

The binary Goldbach's conjecture. Geometric associations.

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The ellipses of the decomposition of prime numbers.

Let us represent the equation for decomposing an even number into 2 prime numbers as an ellipse equation:

$$|p_k| + |p_t| = 2n$$

where p_k and p_t are prime numbers ($p_1 = 2, p_2 = 3, p_3 = 5, p_4 = 7, \dots$),

k and t are indices of prime numbers,

$2n$ is a given even number,

$k, t, n \in N$.

Consider the following equation:

$$|p_{min}| + |p_{max}| = 2n = 2a$$

where p_{min} is the smallest prime number that satisfies the above equation,

$p_{max} = (2n - p_{min})$ is the largest prime number that satisfies the above equation,

$2n = 2a \Rightarrow a = n$ (semi-major axis).

Then there are ellipse parameters:

perifocal distance $r_p = p_{min}$

apofocal distance $r_a = p_{max}$

focal distance (linear eccentricity) $c = F1F2/2 = (r_a - r_p)/2 = (p_{max} - p_{min})/2 = n - p_{min}$

semi-major axis $a = (r_a + r_p)/2 = (p_{max} + p_{min})/2 = 2n/2 = n$

semi-minor axis $b = \sqrt{a^2 - c^2} = \sqrt{((p_{max} + p_{min})/2)^2 - ((p_{max} - p_{min})/2)^2} = \sqrt{p_{max} * p_{min}}$

focal parameter $f_p = (b^2)/a = (\sqrt{p_{max} * p_{min}})^2/n = (p_{max} * p_{min})/n = (2n - p_{min}) * p_{min}/n$

eccentricity $e = c/a = (n - p_{min})/n = 1 - p_{min}/n$

directrix $d = a^2/c = n^2/(n - p_{min})$

flattening $f = (a - b)/a = 1 - b/a = 1 - (\sqrt{p_{max} * p_{min}})/n$

Each even number corresponds to 1 unique decomposition ellipse.

If $2n \rightarrow \infty$ then $p_{max} \rightarrow \infty$.

Then focal parameter $f_p = (p_{max} * p_{min})/n = (2n - p_{min}) * p_{min}/n = (2 - p_{min}/n) * p_{min} \rightarrow 2 * p_{min}$

eccentricity $e = c/a = (n - p_{min})/n = 1 - p_{min}/n \rightarrow 1$ (ellipse turns into a parabola)

flattening $f = 1 - b/a = 1 - (\sqrt{p_{max} * p_{min}})/n = 1 - (\sqrt{(2n - p_{min}) * p_{min}})/n \rightarrow 1 - (\sqrt{2n * p_{min}})/n = 1 - \sqrt{2 * p_{min}/n} \rightarrow 1$

Conclusion: when $2n \rightarrow \infty$ and $p_{max} \rightarrow \infty$, the length of the minor axis of the ellipse lags behind the length of the major axis and the ellipse is stretched along the major axis.

Hypothesis of intersecting decomposition ellipses: there are only 5 non-intersecting curves (for $2n = 4, 2n = 6, 2n = 8, 2n = 10, 2n = 16$). The remaining ellipses have intersection points.

The decompositions of the numbers 4 and 6 can be represented as circles with radii 2 and 3, respectively.

Decompositions of even numbers ≥ 8 are ellipses.

Canonical equation of an ellipse:

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

or

$$\frac{x^2}{n^2} + \frac{y^2}{p_{maj} * p_{min}} = 1$$

Let's define the intersection points of the ellipses.

$$\begin{aligned}
& \begin{cases} \frac{x^2}{n_1^2} + \frac{y^2}{p_{1max}*p_{1min}} = 1 \\ \frac{x^2}{n_2^2} + \frac{y^2}{p_{2max}*p_{2min}} = 1 \end{cases} \\
& \begin{cases} y^2 = (1 - x^2/n_1^2) * p_{1max} * p_{1min} \\ y^2 = (1 - x^2/n_2^2) * p_{2max} * p_{2min} \end{cases} \\
& (1 - x^2/n_1^2) * p_{1max} * p_{1min} = (1 - x^2/n_2^2) * p_{2max} * p_{2min} \\
& p_{1max} * p_{1min} - \frac{x^2 * p_{1max} * p_{1min}}{n_1^2} = p_{2max} * p_{2min} - \frac{x^2 * p_{2max} * p_{2min}}{n_2^2} \\
& \frac{x^2 * p_{2max} * p_{2min}}{n_2^2} - \frac{x^2 * p_{1max} * p_{1min}}{n_1^2} = p_{2max} * p_{2min} - p_{1max} * p_{1min} \\
& x^2 * \left(\frac{p_{2max} * p_{2min}}{n_2^2} - \frac{p_{1max} * p_{1min}}{n_1^2} \right) = p_{2max} * p_{2min} - p_{1max} * p_{1min} \\
& x^2 = \frac{p_{2max} * p_{2min} - p_{1max} * p_{1min}}{(p_{2max} * p_{2min})/n_2^2 - (p_{1max} * p_{1min})/n_1^2} \\
& x = \pm \sqrt{\frac{p_{2max} * p_{2min} - p_{1max} * p_{1min}}{(p_{2max} * p_{2min})/n_2^2 - (p_{1max} * p_{1min})/n_1^2}} \\
& y = \pm \sqrt{(1 - x^2/n_1^2) * p_{1max} * p_{1min}} \\
& y = \pm \sqrt{(1 - x^2/n_2^2) * p_{2max} * p_{2min}}
\end{aligned}$$

A necessary condition for the existence of ellipse intersection points:

$$\begin{cases} \frac{p_{2max} * p_{2min} - p_{1max} * p_{1min}}{(p_{2max} * p_{2min})/n_2^2 - (p_{1max} * p_{1min})/n_1^2} > 0 \\ (1 - x^2/n_1^2) * p_{1max} * p_{1min} > 0 \\ (1 - x^2/n_2^2) * p_{2max} * p_{2min} > 0 \end{cases}$$

Case 1:

$$\begin{cases} p_{2max} * p_{2min} - p_{1max} * p_{1min} > 0 \\ (p_{2max} * p_{2min})/n_2^2 - (p_{1max} * p_{1min})/n_1^2 > 0 \\ (1 - x^2/n_1^2) * p_{1max} * p_{1min} > 0 \\ (1 - x^2/n_2^2) * p_{2max} * p_{2min} > 0 \end{cases}$$

$$\begin{cases} p_{2max} * p_{2min} > p_{1max} * p_{1min} \\ (p_{2max} * p_{2min})/n_2^2 > (p_{1max} * p_{1min})/n_1^2 \\ 1 - x^2/n_1^2 > 0 \\ 1 - x^2/n_2^2 > 0 \end{cases}$$

$$\begin{cases} p_{2max} * p_{2min} > p_{1max} * p_{1min} \\ (p_{2max} * p_{2min})/n_2^2 > (p_{1max} * p_{1min})/n_1^2 \\ x^2 < n_1^2 \\ x^2 < n_2^2 \end{cases}$$

$$\begin{cases} p_{2max} * p_{2min} > p_{1max} * p_{1min} \\ (p_{2max} * p_{2min})/n_2^2 > (p_{1max} * p_{1min})/n_1^2 \\ -n_1 < x < n_1 \\ -n_2 < x < n_2 \end{cases}$$

