

# **A function that represents all primes exactly and without exception**

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## **Abstract**

We can find all prime numbers in steps of Fibonacci or Lucas numbers.

The function that generates those prime numbers is:

$$dn / dx = x^{(4/p)} - 3x^{(2/p)} + 1$$

Where n is the derivative of order n (which must be a Lucas number) and p is the distance in units of the separation between primes that we want to find.

The relationship between this function and the Lucas numbers is that in the undifferentiated function  $x^{(4/p)} - 3x^{(2/p)} + 1$  its zeros are the Lucas numbers.

For example  $x^{(4/7)} - 3x^{(2/7)} + 1 = 0$

One of its zeros is 29 which is the 7th number of Lucas

For the particular case of p=4 the function returns all prime numbers without exception for n= Fibonacci number or Lucas number

For example for n=29 and p=4

We use the numerator of the derivative. We use always use the same number in the expression of the derivative.

$$d^{29}/dx^{29}(x^{(4/4)} - 3x^{(2/4)} + 1) = -26062093105685253599480874300846796875 / (536870912 x^{(57/2)})$$

The factorization of this number is:

$$-3^{14} \times 5^7 \times 7^5 \times 11^3 \times 13^2 \times 17^2 \times 19 \times 23 \times 29 \times 31 \times 37 \times 41 \times 43 \times 47 \times 53$$

Also the quotient between the last prime found and n is approximately 2

$$\text{Last prime found} / n \approx 2$$