

## Refutation of Lean theorem prover from Microsoft

Copyright © 2018 by Colin James III All rights reserved.

We assume the method and apparatus of Meth8/VL4 with  $\mathbb{T}$  as the designated *proof* value,  $\mathbb{F}$  as contradiction,  $\mathbb{N}$  as truthity (non-contingency), and  $\mathbb{C}$  as falsity (contingency). Results are a 16-valued truth table in row-major and horizontal, or repeating fragments of 128-tables for more variables.

LET  $p, r, s$ :  $p, r, x$ ;  
 $\sim$  Not;  $\&$  And;  $>$  Imply,  $\rightarrow$ ;  $=$  Equivalent,  $\leftrightarrow$ ;  
 $\#$  necessity,  $\forall$ , for all or every;  $\%$  possibility,  $\exists$ , for one or some.

From: Avigad, J.; de Moura, L.; Kong, S. (2018). Theorem proving in Lean. Rel. 3.40.  
[leanprover.github.io/theorem\\_proving\\_in\\_lean/quantifiers\\_and\\_equality.html](https://leanprover.github.io/theorem_proving_in_lean/quantifiers_and_equality.html)

$$\text{example: } (\forall x, p x \rightarrow r) \leftrightarrow (\exists x, p x) \rightarrow r \quad (4.4.1.1)$$

$$((\#s\&(p\&s))>r)=((\%s\&(p\&s))>r) ; \quad \text{TTTT TTTT TNTN TTTT} \quad (4.4.1.2)$$

$$\text{example: } (\exists x, p x \rightarrow r) \leftrightarrow (\forall x, p x) \rightarrow r \quad (4.4.2.1)$$

$$((\%s\&(p\&s))>r)=((\#s\&(p\&s))>r) ; \quad \text{TTTT TTTT TNTN TTTT} \quad (4.4.2.2)$$

$$\text{example: } (\exists x, r \rightarrow p x) \leftrightarrow (r \rightarrow \exists x, p x) \quad (4.4.3.1)$$

$$(\%s\&(r>(p\&s)))=(r>(\%s\&(p\&s))) ; \quad \text{CCCC TTTT TTTT TTTT} \quad (4.4.3.2)$$

Eqs. 4.4.1.2, /2.2, and /3.2 are *not* tautologous. Hence Lean prover from Microsoft is not bivalent and refuted.