

Title: Goldbach Conjecture – A Proof (?)

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Abstract: The Goldbach Conjecture may be stated as follows:

Every even number greater than 4 can be written as the sum of two primes.

Examples:

$$6 = 3+3$$

$$8 = 3+5$$

$$10 = 3+7; 5+5$$

We will call the two primes summing to a particular number a Goldbach Pair (GP) for that number.

Consider the following identity for positive even numbers (N,u,v)

$$N = (N-u) + (N-v) - (N-u-v) \quad \{N > v >= u\} \quad (1)$$

Assume the even numbers 6, 8, ..., N-2 are GP's so that their component primes are ≥ 3 and $< N-3$.

i.e. $(N-u), (N-v), (N-u-v)$ are GP's $\{(N-u-v) \geq 6\}$

We must show N is also a GP.

We will restrict the terms we consider in (1) to those where:

$$2N > (N-u) + (N-v) > N \quad (2)$$

Assume $N = (A+B)$ $\{(A, B) \text{ prime}; A \geq N/2 \geq B\}$

From (1) $(A+B) = (A+a) + (B+b) - (N-u-v)$ $\{(a, b) \text{ prime}; B > a \geq b\}$

Where $(N-u) = (A+a)$
 $(N-v) = (B+b)$
 $(N-u-v) = (N-u) + (N-v) - N = a+b$

Using $N = 12$ as an example the restrictions (2) allow the following representations for (1).

	N	a+b	u	v	N-u	N-v	N-u-v
(i)	12	3+3	2	4	10	8	6
(ii)	12	3+5	2	2	10	10	8

Thus (i) $12 = 10 + 8 - 6$
 $= (7+3) + (5+3) - (3+3)$
 $= (7+5)$

(ii) $12 = 10 + 10 - 8$
 $= (7+3) + (5+5) - (5+3)$
 $= (7+5)$

And 12 is a GP as required.

This method may be used for any N apparently.