## Time Evolution Juxtaposition Of The Observables Based Dirac Type Commutator And The Consequential Wave Equation Of Photon

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Author: Ramesh Chandra Bagadi
Founder, Owner, Co-Director And Advising Scientist In Principal
Ramesh Bagadi Consulting LLC, Madison, Wisconsin-53715, United States Of America.
Email: rameshcbagadi@netscape.net

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Ramesh Bagadi Consuting LLC, Advanced Concepts \& Think-Tank, Technology Assistance \& Innovation Center, Madison, Wisconsin-53715, United States Of America

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## 1 Abstract

A novel kind of classical bracket of classical observables is proposed. This bracket is used directly as a derivation* of the commutator of the quantum mechanical observables that are simply obtained by Dirac quantization of the classical observables. Light bending in the presence of a massive object in Schwarzschild's metric is considered and the above bracket is used to obtain a second quantized equation of the wave function of the photon in this situation via the Dirac quantization.

## 2 Notation

$\theta=$ Azimuthal Angle
$\phi=$ Polar Angle, Also a Canonical Co-ordinate
$r=$ Radial co-ordinate in the Schwarzschild setting
$V=$ Velocity of a photon
$G=$ Universal Gravitational Constant
$M=$ Massive object in a Schwarzschild setting
$t=$ Proper time
$\lambda=$ a constant of motion
$\varepsilon=$ a constant of motion
$d s=$ line element in the Schwarzschild metric
$r_{0}=$ impact parameter
$p_{\phi}=$ Canonical momentum
$L=$ Lagrangian
$v=$ Frequency of a photon
$q=$ Canonical Co-ordinate
$p=$ Canonical Momentum
$\psi=$ Eigen Wave-function of the Photon in the canonical representation

## 3 Light Bending, Classical Observables (Canonical Co-ordinates) in Schwarzschild Metric

Considering the well known Schwarzschild metric, specially the case of the line element lying in the equatorial plane ( $\theta=\pi / 2$ ), where $r, \theta$ and $\phi$ have their usual meaning
$d s^{2} / V^{2}=\left(1-\frac{2 G M}{r}\right) d t^{2}-\left(1-\frac{2 G M}{r}\right)^{-1} d r^{2}-r^{2} d \phi^{2}$

We have the following relationships regarding the photon orbit locally in the presence of a massive object of mass $M$.

From the constant of motion
$g_{t t} \frac{d t}{d s}=\varepsilon \quad$ we have $\quad\left(1-\frac{2 G M}{r}\right) \frac{d t}{d s}=\varepsilon \quad$ giving
$\frac{d t}{d s}=\frac{\varepsilon}{\left(1-\frac{2 G M}{r}\right)}$

Similarly from another constant of motion
$g_{\phi \phi} \frac{d \phi}{d s}=\lambda \quad$ we have $\quad-r^{2} \frac{d \phi}{d s}=\lambda$
giving $\frac{d \phi}{d s}=\frac{-\lambda}{r^{2}}$

As $\mathrm{r} \rightarrow \infty$ we note that $\frac{1}{V^{2}}=\varepsilon^{2}-1$ and also that $\varepsilon=\gamma$. We, therefore have
$\frac{d r}{d s}=\left[-\frac{1}{V^{2}}\left(1-\frac{2 G M}{r}\right)+\varepsilon^{2}-\left(1-\frac{2 G M}{r}\right) \frac{\lambda^{2}}{r^{2}}\right]^{\frac{1}{2}}$
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At $\quad r=r_{0} \quad$ we have
$\frac{1}{V^{2}}=\gamma^{2}-\frac{\lambda^{2}}{r_{0}^{2}}$

From the quotient of 2 and 3 we have
$\frac{d t}{d \phi}=\frac{\varepsilon}{\left(1-\frac{2 G M}{r}\right)}\left(\frac{-r^{2}}{\lambda}\right)$

Also from the quotient of 3 and 4, we have
$\frac{d \phi}{d r}=\frac{-\lambda}{r^{2} \sqrt{-\frac{1}{V^{2}}\left(1-\frac{2 G M}{r}\right)+\varepsilon^{2}-\left(1-\frac{2 G M}{r}\right) \frac{\lambda^{2}}{r^{2}}}}$

