

Electron & Positron Model Wave Function and Field calculation code

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This is a portion of the model I wrote to model the Electron/Positron and their associated fields; such as Electric, Magnetic, Vector Potential fields. It is written in the Delphi language and is the function that calculates the fields from the mathematical wave function.

```
procedure TForm1.RecalcFields(scr:smallint);
var
  Current_Ex,Current_Ey,Current_Ez: extended;
  Current_Bx,Current_By,Current_Bz : extended;
  r,x,y,z,unit_x,unit_y,unit_z,k : extended;
  theta, delta, theta_const, expTheta, lnTheta, term0, term1, term2, term3 : extended;
  normal_x,normal_y,normal_z,dir_x,dir_y,dir_z : extended;
  scalar_amp, Vector_amp, SpinConstant, E_amp : extended;
  NewScreen : smallint;
  xpos,ypos,zpos,midx,midy,midz:smallint;
  ThisGroup,NewGroup: PointGrp;
  vect,CurlVect,DivVect: vector;
  Scalar_Group: ScalarGrp;
  VectGrp: VectorGrp;
  I: Integer;
  Etotal: Extended;
  ShellThickness: Extended;
  dist: longint;

begin

  if scr=0 then NewScreen:=1 else NewScreen:=0; {determine which data to update}

  if not Flip_YZ then begin

    midx:=Trunc(GridWidth/2);
    midy:=Trunc(GridHeight/2);
    midz:=Trunc(GridDepth/2);
    //////////////////////////////////////

    SpinConstant:=( Hhat / ElectronMass );      // Metres^2/(Radians*Second)
    delta := ( sqrt(2) * ElectronCharge * Hhat ) / ( 8 * Pi * ElectronMass * SpeedOfLight * Permittivity );
```

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// theta_const is in Radians/Second ( i.e. the same as solving E = hf for f, where E=mc^2, and h=2*Pi*Hhat,
// then converting f to angular frequency w, via w = 2*Pi*f )
// ( theta_const could be, equivalently : - c^2/SpinConstant )
theta_const:=( -ElectronMass * sqr(SpeedOfLight) ) / Hhat;

k:=FREQ_FACTOR/SpeedOfLight; // Seconds/Metre ( multiply by 1E-5 to make PsiWave visible (magnify) in model )

//
// Thus Total Electron Wave Equation (Ye) is:
//
// Ye = (sqrt(2) * Qe*Hhat) / (8 * Pi * Me*c*Eo ) * Exp( ( - i * Me * c^2 / Hhat ) * ( T - r/c ) )
//
// and the Electric Potential div(psi) in spherical coordinates is
//
// V = (sqrt(2) * Qe / ( 4 * Pi * r * Eo ) ) * Exp( ( - i * Me * c^2 / Hhat ) * ( T - r/c ) )
//
// Where:
//   Ye is Electron Wave Function
//   Qe is Electron's Charge
//   Pi is 3.14159 etc
//   Eo is the Permittivity of free space
//   Exp is the Exponential function
//   i is the Complex number (square root of -1)
//   Me is the Mass of an Electron
//   c is the speed of light
//   Hhat is the reduced Plancks constant ( i.e. h/(2*Pi) )
//   T is Time
//   r is the radial distance from the center of the Electron
//
// exp(-theta) = cos(theta) - isin(theta)
// using x,y,z coordinates:
// x = cos(theta)
// y = sin(theta)

// theta:=theta_const*(Time - k*r);
//
// term1:=delta
//
// term2:=cos(theta);
// term3:=-sin(theta);
//
// if ( ViewTop ) then begin           // Assign values to x, y, z coordinates, depending on view from the side or top.
// x:=term1 * term2;
// y:=term1 * term3;
// z:=0;
// end
// else begin
// x:=term1 * term2;
// y:=0;
// z:=term1 * term3;

```

```

// end;

////////////////////////////////////
for xpos:=0 to GridWidth-1 do begin      {scan grid's x coords}
  for ypos:=0 to GridHeight-1 do begin   {scan grid's y coords}
    for zpos:=0 to GridDepth-1 do begin  {scan grid's z coords}
      ThisGroup:=PointGroup(scr, xpos, ypos, zpos);

      x:= xpos - midx;
      y:= ypos - midy;
      z:= zpos - midz;

      r:=sqrt( sqr(x) + sqr(y) + sqr(z) );
      if ( r < 0.00000000001 ) then r:=0.00000000001; // prevent divide by zero errors

      unit_x:= x/r;
      unit_y:= y/r;
      unit_z:= z/r;

      r:=r*(ActualWidth/GridWidth); // get actual distance in metres
      if ( r < 0.00000000001 ) then r:=0.00000000001;

      //////////////////////////////////////
      /// WAVE FUNCTION TO TEST
      ///
      ///

      case StartOption of

      1: begin

          if ( electron ) then begin      // if electron being modelled
            theta:=theta_const*(Time - k*r);
            term1:=delta;
          end
          else begin                       // if positron being modelled
            theta:=theta_const*(Time + k*r);
            term1:=-delta;
          end;

          term2:=cos(theta);
          term3:=-sin(theta);

          with points[NewScreen,xpos,ypos,zpos].PsiVect do begin
            if ( ViewTop ) then begin
              x:=term1 * term2;
              y:=term1 * term3;
              z:=0;
            end
            else begin
              x:=term1 * term2;

```

