Cosmological Constant from Rotating Universe Interpretation of Time and Energy

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Abstract

The cosmological constant ($\Lambda$) problem is resolved within the framework of The Rotating Universe interpretation of Time and Energy (RUTE) which depends on a key dimensional symmetry that doubles every spacetime dimension. RUTE as proposed in this paper is a holistic model of the fundamental structure of spacetime describing the relative projections of Velocity, Force and Energy into the visible spatial dimensions. Specifically however, it is a spill model of dark energy defining the nature of time and time dimension and can be summarized into 3 relativistic constraints of Speed, Force and Energy. It constrains the resultant velocity of a reference frame, strength of particle interaction and energy density in spacetime, to always equal the upper limit of light speed $c$, Planck force and Planck energy density respectively. In RUTE, a non-zero $\Lambda$ dark energy essentially arises from an asymmetry in the Planck energy density of two vacuum states coupled with its Energy density constraint. The asymmetry is described by a cosmological factor $\Gamma$ asymptotically approaching zero with the entropic growth of time dimension $T_1$. Tantalizing prospects of a $\Lambda$ driven inflation with Gravitational Wave Reheating (GWR) mechanism, light speed oscillation and matter-antimatter transmutation among other predictions are briefly discussed.
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1. Introduction

Dark energy have so far constituted an enigma since 1998 after Riess et al.[1] followed by Perlmutter et al.[2] published their supernova observations of the accelerated expansion of our Universe. Since then, several independent lines of evidence have led to the conclusion that there is a mysterious negative pressure dark energy component driving the accelerated expansion of our Universe. Results published by the Planck collaboration (Planck 2013) [3], shows that dark energy density constitutes about 68.3% of the total energy density of our Universe, while ordinary baryonic matter constitutes 4.9%. The invisible dark matter component makes up 26.8%.

Dark Energy, according to the standard model of cosmology known as the ΛCDM (Lambda Cold Dark Matter) model, is in the form of Einstein’s cosmological constant (Λ). Λ in turn, is known to arise from vacuum energy, an intrinsic energy associated with empty space. But quantum field theory estimated a vacuum energy density $10^{120}$ times more than the observed dark energy density. This is the cosmological constant problem. It is also not known what the connection of Λ if any, is to inflation [4] (a brief period of exponential expansion of the early Universe).

Supersymmetry (SUSY) provides an elegant frame work for the cancellation of large Λ to a very small value. In unbroken SUSY, every bosonic particle has its own fermionic superpartner with same mass but with each contributing opposite signs thereby cancelling vacuum energy and resulting in zero Λ. Null search result for SUSY partners of the standard model particles shows that SUSY, if at all describes our universe, must be broken. Even with SUSY breaking around $10^3$ GeV, it’s still very far above the observed dark energy density. There are a number of other cancellation models such as that from string theory which cancels the bare Λ down to a small effective value [5]. There are also relaxation models where the value of the vacuum energy density is relaxed [6] including anthropic considerations [7] and even an approach that makes the space-time metric insensitive to the cosmological constant [8]. There are several other alternative approaches which avoid the thorny problem of Λ such as quintessence, unification of dark energy and dark matter [9] and modification of gravity [10]. For detailed review see Ref. [11, 12].

On appreciating the seriousness of the Λ Problem, It becomes more apparent that a satisfactory solution requires drastic revolution in our understanding of the Universe. Such a solution should provide at least some clues to other problems like the Physics of inflation, baryogenesis, the nature of time and even quantum gravity. In this paper, we resolve the Λ problem using a rotating and oscillating 2 dimensional ring structure of time with an asymptotically vanishing asymmetry between two opposite vacuum energy states. The framework essentially defines time as an irreversible progressive effect of motion of a reference frame along either direction of time, clearly differentiating between time as an effect and time as a dimension. The required dimensional symmetry which doubles the time dimension also
doubles the spatial dimensions resulting in 8 spacetime dimensions. Expectedly, a number of related prospects pertaining to other unsolved problems were however uncovered while digging out this deep rooted mystery. So it’s only appropriate to briefly touch these areas in this paper.

RUTE is not a cancellation model per se but a sort of spill model. In this framework, energy can be interpreted as a vector quantity in space time $T_2$ ($S_1+T_2$) as illustrated in figure 5 in section 3. With the bulk of vacuum energy being directed along the second time dimension $T_2$, the space-time metric is insensitive to it as the opposite terms of the its two vacuum states precisely cancel out despite their asymmetry. It is only sensitive to energy/momentum component directed along the macroscopic spatial dimensions $S_1$. This includes a very small component of vacuum energy projecting into the spatial dimensions as dark energy. This is due to a deficit in the Planck density (energy capacity) of one of the 2 vacuum states, coupled with its energy density constraint which constrains the energy density of a spacetime reference frame to always equal the upper limit of the Planck density. That is, the magnitude of the vector sum of spatial dimension and time dimension $T_2$ components of energy must always equal the upper limit of the Planck density.

