

Refutation of the algorithm to generate preference profiles

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Abstract: We evaluate six equations of the proposed algorithm to generate preference profiles. *None* is tautologous, hence refuting the proposal.

We assume the method and apparatus of Meth8/VL4 with Tautology as the designated *proof* value, **F** as contradiction, **N** as truthity (non-contingency), and **C** as falsity (contingency). For results, the 16-valued truth table is row-major and horizontal, or repeating fragments of 128-tables, sometimes with table counts, for more variables. (See ersatz-systems.com.)

LET p, q, r, s: v, P₁, P₂, s;
 ~ Not, ¬; + Or, ∨, ∪; - Not Or; & And, ∧, ∩; \ Not And;
 > Imply, greater than, →, ⊃, ▷, ▷; < Not Imply, less than, ∈, <, ⊂;
 = Equivalent, ≡, ≐, :=, ⇔, ↔; @ Not Equivalent, ≠;
 % possibility, for one or some, ∃, ∅, M; # necessity, for every or all, ∀, □, L;
 (z=z) T as tautology; (z@z) F as contradiction, ∅, Null;
 (%z<#z) C as contingency, Δ, ordinal 1;
 (%z>#z) N as non-contingency, ∇, ordinal 2;
 ~(y < x) (x ≤ y), (x ⊆ y); (A=B) (A~B).

From: Alvira, R. (2018).

Transforming candidate and parties cardinal ratings into weak preference orderings.
 XV Meeting Spanish social choice network [REES], Elche, Alicante, 11.17-18.
vixra.org/pdf/1901.0384v1.pdf ricardo.alvira@gmail.com

[I]f the average preference value of some party voters for another party P₁ is greater than for another party P₂, then every one and all of that party voters strictly prefer P₁ to P₂: (2.0)

$$v[P_1] > v[P_2] \leftrightarrow P_1 > P_2 \quad (2.1.1)$$

$$((p \& q) > (p \& r)) = (q > r); \quad \text{TTF T TTF T TTF T TTF} \quad (2.1.2)$$

$$v[P_1] = v[P_2] \leftrightarrow P_1 \sim P_2 \quad (2.2.1)$$

$$((p \& q) = (p \& r)) = (q = r); \quad \text{TTF FTT TTF FTT} \quad (2.2.2)$$

$$v[P_1] > v[P_2] \leftrightarrow P_1 > P_2 \vee v[P_1] = v[P_2] \leftrightarrow P_1 \sim P_2 \quad (2.3.1)$$

$$(((p \& q) > (p \& r)) = (q > r)) + (((p \& q) = (p \& r)) = (q = r)); \quad \text{TTF TTT TTF TTT} \quad (2.3.2)$$

LET $p, q, r, s: v, A, B, s.$

Strict indifference:

$$v(A)-v(B)=0 \rightarrow A \sim B \quad (2.4.1)$$

$$(((p \& q) - (p \& r)) = (s @ s)) > (q = r) ; \quad \mathbf{TTTF \ TFTT \ TTTF \ TFTT} \quad (2.4.2)$$

Strict preference:

$$v(A)-v(B) \geq 1 \rightarrow A \succ B \quad (2.5.1)$$

$$\sim((\%s \> \#s) > ((p \& q) - (p \& r))) > (p > q) ; \quad \mathbf{TTTT \ TCTT \ TTTT \ TCTT} \quad (2.5.2)$$

Partial indifference and partial preference:

$$1 > v(A) - v(B) > 0 \rightarrow (1 - (v(A) - v(B))) (A \sim B) \wedge (v(A) - v(B)) (A \succ B) \quad (2.6.1)$$

$$(((\%s \> \#s) > ((p \& q) - (p \& r))) > (s @ s)) > (((\%s \> \#s) - ((p \& q) - (p \& r))) \& (q = r)) \& \\ ((p \& q) - (p \& r)) \& (q \& r) ; \quad \mathbf{FFFF \ FFTF \ FFFF \ FFTF} \quad (2.6.2)$$

Eqs. 2.1.2-2.6.2 as rendered are not tautologous. This refutes the proposed algorithm to generate preference profiles.