

## Refutation of Cantor's original continuum hypothesis via injection and binary trees

© Copyright 2018 by Colin James III All rights reserved.

From: Pindsle, C. (2018). "The continuum hypothesis". vixra.org/pdf/1803.0088v1.pdf

**Note:** Because of no email contact disclosed at that venue, that author name is likely a pseudonym.

"[With representation using binary trees: the intention was] to prove the hypothesis in its original form as proposed by Georg Cantor in 1878: Any uncountable set of real numbers is equinumerous with  $\mathbb{R}$ . Since there is a bijection between the open interval (0,1) and the set of all the real numbers, there is a bijection between any subset of (0,1) and a subset of  $\mathbb{R}$ . Therefore it is sufficient to prove: Any uncountable subset of (0,1) is equinumerous with  $\mathbb{R}$ ."

$\phi : RJ \mapsto RJT$  is bijective: It is injective because:  
 $\phi(r1) = \phi(r2) \Rightarrow (\phi(r1) \succ \phi(r2) \text{ and } \phi(r2) \succ \phi(r1)) \Rightarrow (r1 \succ r2 \text{ and } r2 \succ r1) \Rightarrow r1 = r2$  (3.5.1.)

Because the intention the proof was to show  $\phi(r1) = \phi(r2) \Rightarrow \dots \Rightarrow r1 = r2$ , we rewrite Eq. 3.5.1.

$$\phi(r1) = \phi(r2) \Rightarrow r1 = r2 \quad (3.5.1.1)$$

We assume the apparatus and method of Meth8/VL4 with designated *proof* value  $\mathbb{T}$ , and contradiction value  $\mathbb{F}$ . The 16-valued result table is row-major and presented horizontally.

LET p q r:  $\phi$ ,  $\text{lc\_phi}$ ; r1; r2; & And;  $\succ$  Imply,  $\succ$ ,  $\Rightarrow$ ; = Equivalent to.

$$((p \& q) = (p \& r)) \succ (q = r); \quad \mathbb{T}\mathbb{T}\mathbb{F}\mathbb{T} \quad \mathbb{F}\mathbb{T}\mathbb{T}\mathbb{T} \quad \mathbb{T}\mathbb{T}\mathbb{F}\mathbb{T} \quad \mathbb{F}\mathbb{T}\mathbb{T}\mathbb{T} \quad (3.5.1.2)$$

Eq. 3.5.1.2 as rendered is *not* tautologous. Hence, the hypothesis as Eq. 3.5.1.1 fails.

This is the briefest known such refutation of Cantor's continuum conjecture.

**Remark:** To coerce Eq. 3.5.1.2 into tautology, we weaken the argument by replacing the Equivalent connective with the Imply connective.

$$((p \& q) \succ (p \& r)) \succ (q \succ r); \quad \mathbb{T}\mathbb{T}\mathbb{F}\mathbb{T} \quad \mathbb{T}\mathbb{T}\mathbb{T}\mathbb{T} \quad \mathbb{T}\mathbb{T}\mathbb{F}\mathbb{T} \quad \mathbb{T}\mathbb{T}\mathbb{T}\mathbb{T} \quad (3.5.1.3)$$

Eq. 3.5.1.3 does come closer to tautology with two less contradiction  $\mathbb{F}$  values, but to no avail.