However the resulting $\Lambda$ dark energy has inflationary energy scale in the early Universe since the asymmetry between the 2 vacuum states was large before asymptotically falling to its current value. It is also well known however, that a $\Lambda$ driven inflation usually suffer from the graceful exit and reheating problems as attempted in [13]. But this can be resolved with an asymptotically falling $\Lambda$ and a Gravitational Wave Reheating (GWR) mechanism provided by this framework for projecting vacuum energy from the $T_2$ dimension into the spatial dimensions as standard model particles, obviating the need for a scalar field driven inflation.

Generally, in this model like in most extra dimensional models, the Universe is seen as a spacetime brane like in the DGP model [14] (although DGP is modeled in a different context of cosmic acceleration without dark energy) operating in a multiverse environment with a higher dimensional spacetime structure of its own. Indeed a two time dimensional Universe provides literally, a new degree of freedom in understanding our universe such as in Ref. [15], though in an apparently different context of standard model of particles and forces.

In the next section, we define the nature of time and the relativistic speed constraint where as in section 3 we discuss the second time dimension $T_2$, the frequency and the resulting energy density constraint. In subsection 3.1, we introduce the Digital Gramophone Interpretation of 2 dimensional Time (DIGIT) analogy for pedagogical purpose. In section 4, we achieve an asymptotically vanishing asymmetry between the two vacuum states along time dimension $T_2$. Then in section 5, we describe how the deficit in Planck density of one of the vacuum states results in a non-zero cosmological constant whereas in section 6, a resulting gravitational wave reheating mechanism is examined. This is followed in section 7 with a discussion on RUTE’s dimensional symmetry and the force constraint associated with the anti-spatial dimensions. Discussion follows in section 8.
2. Nature of Time

The actual nature of time has been one of the unsolved problems in Physics [16]. In what follows, we interpret the nature of time as an irreversible progressive effect of motion of a spatial reference frame along either direction of a time dimension. We start by exploring, as shown in figure 1, how the rotation of the brane Universe along its macroscopic time dimension drives time and relativistic effects resulting from speed deficit along such time dimension.

![Figure 1: The 2d ring structure of time in RUTE brane universe. The ring thickness (also the brane thickness) which is Planck length \( l_p \) in size represents a second time dimension \( T_2 \) which we shall discuss in section 3.](image)

All the dimensions in this model have reflective boundary condition. That is, a reference frame is reflected back on reaching the dimensional boundary. If there is such a boundary along \( T_1 \), a particle transmutes into an antiparticle and vice versa including spatial momentum reversal. In line with the Feynman-Stueckelberge interpretation, massive particles and antiparticles are modeled as travelling along opposite directions of time dimension \( T_1 \). Massless particles such as photons having zero orbital speed travel at maximum speed \( c \) along the spatial dimensions \( S_1 \). In this framework, time as an irreversible entropic progression is driven by motion in either direction through a time dimension.

2.1 Speed Constraint

Given the speed of light constraint from special relativity and associated relativistic effects, an interpretation within the RUTE framework requires that all reference frames must always travel at \( c \) through combined spacetime dimensions. That is the vector sum of its velocity \( \mathbf{V}_T \) along time dimension \( T_1 \) and velocity \( \mathbf{V} \), along the spatial dimensions \( S_1 \) must always equal \( C \).
Figure 2: The speed constraint. It is required that the magnitude of the vector sum of the spatial and time dimension components of velocity must always equal $c$.

$$C = V + V_T$$

(1)

$$c^2 = v^2 + v_T^2$$

(2)

For a spatial reference frame or massive particle X with spatial velocity $V$ (relative to an observer), its velocity $v_T$ component along the time dimension $T_1$ becomes

$$v_T = \sqrt{c^2 - v^2}$$

(3)

Given the clock rate factor $\Gamma$

$$\Gamma = \sqrt{1 - \frac{v^2}{c^2}}$$

(4)

Its relative clock rate will be

$$\sqrt{1 - \frac{v^2}{c^2}} \times 100$$

(5)

Percent relative to the reference observer who’s clock ticks at

$$\sqrt{1 - \frac{0^2}{c^2}} \times 100$$

(6)

hundred percent relative to itself. The inverse of the clock rate factor gives the Lorentz factor
\[ \gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} \]  

(7)

### 2.2 Particle-antiparticle Transmutation

As earlier noted, in line with the Feynman-Stueckelberge interpretation, particles and antiparticles rotate in opposite directions along the time dimension \( T_1 \), as illustrated earlier in figure 1. Massless particles with maximum spatial velocity \( c \) have zero orbital speed along \( T_1 \). Thus the speed limit \( c \), serves as a barrier between particle and antiparticle states. As a massive particle or antiparticle asymptotically approach maximum spatial speed \( c \), or zero orbital speed \( v_T \), in an analogous quantum mechanical way, there is in this scenario, a non zero probability of it tunneling into the opposite antiparticle or particle state. The probability \( P \) of such particle-antiparticle transmutations can be expressed as

\[ P = \frac{v^2}{c^2} \]  