Case 2:

$$\begin{cases} p_{2max} * p_{2min} - p_{1max} * p_{1min} < 0 \\ (p_{2max} * p_{2min})/n_2^2 - (p_{1max} * p_{1min})/n_1^2 < 0 \\ (1 - x^2/n_1^2) * p_{1max} * p_{1min} > 0 \\ (1 - x^2/n_2^2) * p_{2max} * p_{2min} > 0 \end{cases}$$

$$\begin{cases} p_{2max} * p_{2min} < p_{1max} * p_{1min} \\ (p_{2max} * p_{2min})/n_2^2 < (p_{1max} * p_{1min})/n_1^2 \\ 1 - x^2/n_1^2 > 0 \\ 1 - x^2/n_2^2 > 0 \end{cases}$$

$$\begin{cases} p_{2max} * p_{2min} < p_{1max} * p_{1min} \\ (p_{2max} * p_{2min})/n_2^2 < (p_{1max} * p_{1min})/n_1^2 \\ x^2 < n_1^2 \\ x^2 < n_2^2 \end{cases}$$

$$\begin{cases} p_{2max} * p_{2min} < p_{1max} * p_{1min} \\ (p_{2max} * p_{2min})/n_2^2 < (p_{1max} * p_{1min})/n_1^2 \\ -n_1 < x < n_1 \\ -n_2 < x < n_2 \end{cases}$$

The note.

Two concentric ellipses intersect each other if $a_2 > a_1$ and $b_2 < b_1$ or $b_2^2 < b_1^2$. That is, the conditions for the intersection of ellipses can be represented as:

$$\begin{cases} n_2 > n_1 \\ \sqrt{p_{2max} * p_{2min}} < \sqrt{p_{1max} * p_{1min}} \end{cases}$$

$$\begin{cases} n_2 > n_1 \\ p_{2max} * p_{2min} < p_{1max} * p_{1min} \end{cases}$$

where $a_2 = n_2$, $a_1 = n_1$, $b_2 = \sqrt{p_{2max} * p_{2min}}$, $b_1 = \sqrt{p_{1max} * p_{1min}}$, $b_2^2 = p_{2max} * p_{2min}$, $b_1^2 = p_{1max} * p_{1min}$.

Examples of intersecting and non-intersecting decomposition ellipses.

Let $2n = 4$, $n = 2$, then $p_{min} = p_{max} = 2$, since $p_{min} + p_{max} = 2 + 2 = 4$.

In this case, the decomposition curve is a circle with radius $r = 2$.

Now let $2n = 6$, $n = 3$, then $p_{min} = p_{max} = 3$, since $p_{min} + p_{max} = 3 + 3 = 6$.

In this case, the decomposition curve is a circle with radius $r = 3$.

For $2n = 4$ and $2n = 6$, we have two concentric circles as decomposition curves, which cannot intersect each other in any way.

Let $2n = 8$, $n = 4$, then $p_{min} = 3$, $p_{max} = 5$, since $p_{min} + p_{max} = 3 + 5 = 8$.
 In this case, the decomposition curve is an ellipse.

Semi-major axis $a = n = 4$.

Semi-minor axis $b = \sqrt{p_{min} * p_{max}} = \sqrt{3 * 5} = \sqrt{15}$.

$$b^2(2n = 8) = p_{min} * p_{max} = 3 * 5 = 15$$

Let $2n = 10$, $n = 5$, then $p_{min} = 3$, $p_{max} = 7$, since $p_{min} + p_{max} = 3 + 7 = 10$.

In this case, the decomposition curve is an ellipse.

Semi-major axis $a = n = 5$.

Semi-minor axis $b = \sqrt{p_{min} * p_{max}} = \sqrt{3 * 7} = \sqrt{21}$.

$$b^2(2n = 10) = p_{min} * p_{max} = 3 * 7 = 21$$

$21 > 15 \Rightarrow$ decomposition ellipses for $2n = 8$ and $2n = 10$ do not intersect.

Let $2n = 12$, $n = 6$, then $p_{min} = 5$, $p_{max} = 7$, since $p_{min} + p_{max} = 5 + 7 = 12$.

In this case, the decomposition curve is an ellipse.

Semi-major axis $a = n = 6$.

Semi-minor axis $b = \sqrt{p_{min} * p_{max}} = \sqrt{5 * 7} = \sqrt{35}$.

$$b^2(2n = 12) = p_{min} * p_{max} = 5 * 7 = 35$$

$35 > 21 \Rightarrow$ decomposition ellipses for $2n = 10$ and $2n = 12$ do not intersect.

Let $2n = 14$, $n = 7$, then $p_{min} = 3$, $p_{max} = 11$, since $p_{min} + p_{max} = 3 + 11 = 14$.

In this case, the decomposition curve is an ellipse.

Semi-major axis $a = n = 7$.

Semi-minor axis $b = \sqrt{p_{min} * p_{max}} = \sqrt{3 * 11} = \sqrt{33}$.

$$b^2(2n = 14) = p_{min} * p_{max} = 3 * 11 = 33$$

$33 < 35 \Rightarrow$ decomposition ellipses for $2n = 12$ and $2n = 14$ intersect.

Let $2n = 16$, $n = 8$, then $p_{min} = 3$, $p_{max} = 13$, since $p_{min} + p_{max} = 3 + 13 = 16$.

In this case, the decomposition curve is an ellipse.

Semi-major axis $a = n = 8$.

Semi-minor axis $b = \sqrt{p_{min} * p_{max}} = \sqrt{3 * 13} = \sqrt{39}$.

$$b^2(2n = 16) = p_{min} * p_{max} = 3 * 13 = 39$$

$39 > 35 \Rightarrow$ decomposition ellipses for $2n = 14$ and $2n = 16$ do not intersect.

Let $2n = 18$, $n = 9$, then $p_{min} = 5$, $p_{max} = 13$, since $p_{min} + p_{max} = 5 + 13 = 18$.

In this case, the decomposition curve is an ellipse.

Semi-major axis $a = n = 9$.

Semi-minor axis $b = \sqrt{p_{min} * p_{max}} = \sqrt{5 * 13} = \sqrt{65}$.

$$b^2(2n = 18) = p_{min} * p_{max} = 5 * 13 = 65$$

$65 > 39 \Rightarrow$ decomposition ellipses for $2n = 16$ and $2n = 18$ do not intersect.

Let $2n = 20$, $n = 10$, then $p_{min} = 3$, $p_{max} = 17$, since $p_{min} + p_{max} = 3 + 17 = 20$.

In this case, the decomposition curve is an ellipse.

Semi-major axis $a = n = 10$.

Semi-minor axis $b = \sqrt{p_{min} * p_{max}} = \sqrt{3 * 17} = \sqrt{51}$.

$$b^2(2n = 20) = p_{min} * p_{max} = 3 * 17 = 51$$

$51 < 65 \Rightarrow$ decomposition ellipses for $2n = 18$ and $2n = 20$ intersect.

Examples of intersection points.

