

Proof of the Riemann hypothesis

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Abstract

Up to now, I have tried to expand this equation and prove Riemann hypothesis with the equation of cos, sin, but the proof was impossible.

However, I realized that a simple formula before expansion can prove it.

The real value is zero only when the real part of s is 1/2. Non-trivial zeros must always have a real value of zero.

The real part of s being 1/2 is the minimum requirement for s to be a non-trivial zeros.

key words

Riemann hypothesis, non-trivial zeros, 1/2, minimum requirement

1 introduction

if s is non-trivial zeos.

$$a^s = \sqrt{a} \quad (1)$$

and

$$a^{2s} = a \quad (2)$$

if s=1/2+i21.022

$2^s = -0.594904 + 1.28300i$

$\text{abs}(-0.594904+1.28300i)=1.41421\dots$

if s=1/2+i65.1125

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$$2^s = 0.577368... + 1.29099...i$$

$$\text{abs}(0.577368 + 1.29099i) = 1.41422...$$

$$\text{if } s = 1/2 + i21.022$$

$$3^s = -0.779658 - 1.54665i$$

$$\text{abs}(-0.779658 - 1.54665i) = 1.73205...$$

$$\text{if } s = 1/2 + i69.5464$$

$$3^s = 0.926622 + 1.46334i$$

$$\text{abs}(0.926622 + 1.46334i) = 1.73205...$$

$$\text{if } s = 1/2 + i69.5464$$

$$3^{2s} = -1.28274 + 2.71193i$$

$$\text{abs}(-1.28274 + 2.71193i) = 3$$

$$\text{if } s = 1/2 + i15$$

$$2^s = -0.796617... - 1.1685...i$$

$$\text{abs}(-0.796617 - 1.1685i) = 1.41421...$$

$$\text{if } s = 1/2 + i15$$

$$3^s = -1.24198... - 1.20726...i$$

$$\text{abs}(-1.24198 - 1.20726i) = 1.73205...$$

$$\text{if } s = 0.4 + i15$$

$$3^s = -1.11277... - 1.08165...i$$

$$\text{abs}(-1.11277 - 1.08165i) = 1.55185...$$

$$3^{0.4} = 1.55185...$$

In the case of a power, even if it is raised to a complex number, only the real value is involved in the absolute value, and the imaginary value is not involved at all.

That is, no matter how large the imaginary value is, if the real value is constant, it is not related to the absolute value of the power at all.

$$\zeta(s) = 2^s \pi^{s-1} \sin\left(\frac{s\pi}{2}\right) \Gamma(1-s) \zeta(1-s) \quad (3)$$

Let's calculate the sin part of Eq.(3).

$$\{\sin(s\pi/2)\}, \{s = 1/2 + i14.1347\} = 1.55232... \times 10^9 + 1.55232... \times 10^9i$$

$$\{\sin(s\pi/2)\}, \{s = 1/2 + i21.022\} = 7.75202... \times 10^{13} + 7.75202... \times 10^{13}i$$

$$\{\sin(s\pi/2)\}, \{s = 1/2 + i25.01086\} = 4.07913... \times 10^{16} + 4.07913... \times 10^{16}i$$

$$\{\sin(s\pi/2)\}, \{s = 1/2 + i30.4249\} = 2.01355... \times 10^{20} + 2.01355... \times 10^{20}i$$

$$\{\sin(s\pi/2)\}, \{s = 1/2 + i32.9351\} = 1.03846 \times 10^{22} + 1.03846 \times 10^{22}i$$

$$\{\sin(s\pi/2)\}, \{s = 1/2 + i315.4756\} = 5.78335 \times 10^{214} + 5.78335 \times 10^{214}i$$

$$\{\sin(s\pi/2)\}, \{s = 1/2 + i1393.4334\} = 1.35595667 \times 10^{950} + 1.35595667 \times 10^{950}i$$

$$\{\sin(s\pi/2)\}, \{s = 1/2 + i74920.8275\} = 4.4789956... \times 10^{51109} + 4.4789956... \times 10^{51109}i$$

Thus, it does not change while maintaining the 45° angle.

This is also a mysterious property of the non-trivial zeros.

Thus, the sin part of Eq.(3) becomes extremely large when the imaginary value becomes huge, but $\Gamma(1-s)$ cancels it.

It is shown below.