Now considering
$\phi$ as our canonical co-ordinate
we find the canonical momentum $p_{\phi}$ given by
$p_{\phi}=\frac{\partial L}{\partial \dot{\phi}} \quad$ where
$L=-\left(\left(1-\frac{2 G M}{r}\right)-\frac{1}{\left(1-\frac{2 G M}{r}\right)}\left(\frac{d r}{d t}\right)^{2}-r^{2}\left(\frac{d \phi}{d t}\right)^{2}\right)^{\frac{1}{2}}$
which is gotten by using $\delta \int d s=0$

Therefore,
$p_{\phi}=r^{2} \frac{d \phi}{d s}$
4. A Novel Bracket as the Derivation of the Commutator of the Quantum Mechanical Observables

We propose the bracket of the form:
$\{q, p\}_{A}=\left(q_{t} p_{t+d t}-p_{t} q_{t+d t}\right)$
where the subscript denotes the time at which the canonical co-ordinate or the canonical momentum is evaluated. Taking $d t \approx \frac{1}{v}$ where $v$ is a property of the photon, say its frequency, we note that in the limit of $d t \rightarrow 0$ we have
$\{q, p\}_{A} \approx \frac{1}{v}(q \dot{p}-p \dot{q}) \quad$ i.e
$\{q, p\}_{A} \approx \frac{1}{v}\left(q \frac{d p}{d t}-p \frac{d q}{d t}\right)$

We further extend it to many co-ordinates in a similar fashion

$$
\begin{equation*}
\left\{q_{i}, p_{i}\right\}_{A} \approx \sum_{i=1}^{n} \frac{1}{v}\left(q_{i} \frac{d p_{i}}{d t}-p_{i} \frac{d q_{i}}{d t}\right) \tag{11}
\end{equation*}
$$

where $i$ is an index that runs for the number of co-ordinates.

We will now comment on the motivation and the use of such a bracket. Quantizing classical dynamical systems to quantum mechanical systems involves mapping the Poisson Bracket to a Dirac Commutator by way of canonical quantization methods which incorporate the uncertainty as a function of the commutator by algebraic means. However, if we realize that
a similar uncertainty as a function of the commutator can be incorporated in such a quantization map by perturbation of time in a fashion as in 9 and then evaluating the canonical co-ordinates and the canonical momenta. The inverse of this time can be conveniently taken to be of the order of the frequency of the photon whereby we do not miss any capturing of the of the wave packet nature of the photon. At this stage we can simply promote our new co-ordinates in this bracket to Quantum Mechanical observables by simply using the Dirac map. Since we are using Dirac Quantization in addition to the quantization contributed by the "derivation" nature of the proposed novel bracket, the wave equation developed in this scheme should be a product of what we are motivated to call a second quantization.

We name this kind of bracket an Aryabhatta bracket in the honour of the ancient Indian astronomer Aryabhatta. Hence the subscript A in the notation of this bracket.

Once we promote these canonical variables namely
$q=q_{A} \quad$ and $\quad \xi \frac{1}{v} \frac{d p}{d t}=p_{A}$
12
or
$\zeta \frac{1}{v} \frac{d q}{d t}=q_{A}$ and $\quad p=p_{A}$
where $\xi$ and $\zeta$ are some constants.
which we recognize as canonical variables again ready to be promoted to be quantum operators by simply doing

Note: If $q_{A}$ is the co-ordinate at time $t$ then $p_{A}$ is the co-ordinate at time $t+d t$ and viceversa.
$\hat{q_{A}}=q_{A}=q$
$\hat{p_{A}}=\xi \frac{h}{i v} \frac{\partial}{\partial t}\left(\frac{\partial}{\partial q}\right)=-\xi \frac{i h}{v} \frac{\partial^{2}}{\partial t \partial q}$
or
$\hat{q}_{A}=q_{A}=\zeta \frac{1}{v} \frac{d q}{d t} \quad$ and
$\hat{p_{A}}=p_{A}=-\zeta i n\left(\frac{\partial}{\partial q}\right)$
which satisfy
$\hat{q_{A}} \hat{p}_{A}-\hat{p_{A}} \hat{q}_{A}=1$

Substituting the $14,15,16$ and 17 in 18 according the note mentioned above in the above equation we get
$q \xi\left(-\frac{i h}{v} \frac{\partial^{2}}{\partial t \partial q}\right)-\left(-i h \frac{\partial}{\partial q}\right) \zeta\left(\frac{1}{v} \frac{\partial q}{\partial t}\right)=1$