(8)

With \( v = 0 \), \( P = 0 \) for non-relativistic massive particles. But for photons, \( P = 1 \), making a photon essentially a superposition of particle and antiparticle state or majorana particle. So the question of exceeding \( c \), tachyons and time travel doesn’t even arise as a massive particle on approaching \( c \), simply tunnels into an antiparticle state effectively travelling backward in this case, along time dimension \( T_1 \) (not in time) without exceeding \( c \). It is hoped that higher energy run of the LHC, more powerful accelerators or high energy cosmic ray particles will show evidence of such energy dependent transmutation which is more probable at higher energies and with time.

### 2.3 Baryon Asymmetry

Let’s consider the consequence of particle-antiparticle transmutation in regards to the Sakharov conditions. See Ref. [17] for a review on baryogenesis. In a high energy thermal equilibrium with Planck scale energies such as that obtainable in the early Universe with \( t \sim t_{\text{reheating}} \), and given equal number of particles and antiparticles created according to the standard model, they should freely transmute equally. This creates baryon number violation (condition 1). If the Universe has a net spin along the time dimension \( T_1 \), the probability of a particle type transmuting into the opposite type along the net spin direction is favoured. This creates thermal inequilibrium (condition 2). And finally the type of baryon favoured depends on the net spin direction (condition 3), where the asymmetry parameter \( \eta \) is proportion to the net spin.
3. Second Time Dimension

As noted in the previous section, the speed constraint limits a reference frame to always move at resultant velocity $c$ through space and time dimension $T_1$. In what follows, we discuss the second time dimension $T_2$ in this scenario which is the Planck size brane thickness with which the speed constraint equally applies. Its Planck size and reflective boundary condition makes it an oscillatory time dimension.

![Diagram](image)

Figure 3: A vacuum reference frame oscillates between the 2 vacuum states a and b along $T_2$ dimension at the Planck frequency $f_{\text{Planck}}$

3.1 Frequency Constraint

Applying the speed constraint to time dimension $T_2$, a vacuum reference frame (empty space) must travel at $c$ along $T_2$ dimension, but with the Planck size of $T_2$ and its reflective boundary condition, such a vacuum state must oscillate at $f_{\text{Planck}} = c/l_p$. The speed constraint in eq. (2) results in the frequency constraint.

$$f_{\text{Planck}}^2 = f^2 + f_{\text{vac}}^2.$$  \hspace{1cm} (9)

Where $f_{\text{vac}}$ is the vacuum oscillation frequency along $T_2$ dimension and $f$ is the oscillation frequency along the spatial dimensions $S_1$. 
Just like in the case of T₁ dimension, if a particle or reference frame in space time oscillates with a frequency \( f \) along the spatial dimensions S, its clock rate along T₂ will tick at

\[
\sqrt{1 - \frac{f^2}{f_{Planck}^2}} \times 100
\]  

(10)

percent relatively to a vacuum (non spatially oscillating reference frame) with clock rate ticking at

\[
\sqrt{1 - \frac{0^2}{f_{Planck}^2}} \times 100
\]  

(11)

(hundred) percent of the Planck frequency along T₂.

Given the factor \( \Gamma \)

\[
\Gamma^2 = 1 - \frac{f^2}{f_{Planck}^2}
\]  

(12)

\[
\Gamma = \sqrt{1 - \frac{f^2}{f_{Planck}^2}}
\]  

(13)

Where \( \frac{1}{\Gamma} \) equals the Lorentz factor \( \gamma \) for 2nd time dimension T₂

\[
\gamma = \frac{1}{\sqrt{1 - \frac{f^2}{f_{Planck}^2}}}
\]  

(14)

It follows that a vacuum with no spatial oscillation must oscillate along T₂ dimension at the Planck frequency.

\[
f_{Planck} = \sqrt{f_{vac}^2 + 0}.
\]  

(15)
Figure 4: The oscillatory and speed time dimensions $T_2$ and $T_1$ in relation to the spatial dimensions $S_1$.

3.2 Energy Density Constraint

These oscillations translate to energy as $E = hf$, where $h$ is the Planck constant, leading to the Planck energy and Planck energy density constraints.

$$E_{\text{Planck}}^2 = E^2 + E_{\text{vac}}^2$$  \hspace{1cm} (16)

$$\rho_{\text{Planck}}^2 = \rho^2 + \rho_{\text{vac}}^2$$  \hspace{1cm} (17)

Where $E$ and $E_{\text{vac}}$ are the energy of a particle and its associated vacuum energy along the time dimension $T_2$. $\rho$ and $\rho_{\text{vac}}$ are the spatial component of energy density and component vacuum energy density along $T_2$ dimension respectively. In essence, the magnitude of the vector sum of spatially observable energy density $\rho$ of a given reference and its component vacuum energy density $\rho_{\text{vac}}$ along time dimension $T_2$ must always equal the upper limit of the Planck density $\rho_{\text{Planck}}$. Note the reference to upper limit here as there is an intrinsic asymmetry between the 2 vacuum states along $T_2$ dimension which we shall discuss in section 4.
Figure 5: Relativistic relationship between the spatial dimensions $S_1$ and the 2 time dimensions in terms of speed and frequency or energy constraints. The surface area of the 2 time dimensions gives the entropy of the universe in an analogous way $\frac{1}{4}$ of a black hole's (event horizon) surface area gives its entropy.