Let $2n_1 = 12$ and $2n_2 = 14$, then $n_1 = 6$, $n_2 = 7$

$$\begin{cases} 12 = 7 + 5 \\ p_{1max} = p_{1max}(12) = 7 \\ p_{1min} = p_{1min}(12) = 5 \end{cases}$$

$$\begin{cases} 14 = 11 + 3 \\ p_{2max} = p_{2max}(14) = 11 \\ p_{2min} = p_{2min}(14) = 3 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2max} * p_{2min} - p_{1max} * p_{1min}}{(p_{2max} * p_{2min})/n_2^2 - (p_{1max} * p_{1min})/n_1^2}} = \pm \sqrt{\frac{11 * 3 - 7 * 5}{(11 * 3)/7^2 - (7 * 5)/6^2}} \approx \pm 2.5874$$

$$y = \pm \sqrt{(1 - x^2/n_1^2) * p_{1max} * p_{1min}} \approx \pm \sqrt{(1 - 2.5874^2/6^2) * 7 * 5} \approx \pm 5.3377$$

Intersection points S of two ellipses with coordinates:

- S1(2.5874; 5.3377)
- S2(-2.5874; 5.3377)
- S3(2.5874; -5.3377)
- S4(-2.5874; -5.33773)

Let $2n_1 = 18$ and $2n_2 = 20$, then $n_1 = 9$, $n_2 = 10$

$$\begin{cases} 18 = 13 + 5 \\ p_{1max} = p_{1max}(18) = 13 \\ p_{1min} = p_{1min}(18) = 5 \end{cases}$$

$$\begin{cases} 20 = 17 + 3 \\ p_{2max} = p_{2max}(20) = 17 \\ p_{2min} = p_{2min}(20) = 3 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2max} * p_{2min} - p_{1max} * p_{1min}}{(p_{2max} * p_{2min})/n_2^2 - (p_{1max} * p_{1min})/n_1^2}} = \pm \sqrt{\frac{17 * 3 - 13 * 5}{17 * 3/10^2 - 13 * 5/9^2}} \approx \pm 6.9187$$

$$y = \pm \sqrt{(1 - x^2/n_1^2) * p_{1max} * p_{1min}} \approx \pm \sqrt{(1 - 6.9187^2/9^2) * 13 * 5} \approx \pm 5.1563$$

Intersection points S of two ellipses with coordinates:

- S1(6.9187; 5.1563)
- S2(-6.9187; 5.1563)
- S3(6.9187; -5.1563)
- S4(-6.9187; -5.1563)

Let $2n_1 = 24$ and $2n_2 = 26$, then $n_1 = 12$, $n_2 = 13$

$$\begin{cases} 24 = 19 + 5 \\ p_{1max} = p_{1max}(24) = 19 \\ p_{1min} = p_{1min}(24) = 5 \end{cases}$$

$$\begin{cases} 26 = 23 + 3 \\ p_{2max} = p_{2max}(26) = 23 \\ p_{2min} = p_{2min}(26) = 3 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2max} * p_{2min} - p_{1max} * p_{1min}}{(p_{2max} * p_{2min})/n_2^2 - (p_{1max} * p_{1min})/n_1^2}} = \pm \sqrt{\frac{23 * 3 - 19 * 5}{23 * 3/13^2 - 19 * 5/12^2}} \approx \pm 10.1688$$

$$y = \pm \sqrt{(1 - x^2/n_1^2) * p_{1max} * p_{1min}} \approx \pm \sqrt{(1 - 10.1688^2/12^2) * 19 * 5} \approx \pm 5.1751$$

Intersection points S of two ellipses with coordinates:

$$S1(10.1688; 5.1751)$$

$$S2(-10.1688; 5.1751)$$

$$S3(10.1688; -5.1751)$$

$$S4(-10.1688; -5.1751)$$

Let $2n_1 = 42$ and $2n_2 = 44$, then $n_1 = 21$, $n_2 = 22$

$$\begin{cases} 42 = 37 + 5 \\ p_{1max} = p_{1max}(42) = 37 \\ p_{1min} = p_{1min}(42) = 5 \end{cases}$$

$$\begin{cases} 44 = 41 + 3 \\ p_{2max} = p_{2max}(44) = 41 \\ p_{2min} = p_{2min}(44) = 3 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2max} * p_{2min} - p_{1max} * p_{1min}}{(p_{2max} * p_{2min})/n_2^2 - (p_{1max} * p_{1min})/n_1^2}} = \pm \sqrt{\frac{41 * 3 - 37 * 5}{41 * 3/22^2 - 37 * 5/21^2}} \approx \pm 19.3628$$

$$y = \pm \sqrt{(1 - x^2/n_1^2) * p_{1max} * p_{1min}} \approx \pm \sqrt{(1 - 19.3628^2/21^2) * 37 * 5} \approx \pm 5.2651$$

Intersection points S of two ellipses with coordinates:

$$S1(19.3628; 5.2651)$$

$$S2(-19.3628; 5.2651)$$

$$S3(19.3628; -5.2651)$$

$$S4(-19.3628; -5.2651)$$

Let $2n_1 = 48$ and $2n_2 = 50$, then $n_1 = 24$, $n_2 = 25$

$$\begin{cases} 48 = 43 + 5 \\ p_{1max} = p_{1max}(48) = 43 \\ p_{1min} = p_{1min}(48) = 5 \end{cases}$$

$$\begin{cases} 50 = 47 + 3 \\ p_{2max} = p_{2max}(50) = 47 \\ p_{2min} = p_{2min}(50) = 3 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2max} * p_{2min} - p_{1max} * p_{1min}}{(p_{2max} * p_{2min})/n_2^2 - (p_{1max} * p_{1min})/n_1^2}} = \pm \sqrt{\frac{47 * 3 - 43 * 5}{47 * 3/25^2 - 43 * 5/24^2}} \approx \pm 22.3861$$

$$y = \pm \sqrt{(1 - x^2/n_1^2) * p_{1max} * p_{1min}} \approx \pm \sqrt{(1 - 22.3861^2/24^2) * 43 * 5} \approx \pm 5.2861$$

Intersection points S of two ellipses with coordinates:

