needed.

2 Do We Need Dark Energy?

Here we will look at our Newton relativistic model to see if it predicts supernova data correctly. Our model needs to take both Newton relativistic effects and relativistic Doppler effects into account. The Einstein relativistic Doppler shift is given by

\[ z = \frac{1 - \frac{v}{c}}{\sqrt{1 - \frac{v^2}{c^2}}} - 1 = \frac{1 - \frac{v}{c}}{1 + \frac{v}{c}} - 1 \] (5)

Solved with respect to \( v \), this gives the well-known formula

\[ v_{pec}(z) = c \frac{(1 + z)^2 - 1}{(1 + z)^2 + 1} \] (6)

where the luminous distance (as a first approximation) is given by

\[ D \approx z \frac{c}{H_o} \frac{(1 + z)^2 - 1}{(1 + z)^2 + 1} \] (7)
where $H_o$ is the Hubble constant. However, in the time light takes to travel the distance $D$, that is $t_D = \frac{D}{c}$, then the emitting object will move away $t_Dv_{pec}$. This was not taken into account by Davis and Lineweaver [11], for example, as first pointed out by MacLeod [12] and also discussed by Brissender [13]. The corrected emitter time is therefore given by

$$t_e = t_D + \frac{t_Dv_{pec}}{c} = t_D(1 + v/c)$$

(8)

This means the relationship between the proper time at the emitter $t_e$ and the proper time at the observer $t_o$ is given by

$$t_o = \frac{t_e}{\sqrt{1 - \frac{v^2}{c^2}}} = \frac{t_D(1 + v/c)}{\sqrt{1 - \frac{v^2}{c^2}}} = t_D \left( \frac{1 - v/c}{1 + v/c} \right) = t_D(1+z)$$

(9)

This means the luminous distance is actually given by

$$D = t_{DC} = \frac{c}{H_o} \frac{(1 + z)^2 - 1}{(1 + z)^2 + 1}(1 + z)$$

(10)

The effective magnitude is found by using the following formula is

$$m_B(z) = 5\log(H_oD\gamma_M) + M_B$$

(11)

where $M_B$ is the absolute magnitude in the B-band at the maximum light curve and $log$ is the log with base 10. Be aware that the Hubble constant cancels out with the Hubble constant in the distance formula, so the formula is, in reality, not dependent on the Hubble constant. Davis and Lineweaver suggest that $M_B$ should have a value of around 3.45, as found from data; we will use the same value here. We can say this is what special relativity alone will predict. Davis and Lineweaver compare the SR model with supernova data and conclude, “SR fails this observational test dramatically being 23σ from the general relativistic $\Lambda$CDM model.”. The SR model Davis and Lineweaver uses is the one before taking into account the supernova moves during the time it takes for the light to travel from the supernova to the observer, so it is better than they claimed. Still, we agree that SR cannot explain the supernova data alone. In addition, we need to take relativistic effects in the Newton theory into consideration. The supernova is the large mass $M$ in the Newton formula, and we are observing it from the Earth. If the supernova is moving, the mass will be a relativistic mass in relation to us and is not mathematically identical to the rest-mass, as it is in the standard Newton formula. That is, the following formula is relevant

$$F = \frac{M}{\sqrt{1 - \frac{v^2}{c^2}}}m$$

(12)

This again leads to a gravitational redshift (as observed from a weak gravitational field) of approximately

$$z_{gr} \approx \frac{G \frac{M}{\sqrt{1 - \frac{v^2}{c^2}}}m}{R^2}$$

(13)

This is equal to the standard GR gravitational redshift multiplied by $\gamma_M = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$. It is important that this can be derived independent on GR, as shown by researchers in the past, something we discuss in more detail in Appendix A. We must adjust our luminous distance with this factor to get the correct prediction. This will then give what we can call an apparent distance that, in addition to distance, reflects the missing relativistic mass adjustment for the supernova. Our model will therefore simply be

$$m_B(z) = 5\log(H_oD\gamma_M) + M_B$$

(14)

The difference between this and pure SR is the additional $\gamma_M$ factor. Our result is mathematical “equivalent” to a theory recently suggested by Brissender [13]. However, in his theory the $\gamma$ factor comes from a speculative idea that proper velocity is what is relevant and not the velocity, so he claims $v_{pec}$ is relevant. Proper velocity is defined as taking the distance, as measured from the laboratory frame (“stationary” frame), divided by the time traveled as measured in the moving frame. Brissender has shown that this fits very well with supernova observations. However, there is no deep theory on why we should use proper velocity here rather than the velocity, and, in fact, we will claim the logic falls in the opposite direction; that it is the velocity that should be used and not the proper velocity.