For an eigen wave function $\psi$ in the canonical $\phi$ representation that satisfies our quantum commutator we have
$q \xi\left(-\frac{i h}{v} \frac{\partial^{2} \psi}{\partial t \partial q}\right)-\left(-i h \frac{\partial \psi}{\partial q}\right) \zeta\left(\frac{1}{v} \frac{\partial q}{\partial t}\right)=\psi$ which can be rewritten as
$q \xi\left(-\frac{i h}{v} \frac{\partial^{2} \psi}{\partial t \partial q}\right)-\left(-\frac{i h \zeta}{v} \frac{\partial \psi}{\partial t}\right)=\psi$
$-i h q \xi \frac{\partial^{2} \psi}{\partial t \partial q}+i h \zeta \frac{\partial \psi}{\partial t}=v \psi$
or
$\frac{h}{i} q \xi \frac{\partial^{2} \psi}{\partial t \partial q}-\frac{h}{i} \zeta \frac{\partial \psi}{\partial t}=v \psi$
$q \xi \frac{\partial^{2} \psi}{\partial t \partial q}-\zeta \frac{\partial \psi}{\partial t}=\frac{i v \psi}{h} \quad$ is the differential equation of the wave-function

Choosing the constants $\xi$ and $\zeta$ to be 1 we have
$q \frac{\partial^{2} \psi}{\partial t \partial q}-\frac{\partial \psi}{\partial t}=\frac{i \chi \psi}{h}$

## 5 Wave Function of a Photon

Noting $q$ as our canonical co-ordinate and the canonical momentum $p$
$\{q, p\}_{A}=\frac{1}{v}\left(q \frac{d p}{d t}-p \frac{d q}{d t}\right)$

$$
\begin{aligned}
& =\frac{1}{v}\left(q \frac{d}{d t}\left(-i h \frac{\partial}{\partial q}\right)-\left(-i h \frac{\partial}{\partial q}\right) \frac{d q}{d t}\right) \\
& =\frac{i h}{v}\left(-q \frac{\partial^{2}}{\partial t \partial q}+\left(\frac{\partial}{\partial q}\right) \frac{d q}{d t}\right)
\end{aligned}
$$

$$
\hat{q_{A}} \hat{p_{A}}-\hat{p_{A}} q_{A}=1=\frac{i h}{v}\left(-q \frac{\partial^{2}}{\partial t \partial q}+\left(\frac{\partial}{\partial q}\right) \frac{d q}{d t}\right) \quad \text { From } 18
$$

Therefore for our wave function $\psi$ we have

$$
\begin{equation*}
q \frac{\partial^{2} \psi}{\partial t \partial q}-\frac{\partial \psi}{\partial t}=\frac{i v \psi}{h} \quad \text { From } 25 \tag{27}
\end{equation*}
$$

6 Decomposition of the Wave Function

We write the wave function $\psi(r, \phi, \theta)$ as $\psi(r, \phi, \theta)=R(r) \Phi(\phi) \Theta(\theta)$

In our case, for the photon orbit lying in the equatorial plane we have,
$\psi(r, \phi, \theta)=\psi(r, \phi)=R(r) \Phi(\phi)$

7 Equation of $R(r)$ component of Wave Function of the Photon

Explicitly the momentum operator in the radial and angular co-ordinates respectively is
$p_{r}=r \frac{\partial}{\partial r}$
And

$$
\begin{equation*}
p_{\phi}=\phi \frac{1}{r} \frac{\partial}{\partial \phi} \tag{29}
\end{equation*}
$$

(implying that $p_{\phi}$ is either discontinuous in $\phi$ or multiple valued)

Therefore we have for radial part we have
$\hat{q_{A}}=q=\phi$ and $\quad \hat{p}_{A}=-i h \frac{\partial}{\partial t}\left(r \frac{\partial}{\partial r}\right)=-i h\left(\frac{\partial r}{\partial t} \frac{\partial}{\partial r}+r \frac{\partial^{2}}{\partial t \partial r}\right)$ for the first term in the LHS of 18 and 30
$\hat{p}_{A}=-i h\left(r \frac{\partial}{\partial r}\right)$ and $\quad \hat{q}_{A}=\frac{\partial \phi}{\partial t} \quad$ for the second $\quad$ term in the LHS of 18
31
Therefore we have,

$$
\begin{equation*}
\hat{q}_{A} \hat{p}_{A}-\hat{p}_{A} \hat{q}_{A}=\phi\left(-i h\left(\frac{\partial r}{\partial t} \frac{\partial}{\partial r}+r \frac{\partial^{2}}{\partial t \partial r}\right)\right)--i h\left(r \frac{\partial}{\partial r}\right)\left(\frac{\partial \phi}{\partial t}\right)=1 v \tag{32}
\end{equation*}
$$