$$S1(22.3861; 5.2861)$$

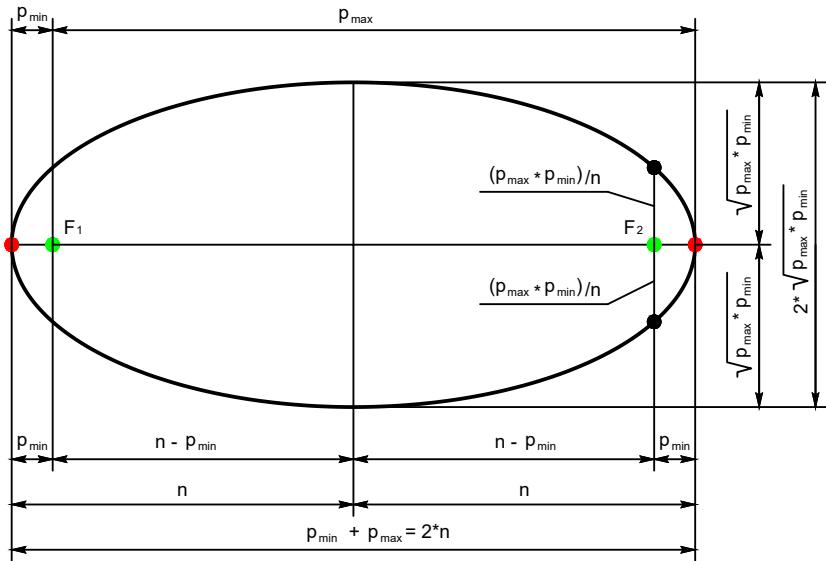
$$S2(-22.3861; 5.2861)$$

$$S3(22.3861; -5.2861)$$

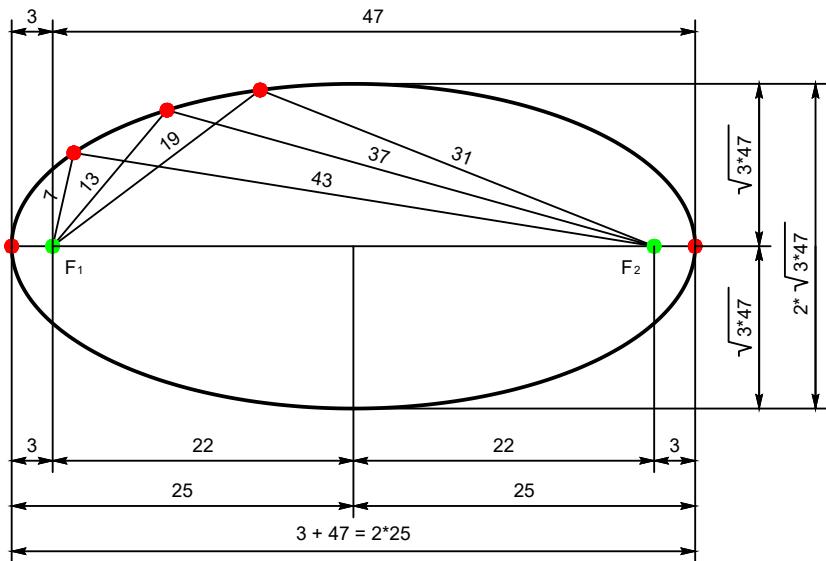
$$S4(-22.3861; -5.2861)$$

It is interesting to know whether there are still non-intersecting decomposition ellipses? Is the proposed hypothesis correct? How to check it? The questions remains open.

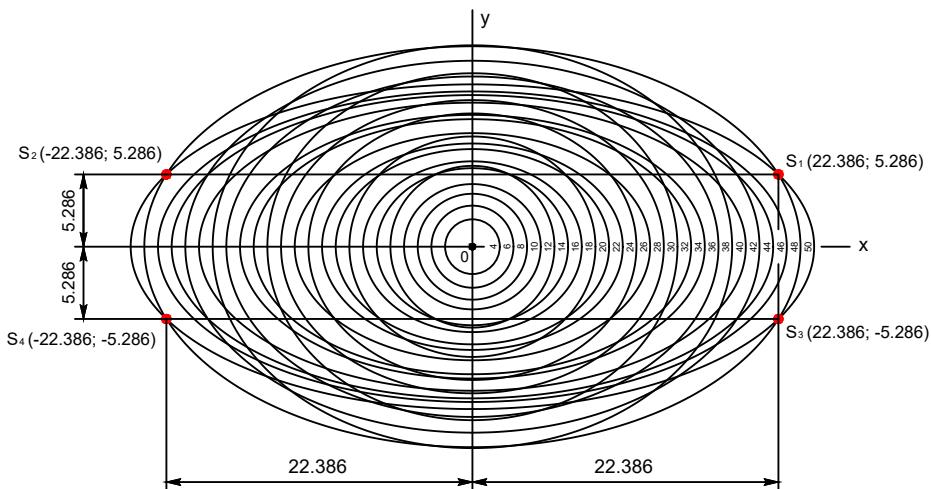
Ellipse of the decomposition of an even number
into the sums of two prime numbers



Ellipse of the decomposition of the number 50
into the sums of two prime numbers



Family of ellipses of decompositions
of even numbers into the sum of 2 prime numbers



The hyperbolas of the decomposition of prime numbers.

Let us represent the equation for decomposing an even number into 2 prime numbers as a hyperbola equation:

$$||p_k| - |p_t|| = 2n$$

where p_k and p_t are prime numbers ($p_1 = 2, p_2 = 3, p_3 = 5, p_4 = 7, \dots$),

k and t are indices of prime numbers,

$2n$ is a given even number,

$k, t, n \in N$.

Consider the following equation:

$$||p_{major} - p_{minor}|| = 2n = 2a$$

where p_{minor} is the smallest prime number that satisfies the above equation,

$p_{major} = (p_{minor} + 2n)$ is the largest prime number that satisfies the above equation,

$2n = 2a \Rightarrow a = n$ (semi-major axis of a hyperbola).

Then there are hyperbola parameters:

semi-major axis of a hyperbola $a = n$

perifocal distance (pericentric distance) $r_p = p_{minor} = p_{min}$

apofocal distance $r_a = p_{major} = p_{maj}$

focal distance (linear eccentricity) $c = n + p_{min}$

semi-minor axis of a hyperbola (impact parameter) $b = \sqrt{c^2 - a^2} = \sqrt{(n + p_{min})^2 - n^2} = \sqrt{(2n + p_{min}) * p_{min}} = \sqrt{p_{maj} * p_{min}}$

focal parameter $f_p = (b^2)/a = p_{maj} * p_{min}/n$

eccentricity $e = c/a = (n + p_{min})/n = 1 + p_{min}/n$

directrix $d = a^2/c = n^2/(n + p_{min})$

hyperbola asymptote equation $y = \pm(b/a) * x = \pm(\frac{\sqrt{p_{maj} * p_{min}}}{n}) * x$

To simplify the hyperbola equation can be written in the following form:

$$||p_{maj} - p_{min}|| = 2n$$

Each even number corresponds to 1 unique decomposition hyperbola.

Canonical equation of a hyperbola:

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

or

$$\frac{x^2}{n^2} - \frac{y^2}{p_{maj} * p_{min}} = 1$$

If $2n \rightarrow \infty$ then $p_{maj} \rightarrow \infty$

then focal parameter $f_p = (2n + p_{min}) * p_{min}/n = (2 + p_{min}/n) * p_{min} \rightarrow 2 * p_{min}$

eccentricity $e = c/a = 1 + p_{min}/n \rightarrow 1$ (hyperbola turns into a parabola)

flattening $f = 1 - b/a = 1 - (\sqrt{p_{maj} * p_{min}})/n = 1 - (\sqrt{(2n + p_{min}) * p_{min}})/n \rightarrow 1 - (\sqrt{2n * p_{min}})/n = 1 - \sqrt{2 * p_{min}/n} \rightarrow 1$

Conclusion: $2n \rightarrow \infty$ and $p_{maj} \rightarrow \infty$, hyperbola stretches along the horizontal axis.

The decompositions of the numbers 0 can be represented as vertical line.

Decompositions of even numbers ≥ 2 can be represented as are hyperbolas.

Hypothesis of intersecting decomposition hyperbolas: there is only 1 non-intersecting hyperbola (for $2n = 2$) and 1 non-intersecting vertical line. The remaining hyperbolas have intersection points.