The energy density constraint eliminates infinite energy densities such as black hole singularity and big bang singularity, while predicting the existence of Planck stars also described by [18]. It also obviates the need for renormalization of vacuum energy density. Also,

$$\frac{1}{\gamma} = \sqrt{1 - \frac{\rho^2}{\rho_{Planck}^2}}$$

(18)

The inverse Lorentz factor in eq. (18) is also a measure of the relative strength of gravity.

3.3 Entropy Constraint

The surface area of the 2 time dimensions is given by $A = 2\pi r l_p - l_p$. In Planck unit, $A$ gives the entropy $S$ of the Universe as $S = A = 2\pi r - 1$. Where $r$ is the orbital radius of the rotating 2d time structured Universe. As such the surface area of the two time dimensions is constrained to be irreducible. Given the relatively constant Planck size of $T_2$ dimension, only $T_1$ dimension expands freely. Gravity in this scenario, essentially contracts the visible spatial dimensions to expand time dimension $T_1$ there by driving entropy while increase the orbital radius $r$ as discussed in the volume constraint of section 7.
3.4 Digital Gramophone Interpretation of 2 Dimensional Time.

Essentially, the two time dimensions can be described by a rotating and oscillating 2 dimensional ring structure. While $T_1$ dimension can be described as relatively analogue, the $T_2$ dimension being Planck size can be described as discrete. In what follows, we briefly introduce the DIGIT analogy (Digital Gramophone Interpretation of 2 dimensional Time) within the RUTE framework.

![Digital Gramophone Interpretation of 2 Dimensional Time](image)

Figure 6: The DIGIT analogy. (a) A dual track gramophone system. While time $T_1$ dimension for the gramophone system is driven by the analogue rotation of the gramophone record, $T_2$ is analogously driven by the digital switching of the stylus between two concentric and identical tracks with different rpm $c$ and $\bar{c}$. $l$ is the inter track distance. (b) Multitrack gramophone system.

In figure 6, we used a gramophone record with only 2 concentric and identical tracks with a stylus switching between the two, to describe our two dimensional time model. The analogue rotation of the record which drives the progression (play) of the record is analogous to the rotation of the Universe along its $T_1$ dimension to drive time $T_1$. The digital switching between the 2 identical but different speed tracks is analogous to the 2nd time progression $T_2$ which is discrete, while the surface area $A = 2\pi nl - l$ of the record is proportional to its entropy. As illustrated in Fig. 6b, if our universe is part of a multibrane system like this gramophone analogy, then we can have spatially parallel but time concentric universes. Gravitational influence of matter and energy in such spatially parallel universes can manifest as a dark matter component in our universe.
4. Vacuum State Asymmetry

The 2 opposite vacuum states a and b for time dimension $T_2$ are analogous to the particle and antiparticles states for time dimension $T_1$. With the oscillation of space time between 2 opposite vacuum states a and b along a second time dimension $T_2$, as illustrated in figure 7 below, we examine the resulting asymmetry.

As illustrated in figure 7 above, a massless photon x with energy less than the Planck scale, oscillates between the 2 vacuum states (brane surface states) a and b which has different orbital speeds (or speed limits $c = \omega r$ and $\bar{c} = \omega (r - l_p)$). At vacuum state a, photon x must have a spatial velocity $c = \omega r$ in order to have zero orbital speed. At vacuum state b, it must have a spatial velocity $\bar{c} = \omega (r - l_p)$. Where Planck length $l_p$ is the brane thickness or the size of $T_2$ dimension. The difference in speed ($c - \bar{c}$) between the vacuum states can be described by the cosmological factor $\Gamma$.

$$\Gamma = 1 - \frac{\bar{c}}{c} \quad (19)$$

$$\Gamma = 1 - \frac{\omega (r - l_p)}{\omega r} \quad (20)$$

$$\Gamma = \frac{l_p}{r} \quad (21)$$
The reduced cosmological factor $\frac{r}{2\pi}$ is the relative size of the two time dimensions $T_1$ and $T_2$.

\[ \gamma = \frac{1}{1-\Gamma} \]  

(22)

Where $\gamma$ is the Lorentz factor associated with this relativistic asymmetry.

\[ \gamma = \frac{r}{r-l_p} \]  

(23)

This asymmetry Lorentz factor describes the asymmetry between the 2 vacuum states with different speed limits and clock rates. It is also the ratio of the orbital radius of the two vacuum states. Since the cosmological factor as expressed in eq. (21) is a function of orbital radius $r$, it evolves asymptotically with the growth of orbital radius with $0 < \Gamma < 1$. The growth of orbital radius $r$ is in turn driven by gravity as it expands the size of the entropic time dimension $T_1$ as $2\pi r$.

