Abstract

In this paper we suggest a new way to write the gravitational constant that makes all of the Planck constants; Planck length, Planck time, Planck mass, and Planck energy much more intuitive and simpler to understand. Most importantly this opens up the way for several new and simpler interpretations in physics. By writing the gravitational constant in a Planck functional form, we can rewrite all of the Planck constants (without changing their values) to a form that surprisingly is fully consistent with mathematical atomism. This strongly indicates that particles have a spatial dimension and that atomism is the correct interpretation of fundamental physics, including the physics of the quantum realm. Unfortunately very few physicists have studied mathematical atomism and we are afraid we may be speaking to deaf ears.

Key words: Gravitational constant, Planck: length, time, mass, energy, Haug mathematical atomism, Quantum physics, Golden ratio.

1 A New Perspective

We suggest that the gravitational constant should be written as a function of Planck’s reduced constant

\[ G_p = \frac{\hbar c^3}{\bar{\hbar} \times 10^{-35}} \]  

where \( \hbar \) is the reduced Planck’s constant and \( c \) is the well tested round-trip speed of light. We could call this Planck’s form of the gravitational constant. The parameter \( \bar{\hbar} \) is an unknown constant that is calibrated so that \( G_p \) matches our best estimate for the gravitational constant. However, we will also suggest an exact and interesting value for \( \bar{\hbar} \) later in this paper. The part \( 10^{-35} \) is just an additional artifice due to particular selected measurement units, in this case meters, kilograms, and seconds. We will use the same units throughout this paper, but the \( 10^{-35} \) could be removed by using other units.

The Planck form of the gravitational constant enables us to rewrite Planck’s constants in a form that, in our view, simplifies and gives much deeper insight and opens up the path for totally new interpretations in physics. Based on this, the Planck length can be simplified to

\[ l_p = \sqrt{\frac{\hbar G_p}{c^3}} = \sqrt{\frac{\frac{\hbar}{\bar{\hbar}} \times 10^{-35}}{c^3}} = \bar{\hbar} \times 10^{-35} \]  

Here the Planck length is simply our constant \( \bar{\hbar} \) times \( 10^{-35} \). Further, the Planck time in this context is

\[ t_p = \sqrt{\frac{\hbar G_p}{c^5}} = \sqrt{\frac{\frac{\hbar}{\bar{\hbar}} \times 10^{-35}}{c^5}} = \bar{\hbar} \times c \times 10^{-35} \]  

In this view, the Planck time is simply the time it takes for the speed of light \( c \) to cross the Planck length. Next the Planck mass in this context results in

\[ m_p = \sqrt{\frac{\hbar c}{G_p}} = \sqrt{\frac{\hbar c}{\bar{\hbar} \times 10^{-35}}} = \frac{\hbar}{\bar{\hbar} \times c} \times 10^{-35} \]  

---

*e-mail espenhaug@mac.com. Thanks to Victoria Terces for helping me editing this manuscript.*
The Planck mass in this form is very interesting. In 2014, Haug showed that mass derived from ancient atomism had to be \( \frac{2}{3} \), where his \( H \) was the diameter of an indivisible particle and \( w \) the distance between the indivisible particles in the mass.\(^1\) Based on mathematical atomism, the \( \hbar \) in the Planck mass is then likely the diameter of the indivisible particles and \( \mathcal{N} \) the distance\(^2\) between the particles. Significantly in that work, Haug shows that to truly understand what mass (matter) is relative to energy the very essence is in \( \frac{1}{2} \). This is what he defines or points out must be time-speed. Bear in mind that \( c \) is a velocity and a distance is the length traveled divided by the time it takes for light to travel that distance. In other words, \( c = \frac{L}{T} \) and this means \( \frac{1}{2} = \frac{2}{L} \), that is how many seconds goes by per meter traveled. The time-speed of light is about 3 nanoseconds per meter. As discussed by Haug in 2014, the part \( \frac{1}{2} \) only represents how much equivalent continuous mass (continuous time) this particular mass contains. In the special case where \( \mathcal{N} = \hbar \) then we have a true continuous mass. To fully understand this and to get a completely new perspective on the interpretation of physics one must study Haug (2014) New Fundamental Physics in detail, in particular the chapter where he discusses energy and mass derived from atomism. Haug derives a complete new relativity theory from the postulates of ancient atomism and he obtains all of the same mathematical end results as Einstein when using Einstein synchronized clocks, but he also get a long series of additional equations. In addition, he obtains the famous equation \( E = mc^2 \) as well as the same relativistic mass energy relationship given by Einstein, however, in his work this is derived from the quantum realm of atomism. That the quantum realm of atomism gives exactly the same end results and matches up well with Planck seems to be no coincidence, but this has not been discovered until now.