In other approaches, Kipreos [14] has what we would call a structural equivalent mathematical model, where he argues that his $\gamma$ factor adjustment relative to SR is due to the need for a suggested time-contraction ratio. In order to get a $\gamma$ factor here, he needs to use the Mansouri and Sexl [15] transformation rather than the Lorentz transformation, something we will get back to later. So, Kipreos work is basically identical to ours in that the time must be adjusted by a $\gamma_z = 1/\sqrt{1 - \frac{v^2}{c^2}}$. However, again, there is no deep theory for why he has to do this suggested time-contraction ratio (by this we do not mean the lack of a solid transformation theory, but rather, why he needs the time-contraction in the first place).

We propose that we may have found the correct explanation for why there is time adjustment needed, namely because we also need to do relativistic adjustments for the mass in the Newtonian gravity formula. In short, we need to take into account that masses moving relative to an observer are observed as relativistic masses and not rest-masses. We will discuss this further in the coming sections.
Testing the model against 580 supernova 1A data points

To assess the prediction power of our model, we test it against 580 data points from the Union-2 supernova 1A database, [16]. Figure 2 shows the observations in black points. The red line corresponds to our Newton relativistic model in addition to SR. The red line will be the predictions from the Brissender model and also from the Kipreos model. However, these approaches have very different interpretations than our model. The blue line is when we are only taking standard SR into account; as stated previously, our model is simply a logical extension of SR. That is, we assume any mass when moving relative to us is a relativistic mass. Further, we do not see the logic for why there should be different masses for gravitational and non-gravitational phenomena.

![Figure 2](image)

Figure 2: The figure shows 580 supernova data points from the Union-2 database, in black. The red line represents the predictions from our relativistic Newton gravity, the blue line is predictions from SR only, and the green line is what we call the naive SR model where we do not take into account that the supernova is moving during the time it takes for the light to move from the supernova to the observer.

The green line is an even more naive use of SR, where we neglect to take into account that the supernova have moved even further away in the time it takes for light to travel the distance from the supernova to the observer (Earth); this corresponds to using formula 7.

Summary and Discussion

In this paper, we have introduced three basically mathematical “identical” models that all predict supernova observations without relying on dark matter. Naturally there may be some debate on whether or not they are really identical mathematically, as the inputs and assumptions are not the same for all of them. To be clear, these are then three considerably different models in their assumptions and interpretation of explanatory causes that give the correct prediction of supernovas. However, these models are basically identical, from a structural point of view. We summarize the three alternatives plus the standard GR, Newton model below

1. The relativistic modified Newtonian model presented here simply states that we need to take into account relativistic masses for moving objects. Gravitational masses are no exception. Since the standard model does not do this, we get a correction factor of $\gamma_z = 1/\sqrt{1 - v^2_{pec}/c^2}$. This gives a nice fit to supernova observations. This model was suggested in 2020 and is fully consistent with Haug’s [9] recently presented quantum gravity theory that unifies gravity with quantum mechanics.

2. The model presented by Brissender in 2019 in relation to predicting supernovas is mathematically “identical” to the model above, but it has very different interpretation. In the Brissender model, the $\gamma$ adjustment factor is due to what we would claim is a speculative idea: that it is the proper supernova velocity that is relevant and not the standard velocity. We doubt this explanation. That said, the Brissender paper together with the Kipreos model made us think more deeply about the need for a $\gamma$ correction to get the correct supernova predictions. Taken together with our view that we must also have relativistic masses in the Newton gravity model, this helps to develop a new perspective.

3. The Kipreos [14] model published in 2014, where the end result is mathematically identical to the two models described above. This model also has a $\gamma$ factor that it claims is a correction factor for time dilation of the signal sent in the past versus the one received in the present. The explanation for exactly why this should be the case seems to be the weakness in this approach. Still, this paper strongly indicates that something may be missing in the standard theory and pointed us towards the need for further research.