![Figure 8: The asymptotic vanishing of $\Gamma$ with the growth of orbital radius $r$.](image)
4.1 Gravitational Neutrality of Vacuum Energy.

The gravitationally inert nature of vacuum energy like in [8] along T_2 dimension can be accounted for in RUTE as vacuum states a and b provides opposite gravitational terms that cancels each other’s effect along T_2. Despite the asymmetry, vacuum contributions from vacuum states a and b precisely cancels out giving:

\[ \Lambda_a - \Lambda_b = 0 \]  

(24)

i.e.

\[ \frac{8\pi G}{c^4} \rho_{\text{Planck}} - \frac{8\pi \bar{G}}{\bar{c}^4} \bar{\rho}_{\text{Planck}} = 0 \]  

(25)

Where \( G \) and \( \bar{G} \) are the gravitational constants for vacuum states a and b respectively.

Since

\[ \frac{G}{c^2} = \frac{\bar{G}}{\bar{c}^2} \]  

(26)

and

\[ \frac{\rho_{\text{Planck}}}{c^2} = \frac{\bar{\rho}_{\text{Planck}}}{\bar{c}^2} \]  

(27)
5. Non-Zero and Running Cosmological Constant

The state asymmetry discussed in the previous section results in the following relativistic relationship between the 2 vacuum states.

\[ \rho_{\text{planck}} - \bar{\rho}_{\text{planck}} = \Gamma^2 \rho_{\text{planck}} \]  \hspace{1cm} (28)

Where \( \rho_{\text{planck}} \) is the maximum vacuum energy of vacuum state a with a maximum speed limit \( c \) as illustrated in figure 10 below. \( \bar{\rho}_{\text{planck}} \) is the deficit vacuum energy density of vacuum state b with deficit speed limit \( \bar{c} \). \( \Gamma \sim 10^{-60} \) is the cosmological factor, now asymptotically approaching zero as a function of orbital radius \( r \).

Figure 9: Asymmetry between vacuum states a and b with densities \( \rho_{\text{planck}} > \bar{\rho}_{\text{planck}} \). The vacuum oscillates between states a and b. When at vacuum state a, the time dimension T2 Component has the maximum value of energy density \( \rho_{\text{vac}} = \rho_{\text{planck}} \) and zero spatial value \( \rho = 0 \). When at vacuum state b, the T2 dimension component has a deficit value of energy density \( \rho_{\text{vac}} = \bar{\rho}_{\text{planck}} \) and therefore the spatial component of vacuum energy \( \rho = \rho_{\text{DE}} \neq 0 \) to satisfy the energy density constraint \( \rho_{\text{planck}}^2 = \rho^2 + \rho_{\text{DE}}^2 \).

Given the energy density constraint earlier arrived at in section 3, the energy density in spacetime must always equal the upper limit of the Planck density \( \rho_{\text{planck}} \). Any deficit in vacuum energy density along T2 dimension must be compensated for with a corresponding amount of energy density being projected along the spatial dimension \( S_1 \). Therefore, as the vacuum oscillates at \( f_{\text{planck}} \), moving from state a to state b as shown in figure 9, the resulting
deficit along $T_2$ as the energy density changes from $\rho_{\text{planck}}$ to $\dot{\rho}_{\text{planck}}$ has to be compensated for with the emergence of dark energy $\rho_{DE}$ along the spatial dimensions where

$$\rho_{DE} = \Gamma^2 \rho_{\text{planck}}$$  \hspace{1cm} (29)

With equation of state $\omega = -p/\rho = -1$, it results as a negative pressure cosmological constant

$$\Lambda = \frac{8\pi G}{c^4} \rho_{DE}$$  \hspace{1cm} (30)

With $\Gamma$ evolving asymptotically with gravity driven growth of orbital radius $r$, $\Lambda$ runs in a step wise manner. The possible running of $\Lambda$ was explored in [18]. In the early universe, with $r \sim l_p$ and $\Gamma \sim 1$, $\Lambda \sim M_{\text{Planck}}^4$ in reduced Planck unit ($\rho_{DE} \sim 10^{73} \text{ GeV}^4$), enough to power the inflation of the early Universe. However the energy scale here asymptotically falls from the Planck scale with increasing orbital radius $r$ as $r \gg l_p$, $\Gamma \to 0$ and with reheating effectively ending inflation and leaving a residual asymptotically vanishing cosmological constant now driving the late time acceleration of our Universe.
6. Gravitational Wave Reheating (GWR) Mechanism

In RUTE with two time dimensions, where gravity drives the expansion of the time dimension $T_1$, a Gravitational Wave (GW) oscillation along the spatial dimensions $S_1$ has to be mirrored by a corresponding GW oscillation along the $T_1$-$T_2$ time dimensions. In what follows, we examine how a $T_1$-$T_2$ component of the GW oscillation produces heating effect on empty space releasing some vacuum energy as standard model photons. GW oscillation as seen at the fundamental Planck scale in this frame work, is essentially an oscillation of the Planck length $l_p$, while the Planck area $A_p$ remains constant.

