

## Two conjectures on the number of primes obtained concatenating to the left with numbers lesser than p a prime p (II)

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**Abstract.** In this paper I conjecture that there exist an infinity of primes  $p = 30 \cdot h + j$ , where  $j$  can be 1, 7, 11, 13, 17, 19, 23 or 29, such that, concatenating to the left  $p$  with a number  $m$ ,  $m < p$ , is obtained a number  $n$  having the property that the number of primes of the form  $30 \cdot k + j$  up to  $n$  is equal to  $p$ . Example: such a number  $p$  is  $67 = 30 \cdot 2 + 7$ , because there are 67 primes of the form  $30 \cdot k + 7$  up to 3767 and  $37 < 67$ . I also conjecture that there exist an infinity of primes  $q$  that don't belong to the set above, i.e. doesn't exist  $m$ ,  $m < q$ , such that, concatenating to the left  $q$  with  $m$ , is obtained a number  $n$  having the property shown. Primes can be classified based on this criteria in two sets: primes  $p$  that have the shown property like 13, 17, 23, 31, 37, 41, 47, 59, 61, 67, 71, 73, 89, 103 (...) and primes  $q$  that don't have it like 7, 11, 19, 29, 43, 53, 79, 83, 101 (...).

### Conjecture 1:

There exist an infinity of primes  $p = 30 \cdot h + j$ , where  $j$  can be 1, 7, 11, 13, 17, 19, 23 or 29, such that, concatenating to the left  $p$  with a number  $m$ ,  $m < p$ , is obtained a number  $n$  having the property that the number of primes of the form  $30 \cdot k + j$  up to  $n$  is equal to  $p$ .

Example:

Such a number  $p$  is  $67 = 30 \cdot 2 + 7$ , because there are 67 primes of the form  $30 \cdot k + 7$  up to 3767 and  $37 < 67$ .

### The sequence of primes $p$ :

- :  $p = 13$ , because there are 13 primes of the form  $30k + 13$  up to 613 and  $6 < 13$ ;
- :  $p = 17$ , because there are 17 primes of the form  $30k + 17$  up to 817 and  $8 < 17$ ;
- :  $p = 23$ , because there are 23 primes of the form  $30k + 23$  up to 1123 and  $11 < 23$ ;

- :  $p = 31$ , because there are 31 primes of the form  $30k + 1$  up to 1831 and  $18 < 31$ ;
- :  $p = 37$ , because there are 37 primes of the form  $30k + 7$  up to 1937 and  $19 < 37$ ;
- :  $p = 41$ , because there are 41 primes of the form  $30k + 11$  up to 2141 and  $21 < 41$ ;
- :  $p = 47$ , because there are 47 primes of the form  $30k + 17$  up to 2447 and  $24 < 47$ ;
- :  $p = 59$ , because there are 59 primes of the form  $30k + 29$  up to 3259 and  $32 < 59$ ;
- :  $p = 61$ , because there are 61 primes of the form  $30k + 1$  up to 3561 and  $35 < 61$ ;
- :  $p = 67$ , because there are 67 primes of the form  $30k + 7$  up to 3767 and  $37 < 67$ ;
- :  $p = 71$ , because there are 71 primes of the form  $30k + 11$  up to 4171 and  $41 < 71$ ;
- :  $p = 73$ , because there are 73 primes of the form  $30k + 13$  up to 4173 and  $41 < 73$ ;
- :  $p = 89$ , because there are 89 primes of the form  $30k + 29$  up to 5289 and  $52 < 89$ ;
- :  $p = 103$ , because there are 103 primes of the form  $30k + 13$  up to 6103 and  $6 < 103$ ;
- (...)

Note that, in few cases above:

- :  $m = (p - 1)/2$  [ $n = 613, 817, 1123$ ]
- :  $m = (p + 1)/2$  [ $n = 1937, 2141, 2447$ ]
- :  $m = (p + 5)/2$  [ $n = 1831, 3259$ ]
- :  $m = (p + 9)/2$  [ $n = 3561, 4173$ ]
- :  $m = p - 30$  [ $n = 3767, 4171$ ]

### **Conjecture 2:**

There exist an infinity of primes  $q$  that don't belong to the set above, i.e. doesn't exist  $m$ ,  $m < q$ , such that, concatenating to the left  $q$  with  $m$ , is obtained a number  $n$  having the property shown.

### **The sequence of primes $q$ :**

7, 11, 19, 29, 43, 53, 79, 83, 101 (...)