Let's define the intersection points of the hyperbolas.

$$\begin{cases} \frac{x^2}{a_2^2} - \frac{y^2}{b_2^2} = 1 \\ \frac{x^2}{a_1^2} - \frac{y^2}{b_1^2} = 1 \end{cases}$$

$$\begin{cases} y^2 = (x^2/a_1^2 - 1) * b_1^2 \\ y^2 = (x^2/a_2^2 - 1) * b_2^2 \end{cases}$$

$$(x^2/a_2^2 - 1) * b_2^2 = (x^2/a_1^2 - 1) * b_1^2$$

$$x^2 * b_2^2/a_2^2 - b_2^2 = x^2 * b_1^2/a_1^2 - b_1^2$$

$$x^2 * b_2^2/a_2^2 - x^2 * b_1^2/a_1^2 = b_2^2 - b_1^2$$

$$x^2 * (b_2^2/a_2^2 - b_1^2/a_1^2) = b_2^2 - b_1^2$$

$$x^2 = \frac{b_2^2 - b_1^2}{b_2^2/a_2^2 - b_1^2/a_1^2}$$

$$x = \pm \sqrt{\frac{b_2^2 - b_1^2}{b_2^2/a_2^2 - b_1^2/a_1^2}}$$

$$\begin{cases} b_2^2 = p_{2maj} * p_{2min} \\ b_1^2 = p_{1maj} * p_{1min} \\ a_2^2 = n_2^2 \\ a_1^2 = n_1^2 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2maj} * p_{2min} - p_{1maj} * p_{1min}}{p_{2maj} * p_{2min}/n_2^2 - p_{1maj} * p_{1min}/n_1^2}}$$

$$\begin{cases} y^2 = (x^2/n_1^2 - 1) * p_{1maj} * p_{1min} \\ y^2 = (x^2/n_2^2 - 1) * p_{2maj} * p_{2min} \end{cases}$$

$$\begin{cases} y = \pm \sqrt{(x^2/n_1^2 - 1) * p_{1maj} * p_{1min}} \\ y = \pm \sqrt{(x^2/n_2^2 - 1) * p_{2maj} * p_{2min}} \end{cases}$$

Necessary conditions for the existence of intersection points hyperbolas:

$$\begin{cases} x^2 = \frac{b_2^2 - b_1^2}{b_2^2/a_2^2 - b_1^2/a_1^2} > 0 \\ y^2 = (x^2/a_1^2 - 1) * b_1^2 \\ y^2 = (x^2/a_2^2 - 1) * b_2^2 \end{cases}$$

Case 1:

$$\begin{cases} b_2^2 - b_1^2 > 0 \\ b_2^2/a_2^2 - b_1^2/a_1^2 > 0 \\ x^2/n_1^2 - 1 > 0 \\ x^2/n_2^2 - 1 > 0 \end{cases}$$

$$\begin{cases} b_2^2 > b_1^2 \\ b_2^2/a_2^2 > b_1^2/a_1^2 \\ x^2/n_1^2 > 1 \\ x^2/n_2^2 > 1 \end{cases}$$

$$\begin{cases} p_{2maj} * p_{2min} > p_{1maj} * p_{1min} \\ p_{2maj} * p_{2min}/n_2^2 > p_{1maj} * p_{1min}/n_1^2 \\ x^2 > n_1^2 \\ x^2 > n_2^2 \end{cases}$$

$$\begin{cases} p_{2maj} * p_{2min} > p_{1maj} * p_{1min} \\ p_{2maj} * p_{2min}/n_2^2 > p_{1maj} * p_{1min}/n_1^2 \\ -n_1 > x \cup x > n_1 \\ -n_2 > x \cup x > n_2 \end{cases}$$

Consider the inequality:

$$p_{2maj} * p_{2min}/n_2^2 > p_{1maj} * p_{1min}/n_1^2$$

$$\begin{cases} p_{2maj} = 2n_2 + p_{2min} \\ p_{1maj} = 2n_1 + p_{1min} \end{cases}$$

$$(2n_2 + p_{2min}) * p_{2min}/n_2^2 > (2n_1 + p_{1min}) * p_{1min}/n_1^2$$

$$2n_2 * p_{2min}/n_2^2 + p_{2min}^2/n_2^2 > 2n_1 * p_{1min}/n_1^2 + p_{1min}^2/n_1^2$$

$$2 * p_{2min}/n_2 + p_{2min}^2/n_2^2 > 2 * p_{1min}/n_1 + p_{1min}^2/n_1^2$$

$$2 * p_{2min}/n_2 - 2 * p_{1min}/n_1 + p_{2min}^2/n_2^2 - p_{1min}^2/n_1^2 > 0$$

$$2 * (p_{2min}/n_2 - p_{1min}/n_1) + (p_{2min}/n_2 - p_{1min}/n_1) * (p_{2min}/n_2 + p_{1min}/n_1) > 0$$

$$(p_{2min}/n_2 - p_{1min}/n_1) * (2 + p_{2min}/n_2 + p_{1min}/n_1) > 0$$

$$2 + p_{2min}/n_2 + p_{1min}/n_1 > 0, \text{ because } p_{2min}/n_2 > 0 \text{ and } p_{1min}/n_1 > 0$$

$$p_{2min}/n_2 - p_{1min}/n_1 > 0$$

$$p_{2min}/n_2 > p_{1min}/n_1$$

Let us replace the inequality $p_{2maj} * p_{2min}/n_2^2 > p_{1maj} * p_{1min}/n_1^2$ by the inequality $p_{2min}/n_2 > p_{1min}/n_1$.

Then the conditions for intersection of hyperbolas can be written as follows:

$$\begin{cases} p_{2maj} * p_{2min} > p_{1maj} * p_{1min} \\ p_{2min}/n_2 > p_{1min}/n_1 \\ -n_1 > x \cup x > n_1 \\ -n_2 > x \cup x > n_2 \end{cases}$$

Case 2:

$$\begin{cases} b_2^2 - b_1^2 < 0 \\ b_2^2/a_2^2 - b_1^2/a_1^2 < 0 \\ x^2/n_1^2 - 1 > 0 \\ x^2/n_2^2 - 1 > 0 \end{cases}$$

$$\begin{cases} b_2^2 < b_1^2 \\ b_2^2/a_2^2 < b_1^2/a_1^2 \\ x^2/n_1^2 > 1 \\ x^2/n_2^2 > 1 \end{cases}$$

$$\begin{cases} p_{2maj} * p_{2min} < p_{1maj} * p_{1min} \\ p_{2maj} * p_{2min}/n_2^2 < p_{1maj} * p_{1min}/n_1^2 \\ x^2 > n_1^2 \\ x^2 > n_2^2 \end{cases}$$

$$\begin{cases} p_{2maj} * p_{2min} < p_{1maj} * p_{1min} \\ p_{2maj} * p_{2min}/n_2^2 < p_{1maj} * p_{1min}/n_1^2 \\ -n_1 > x \cup x > n_1 \\ -n_2 > x \cup x > n_2 \end{cases}$$

$$\begin{cases} p_{2maj} * p_{2min} < p_{1maj} * p_{1min} \\ p_{2min}/n_2 < p_{1min}/n_1 \\ -n_1 > x \cup x > n_1 \\ -n_2 > x \cup x > n_2 \end{cases}$$

