

Any square of a prime larger than 7 can be written as $30n^2+60n+p$ where p prime or power of prime

Abstract. In this paper I make the following conjecture:
Any square of a prime larger than 7 can be written as $30n^2 + 60n + p$, where p prime or power of prime and n positive integer.

Conjecture:

Any square of a prime larger than 7 can be written as $30n^2 + 60n + p$, where p prime or power of prime and n positive integer.

Verifying the conjecture:

(for the first fifteen primes larger than 7)

: $11^2 = 121 = 30 \cdot 1^2 + 60 \cdot 1 + 31$;
: $13^2 = 169 = 30 \cdot 1^2 + 60 \cdot 1 + 79$;
: $17^2 = 289 = 30 \cdot 1^2 + 60 \cdot 1 + 199 = 30 \cdot 2^2 + 60 \cdot 2 + 7^2$;
: $19^2 = 361 = 30 \cdot 1^2 + 60 \cdot 1 + 271 = 30 \cdot 2^2 + 60 \cdot 2 + 11^2$;
: $23^2 = 529 = 30 \cdot 1^2 + 60 \cdot 1 + 439 = 30 \cdot 2^2 + 60 \cdot 2 + 17^2 = 30 \cdot 3^2 + 60 \cdot 3 + 79$;
: $29^2 = 841 = 30 \cdot 1^2 + 60 \cdot 1 + 751 = 30 \cdot 2^2 + 60 \cdot 2 + 601 = 30 \cdot 4^2 + 60 \cdot 4 + 11^2$;
: $31^2 = 961 = 30 \cdot 4^2 + 60 \cdot 4 + 241$;
: $37^2 = 1369 = 30 \cdot 1^2 + 60 \cdot 1 + 1279 = 30 \cdot 2^2 + 60 \cdot 2 + 1129 = 30 \cdot 3^2 + 60 \cdot 3 + 919$;
: $41^2 = 1681 = 30 \cdot 3^2 + 60 \cdot 3 + 1231 = 30 \cdot 4^2 + 60 \cdot 4 + 31^2 = 30 \cdot 5^2 + 60 \cdot 5 + 631 = 30 \cdot 6^2 + 60 \cdot 6 + 241$;
: $43^2 = 1849 = 30 \cdot 1^2 + 60 \cdot 1 + 1759 = 30 \cdot 2^2 + 60 \cdot 2 + 1609 = 30 \cdot 3^2 + 60 \cdot 3 + 1399 = 30 \cdot 4^2 + 60 \cdot 4 + 1129 = 30 \cdot 6^2 + 60 \cdot 6 + 409$;
: $47^2 = 2209 = 30 \cdot 3^2 + 60 \cdot 3 + 1759 = 30 \cdot 4^2 + 60 \cdot 4 + 1489 = 30 \cdot 6^2 + 60 \cdot 6 + 769$;
: $53^2 = 2809 = 30 \cdot 1^2 + 60 \cdot 1 + 2719 = 30 \cdot 4^2 + 60 \cdot 4 + 2089 = 30 \cdot 5^2 + 60 \cdot 5 + 1759 = 30 \cdot 6^2 + 60 \cdot 6 + 37^2 = 30 \cdot 7^2 + 60 \cdot 7 + 919 = 30 \cdot 8^2 + 60 \cdot 8 + 409$;
: $59^2 = 3481 = 30 \cdot 1^2 + 60 \cdot 1 + 3391$;
: $61^2 = 3721 = 30 \cdot 1^2 + 60 \cdot 1 + 3631 = 30 \cdot 2^2 + 60 \cdot 2 + 59^2 = 30 \cdot 3^2 + 60 \cdot 3 + 3271 = 30 \cdot 4^2 + 60 \cdot 4 + 3001 = 30 \cdot 5^2 + 60 \cdot 5 + 2671 = 30 \cdot 6^2 + 60 \cdot 6 + 2281 = 30 \cdot 7^2 + 60 \cdot 7 + 1831 = 30 \cdot 8^2 + 60 \cdot 8 + 1321 = 30 \cdot 9^2 + 60 \cdot 9 + 751 = 30 \cdot 10^2 + 60 \cdot 10 + 11^2$;
: $67^2 = 4489 = 30 \cdot 4^2 + 60 \cdot 4 + 3769 = 30 \cdot 6^2 + 60 \cdot 6 + 3049 = 30 \cdot 8^2 + 60 \cdot 8 + 2089 = 30 \cdot 11^2 + 60 \cdot 11 + 199$.