And if omit the $\zeta(1-s)$ part and calculate, it will be as follows.

$$\begin{aligned}
\{2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)\}, \{s = 1/2 + i14.1347\} &= -0.950558 - 0.310547i \\
\{2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)\}, \{s = 1/2 + i21.022\} &= -0.904282 + 0.426936i \\
\{2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)\}, \{s = 1/2 + i25.0109\} &= -0.784761 - 0.619798i \\
\{2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)\}, \{s = 1/2 + i30.4249\} &= -0.475849 + 0.879527i \\
\{2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)\}, \{s = 1/2 + i32.9351\} &= -0.410261 - 0.911968i \\
\{2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)\}, \{s = 1/2 + i37.58618\} &= -0.832147 + 0.554555i \\
\{2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)\}, \{s = 1/2 + i40.91872\} &= -0.917431 + 0.397894i \\
\{2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)\}, \{s = 1/2 + i43.32707\} &= -0.275249 - 0.961373i \\
\{2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)\}, \{s = 1/2 + i48.00515\} &= 0.130432 + 0.991457i \\
\{2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)\}, \{s = 1/2 + i49.77383\} &= -0.579292 - 0.81512i \\
\{2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)\}, \{s = 1/2 + i52.97032\} &= -0.867736 - 0.497025i \\
\{2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)\}, \{s = 1/2 + i56.44625\} &= -0.752855 + 0.658186i \\
\{2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)\}, \{s = 1/2 + i315.4756\} &= -0.286121 - 0.958193i \\
\{2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)\}, \{s = 1/2 + i1393.4334\} &= 0.973556 - 0.228449i \\
\{2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)\}, \{s = 1/2 + i74920.8275\} &= -0.827399 - 0.561615i
\end{aligned}$$

From the above calculation, in Euler's formula Eq.(3), $\zeta(s)=0$ (s is non-trivial zeros) is not from $2^s \pi^{s-1} \sin(\frac{s\pi}{2}) \Gamma(1-s)$ but $\zeta(1-s) = 0$.

$$\zeta(s) = \zeta(1-s) = 0 \quad (4)$$

At the non-trivial zeros, $\zeta(s) = \zeta(1-s) = 0$ holds. in this case. Eq.(10)=0, Eq(11)=0, and $\eta(s) = \eta(1-s) = 0$ holds.

$$\eta(1-s) = (1 - \frac{2}{2^{1-s}}) \zeta(1-s) = \frac{2^{1-s} - 2}{2^{1-s}} \zeta(1-s) = \frac{2 - 2^{s+1}}{2} \zeta(1-s) = (1 - 2^s) \zeta(1-s) \quad (5)$$

$$\eta(s) + \frac{2}{2^s} \zeta(s) = \eta(1-s) + \frac{2}{2^{1-s}} \zeta(1-s) \quad (6)$$

$$\eta(s) = \frac{2^s - 2}{2^s} \frac{2^{1-s}}{2^{1-s} - 2} \eta(1-s) = \frac{2^s - 2}{2^s} \zeta(1-s) = (1 - \frac{2}{2^s}) \zeta(1-s) = 0 \quad (7)$$

$$\begin{aligned}
\{\frac{2^s-2}{2^s} \zeta(1-s)\}, \{s = 1/2 + i14.1347\} &= -2.87486 \times 10^{-6} + 0.0000472469i \\
\{\frac{2^s-2}{2^s} \zeta(1-s)\}, \{s = 1/2 + i21.022\} &= 0.0000406923 + 0.0000827784i \\
\{\frac{2^s-2}{2^s} \zeta(1-s)\}, \{s = 1/2 + i25.0109\} &= 0.0000600703 - 0.0000774542i
\end{aligned}$$

$$\begin{aligned}
& \left\{ \frac{2^s-2}{2^s} \zeta(1-s) \right\}, \{s = 1/2 + i30.4249\} = 2.30973 \times 10^{-7} - 0.0000678699i \\
& \left\{ \frac{2^s-2}{2^s} \zeta(1-s) \right\}, \{s = 1/2 + i32.9351\} = -9.25931 \times 10^{-6} - 0.000117068i \\
& \left\{ \frac{2^s-2}{2^s} \zeta(1-s) \right\}, \{s = 1/2 + i37.5862\} = -0.0000437932 - 0.0000195875i \\
& \left\{ \frac{2^s-2}{2^s} \zeta(1-s) \right\}, \{s = 1/2 + i40.9187\} = -0.0000173311 + 0.0000661198i \\
& \left\{ \frac{2^s-2}{2^s} \zeta(1-s) \right\}, \{s = 1/2 + i74919.0752\} = -0.0000827382 - 0.000177009i \\
& \left\{ \frac{2^s-2}{2^s} \zeta(1-s) \right\}, \{s = 1/2 + i74920.8275\} = -0.0000166426 + 8.31396 \times 10^{-6}i
\end{aligned}$$

$$\eta(1-s) = \frac{2^{1-s}-2}{2^{1-s}-2} \frac{2^s}{2^s-2} \eta(s) = \frac{2^{1-s}-2}{2^{1-s}-2} \zeta(s) = \left(1 - \frac{2}{2^{1-s}}\right) \zeta(s) = 0 \quad (8)$$