```

        y:=0;
        z:=term1 * term3;
    end;
end;
points[NewScreen,xpos,ypos,zpos].Psi := term1;
end;
end;

///
///
////////////////////////////////////

end;
end;
end; // end {scan grid's x coords}

for xpos:=0 to GridWidth-1 do begin      {scan grid's x coords}
for ypos:=0 to GridHeight-1 do begin    {scan grid's y coords}
for zpos:=0 to GridDepth-1 do begin     {scan grid's z coords}

    ThisGroup:=PointGroup(scr, xpos, ypos, zpos);
    NewGroup:=PointGroup(NewScreen, xpos, ypos, zpos);

    with points[NewScreen,xpos,ypos,zpos] do begin
    if (smoothing) then begin
        x:= xpos - midx;
        y:= ypos - midy;
        z:= zpos - midz;

        r:=sqrt( sqr(x) + sqr(y) + sqr(z) );
        if ( r < 0.004 ) then r:=0.004; // prevent divide by zero errors

        ElectricPotential:=ElectronCharge/(4*Pi*r*Permittivity);
    end
    else begin
        VectGrp:=VectorGroup(NewGroup, PSI_VECTOR_FIELD);
        ElectricPotential:=VectDiv(VectGrp);
    end;
    end;

end;
end;
end; // end {scan grid's x coords}

for xpos:=0 to GridWidth-1 do begin      {scan grid's x coords}
for ypos:=0 to GridHeight-1 do begin    {scan grid's y coords}
for zpos:=0 to GridDepth-1 do begin     {scan grid's z coords}

    ThisGroup:=PointGroup(scr, xpos, ypos, zpos);
    NewGroup:=PointGroup(NewScreen, xpos, ypos, zpos);

```

```

{ ThisGroup's points are assigned as follows:  P3          P5
                                                P1 P0 P2
                                                P4          P6

```

Where P5 & P6 are in the Z plane (P5 at the back and P6 at the front) }

```

x:= xpos - midx;
y:= ypos - midy;
z:= zpos - midz;

r:=sqrt( sqr(x) + sqr(y) + sqr(z) );
if ( r < 0.00000000001 ) then r:=0.00000000001; // prevent divide by zero errors

unit_x:= x/r;
unit_y:= y/r;
unit_z:= z/r;

r:=r*(ActualWidth/GridWidth); // get actual distance in metres

if ( ViewTop ) then begin
  normal_x:=unit_y;
  normal_y:=-unit_x;
  normal_z:=unit_z;
end
else begin
  normal_x:=unit_z;
  normal_y:=unit_y;
  normal_z:=-unit_x;
end;

// Electric Field is: -div of ElectricPotential Field - d/dt of Vector Potential field
Scalar_Group:=ScalarGroup(NewGroup, ELECTRIC_POTENTIAL_FIELD);

// This is the div of ElectricPotential Field
points[NewScreen,xpos,ypos,zpos].Electric:=ScalarGrad(Scalar_Group);

// get amplitude of Static Electric field component
E_amp:=VectSize(points[NewScreen,xpos,ypos,zpos].Electric);

// From Schrodinger's wave equation:
//
// VectorPotential = -i*SpinConstant*div(V)
// SpinConstant = Hhat/ElectronMass
//
// A is orthogonal to div(V) and also proportional to to div(V)
// note: div(V) = Laplacian(Z)
with points[NewScreen,xpos,ypos,zpos].VectorPotential do begin
  x := normal_x*SpinConstant*E_amp;
  y := normal_y*SpinConstant*E_amp;
  z := normal_z*SpinConstant*E_amp;
end;

```

```

// Electric Field is: -div of ElectricPotential Field - d/dt of Vector Potential field
// In Electric, we already have div of ElectricPotential Field, now make negative & subtract
// d/dt of Vector Potential field
with points[NewScreen,xpos,ypos,zpos].Electric do begin
  // E = -div(V) - (1/c)*dA/dt  { dA/dt = (A^2/r) i.e. like acceleration of angular velocity }
  x := -x - unit_x*((sqr(points[NewScreen,xpos,ypos,zpos].VectorPotential.x)/r)/SpeedOfLight);
  y := -y - unit_y*((sqr(points[NewScreen,xpos,ypos,zpos].VectorPotential.y)/r)/SpeedOfLight);
  z := -z - unit_z*((sqr(points[NewScreen,xpos,ypos,zpos].VectorPotential.z)/r)/SpeedOfLight);
end;

// Magnetic Field is Curl of Vector Potential Field
VectGrp:=VectorGroup(NewGroup, VECTOR_POTENTIAL_FIELD);
CurlVect:=VectCurl(VectGrp);

with points[NewScreen,xpos,ypos,zpos].Magnetic do begin
  x:=Permeability*CurlVect.x;
  y:=Permeability*CurlVect.y;
  z:=Permeability*CurlVect.z;
end;
end;
end; // end {scan grid's x coords}
end; //if Flip_YZ
end;

```