The note.

$$\tan \alpha = b/a, \tan \alpha_2 = b_2/a_2, \tan \alpha_1 = b_1/a_1$$

$$b = \sqrt{p_{maj} * p_{min}}, b_2 = \sqrt{p_{2maj} * p_{2min}}, b_1 = \sqrt{p_{1maj} * p_{1min}}$$

$$a = n, a_2 = n_2, a_1 = n_1, a_2 > a_1, n_2 > n_1, 2n_2 > 2n_1, n_2 > n_1.$$

Condition for the existence of intersection points hyperbolas:

an angle between the asymptote of hyperbola and the horizontal axis must increase $\alpha_2 > \alpha_1$ for $n_2 > n_1$.

$$\tan \alpha_2 > \tan \alpha_1$$

$$\frac{b_2}{a_2} > \frac{b_1}{a_1}$$

$$\frac{\sqrt{p_{2maj} * p_{2min}}}{n_2} > \frac{\sqrt{p_{1maj} * p_{1min}}}{n_1}$$

$$\frac{b_2^2}{a_2^2} > \frac{b_1^2}{a_1^2}$$

$$\frac{p_{2maj} * p_{2min}}{n_2^2} > \frac{p_{1maj} * p_{1min}}{n_1^2}$$

or which is the same

$$p_{2min}/n_2 > p_{1min}/n_1$$

Examples of intersecting and non-intersecting decomposition hyperbolae.

For simplification, we take as the main criterion of intersection: $p_{2min}/n_2 > p_{1min}/n_1$

Let $2n = 2$, $n = 1$, then $p_{min} = 3$, $p_{maj} = 5$, since $||p_{maj}| - |p_{min}|| = ||5| - |3|| = 2$, $p_{min}/n = 3/1 = 3$.

Let $2n = 4$, $n = 2$, then $p_{min} = 3$, $p_{maj} = 7$, since $||p_{maj}| - |p_{min}|| = ||7| - |3|| = 4$, $p_{min}/n = 3/2 = 1.5$

$1.5 < 3 \Rightarrow$ decomposition hyperbolae for $2n = 4$ and $2n = 2$ do not intersect.

Let $2n = 6$, $n = 3$, then $p_{min} = 5$, $p_{maj} = 11$, since $||p_{maj}| - |p_{min}|| = ||11| - |5|| = 6$, $p_{min}/n = 5/3 \approx 1.6667$

$1.6667 > 1.5 \Rightarrow$ decomposition hyperbolae for $2n = 6$ and $2n = 4$ intersect.

Let $2n = 8$, $n = 4$, then $p_{min} = 3$, $p_{maj} = 11$, since $||p_{maj}| - |p_{min}|| = ||11| - |3|| = 8$, $p_{min}/n = 3/4 = 0.75$

$0.75 < 1.6667 \Rightarrow$ decomposition hyperbolae for $2n = 8$ and $2n = 6$ do not intersect.

Let $2n = 10$, $n = 5$, then $p_{min} = 3$, $p_{maj} = 13$, since $||p_{maj}| - |p_{min}|| = ||13| - |3|| = 10$, $p_{min}/n = 3/5 = 0.6$

$0.6 < 0.75 \Rightarrow$ decomposition hyperbolae for $2n = 10$ and $2n = 8$ do not intersect.

Let $2n = 12$, $n = 6$, then $p_{min} = 5$, $p_{maj} = 17$, since $||p_{maj}| - |p_{min}|| = ||17| - |5|| = 12$, $p_{min}/n = 5/6 \approx 0.8333$

$0.8333 > 0.6 \Rightarrow$ decomposition hyperbolae for $2n = 12$ and $2n = 10$ intersect.

Let $2n = 14$, $n = 7$, then $p_{min} = 3$, $p_{maj} = 17$, since $||p_{maj}| - |p_{min}|| = ||17| - |3|| = 14$, $p_{min}/n = 3/7 \approx 0.4286$

$0.4286 < 0.8333 \Rightarrow$ decomposition hyperbolae for $2n = 14$ and $2n = 12$ do not intersect.

Let $2n = 16$, $n = 8$, then $p_{min} = 3$, $p_{maj} = 19$, since $||p_{maj}| - |p_{min}|| = ||19| - |3|| = 16$, $p_{min}/n = 3/8 = 0.375$

$0.375 < 0.8333 \Rightarrow$ decomposition hyperbolae for $2n = 16$ and $2n = 14$ do not intersect.

Let $2n = 18$, $n = 9$, then $p_{min} = 5$, $p_{maj} = 23$, since $||p_{maj}| - |p_{min}|| = ||23| - |5|| = 18$, $p_{min}/n = 5/9 \approx 0.5556$

$0.5556 > 0.375 \Rightarrow$ decomposition hyperbolae for $2n = 18$ and $2n = 16$ intersect.

Examples of intersection points.

Let $2n_1 = 2$ and $2n_2 = 4$, then $n_1 = 1, n_2 = 2$

$$\begin{cases} p_{1maj} = p_{1maj}(2) = 5 \\ p_{1min} = p_{1min}(2) = 3 \end{cases}$$

$$\begin{cases} p_{2maj} = p_{2maj}(4) = 7 \\ p_{2min} = p_{2min}(4) = 3 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2maj} * p_{2min} - p_{1maj} * p_{1min}}{p_{2maj} * p_{2min}/n_2^2 - p_{1maj} * p_{1min}/n_1^2}} = \pm \sqrt{\frac{7 * 3 - 5 * 3}{7 * 3/2^2 - 5 * 3/1^2}} \approx \pm \sqrt{-0.6154}$$

$$y = \pm \sqrt{(x^2/n_1^2 - 1) * p_{1maj} * p_{1min}} \approx \pm \sqrt{(-0.6154/1^2 - 1) * 5 * 3} \approx \pm \sqrt{-24.2308}$$

$-0.6154 < 0$ and $-24.2308 < 0 \Rightarrow x$ and y are not real numbers, that is, there are no intersections of hyperbolas for $2n_1 = 2$ and $2n_2 = 4$ on the real plane.

Let $2n_1 = 4$ and $2n_2 = 6$, then $n_1 = 2, n_2 = 3$

$$\begin{cases} p_{1maj} = p_{1maj}(4) = 7 \\ p_{1min} = p_{1min}(4) = 3 \end{cases}$$

$$\begin{cases} p_{2maj} = p_{2maj}(6) = 11 \\ p_{2min} = p_{2min}(6) = 5 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2maj} * p_{2min} - p_{1maj} * p_{1min}}{p_{2maj} * p_{2min}/n_2^2 - p_{1maj} * p_{1min}/n_1^2}} = \pm \sqrt{\frac{11 * 5 - 7 * 3}{11 * 5/3^2 - 7 * 3/2^2}} \approx \pm 6.2836$$

$$y = \pm \sqrt{(x^2/n_1^2 - 1) * p_{1maj} * p_{1min}} \approx \pm \sqrt{(6.2836^2/2^2 - 1) * 7 * 3} \approx \pm 13.6488$$

Intersection points S of two hyperbolas with coordinates:

S1(6.2836; 13.6488)

S2(-6.2836; 13.6488)