![Figure 10: Time $T_1$-$T_2$ dimension component of gravitational wave oscillation where one time dimension expands at the expense of the other and vice-versa while keeping Area constant (entropy constraint).](image)

At the Planck scale, GWs simply increase Planck length in one dimension while decreasing it in another, keeping the Planck area and volume constant. During GW oscillation of Planck length $l_p$ of $T_2$ dimension, an expansion or contraction in $l_p$ of $T_2$ must be balanced by a corresponding contraction or expansion of $T_1$ respectively, to keep area and entropy from reducing.

During the $l_p$ (size of $T_2$) increasing phase of GW oscillation, vacuum oscillation frequency $f = c/l_p$ drops by a factor $Ak$. Where A is the gravitational wave strain amplitude and $k$ is the relative elasticity of the second time dimension compared to the spatial dimensions. Given that $E = hf$ and with Planck constant $h$ being constant, the vacuum energy of such reference frame drops by the same factor $Ak$ thereby projecting a corresponding amount of energy density

$$E_{\text{photon}} = AkE_{\text{planck}}$$

into the spatial dimensions due to the energy density constraint in RUTE, manifesting as photons or other Standard Model particles depending on the energy scale.
During the $l_p$ reducing phase of the GW oscillation, the vacuum oscillation frequency of the reference frame is prevented from increasing by the factor $Ak$ as this would also increase the vacuum energy density $\rho_{\text{vac}}$ above the Planck density by the same factor violating the energy density constraint. Instead, vacuum oscillation frequency is pegged at the last deficit value during $l_p$ increasing phase, while the vacuum oscillation speed $V_{T2}$ drops from $c$ by $Ak$ ($as V_{T2} = Ack$). That is, $f_{\text{vac}} = V_{T2}/l_p$. This conserves the energy earlier spatially released during $l_p$ increasing phase. As the GW oscillation continues propagating, it should continuously create standard model photons from the vacuum in its wake until its strain falls below a threshold. Thus RUTE provides an ideal reheating mechanism for a $\Lambda$ driven inflation. Powerful astrophysical sources of gravitational waves should have Gamma Ray Bursts (GRB) counterparts. Therefore GRBs need to be investigated in the light of RUTE’s Gravitational Wave Reheating mechanism.

The detection of Gravitational wave event GW150914 [19] has opened an observational window. The detection of Gamma Ray Burst counterpart GW150914-GBM [20] 0.4 seconds later corresponding to peak strain amplitude shows that there is a threshold strain for Gravitational Wave Reheating. With the peak and threshold strain $\sim 10^{-3}$ in the source frame, the relative elasticity $k$ in eq. (31) $\sim 10^{-20}$. Future joint Gravitational Wave and GRB counterpart observations should provide further observational evidence and constraint for Gravitational Wave Reheating and associated parameters.
7. Dimensional Symmetry

Dimensional Symmetry (DIMSY) in RUTE requires that for every macroscopic spacetime dimension, there is a microscopic dimensional partner with a negative dimension number $D_N$, doubling the number of functional spacetime dimensions of our universe to 8d. In this case, the dimensional partner of the macroscopic time dimension $T_1 = 1d$ is the Planck size $T_2$ dimension $T_2 = -1d$ where as for the macroscopic set of spatial dimensions $S_1 = 3d$, the microscopic counterpart is $S_2 = -3d$.

7.1 Volume Constraint

A key element of RUTE’s dimensional symmetry is that the contraction or expansion of a dimension must be balanced by the expansion or contraction of another dimension as the case may be. Since the area $A$ of the two time dimensions $T_1$ and $T_2$ is equal to its entropy $S = 2\pi r - 1$ (see section 3), $T_1$ can only expand and $T_2$ maintains its Planck size which defines the Planck constant and therefore relatively constant. $T_2$ however can oscillate with $T_1$ to mirror the gravitational wave oscillation of the spatial dimensions provided the surface area of $T_1\cdot T_2$ remains irreducible due to the entropy constraint (see section 6). The gravitational contraction of $S_1$ by positive pressure and energy drives the expansion of time $T_1$ dimension as shown in figure 11. The expansion of the 3 macroscopic spatial dimensions $S_1$ driven by negative pressure is required to be fed by the contraction of its microscopic dimensional partner $S_2 = -3d$.

