**Abstract:** We make the following *Ansatz* for the mass ratio of the neutron to the electron:

$$m_n/m_e \approx (4\pi)(4\pi - 1/\pi)(4\pi - 2/\pi) + \ln(4\pi) = 1838.682763$$
 (1)

where  $m_n$  is the neutron rest mass and  $m_e$  is the electron rest mass. The CODATA value is 1838.68366158. The neutron decays into a proton and an electron. If  $\ln(4\pi)$  is the neutron-proton mass difference, then  $m_p/m_e \approx (4\pi)(4\pi - 1/\pi)(4\pi - 2/\pi)$ , where  $m_p$  is the proton rest mass.<sup>12</sup>

**Mass Ratio:** The two particles whose rest masses are most often studied are the electron and the proton. The electron is considered to be a fundamental particle.<sup>3</sup> The electron is also considered to be a perfect ball (solid sphere).<sup>4</sup> The proton, on the other hand is claimed to be composed of fundamental particles, such as quarks, color, and gluons.<sup>5</sup>

The Formulas: Consider the following expression:

$$\frac{m_n}{m_e} \approx (4\pi) \left(4\pi - \frac{1}{\pi}\right) \left(4\pi - \frac{2}{\pi}\right) + \ln(4\pi) = 1838.682763 \tag{2}$$

where  $m_n$  is the neutron rest mass and  $m_e$  is the electron rest mass. The CODATA value is 1838.68366158.<sup>6</sup> The neutron decays into a proton and an electron. If  $\ln(4\pi)$  is the neutron-proton mass difference, then  $m_p/m_e \approx (4\pi)(4\pi - 1/\pi)(4\pi - 2/\pi)$ , where  $m_p$  is the proton rest mass.

$$\frac{m_p}{m_e} \approx (4\pi) \left( 4\pi - \frac{1}{\pi} \right) \left( 4\pi - \frac{2}{\pi} \right) = 1836.151739\dots$$
(3)

The Higgs Boson  $(H^0)$  to electron mass ratio can also be approximated:

$$\frac{m_{H^0}}{m_e} \approx \frac{m_p}{m_e} \cdot \left(4\pi - \frac{3}{\pi}\right) \left(4\pi - \frac{4}{\pi}\right) \tag{4}$$

<sup>&</sup>lt;sup>1</sup>https://en.wikipedia.org/ wiki/Isospin

<sup>&</sup>lt;sup>2</sup>https://arxiv.org/abs/hep-lat/0608023

 $<sup>^{3}</sup> https://www.google.com/search?client=ubuntu&channel=fs&q=electron+fundamental&ie=utf-8&ce=utf-8$ 

<sup>&</sup>lt;sup>4</sup>https://www.sciencedaily.com/releases/2011/05/110525131707.htm

<sup>&</sup>lt;sup>5</sup>https://www.reddit.com/r/askscience/comments/1trc8h/are-electrons-protons-and-neutrons-actually/

<sup>&</sup>lt;sup>6</sup>https://physics.nist.gov/cgi-bin/cuu/Value?mnsmesearch\_for=neutron+mass

For convenience, we look at the mass ratio of the Higgs Boson to the proton<sup>7</sup>

$$\frac{m_{H^0}}{m_p} \approx \left(4\pi - \frac{3}{\pi}\right) \left(4\pi - \frac{4}{\pi}\right) = 131.1295246\dots$$
 (5)

This compares well with the current estimate of  $(m_{H^0}/m_p)$  of 133.

**Geometry:** Associated with the number  $m_p/m_e$ , we have a variety of objects in solid geometry whose volume equals said number. Likewise, the mass differences between the  $m_n$  and  $m_p$  offer more information from their arithmetic value.

The tri-axial ellipsoid with semi-axes  $\{4\pi, (4\pi - 1/\pi), (4\pi - 2/\pi)\}$  has a volume in 3D of  $(4\pi)(4\pi - 1/\pi)(4\pi - 2/\pi)$ . The ball (solid ellipsoid) of axis  $= (4\pi - 1/\pi)$  with the ellipsoid of axes  $\{(4\pi - 1/\pi), (1/\pi), (1/\pi)\}$  removed. The ball of axis  $= (4\pi - 1/\pi)$  with the wedge (ungula) or sector of curved surface area of  $(4\pi) \cdot (1/\pi)(1/\pi)$  removed.

<sup>&</sup>lt;sup>7</sup>https://en.wikipedia.org/wiki/Higgs\_boson