$$\zeta(s) = \frac{2^s}{2^s-2} \eta(s) = \left(\frac{2^s-2+2}{2^s-2}\right) \eta(s) = \left(1 + \frac{2}{2^s-2}\right) \eta(s) \quad (9)$$

$$= \left(1 + \frac{2}{2^s} \frac{2^s}{2^s-2}\right) \eta(s) = \eta(s) + \frac{2}{2^s} \zeta(s) = \eta(s) + \frac{2}{2^s} [\eta(s) + \frac{2}{2^s} \zeta(s)] \quad (10)$$

$$= \eta(s) + \frac{2}{2^s} [\eta(s) + \frac{2}{2^s} (\eta(s) + \frac{2}{2^s} \zeta(s))] = \eta(s) + \frac{2}{2^s} \eta(s) + \left(\frac{2}{2^s}\right)^2 \eta(s) + \left(\frac{2}{2^s}\right)^3 \zeta(s) \quad (11)$$

$$= \eta(s) \left[1 + \frac{2}{2^s} + \left(\frac{2}{2^s}\right)^2\right] + \left(\frac{2}{2^s}\right)^3 \zeta(s) \neq \eta(s) \left[\frac{1 - \left(\frac{2}{2^s}\right)^k}{1 - \frac{2}{2^s}}\right] + \left(\frac{2}{2^s}\right)^{k+1} \zeta(s) \quad (12)$$

when k=2

$$\neq \eta(s) \left[\frac{1 - \left(\frac{2}{2^s}\right)^2}{1 - \frac{2}{2^s}}\right] + \left(\frac{2}{2^s}\right)^3 \zeta(s) = \left(1 - \frac{2}{2^s}\right) \zeta(s) \left[\frac{1 - \left(\frac{2}{2^s}\right)^2}{1 - \frac{2}{2^s}}\right] + \left(\frac{2}{2^s}\right)^3 \zeta(s) \quad (13)$$

$$= (s) \left[1 - \left(\frac{2}{2^s}\right)^2 + \left(\frac{2}{2^s}\right)^3\right] \quad (14)$$

$$\zeta(1-s) = \frac{2^{1-s}}{2^{1-s}-2} \eta(1-s) = \left(\frac{2^{1-s}-2+2}{2^{1-s}-2}\right) \eta(1-s) = \left(1 + \frac{2}{2^{1-s}-2}\right) \eta(1-s) \quad (15)$$

$$= \left(1 + \frac{2}{2^{1-s}} \frac{2^{1-s}}{2^{1-s}-2}\right) \eta(1-s) = \eta(1-s) + \frac{2}{2^{1-s}} \zeta(1-s) \quad (16)$$

$$= \eta(1-s) + \frac{2}{2^{1-s}} [\eta(1-s) + \frac{2}{2^{1-s}} \zeta(1-s)] = \eta(1-s) + \frac{2}{2^{1-s}} \eta(1-s) + \left(\frac{2}{2^{1-s}}\right)^2 \zeta(1-s) \quad (17)$$

$$= \eta(1-s) + \frac{2}{2^{1-s}} [\eta(1-s) + \frac{2}{2^{1-s}} (\eta(1-s) + \frac{2}{2^{1-s}} \zeta(1-s))] \quad (18)$$

$$= \eta(1-s) + \frac{2}{2^{1-s}}\eta(1-s) + \left(\frac{2}{2^{1-s}}\right)^2\eta(1-s) + \left(\frac{2}{2^{1-s}}\right)^3\zeta(1-s) \quad (19)$$

when $\frac{2}{2^{1-s}} = 2^s$

$$= \eta(1-s) + 2^s\eta(1-s) + (2^s)^2\eta(1-s) + (2^s)^3\zeta(1-s) \quad (20)$$

$$= \eta(1-s)[1 + 2^s + (2^s)^2] + (2^s)^3\zeta(1-s) \quad (21)$$

$$\neq \eta(1-s)\left[\frac{1 - (2^s)^k}{1 - 2^s}\right] + (2^s)^{k+1}\zeta(1-s) \quad (22)$$

when $k=2$

$$\neq \eta(1-s)\left[\frac{1 - 2^{2s}}{1 - 2^s}\right] + 2^{3s}\zeta(1-s) \quad (23)$$

$$= \zeta(1-s)(1 - 2^s)\left[\frac{1 - 2^{2s}}{1 - 2^s}\right] + 2^{3s}\zeta(1-s) \quad (24)$$

$$= \zeta(1-s)[1 - 2^{2s}] + 2^{3s}\zeta(1-s) \quad (25)$$

$$= \zeta(1-s)[1 - 2^{2s} + 2^{3s}] \quad (26)$$

from Eq.(14) and Eq.(26)

$$\zeta(s)\left[1 - \left(\frac{2}{2^s}\right)^2 + \left(\frac{2}{2^s}\right)^3\right] = \zeta(1-s)[1 - 2^{2s} + 2^{3s}] \quad (27)$$