For our previously mentioned $R(r)$ but only the r component (representation) is

$$
\begin{equation*}
\phi\left(-i h\left(\frac{\partial r}{\partial t} \frac{\partial R(r)}{\partial r}+r \frac{\partial^{2} R(r)}{\partial t \partial r}\right)\right)--i h\left(r\left(\frac{\partial R(r)}{\partial r}\right)\left(\frac{\partial \phi}{\partial t}\right)=1 v\right. \tag{33}
\end{equation*}
$$

i.e we have

$$
\begin{gather*}
\phi\left(\frac{\partial r}{\partial t} \frac{\partial R(r)}{\partial r}+r \frac{\partial^{2} R(r)}{\partial t \partial r}\right)-\left(r \frac{\partial R(r)}{\partial r}\right)\left(\frac{\partial \phi}{\partial t}\right)=-\frac{v}{i h}  \tag{34}\\
\phi \frac{\partial r}{\partial t} \frac{\partial R(r)}{\partial r}+\phi r \frac{\partial^{2} R(r)}{\partial t \partial r}-r \frac{\partial R(r)}{\partial r} \frac{\partial \phi}{\partial t}=\frac{-v}{i h} \tag{35}
\end{gather*}
$$

Since $r$ and $t$ are independent variables, we have

$$
\phi r \frac{\partial^{2} R(r)}{\partial t \partial r}-r \frac{\partial R(r)}{\partial r} \frac{\partial \phi}{\partial t}=\frac{-v}{i h}
$$

for the $R(r)$ component wave function of the photon.
8 Equation of $R(r)$ component of Wave Function of the Photon in the Limit of mass $M$ considered in the Schwarzschild setting going to zero

The equation
$\phi r \frac{\partial^{2} R(r)}{\partial t \partial r}-r \frac{\partial R(r)}{\partial r} \frac{\partial \phi}{\partial t}=\frac{-v}{i h}$
$\phi r \frac{\partial^{2} R(r)}{\partial t \partial r}-r \frac{\partial R(r)}{\partial r}\left(\frac{-\lambda}{\varepsilon r^{2}}\right)=\frac{-v}{i h} \quad$ Note: $\lambda$ is the constant of motion; momentum.

As $\frac{\partial \phi}{\partial t}=\left(\frac{-\lambda}{\varepsilon r^{2}}\right)$ as $M \rightarrow 0$ in equation 6 7a
giving
$\phi r \frac{\partial^{2} R(r)}{\partial t \partial r}+\frac{\partial R(r)}{\partial r}\left(\frac{\lambda}{\varepsilon r}\right)=\frac{-v}{i h}$

In the limit of $M \rightarrow 0$ equation 6 becomes
$\frac{d \phi}{d r}=\frac{-\lambda}{r^{2} \sqrt{\varepsilon^{2}-\left(\frac{\lambda^{2}}{r^{2}}+\frac{1}{V^{2}}\right)}}$
$\frac{d \phi}{d r}=\frac{-\lambda^{2}}{\sqrt{\left(\frac{\varepsilon^{2}}{\lambda^{2}}-\frac{1}{V^{2} \lambda^{2}}\right) r^{4}-r^{2}}}$
$\frac{d \phi}{d r}=\frac{A}{\sqrt{B r^{4}-r^{2}}} \quad$ where $\quad A=-\lambda^{2} \quad$ and $\quad B=\frac{\varepsilon^{2}}{\lambda^{2}}-\frac{1}{V^{2} \lambda^{2}}$

Therefore,
$\phi=\int \frac{A d r}{\sqrt{B r^{4}-r^{2}}}$

We simply write this as $\phi=f(r)$

9 Equation of $\Phi(\phi)$ component of Wave Function of the Photon
$p_{\phi}=\phi \frac{1}{r} \frac{\partial}{\partial \phi} \quad$ From 30

Therefore we have for angular part we have
$\hat{q_{A}}=q=\phi$ and $\hat{p_{A}}=-i h \frac{\partial}{\partial t}\left(\phi \frac{1}{r} \frac{\partial}{\partial \phi}\right)=-i h\left(\frac{\partial \phi}{\partial t} \frac{1}{r} \frac{\partial}{\partial \phi}+\phi \frac{\partial\left(r^{-1}\right)}{\partial t} \frac{\partial}{\partial \phi}+\phi \frac{1}{r} \frac{\partial^{2}}{\partial t \partial \phi}\right)$
for the first term in the LHS of 18 and

$$
\begin{equation*}
\hat{p}_{A}=-i h\left(\phi \frac{1}{r} \frac{\partial}{\partial \phi}\right) \text { and } \hat{q}_{A}=\frac{\partial \phi}{\partial t} \quad \text { for the second term in the LHS of } 18 \tag{39}
\end{equation*}
$$

