

Refutation of set theory by supremum and infimum

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We assume the method and apparatus of Meth8/VL4 with Tautology as the designated *proof* value, **F** as contradiction, **N** as truthity (non-contingency), and **C** as falsity (contingency). Results are a 16-valued truth table in row-major and horizontal, or repeating fragments of 128-tables for more variables.

LET $p, q, r, s, t: A, M$ or m, R, x, B
 \sim Not; $+$ Or; $\&$ And; $>$ Imply, greater than; $<$ Not Imply, lesser than, \in ;
 $\#$ necessity, for all or every, \square, \forall ; $\%$ possibility, for one or some, \diamond, \exists
 $y \leq z \sim (z < y)$; $y \geq z \sim (z > y)$;

LET $p, q, r, s, t: A, M$ or m, R, x, B

From: math.ucdavis.edu/~hunter/m125b/ch2.pdf

Definition(s) 2.1:

If for every x in A then $x \leq M$ implies $M < R$, then $A < R$, named $\text{sup}(\text{remum}) M$. (2.1.1.1)

$((\#s < p) \& \sim (s > q)) \> \% (q > r) \> (p < r)$; **F T F T F F F F F T N T F F F F** (2.1.1.2)

If for every x in A then $x \geq m$ implies $m < R$, then $A < R$, named $\text{inf}(\text{imum}) m$. (2.1.2.1)

$((\#s < p) \& \sim (s < q)) \> \% (q > r) \> (p < r)$; **F T F T F F F F F T F T F F F F** (2.1.2.2)

A is bounded if it is bounded by both a $\text{sup} M$ and an $\text{inf} m$. (2.1.3.1)

$((\#s < p) \& \sim (s > q)) \> \% (q > r) \& ((\#s < p) \& \sim (s < q)) \> \% (q > r)$; **T T T T T T T T T T C T T T T T** (2.1.3.2)

Remark 2.1.3.2: Because Eq. 2.1.3.2 as rendered is *not* tautologous, diverging by one **C** contingency value, the supremum and infimum refute set theory.