

## Bond Lengths in Helium Hydrides as Sums of the Relevant Radii of He and H

**Raji Heyrovská**

Academy of Sciences of the Czech Republic (Emeritus); Private Research Scientist (present);

Email: rheyrovs@hotmail.com

**Abstract.** The latest astrophysical discovery for the first time of  $\text{HeH}^+$  inspired the author to look into its bond length. Using the previously calculated values of the various radii of He and H, it is shown here that the reported inter-nuclear distance in  $\text{HeH}^+$  is the sum of the radii of  $\text{He}^-$  and the section of the Bohr radius pertaining to the proton. Interpreted here also is the inter-nuclear distance of the  $\text{He}\cdots\text{H}$  bond in  $\text{He}\cdots\text{H}\cdots\text{He}^+$ , as the sum of the covalent radius of He and the Bohr radius of H. Both cases support the rule of additivity of radii of adjacent atoms and or ions in bond lengths established by the author over the years.

### 1. Introduction

The author has shown over the years (see for collected papers [1]) that inter-atomic distances are sums of the radii of adjacent atoms or ions, whether the bond is completely or partially covalent or ionic. The covalent inter-atomic distance,  $d(\text{AA})$  between two atoms (A) of the same kind was shown to be the sum of the radii of its cation and anion (Pauling's resonance forms),  $R_{\text{A}^+}$  and  $R_{\text{A}^-}$  respectively,

$$d(\text{AA}) = 2R_{\text{A}} = R_{\text{A}^+} + R_{\text{A}^-} \quad (1)$$

where  $R_{\text{A}}$  is the covalent radius of A. The ionic radii are the Golden sections of  $d(\text{AA})$  given by,

$$R_{\text{A}^+} = d(\text{AA})/\phi^2 \text{ and } R_{\text{A}^-} = d(\text{AA})/\phi \quad (2)$$

where  $\phi$  is the Golden ratio [1]. It was shown [1] that the Golden ratio divides the ground state Bohr radius,  $a_{\text{BA}}$  of an atom A (calculated from its first ionization potential,  $I_1$ ) into two sections,  $a_{\text{B,e}^-}$  and  $a_{\text{B,n}^+}$  pertaining to the outer electron ( $e^-$ ) and the nucleus ( $n^+$ ) as follows,

$$a_{B,n+} = a_{B,A}/\phi^2 \text{ and } a_{B,e-} = a_{B,A}/\phi \quad (3)$$

The above radii have been tabulated for all the elements of The Periodic Table in [2,3]. This report pertains to the bond in helium hydride  $\text{HeH}^+$ , [4-6] which has roused great interest recently [4] and also to  $\text{He}\cdots\text{H}$  in  $\text{He}\cdots\text{HHe}^+$  reported earlier [5]. For an introduction and review of research on  $\text{HeH}^+$ , see [7].

## 2. Interpretation of the observed inter-nuclear distance, $d(\text{HeH}^+)$

The observed distance  $d(\text{HeH}^+)$  as reported in [4-6] is  $0.77 \text{ \AA}$ . The various radii for H and He copied from [2,3] are given here in Table 1. See the Figures in [2] for the radii of H and He.

**Table 1. The various radii in  $\text{\AA}$  for H and He, data from [2,3].**

A	$I_1$ (ev)	$a_{B,A}$	$a_{e-}$	$a_{p+}$	$R_A$	$R_{A-}$	$R_{A+}$	$R_A/a_{B,A}$	
H	13.598	0.53	0.33	0.20	0.37	0.46	0.28	$1/2^{1/2}$	= 0.707
He	24.587	0.29	0.18	0.11	0.46	0.57	0.35	$\phi$	= 1.618

From the data in Table 1, the observed distance [4],  $d(\text{HeH}^+) = 0.77 \text{ \AA}$  is interpreted here as the sum of radii,

$$d(\text{He}\cdots\text{H}^+) = R_{\text{He}} + a_{p+} = 0.57 + 0.20 = 0.77 \text{ \AA} \quad (4)$$

## 3. Interpretation of the observed [6] inter-nuclear distance, $d(\text{He}\cdots\text{H})$ in $\text{He}\cdots\text{H}\cdots\text{He}^+$

The reported [6] inter-nuclear distance,  $d(\text{He}\cdots\text{H}) = 0.95 \text{ \AA}$  in  $\text{He}\cdots\text{HH}^+$  corresponds to the sum,

$$d(\text{He}\cdots\text{H}) = R_{\text{He}} + a_{B,H} = 0.46 + 0.53 = 0.96 \text{ \AA} \quad (5)$$

Thus, additivity of atomic and or ionic radii found [1] for chemical bonds in small as well as large molecules holds for the bond distances in  $\text{HeH}^+$  and in  $\text{He}\cdots\text{H}$  as well.

## References

1. R. Heyrovská, Bohr Radius as the Sum of Golden Sections Pertaining to the Electron and Proton, Covalent Bond Lengths Between Same Two Atoms as Exact Sums of Their Cationic and Anionic Radii and Additivity of Atomic and or Ionic Radii in Bond Lengths – Collected work dedicated to Johannes Kepler (1571 - 1630). <http://vixra.org/abs/1709.0066> (abstract); <http://vixra.org/pdf/1709.0066v1.pdf> (full text)
2. R. Heyrovská, Atomic and Ionic Radii of Elements and Bohr Radii from Ionization Potentials are Linked Through the Golden Ratio. International Journal of Sciences 03(2013):82-92 , <http://www.ijsciences.com/pub/article/155>, <http://www.ijsciences.com/pub/pdf/V2-201303-19.pdf>
3. R. Heyrovská, Atomic, Ionic and Bohr Radii Linked via the Golden Ratio for Elements Including Lanthanides and Actinides International Journal of Sciences 04(2013):63-68 , <http://www.ijsciences.com/pub/article/176>, <http://www.ijsciences.com/pub/pdf/V2-201304-18.pdf>
4. R. Gusten et al, Astrophysical detection of the helium hydride ion  $\text{HeH}^+$ ". Nature. **568** (7752): 357, 2019, [doi:10.1038/s41586-019-1090-x](https://doi.org/10.1038/s41586-019-1090-x). PMID 30996316.
5. J. P. Coyne, D.W. Ball, David W. "Alpha particle chemistry. On the formation of stable complexes between  $\text{He}^{2+}$  and other simple species: implications for atmospheric and interstellar chemistry". Journal of Molecular Modeling. **15** (1): 35–40, 2009. [doi:10.1007/s00894-008-0371-3](https://doi.org/10.1007/s00894-008-0371-3). PMID 18936986.
6. F. G. Grandinetti, Felice. "Helium chemistry: a survey of the role of the ionic species". International Journal of Mass Spectrometry. **237** (2–3): 243–267, 2004. [Bibcode:2004IJMSp.237..243G. doi:10.1016/j.ijms.2004.07.012](https://doi.org/10.1016/j.ijms.2004.07.012).
7. [https://en.wikipedia.org/wiki/Helium\\_hydride\\_ion](https://en.wikipedia.org/wiki/Helium_hydride_ion)