Therefore we have,
$\hat{q_{A}} \hat{p}_{A}-\hat{p}_{A} \hat{q}_{A}=-i h \phi\left(\frac{\partial \phi}{\partial t} \frac{1}{r} \frac{\partial}{\partial \phi}+\phi \frac{\partial\left(r^{-1}\right)}{\partial t} \frac{\partial}{\partial \phi}+\phi \frac{1}{r} \frac{\partial^{2}}{\partial t \partial \phi}\right)--i h\left(\phi \frac{1}{r} \frac{\partial}{\partial \phi}\right) \frac{\partial \phi}{\partial t}=1 v$

Since $r$ and $t$ are independent variables, we have
$\hat{q}_{A} \hat{p}_{A}-\hat{p}_{A} \hat{q}_{A}=-i h \phi\left(\frac{\partial \phi}{\partial t} \frac{1}{r} \frac{\partial}{\partial \phi}+\phi \frac{1}{r} \frac{\partial^{2}}{\partial t \partial \phi}\right)--i h\left(\phi \frac{1}{r} \frac{\partial}{\partial \phi}\right) \frac{\partial \phi}{\partial t}=1 v$ 40 a
i.e. for our previously mentioned $\Phi(\phi)$ but only the $\phi$ component (representation) is
$-i h \phi\left(\frac{\partial \phi}{\partial t} \frac{1}{r} \frac{\partial \Phi(\phi)}{\partial \phi}+\phi \frac{1}{r} \frac{\partial^{2} \Phi(\phi)}{\partial t \partial \phi}\right)--i h\left(\phi \frac{1}{r} \frac{\partial \Phi(\phi)}{\partial \phi}\right) \frac{\partial \phi}{\partial t}=1 v$
i.e. we have
$\phi \frac{\partial \phi}{\partial t} \frac{1}{r} \frac{\partial \Phi(\phi)}{\partial \phi}+\phi \frac{1}{r} \frac{\partial^{2} \Phi(\phi)}{\partial t \partial \phi}-\phi \frac{1}{r} \frac{\partial \Phi(\phi)}{\partial \phi} \frac{\partial \phi}{\partial t}=\frac{-v}{i h}$
i.e. $\phi \frac{1}{r} \frac{\partial^{2} \Phi(\phi)}{\partial t \partial \phi}=\frac{i v}{h}$
for the $\Phi(\phi)$ component of wave function of the photon.

10 Equation of $\Phi(\phi)$ component of Wave Function of the Photon in the Limit of mass M considered in the Schwarzschild setting going to zero.

In the limit of $M \rightarrow 0$ equation 6 becomes
$\frac{d \phi}{d r}=\frac{-\lambda}{r^{2} \sqrt{\varepsilon^{2}-\left(\frac{\lambda^{2}}{r^{2}}+\frac{1}{V^{2}}\right)}}$
$\frac{d \phi}{d r}=\frac{-\lambda^{2}}{\sqrt{\left(\frac{\varepsilon^{2}}{\lambda^{2}}-\frac{1}{V^{2} \lambda^{2}}\right) r^{4}-r^{2}}}$
$\frac{d \phi}{d r}=\frac{A}{\sqrt{B r^{4}-r^{2}}} \quad$ where $\quad A=-\lambda^{2} \quad$ and $\quad B=\frac{\varepsilon^{2}}{\lambda^{2}}-\frac{1}{V^{2} \lambda^{2}}$

Therefore,
$\phi=\int \frac{A d r}{\sqrt{B r^{4}-r^{2}}}$
We simply write this as

$$
\phi=f(r)
$$

The solution of 43 being

$$
\Phi(\phi)=\frac{i v r}{h} \ln (\phi)=\ln \left(\phi^{\left(\frac{i v r}{h}\right)}\right)=\ln \left|\phi^{\left(\frac{i v r}{h}\right)}\right|+i \arg \left(\phi^{\left(\frac{i v r}{h}\right)}\right)
$$

## 11Conclusions

We also note that this wave equation of photon involves the local space-time curvature term $R$ (One can refer to Steven Weinberg's text book on Gravitation for help). Exclusive computation of this bracket for this photon example clearly exhibits this.

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## Note

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