

The curse of Riemann.

Proof of the Riemann hypothesis

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Abstract

Up to now, I have tried to expand this equation and prove Riemann hypothesis with the equation of cos, sin, but the proof was impossible.

However, I realized that a simple formula before expansion can prove it.

The real value is zero only when the real part of s is 1/2. Non-trivial zeros must always have a real value of zero.

key words

Riemann hypothesis, non-trivial zeros, critical line, 1/2

1 introduction

This is clear from $\zeta(s) = \frac{2^s}{2^s-2}\eta(s)$, that $\zeta(s) = \zeta(1-s)$ and $\eta(s) = \eta(1-s)$ have the same significance.

Both equations are valid only for non-trivial zeros.

In the case of $\eta(s)$, the proof of Riemann hypothesis is completed if it is proved that the value of the non-trivial zeros is taken only when the real part is 1/2.

Define $0 < \Re(s) < 1$

$$\eta(s) = \frac{2^s - 2}{2^s} \zeta(s) = \zeta(s) - \frac{2}{2^s} \zeta(s) \quad (1)$$

$$\sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{0.2+i14.1347}} = -0.7106998802\dots - 0.0393256547631\dots i$$
$$\sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{0.4+i14.1347}} = -0.20168483321\dots - 0.0003986577711\dots i$$

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$$\begin{aligned} \sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{0.49+i14.1347}} &= -0.01791363\dots - 0.004282038\dots i \\ \sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{1/2+i14.1347}} &= 0.0009413486\dots - 0.0049571556\dots i \\ \sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{1/2-i14.1347}} &= 0.0009413486\dots + 0.0049571556\dots i \\ \sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{0.6+i14.1347}} &= 0.17375337127\dots - 0.01283865007\dots i \end{aligned}$$

$$\begin{aligned} \left\{ \frac{2^s}{2^s-2} \right\}, \{s = 1/2 + i14.1347\} &= 0.411258\dots + 0.0913854\dots i \\ \left\{ \frac{2^s}{2^s-2} \right\}, \{s = 1/2 - i14.1347\} &= 0.411258\dots - 0.0913854\dots i \\ \left\{ \frac{2^s-2}{2^s} \right\}, \{s = 1/2 + i14.1347\} &= 2.31715\dots - 0.514893\dots i \\ \left\{ \frac{2^s-2}{2^s} \right\}, \{s = 1/2 - i14.1347\} &= 2.31715\dots + 0.514893\dots i \end{aligned}$$

$$\begin{aligned} \sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{0.4+i21.022}} &= -0.23505068\dots - 0.12926123561\dots i \\ \sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{1/2+i21.022}} &= -0.00196549\dots - 0.00466251514\dots i \\ \sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{1/2-i21.022}} &= -0.00196549\dots + 0.00466251514\dots i \\ \sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{0.6+i21.022}} &= 0.18930834\dots + 0.08779032048\dots i \end{aligned}$$

$$\begin{aligned} \sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{0.4+i25.01086}} &= -0.195508869\dots + 0.152868555478\dots i \\ \sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{0.4-i25.01086}} &= -0.195508869\dots - 0.152868555478\dots i \\ \sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{1/2+i25.01086}} &= 0.002605178\dots - 0.0042652041\dots i \\ \sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{1/2-i25.01086}} &= 0.002605178\dots + 0.0042652041\dots i \\ \sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{0.6+i25.01086}} &= 0.1667076253\dots - 0.124423449\dots i \\ \sum_{n=1}^{10000} \frac{(-1)^{n-1}}{n^{0.6-i25.01086}} &= 0.1667076253\dots + 0.124423449\dots i \end{aligned}$$

$$\begin{aligned} \left\{ \frac{2^s-2}{2^s} \zeta(s) \right\}, \{s = 0.4 + i25.01086\} &= -0.202044\dots + 0.163593\dots i \\ \left\{ \frac{2^s-2}{2^s} \zeta(s) \right\}, \{s = 1/2 + i25.01086\} &= 3.42656\dots \times 10^{-6} + 4.41859\dots \times 10^{-6} i \\ \left\{ \frac{2^s-2}{2^s} \zeta(s) \right\}, \{s = 1/2 - i25.01086\} &= 3.42656\dots \times 10^{-6} - 4.41859\dots \times 10^{-6} i \\ \left\{ \frac{2^s-2}{2^s} \zeta(s) \right\}, \{s = 0.6 + i25.01086\} &= 0.165672\dots - 0.122724\dots i \\ \left\{ \frac{2^s-2}{2^s} \zeta(s) \right\}, \{s = 0.6 - i25.01086\} &= 0.165672\dots + 0.122724\dots i \end{aligned}$$

In $\eta(s)$, even if the plus or minus of the imaginary value of s is switched, the real value shows the same value, but the plus or minus of the imaginary value is different.

If s is a non-trivial zeros, both real and imaginary values converge to zero.