S3(6.2836; -13.6488)

S4(-6.2836; -13.6488)

Let $2n_1 = 6$ and $2n_2 = 8$, then $n_1 = 3, n_2 = 4$

$$\begin{cases} p_{1maj} = p_{1maj}(6) = 11 \\ p_{1min} = p_{1min}(6) = 5 \end{cases}$$

$$\begin{cases} p_{2maj} = p_{2maj}(8) = 11 \\ p_{2min} = p_{2min}(8) = 3 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2maj} * p_{2min} - p_{1maj} * p_{1min}}{p_{2maj} * p_{2min}/n_2^2 - p_{1maj} * p_{1min}/n_1^2}} = \pm \sqrt{\frac{11 * 3 - 11 * 5}{11 * 3/4^2 - 11 * 5/3^2}} \approx \pm 2.3311$$

$$y = \pm \sqrt{(x^2/n_1^2 - 1) * p_{1maj} * p_{1min}} \approx \pm \sqrt{(2.3311^2/3^2 - 1) * 11 * 5} \approx \pm \sqrt{-21.7925}$$

$-21.7925 < 0 \Rightarrow y$ is not real numbers, that is, there are no intersections of hyperbolas for $2n_1 = 6$ and $2n_2 = 8$ on the real plane.

Let $2n_1 = 8$ and $2n_2 = 10$, then $n_1 = 4$, $n_2 = 5$

$$\begin{cases} p_{1maj} = p_{1maj}(8) = 11 \\ p_{1min} = p_{1min}(8) = 3 \end{cases}$$

$$\begin{cases} p_{2maj} = p_{2maj}(10) = 13 \\ p_{2min} = p_{2min}(10) = 3 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2maj} * p_{2min} - p_{1maj} * p_{1min}}{p_{2maj} * p_{2min}/n_2^2 - p_{1maj} * p_{1min}/n_1^2}} = \pm \sqrt{\frac{13 * 3 - 11 * 3}{13 * 3/5^2 - 11 * 3/4^2}} \approx \pm \sqrt{-11.9403}$$

$$y = \pm \sqrt{(x^2/n_1^2 - 1) * p_{1maj} * p_{1min}} \approx \pm \sqrt{(-11.9403/4^2 - 1) * 11 * 3} \approx \pm \sqrt{-57.6269}$$

$-11.9403 < 0$ and $-57.6269 < 0 \Rightarrow x$ and y are not real numbers, that is, there are no intersections of hyperbolas for $2n_1 = 2$ and $2n_2 = 4$ on the real plane.

Let $2n_1 = 8$ and $2n_2 = 12$, then $n_1 = 4$, $n_2 = 6$

$$\begin{cases} p_{1maj} = p_{1maj}(8) = 11 \\ p_{1min} = p_{1min}(8) = 3 \end{cases}$$

$$\begin{cases} p_{2maj} = p_{2maj}(12) = 17 \\ p_{2min} = p_{2min}(12) = 5 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2maj} * p_{2min} - p_{1maj} * p_{1min}}{p_{2maj} * p_{2min}/n_2^2 - p_{1maj} * p_{1min}/n_1^2}} = \pm \sqrt{\frac{17 * 5 - 11 * 3}{17 * 5/6^2 - 11 * 3/4^2}} \approx \pm 13.1962$$

$$y = \pm \sqrt{(x^2/n_1^2 - 1) * p_{1maj} * p_{1min}} \approx \pm \sqrt{(13.1962^2/4^2 - 1) * 11 * 3} \approx \pm 18.0600$$

Intersection points S of two hyperbolas with coordinates:

S1(13.1962; 18.0600)

S2(-13.1962; 18.0600)

S3(13.1962; -18.0600)

S4(-13.1962; -18.0600)

Let $2n_1 = 10$ and $2n_2 = 12$, then $n_1 = 5$, $n_2 = 6$

$$\begin{cases} p_{2maj} = p_{2maj}(10) = 13 \\ p_{2min} = p_{2min}(10) = 3 \end{cases}$$

$$\begin{cases} p_{2maj} = p_{2maj}(12) = 17 \\ p_{2min} = p_{2min}(12) = 5 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2maj} * p_{2min} - p_{1maj} * p_{1min}}{p_{2maj} * p_{2min}/n_2^2 - p_{1maj} * p_{1min}/n_1^2}} = \pm \sqrt{\frac{17 * 5 - 13 * 3}{17 * 5/6^2 - 13 * 3/5^2}} \approx \pm 7.5776$$

$$y = \pm \sqrt{(x^2/n_1^2 - 1) * p_{1maj} * p_{1min}} \approx \pm \sqrt{(7.5776^2/5^2 - 1) * 13 * 3} \approx \pm 7.1117$$

Intersection points S of two hyperbolas with coordinates:

$$S1(7.5776; 7.1117)$$

$$S2(-7.5776; 7.1117)$$

$$S3(7.5776; -7.1117)$$

$$S4(-7.5776; -7.1117)$$

Let $2n_1 = 12$ and $2n_2 = 14$, then $n_1 = 6, n_2 = 7$

$$\begin{cases} p_{1maj} = p_{1maj}(12) = 17 \\ p_{1min} = p_{1min}(12) = 5 \end{cases}$$

$$\begin{cases} p_{2maj} = p_{2maj}(14) = 17 \\ p_{2min} = p_{2min}(14) = 3 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2maj} * p_{2min} - p_{1maj} * p_{1min}}{p_{2maj} * p_{2min}/n_2^2 - p_{1maj} * p_{1min}/n_1^2}} = \pm \sqrt{\frac{17 * 3 - 17 * 5}{17 * 3/7^2 - 17 * 5/6^2}} \approx \pm 5.0746$$

$$y = \pm \sqrt{(x^2/n_1^2 - 1) * p_{1maj} * p_{1min}} \approx \pm \sqrt{(5.0746^2/6^2 - 1) * 17 * 5} \approx \pm \sqrt{-24.1971}$$

$-24.1971 < 0 \Rightarrow y$ is not real numbers, that is, there are no intersections of hyperbolas for $2n_1 = 12$ and $2n_2 = 14$ on the real plane.

Let $2n_1 = 14$ and $2n_2 = 16$, then $n_1 = 7, n_2 = 8$

$$\begin{cases} p_{1maj} = p_{1maj}(14) = 17 \\ p_{1min} = p_{1min}(14) = 3 \end{cases}$$

$$\begin{cases} p_{2maj} = p_{2maj}(16) = 19 \\ p_{2min} = p_{2min}(16) = 3 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2maj} * p_{2min} - p_{1maj} * p_{1min}}{p_{2maj} * p_{2min}/n_2^2 - p_{1maj} * p_{1min}/n_1^2}} = \pm \sqrt{\frac{19 * 3 - 17 * 3}{19 * 3/8^2 - 17 * 3/7^2}} \approx \pm \sqrt{-39.9490}$$

$$y = \pm \sqrt{(x^2/n_1^2 - 1) * p_{1maj} * p_{1min}} \approx \pm \sqrt{(-39.9490/7^2 - 1) * 17 * 3} \approx \pm \sqrt{-92.5796}$$

$-39.9490 < 0$ and $-92.5796 < 0 \Rightarrow x$ and y are not real numbers, that is, there are no intersections of hyperbolas for $2n_1 = 14$ and $2n_2 = 16$ on the real plane.