Figure 11: Gravitational traffic across the 7 dimensions of $T_1 = 1d$, $S_1 = 3d$ and $S_2 = -3d$. $T_2$ is gravitationally inert.
In what follows, we analyze the equation of state constraint of \( S_2 = -3d \) consistent with \( T_1 = 1 \) based on the gravitational traffic across the \( S_1^{\rho,+p} \rightarrow T_1 \) and \( S_2^{-p} \rightarrow S_1 \) dimensions with \( T_2 \) being gravitationally inert as illustrated in figure 11.

The dimension number \( D_N \) of a dimension set, interacting gravitationally with the visible set of 3 spatial dimensions \( S_1 \) is given by

\[
D_N = 3\omega
\]  

(32)

Where \( \omega \) is the equation of state parameter of the most gravitationally attractive or repulsive component existing for a dimension set, which is radiation for \( S_1^{\rho,+p} \) gravitational interaction and \( \Lambda \) for \( S_2^{-p} \rightarrow S_1 \). The absolute value of the dimension number \( D_N \) gives the number of dimensions.

For the \( S_1^{\rho,+p} \) gravitational interaction, radiation equation of state \( \omega_r = 1/3 \). \( D_N \) of \( T_1 \) dimension is given by

\[
T_1 = 3\omega_r
\]  

(33)

Therefore, \( T_1 = 1d \) consistent with observation.

For the \( S_2^{-p} \rightarrow S_1 \) gravitational interaction, \( \Lambda \) equation of state \( \omega_\Lambda = -1 \). \( D_N \) of \( S_2 \) dimension is given by

\[
S_2 = 3\omega_\Lambda.
\]  

(34)

Therefore \( S_2 = -3d \).

Dimensional symmetry also requires that a component with \( \omega = -1/3 \) in the early universe contracted the \( T_2 \) dimension to expand the \( T_1 \) dimension through \( S_1 \) (that is, \( T_2^{-p} \rightarrow S_1 \rightleftharpoons T_1 \)) until \( T_2 \) reached the minimum Planck length scale. The \( D_N \) of \( T_2 \) dimension is the given by

\[
T_2 = 3(-1/3)
\]  

(35)

Therefore \( T_2 = -1d \) giving a total of 8 functional spacetime dimensions \([3+3) + (1+1)]\) even though the total dimension number of the universe is zero. i.e \( D_N = [(3 - 3) + (1 - 1)] \).
7.2 Force Constraint

So far in section 2, we’ve shown how the relative projection of velocity from $T_1$ into the visible spatial dimension $S_2$ gives rise to relativistic effects in a speed constraint. Also, in section 3 we extended this relativistic speed constraint to the interaction between the second time dimension $T_2$ and the visible spatial dimension giving rise to the energy constraint.

In a similar way, the dimensional partners of the visible set of 3 spatial dimensions (the microscopic antispatial dimension set $S_2$) in this frame work are associated with the 3 Standard Model forces. That is, the relative strengths of the electromagnetic, the strong and weak nuclear interactions are determined by the relative projection of Force from the 3 antispatial dimensions into the visible spatial dimensions.

The associated constraint for the $S_1$-$S_2$ interaction is that any reference frame in space-antispace dimension must always experience the Planck Force. This is such that the vector sum of the forces directed along the spatial dimensions $S_1$ and that directed along $S_2$ dimension must always equal the Planck Force. For any of the 3 interactions, the corresponding Lorentz factor associated with this force constraint can be expressed as

$$\gamma = \frac{1}{\sqrt{1-\beta}} \quad (36)$$

and

$$\beta = \frac{F}{F_{Planck}} \quad (37)$$

Where $\beta$ is the coupling parameter which is a function of separation $r$, $F$ is the resultant force along the visible spatial dimensions and $F_{Planck}$ is the Planck Force.

The maximum coupling parameter $\beta_{max}$ for close up interaction at low energy scale gives the coupling constant for such interaction. For instance, for the electromagnetic interaction, $\beta_{max} = \alpha$ the fine structure constant. Eq. (36) becomes

$$\gamma = \frac{1}{\sqrt{1-\frac{e^2}{Q_{Planck}^2}}} \quad (38)$$

Where $e$ is the electronic charge and $Q_{Planck}$ is the Planck charge. Figure 12 shows the 3 relativistic constraints in RUTE.
Figure 12: The basic structure of 8 dimensional spacetime showing the relative projections of Velocity, Energy and Force into the visible spatial dimensions.

7.3 Vacuum Energy Prospect

If the antispatial dimension $S_2$ and anti-time dimension $T_2$ are directly coupled like the visible spatial and time dimension, then a sudden change in the distance dependent coupling parameter in eq. (38) should disturb the vacuum equilibrium of $T_2$ dimension (see section 4.1) and generate high frequency gravitational waves. These Gravitational Waves then generate Standard Model photons through GWR mechanism. In the light of these, the effects of Sonoluminescence, Triboluminescence, and Thunderstorm X-ray and gamma ray flashes need to be investigated.