Based on the gravitational constant, the Planck energy can be simplified to

\[
E_p = m_p c^2 = \sqrt{\frac{\hbar c}{G_p}} c^2 = \frac{\hbar}{\mathcal{N} c^2} \times \frac{1}{10^{-35}} = \frac{\hbar}{\mathcal{N} c} \times \frac{1}{10^{-35}} \tag{5}
\]

We can see from the derivation above that \( c^2 \) factor in the famous Einstein formula \( E = mc^2 \) is just a conversion factor to convert time-speed to speed as already proven by Haug (2014). In the Planck energy formula, \( \frac{\hbar}{c} \) is simply equivalent continuous meters per second (passing a detector). In other words, as proven elegantly and intuitively by Haug (2014) energy is simply speed and mass is time-speed. The Planck equations are fully consistent with ancient atomism.

And finally we will also rewrite the reduced Compton wavelength:

\[
\frac{\hbar}{2m_p c} = \frac{\hbar}{\mathcal{N} c} \times \frac{1}{10^{-35}} = \mathcal{N} \times 10^{-35} \tag{6}
\]

We summarize or results in the table below, the Planck form and the Haug form derived from ancient atomism are identical. Based on Haug (2014), the interpretation of mass and energy is quite different and much more profound and logical than the standard interpretations given in modern physics.

<table>
<thead>
<tr>
<th></th>
<th>Planck-form</th>
<th>Haug-form</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Gravitational constant</strong></td>
<td>( G \approx 6.67408 \times 10^{-11} )</td>
<td>( G_p = \frac{\hbar}{\mathcal{N} c} )</td>
</tr>
<tr>
<td><strong>Planck length</strong></td>
<td>( l_p = \sqrt{\frac{\hbar c}{G_p}} )</td>
<td>( l_p = \mathcal{N} )</td>
</tr>
<tr>
<td><strong>Planck time</strong></td>
<td>( t_p = \sqrt{\frac{\hbar c}{G_p}} )</td>
<td>( t_p = \frac{\hbar}{\mathcal{N} c} )</td>
</tr>
<tr>
<td><strong>Planck mass</strong></td>
<td>( m_p = \sqrt{\frac{\hbar c}{G_p}} )</td>
<td>( m_p = \frac{\hbar}{\mathcal{N} c} )</td>
</tr>
<tr>
<td><strong>Planck energy</strong></td>
<td>( E_p = \frac{\hbar c}{G_p} )</td>
<td>( E_p = \frac{\hbar}{\mathcal{N} c} )</td>
</tr>
<tr>
<td><strong>Relationship mass and energy</strong></td>
<td>( E_p = m_p c^2 )</td>
<td>( E_p = \frac{\hbar}{\mathcal{N} c} )</td>
</tr>
<tr>
<td><strong>Reduced Compton wavelength</strong></td>
<td>( \frac{\hbar}{m_p c} )</td>
<td>( \mathcal{N} )</td>
</tr>
</tbody>
</table>

\(^1\)Haug (2014) uses a slightly different notation in his book.

\(^2\)What Haug (2014) calls the i-distance in his theory, which is the distance center to center, or front to front, or back to back between two indivisible particles; it is the equivalent to the wave-length in modern physics. This distance must be larger or equal to the diameter of the indivisible particle. One should not compare the indivisible particles in Haug’s theory with the standard idea of particles in modern physics. The indivisible particles are very different than the particles in modern physics, please study some mathematical atomism before attacking the indivisible particles.
As shown more elegantly by Haug (2014) the factor $\frac{1}{2}$ in the mass is time divided by distance, that is $\frac{t}{r}$ and $c$ is $\frac{h}{\Phi}$. This means that in its most pure form the relationship between energy and mass is nothing more than $\frac{E}{c^2} = \frac{\hbar}{m c^3} \Phi$ that can be written on the compact form $c = \frac{\hbar}{m c^3} \Phi$. Einstein (1905) famous formula $E = mc^2$ is ultimately nothing more than $c = \frac{\hbar}{m c^3} \Phi$, but this is also the extreme beauty of the formula. Time is indivisible particles traveling back and forth counter-striking (creating or we could say maintaining the mass) and energy is indivisible particles freed from this. This explains why a small amount of mass can give so much energy. Continuous pure energy is time-speed times $c^2$. Again $c^2$ is simply a conversion factor between mass (time-speed) and energy (speed). This is hard to fully understand at the deepest level without seeing how this can be derived from atomism as published by Haug in 2014. Bear in mind that $\frac{\hbar}{m}$ actually just is a factor adjusting for how much equivalent continuous mass or continuous energy there is in this particular mass or energy.

As I am Haug, I have to admit I had no idea that the energy and mass relationships I derived years ago directly from atomism are basically the same equations as Planck’s, but derived from a deeper and much simpler and more logical perspective. From atomism we automatically get quantization, but we do not get the silly point particles of modern physics interpretations.