2 Discussion

Define $0 < \Re(s) < 1$

from Eq.(27)

$$\begin{aligned} & \left\{ \zeta(s)\left[1 - \frac{2}{2^s} + \left(\frac{2}{2^s}\right)^2\right] - \zeta(1-s)[1 - 2^s + 2^{2s}] \right\}, \{s = 1/2 + i14.1347\} = -0.000160889i \\ & \left\{ \zeta(s)\left[1 - \frac{2}{2^s} + \left(\frac{2}{2^s}\right)^2\right] - \zeta(1-s)[1 - 2^s + 2^{2s}] \right\}, \{s = 1/2 + i15.1347\} = -0.280343i \\ & \left\{ \zeta(s)\left[1 - \frac{2}{2^s} + \left(\frac{2}{2^s}\right)^2\right] - \zeta(1-s)[1 - 2^s + 2^{2s}] \right\}, \{s = 1/2 + i16.1347\} = -4.17572i \\ & \left\{ \zeta(s)\left[1 - \frac{2}{2^s} + \left(\frac{2}{2^s}\right)^2\right] - \zeta(1-s)[1 - 2^s + 2^{2s}] \right\}, \{s = 1/2 - i16.1347\} = 4.17572i \\ & \left\{ \zeta(s)\left[1 - \frac{2}{2^s} + \left(\frac{2}{2^s}\right)^2\right] - \zeta(1-s)[1 - 2^s + 2^{2s}] \right\}, \{s = 1/2 + i17.1347\} = 4.82094i \end{aligned}$$

$$\begin{aligned}
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 - i17.1347\} = -4.82094i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i21.022\} = -0.0000820167i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 - i21.022\} = 0.0000820167i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 - i74879.422\} = 0.00056128i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 - i74879.8804\} = -0.00111728i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 - i74891.93\} = 0.0000554776i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i74892.5452\} = -0.000641199i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i74895.7013\} = 0.00117245i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i74896.2133\} = 0.000808722i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i74896.6987\} = -0.00106666i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i74897.0517\} = 0.000224195i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i74898.1134\} = -0.000935263i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i74898.9041\} = 0.000102353i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 0.49999 + i74911.8951\} = 0.000232008 + 0.000914211i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i74911.9\} = 2.7105110^{-20} + 0.000914218i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 0.5 + i74911.9\} = 2.7105110^{-20} + 0.000914218i \\
& \zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}], s = 0.51 + i74911.8951 = -0.232499 - 0.00586949i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 - i74912.4918\} = -0.0000277175i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i74916.2765\} = 0.000952275i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i74918.7\} = 0.000152616i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i74919.1\} = -8.4703310^{-22} + 0.0000171143i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 0.5 + i74919.1\} = -8.4703310^{-22} + 0.0000171143i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i74920.2598\} = 0.000360484i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 0.5 + i74920.3\} = 0.000360484i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i74920.8275\} = 0.0000329616i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i99999.422\} = -9.48598i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i999999.422\} = -0.270142i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i9999999.422\} = -6.86408i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i99999999.422\} = 0.0172762i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i999999999.422\} = -0.0048036i \\
& \{\zeta(s)[1 - \frac{2}{2^s} + (\frac{2}{2^s})^2] - \zeta(1-s)[1 - 2^s + 2^{2s}]\}, \{s = 1/2 + i9999999999.422\} = no\ result
\end{aligned}$$

As in these examples, when the real part of s is $1/2$, the real value is 0 or almost 0, but the imaginary value remains.

Even if s is a non-trivial zero, the imaginary value is close to 0 but not 0.

However, even if the real part of s is $1/2$, a real value close to 0 but not 0 is frequently generated.

If the real value of s is $1/2$, the output real value is 0 or a value very close to 0 even if the imaginary value is other than the non-trivial zero value (However, in this case, the output imaginary value is far from 0).

That is, the minimum requirement for the non-trivial zeros is that the real part of s is $1/2$.

That is, the lowest condition in which a non-trivial zero exists is a real part value of $1/2$.

That is, a non-trivial zero can have a real part only $1/2$.

$$\Re(s) = \frac{1}{2} \tag{28}$$

Proof complete.

3 Postscript

These calculations were performed with WolframAlpha.

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I was finally crazy because of the curse of Riemann.

Please raise the prize money to my little son and daughter who are still young.