4. The standard gravity model. This model needs dark energy in order to be consistent with supernova data, but we strongly suspect that dark energy is simply a fudge factor. Unfortunately, much money has gone into this model and it has considerable prestige. Many of the best-known physicists working in cosmology today are heavily invested in this model, which leads to biases against considering the findings from the three alternative models explained in this paper.

is linked to absolute simultaneity rather than relativity of simultaneity, something that has been supported by some recent research [17–20]. The Mansouri and Sexl transformation has the same length transformation as the Lorentz transformation, but the time transformation is just \( t' = t \gamma \) compared to the Lorentz time transformation of \( t' = (t - vx/c^2) \gamma \). The suggested interpretation in this paper seems to be compatible both with SR and with the Mansouri and Sexl transformation. This is because it does not rely on any time-transformation; the same seems to be the case with the Brissender interpretation. Therefore, the essential question is: what is the most likely cause for the \( \gamma \) adjustment that leads to a good fit of supernova predictions? Is it the time adjustment suggested by Kipreos? Is it that we should rely on proper velocity? Or is it simply that the masses in the Newton gravity formula are also relativistic? We believe that the last suggestion, as presented in this paper, makes the most sense. In particular, this is true since this method also seems to lead to the correct prediction of Mercury precession, gives an escape velocity that is compatible with a Planck mass particle, and is, in general, a more consistent and logical theory, see [9, 21].

5 Conclusion

Both Kipreos [14] and Brissender [13] have recently suggested basically “identical” mathematical models that seems to predict supernova 1A data very well without relying on dark energy. However, we question the assumptions behind their models. Here we have shown a third alternative that is mathematically “identical” to the two other models, but provides a very different explanation for why this adjustment is needed. We claim the mass in gravity and, more precisely, in the Newton formula it is not exonerated from velocity related relativistic effects. By taking into account relativistic mass correctly, we create a model that predicts supernova 1A data, and that addresses redshift versus magnitude correctly without relying on dark energy.

This also shows the importance of letting speculative ideas be published and circulate, even if they are in conflict with mainstream models (such as the dark energy hypothesis). The Kipreos model and the Brissender model, for example, are much more speculative than our model. Still, they both show how a small adjustment to SR doppler shift leads to correct prediction of supernovas without relying on dark energy. Instead of ignoring this work, we have investigated these lines of thought further and have developed a robust and sound explanatory model for both simple multibody planetary system and also for supernovas. It is logical and consistent to say that there only is one type of mass at the most fundamental level and that this mass is affected by velocity from the perspective of the observer as well as in relation to gravity. Further study is merited.

References

In 1965, Adler and Bazin [24] showed that one could derive gravitational redshift completely independent of general relativity. From Einstein’s energy mass relation, we have

$$E = mc^2$$  \hspace{1cm} (15)$$

We also have that the equivalent mass of a photon must be

$$m = E/c^2 = hf/c^2$$  \hspace{1cm} (16)$$

Now, for the conservation of energy we must have

$$hf - G\frac{Mm}{R} = hf - G\frac{Mhf}{Rc^2}$$  \hspace{1cm} (17)$$

Further, when \( R \to \infty \) we must have \( f \to \infty \). This means we have

$$hf - G\frac{Mhf}{Rc^2} = hf_{\infty}$$

$$f - G\frac{Mf}{Rc^2} = f_{\infty}$$

$$\frac{f_{\infty} - f}{f} = \frac{GM}{Rc^2}$$  \hspace{1cm} (18)$$

which is identical to the gravitational redshift predicted by GR in a weak field. See also [25] for discussions on this. We have just extended this to assume the large mass is moving relative to the observer, and claim we then must have

$$hf - G\frac{M}{\sqrt{1 - \frac{v^2}{c^2}}m} = hf - G\frac{Mhf}{Rc^2}$$  \hspace{1cm} (19)$$
that will lead to

\[ \frac{f_\infty - f}{f} = -\frac{G \frac{M}{\sqrt{1-v_s^2/c^2}}}{Rc^2} \]  

(20)

This difference between the GR prediction and our prediction is what leads to our model fitting supernova data without relying on the hypothesis of dark energy.