Let $2n_1 = 10$ and $2n_2 = 18$, then $n_1 = 5, n_2 = 9$

$$\begin{cases} p_{1maj} = p_{1maj}(10) = 13 \\ p_{1min} = p_{1min}(10) = 3 \end{cases}$$

$$\begin{cases} p_{2maj} = p_{2maj}(18) = 23 \\ p_{2min} = p_{2min}(18) = 5 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2maj} * p_{2min} - p_{1maj} * p_{1min}}{p_{2maj} * p_{2min}/n_2^2 - p_{1maj} * p_{1min}/n_1^2}} = \pm \sqrt{\frac{23 * 5 - 13 * 3}{23 * 5/9^2 - 13 * 3/5^2}} \approx \pm \sqrt{-541.9014}$$

$$y = \pm \sqrt{(x^2/n_1^2 - 1) * p_{1maj} * p_{1min}} \approx \pm \sqrt{(-541.9014/5^2 - 1) * 13 * 3} \approx \pm \sqrt{-884.3662}$$

$-541.9014 < 0$ and $-884.3662 < 0 \Rightarrow x$ and y are not real numbers, that is, there are no intersections of hyperbolas for $2n_1 = 10$ and $2n_2 = 18$ on the real plane.

Let $2n_1 = 14$ and $2n_2 = 18$, then $n_1 = 7$, $n_2 = 9$

$$\begin{cases} p_{1maj} = p_{1maj}(14) = 17 \\ p_{1min} = p_{1min}(14) = 3 \end{cases}$$

$$\begin{cases} p_{2maj} = p_{2maj}(18) = 23 \\ p_{2min} = p_{2min}(18) = 5 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2maj} * p_{2min} - p_{1maj} * p_{1min}}{p_{2maj} * p_{2min}/n_2^2 - p_{1maj} * p_{1min}/n_1^2}} = \pm \sqrt{\frac{23 * 5 - 17 * 3}{23 * 5/9^2 - 17 * 3/7^2}} \approx \pm 12.9959$$

$$y = \pm \sqrt{(x^2/n_1^2 - 1) * p_{1maj} * p_{1min}} \approx \pm \sqrt{(12.9959^2/7^2 - 1) * 17 * 3} \approx \pm 11.1708$$

Intersection points S of two hyperbolas with coordinates:

S1(12.9959; 11.1708)

S2(-12.9959; 11.1708)

S3(12.9959; -11.1708)

S4(-12.9959; -11.1708)

Let $2n_1 = 16$ and $2n_2 = 18$, then $n_1 = 8$, $n_2 = 9$

$$\begin{cases} p_{1maj} = p_{1maj}(16) = 19 \\ p_{1min} = p_{1min}(16) = 3 \end{cases}$$

$$\begin{cases} p_{2maj} = p_{2maj}(18) = 23 \\ p_{2min} = p_{2min}(18) = 5 \end{cases}$$

$$x = \pm \sqrt{\frac{p_{2maj} * p_{2min} - p_{1maj} * p_{1min}}{p_{2maj} * p_{2min}/n_2^2 - p_{1maj} * p_{1min}/n_1^2}} = \pm \sqrt{\frac{23 * 5 - 19 * 3}{23 * 5/9^2 - 19 * 3/8^2}} \approx \pm 10.4697$$

$$y = \pm \sqrt{(x^2/n_1^2 - 1) * p_{1maj} * p_{1min}} \approx \pm \sqrt{(10.4697^2/8^2 - 1) * 19 * 3} \approx \pm 6.3738$$

Intersection points S of two hyperbolas with coordinates:

S1(10.4697; 6.3738)

S2(-10.4697; 6.3738)

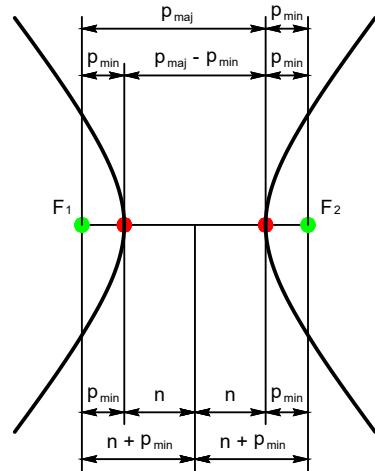
S3(10.4697; -6.3738)

S4(-10.4697; -6.3738)

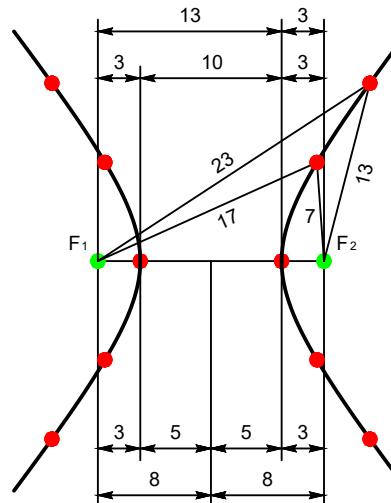
Unfortunately, I cannot check all the hyperbolas of the decomposition of numbers.
There are infinitely many decomposition hyperbolas.

It is interesting to know whether there are still non-intersecting decomposition hyperbolas?
Is the proposed hypothesis correct? How to check it? The questions remains open.

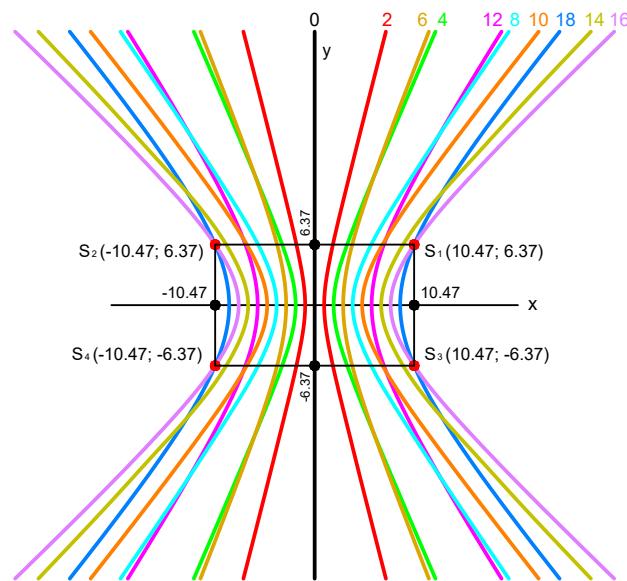
Hyperbola of the decomposition of an even number
into pairs of differences of odd prime numbers



Hyperbola of the decomposition of an even number 10
into pairs of differences of odd prime numbers



Family of hyperbolas of decompositions
into pairs of differences of odd prime numbers



References

- [1] Wikipedia: Goldbach's conjecture. https://en.wikipedia.org/wiki/Goldbach%27s_conjecture
- [2] Wikipedia: Ellipse <https://en.wikipedia.org/wiki/Ellipse>
- [3] Wikipedia: Hyperbola <https://en.wikipedia.org/wiki/Hyperbola>
- [4] Wikipedia: Flattening <https://en.wikipedia.org/wiki/Flattening>