The relativistic constraints

\[
C^2 = V^2 + V_T^2
\]

\[
P_{Planck}^2 = F^2 + F_{vac}^2
\]

\[
E_{Planck}^2 = E^2 + E_{vac}^2
\]
8. Discussion and Conclusion

RUTE, with its holistic approach, has provided an elegant resolution of dark energy’s cosmological constant problem. Specifically, it is a spill model of $\Lambda$. It relies on its key dimensional symmetry which doubles every spacetime dimension to 8d, the resulting rotating and oscillating 2d ring model of time dimension as defined with the Digit analogy, and the emergent energy density constraint and vacuum state asymmetry.

The energy density constraint ensures that the total energy density available in the visible spatial dimension and vacuum energy which is only available along $T_2$, must always equal the Planck density. The deficit vacuum energy density of one of the vacuum states along $T_2$, ensures a spill of energy into the visible spatial dimensions as dark energy as described by the asymptotically evolving asymmetry parameter – the cosmological factor $\Gamma$. $\Gamma \sim 1$ in the early Universe provided a Planck scale $\Lambda$ that can automatically power inflation before falling asymptotically to its present small value coupled with reheating effectively ending inflation.

The energy density constraint also forbids all forms of infinite energy densities like black hole and big bang singularities. Just like the speed constraint it was derived from, exceeding the Planck density is equivalent to exceeding the speed limit $c$. Instead, black holes are replaced with Planck stars like in [21]. Moreover, the vacuum energy density in such a Planck star must be zero, since the spatial component is already at the maximum Planck value and as such a breakdown of the electromagnetic, the strong and weak nuclear forces should be expected.

RUTE’s Gravitational Wave Reheating mechanism is an interesting outcome where gravitational Waves release vacuum energy as electromagnetic counterpart. This conveniently provides a reheating mechanism for $\Lambda$ driven inflation obviating the need for scalar field inflation. Powerful astrophysical Gravitational Waves should always have Gamma Ray counterpart once their strain exceeds the threshold. Therefore Gamma Ray Bursts needs to be investigated in association with astrophysical sources of gravitational waves.

One major prediction of this RUTE model is light speed oscillation. A photon with frequency $f$ less than the Planck frequency will oscillate its speed between $c$ and $\bar{c}$ (Where $\bar{c}$ is the deficit speed of vacuum state b) at a frequency $f_{\text{vac}} = \sqrt{f_{\text{Planck}}^2 - f^2}$. Again the size of this asymmetry is a function of the cosmological factor $\Gamma$ and therefore asymptotically vanishes with the growth of orbital radius. However, with this speed asymmetry more pronounced in the early universe, it is hoped that some relic evidence is imprinted in the CMB photons.

It is also interesting, how the surface area $A$ of the 2 time dimensions describe the entropy $S$ of our Universe (with $S = 2\pi r - 1$) in an analogous way the surface area $A$ of the event horizon of a black hole describes its entropy $S$ (with $s = \frac{1}{4}A$). This raises the question: Is our Universe a holographic black hole in a much bigger and older Universe as also suggested in [22]? We also discussed in subsection 3.1 about particles–antiparticle transmutation at high
energies, and how disequilibrium from a net spinning Universe can give rise to baryon asymmetry.

If there is discontinuity along $T_1$ time dimension, the reflective boundary condition in this RUTE model ensures a reflection, but in this case, a cyclic particle-antiparticle transmutation with momentum reversal and with a progressively growing wavelength of $2\pi r$. Given that $r = \frac{i_p}{\Gamma} \sim 10^{25} m$ and $\Gamma \sim 10^{-60}$, we should have a present cycle period $t_{p\leftrightarrow\bar{p}} = \frac{2\pi r}{c} \sim 10^{17} s$ though progressively more frequent in the earlier Universe with smaller $r$. The effect of this on the spin reversal of spiral galaxies should provide some observational constraints regarding previous reversals.

In all of this, the DIMSY requirement which doubled the spacetime dimensions here is key and the very idea of using equation of state parameter to constrain the number of functional spacetime dimensions is interesting. If spacetime is quantized according to loop quantum gravity [23], then as the contracting extra spatial dimension $S_2$ reach the minimum Planck scale, the expansion of the 3 macroscopic spatial dimensions $S_1$ stops, leading to the contraction of our Universe as gravity reigns. As the Universe reaches the Planck density during the contraction phase, the density constraint (or Planck degeneracy pressure) stops the contraction, effectively preventing a singularity. What happens from this point depends precisely on the nature of quantum gravity. Nevertheless, if contraction is to proceed, the spatial energy content of the Universe has to be emptied into the $T_2$ dimension until the Hubble length reaches the Planck scale.

RUTE as a model of the fundamental structure of spacetime describing its Velocity, Force and Energy components, demonstrates a holistic approach to the resolution of the cosmological constant problem among other unsolved problems in Physics. Going forward however, there is still a lot of work to be done such as getting to the root of the extra dimensional relationship of the 3 Standard Model forces and unifying general relativity and quantum mechanics among others. Most importantly, RUTE is a viable and testable model.

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