

Title: Goldbach Conjecture – A Proof (?)

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Abstract: The Goldbach Conjecture may be stated as follows:

Every even number greater than 4 can be written as the sum of two primes.

Examples:

$$6 = 3+3$$

$$8 = 3+5$$

$$10 = 3+7; 5+5$$

We will call the two primes summing to a particular number a Goldbach Pair (GP) for that number.

Consider the following identity for positive even numbers  $\{N, u, v\}$ :

$$N = (N-u) + (N-v) - (N-u-v) \quad \{u, v; N > v >= u\} \quad (1)$$

Assume all the even numbers  $\{6, 8, \dots, N-2\}$  are GP's: we wish to show N is also a GP.

Thus  $N = (A+B)$   $\{(A,B) \text{ prime}; A >= N/2 >= B\}$   
 $(N-u), (N-v), (N-u-v)$  are GP's  $\{(N-u-v) >= 6\}$

In (1)  $(A+B) = (A+a) + (B+b) - (N-u-v)$   $\{(a,b) \text{ prime}; A > a >= b\}$

Where  $(N-u) = (A+a)$   
 $(N-v) = (B+b)$   
 $(N-u-v) = (N-u) + (N-v) - N = a+b$

Using  $N = 12$  as an example the following table displays eligible values

<b>N</b>	<b>a+b</b>	<b>u</b>	<b>v</b>
12	3+3	2	4
12	6+2	2	2

Therefore (1) occurs in 2 ways:

$$12 = 10 + 8 - 6$$

$$= (7+3) + (5+3) - (3+3) = (7+5)$$

$$12 = 10 + 10 - 8$$

$$= (7+3) + (5+5) - (5+3) = (7+5)$$

And 12 is a GP.

This method may be used for any N apparently.