2 Discussion

from Eq.(1)

$$\zeta(s) = \eta(s) + \frac{2}{2^s} \zeta(s) \quad (2)$$

and

$$\zeta(1-s) = \eta(1-s) + \frac{2}{2^{1-s}} \zeta(1-s) \quad (3)$$

from $\zeta(s) = \zeta(1 - s)$

$$[\eta(s) + \frac{2}{2^s}\zeta(s)] - [\eta(1 - s) + \frac{2}{2^{1-s}}\zeta(1 - s)] = 0 \quad (4)$$

$$[\eta(s) - \eta(1 - s)] + [\frac{2}{2^s}\zeta(s) - \frac{2}{2^{1-s}}\zeta(1 - s)] = 0 \quad (5)$$

$$[\eta(s) - \eta(1 - s)] + [2^{1-s}\zeta(s) - 2^s\zeta(1 - s)] = 0 \quad (6)$$

As can be seen from Eq.(6), it becomes 0 when $s=1/2$ is inserted.

That is, it is not 0 except for $s=1/2$.

This can be said to be the end of proof.

from Eq.(4)

$$\begin{aligned} &\{[\eta(s) + \frac{2}{2^s}\zeta(s)] - [\eta(1 - s) + \frac{2}{2^{1-s}}\zeta(1 - s)]\}, \{s = 0.4 + i16.1347\} = -0.493359... + 3.65957...i \\ &\{[\eta(s) + \frac{2}{2^s}\zeta(s)] - [\eta(1 - s) + \frac{2}{2^{1-s}}\zeta(1 - s)]\}, \{s = 0.4 - i16.1347\} = -0.493359... - 3.65957...i \\ &\{[\eta(s) + \frac{2}{2^s}\zeta(s)] - [\eta(1 - s) + \frac{2}{2^{1-s}}\zeta(1 - s)]\}, \{s = 1/2 + i14.1347\} = 0.000055107...i \\ &\{[\eta(s) + \frac{2}{2^s}\zeta(s)] - [\eta(1 - s) + \frac{2}{2^{1-s}}\zeta(1 - s)]\}, \{s = 1/2 + i16.1347\} = 3.64713...i \\ &\{[\eta(s) + \frac{2}{2^s}\zeta(s)] - [\eta(1 - s) + \frac{2}{2^{1-s}}\zeta(1 - s)]\}, \{s = 0.6 + i16.1347\} = 0.493359 + 3.65957...i \\ &\{[\eta(s) + \frac{2}{2^s}\zeta(s)] - [\eta(1 - s) + \frac{2}{2^{1-s}}\zeta(1 - s)]\}, \{s = 0.6 - i16.1347\} = 0.493359... - 3.65957...i \\ &\{[\eta(s) + \frac{2}{2^s}\zeta(s)] - [\eta(1 - s) + \frac{2}{2^{1-s}}\zeta(1 - s)]\}, \{s = 1/2 + i17.1347\} = 5.39992...i \\ &\{[\eta(s) + \frac{2}{2^s}\zeta(s)] - [\eta(1 - s) + \frac{2}{2^{1-s}}\zeta(1 - s)]\}, \{s = 1/2 + i21.022\} = 0.000077614...i \\ &\{[\eta(s) + \frac{2}{2^s}\zeta(s)] - [\eta(1 - s) + \frac{2}{2^{1-s}}\zeta(1 - s)]\}, \{s = 1/2 + i22.022\} = -2.61712...i \end{aligned}$$

As in these examples, when the real part is $1/2$, the real value is 0, but the imaginary value remains.

When the real value of s is $1/2$, the real value is completely 0, but even if the imaginary value is $i14.1347$, it is not removed because it contains an error.

$$\begin{aligned} \zeta(0.4 + i16) &= 0.921882... + 1.32365...i \\ \zeta(0.4 - i16) &= 0.921882... - 1.32365...i \\ \zeta(1/2 + i14.1347) &= 3.13536... \times 10^{-6} - 0.0000196934...i \\ \zeta(1/2 - i14.1347) &= 3.13536... \times 10^{-6} + 0.0000196934...i \\ \zeta(1/2 + i15) &= 0.147109907... + 0.7047522416...i \\ \zeta(1/2 - i15) &= 0.147109907... - 0.7047522416...i \\ \zeta(1/2 + i16) &= 0.938545408... + 1.216587815999...i \\ \zeta(1/2 - i16) &= 0.938545408... - 1.216587815999...i \\ \zeta(0.6 + i16) &= 0.952627... + 1.11841...i \\ \zeta(0.6 - i16) &= 0.952627... - 1.11841...i \end{aligned}$$

In $\zeta(s)$ and $\eta(s)$, even if the imaginary value of s is changed, the real value shows the same value, but the imaginary value is different between plus and minus.

If the real part of s is 0.4, the real part of s is 0.6 from $\zeta(s) = \zeta(1 - s)$.

Then, the real part value and the imaginary part value also change.

Even if $\zeta(s) = \zeta(1 - s)$ is used in addition to $1/2$, the value of the real part is only $1/2$.

$s = 1/2$ is the minimum requirement for $\zeta(s) = \zeta(1 - s)$ and $\eta(s) = \eta(1 - s)$.

That is, the minimum condition for the non-trivial zeros is that the real value is $1/2$.

The real value is zero only when the real part of s is $1/2$. Non-trivial zeros must always have a real value of zero.

$$\Re(s) = \frac{1}{2} \tag{7}$$

Proof complete.

3 Postscript

These calculations were performed with WolframAlpha.

References

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I was finally crazy because of the curse of Riemann.

Please raise the prize money to my little son and daughter who are still young.