2 The Golden Ratio and the $\Phi$ Factor

Above we introduced the following functional form for the gravitational constant

$$G_p = \frac{\Phi c^3}{\hbar} \times 10^{-35} \tag{7}$$

Measurement of the gravitational constant interestingly gives a value of $\Phi$ very close to the Golden ratio $\Phi$. An alternative to try to measure the gravitational constant approximately is simply to set $\Phi = \Phi$

$$G_p = \frac{\Phi c^3}{\hbar} \times 10^{-35} \approx 6.689 \times 10^{-11} \tag{8}$$

That is well inside the “band” of recent gravitational constant measurements, for example Fixler, Foster, McGuirk, and Kasevich (2007) reported a gravitational constant of 6.693(34) $\times 10^{-11}$ while Schlaminger (2014) reported a gravitational constant of 6.67191(99) $\times 10^{-11}$. We do not claim that $\Phi$ must take the value $\Phi$, to use the Golden ratio could very likely just be a good approximation for the real value $\Phi$ must take, or potentially $\Phi$ could contain a untapped secret of a beautiful gravitational constant.3

By using the Golden ratio $\Phi$ for the $\Phi$ we get the following Planck length

$$l_p = \sqrt{\frac{\hbar G_p}{c^3}} = \Phi \times 10^{-35} \approx 1.61803 \times 10^{-35} \tag{9}$$

Thus the Planck length is simply the Golden ratio times $10^{-35}$. This makes it very easy to remember the Planck length and means that the Planck time is simply

$$t_p = \sqrt{\frac{\hbar G_p}{c^2}} = \frac{\Phi}{c} \times 10^{-35} \approx 5.39718 \times 10^{-44} \tag{10}$$

And the Planck mass is

$$m_p = \sqrt{\frac{\hbar c}{G_p}} = \sqrt{\frac{\Phi c}{\hbar}} \times 10^{-35} = \frac{\hbar}{\Phi c} \times 10^{-35} \approx 2.17404 \times 10^{-08} \tag{11}$$

Further, the Planck energy must be

$$E_p = m_p c^2 = \sqrt{\frac{\hbar c}{G}} \times 10^{-35} = \frac{\hbar}{\Phi c} \times 10^{-35} c^2 = \frac{\hbar}{\Phi c} \times 10^{-35} \approx 1953930970 \tag{12}$$

And finally based on this, the reduced Compton wavelength must be

$$r_p = \frac{\hbar}{m_p c} = \frac{\hbar}{\frac{\hbar}{\Phi c}} \times 10^{-35} = \frac{1}{\Phi c} \times 10^{-35} \approx 1.01664 \times 10^{-34} \tag{13}$$

3Well some physicist and mathematicians would possibly considering the Golden ratio in the gravitational constant to be ugly, as it would mean that the gravitational constant and the Planck constants have a infinite number of unknown digits.
Table 2: The table shows the Planck constants re-written on the Haug form when, in addition, we assume $\Phi$ is equal or approximately equal to the Golden ratio $\Phi$. But again we do not claim that $\Phi$ must take exactly this value, $\Phi$ is possibly or even likely just an approximation.

<table>
<thead>
<tr>
<th></th>
<th>Planck-form</th>
<th>Haug-form</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gravitational constant</td>
<td>$6.67 \times 10^{-11} &gt; G &lt; 7 \times 10^{-11}$</td>
<td>$G_p = \frac{\Phi c}{\sqrt{\pi}} \approx 6.689001 \times 10^{-11}$</td>
</tr>
<tr>
<td>Planck length</td>
<td>$l_p = \sqrt{\frac{\hbar G}{\pi}}$</td>
<td>$l_p = \Phi \times 10^{-35}$</td>
</tr>
<tr>
<td>Planck time</td>
<td>$t_p = \sqrt{\frac{\hbar G}{\pi}}$</td>
<td>$t_p = \Phi \times 10^{-35}$</td>
</tr>
<tr>
<td>Planck mass</td>
<td>$m_p = \sqrt{\frac{\hbar G}{\pi}}$</td>
<td>$m_p = \frac{1}{2} \frac{\hbar}{2\pi c} \times 10^{-35}$</td>
</tr>
<tr>
<td>Planck energy</td>
<td>$E_p = \sqrt{\frac{\hbar G}{\pi}}$</td>
<td>$E_p = \frac{1}{2} \frac{\hbar c}{2\pi} \times 10^{-35}$</td>
</tr>
<tr>
<td>Reduced Compton wavelength</td>
<td>$\frac{1}{m_p}$</td>
<td>$\Phi \times 10^{-35}$</td>
</tr>
</tbody>
</table>

3 Conclusion

By making the gravitational constant a function form of the reduced Planck constant, we can rewrite the Planck equations into simpler and much more intuitive forms. We expect very few people to understand the beauty of this paper as almost no physicists today are well studied in atomism and even fewer people have any clues about the wonders of mathematical atomism. We encourage the physics community to strongly consider mathematical atomism as the fundamental theory of everything. Haug has shown that a new mathematical physics derived from atomism gives all the same mathematical end results as Einstein’s special relativity theory when using Einstein synchronized clocks, but with much deeper insight. However, Haug has also shown that Einstein’s special relativity theory is incomplete and he has derived a long series of additional results. Do not take this the wrong way; all of Einstein’s equations are correct under Einstein synchronized clocks. With this paper he has proven that the energy and mass equations he has derived from very simple and intuitive principles rooted in postulates from ancient atomism are the same equations as given by Max Planck. Any serious physicists hoping for a unified theory should now take a close look at mathematical atomism and skip flawed theories that cannot offer much hope, super-string theory being one prominent example.

References


