

NLED Gedankenexperiment for a non singular universe, and a re thinking of what constitutes initial entropy, with reference as to initial universe conditions for relic graviton production

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Abstract.

1. Introduction

We initially look at a non singular universe representation of entropy, based in part on what was brought up by Muller and Lousto, and then generalize it to the question of initial time step as a function of NLED (non linear Electrodynamics) . Speculations as to the contribution of initial entropy to massive gravitons is also included. In addition, the non singular nature of an initial cosmology configuration , with its emphasis upon initial density proportional to 1 over the fourth power of an initial scale factor will lead to an initial time step of the order of Planck time, as opposed to the GR equation which postulates time set at $t = 0$ initially.

First of all we wish to ascertain if there is a way to treat entropy in the universe , initially, by the usual black hole formulas. Our derivation takes advantage of work done by Muller, and Lousto [1] which have a different formulation of entropy cosmology , based upon a modified event horizon, which they call the Cosmological Event Horizon. i.e. it represents the distance a photon emitted at time t can travel.

Afterwards, we give an argument, as an extension of what is presented by Muller and Lousto [1], which we claim ties in with Cai [2], as to a bound to entropy, which is stated to be S (entropy) less than or equal to N , with N , in this case, a micro state numerical factor.

Then, a connection as to Ng's infinite quantum statistics[3] is raised. I.e. afterwards, we are then referencing C.S. Camara a way to ascertain a non zero finite, but extremely small bounce and then we use the scaling, as given by Camara [4], that a resulting density, is scaled as by $\rho \sim a^{-4}$. This scaling with the scale factor as given by Camara[4] has if we look at Walecka [5] a way to make a NLED (non linear electrodynamics) argument as to what to look for in a minimum time step, with the requisite time step given by $t \sim \text{initial time} \sim 1/\text{square root of density(initial)}$. Of course the classical treatment of density and cosmology will have, then that there is infinite initial density, but if the bounce, i.e. minimal non zero scale factor is due to magnetic field strengths, we will have an argument which may have traction and relevancy.

We link entropy, with a non zero scale factor. I.e. if the Muller and Lousto [1] supposition is correct, and we used a modified version of the Camara[4] et al bounce , which in turn is linked to a mix of the Cai [2] bound to entropy, with the value of N as set also by the Ng derivation [3] of infinite quantum

statistics. What the N as stated by the Infinite statistics depends upon, also, is an admissible quantum wave length for a particle. In the case of what was suggested, i.e. that due to what was brought up in [Haranas](#) and [Gkigkitzis](#) [6] that the mass of a graviton would vary as the square root of the cosmological ‘constant’ parameter. We will come back to this, and discuss its startling implications in the conclusion. I.e. this result will be compared directly with Dr. Stoica’s [7] work on admissible procedure as to elimination of removal of the standard pathologies associated with singular cosmology. The review of what is in Stoica’s work will be in the last part of this document.

2. Calculations as to Entropy, and what it says about bouncing, versus non singular universes

We begin first by putting the results of [1] here and subsequently modifying them. To begin with, we look at what was given as to entropy, and this was actually asked me as to a review of a similar article several weeks ago

By [1], as an extension of work which compliments was done in [8], where $a(grid) \sim$ Planck’s length

$$S(universe) \sim .3r_H^2 / a(grid)^2 \quad (1)$$

The specifics of what were done with r_H , is what will be discussed in this section, and Eq.(1) has its counter part in [8] as given by, if R is the radius of a sphere inside of which harmonic oscillation occurs, and $a(grid)_{H.O.}$ is in this case is of a different value, i.e. generalized Harmonic Oscillator based lattice spacing.

$$S(Harmonic.oscillators) \sim \frac{.3}{4\pi} \cdot \left(\frac{4\pi R^2}{a(grid)_{H.O.}^2} \right) \quad (2)$$

The main import of Eq. (1) is that it defacto leads to a ‘non dimensional’ representation of entropy, but before we do that, it is useful to review what is said about r_H . As defined in [1], r_H is called the maximal co-ordinate distance a photon can travel in space-time in a given time, t.

FWIW, we will provisionally in the regime of z (red shift) > 1100 set for inflation from a Planck time interval up to 10^{-20} seconds, when the expansion radii of the universe was about a meter, i.e.

$$r_H|_{min} \sim O(l_{Planck}) < r_H < r_H|_{max} \sim 1 \text{ meter} \quad (3)$$

What we will do in later parts of this paper, to get an approximation as to what the actual value of r_H is, and to use this to comment upon the development of entropy.

2.1 Relevance of Eq. (1) to the concept of dimensionless entropy

Cai, in [2] has an abbreviated version of entropy as part of a generalized information measurement protocol which we will render as having T.F.A.E.

$$\begin{aligned}
S &\leq \tilde{N} \Leftrightarrow \\
\Lambda &\sim \tilde{N} \Leftrightarrow \\
e^{\tilde{N}} &\text{ states} \Leftrightarrow \\
\text{set of all } \Lambda(\tilde{N}) &\text{ of space-times} \Leftrightarrow \\
\tilde{N} &= 3G / G\Lambda
\end{aligned} \tag{4}$$

We will assume that $N = \tilde{N}$, and then connect the entropy of Eq.(4) with Ng's entropy [3] with the result that

$$S \approx \tilde{N} = N \tag{5}$$

While assuming Eq. (5) we will through [3] be examining the consequences of infinite quantum statistics for which, if the "Horizon" value r_H as defined above is made roughly commensurate with say graviton wavelength

$$\begin{aligned}
r_H &\sim \lambda(\text{wavelength}) \& \\
S &\sim N \cdot \left[\log(V(\text{volume}) / [\lambda(\text{wavelength})]^3) + \frac{5}{2} \right] \\
&\propto N \cdot \left[+ \frac{5}{2} \right] \sim N
\end{aligned} \tag{6}$$

The entropy so mentioned, above, is commensurate with the following identification, namely how to link a measure of distance with scale factor $a(t)$. We will as a starting point use the following identification, namely start with the radiation dependence of $a(t)$ [4,6]

$$\begin{aligned}
a(t) &\sim (t / t(\text{present}))^{1/2} \\
\Leftrightarrow t &= [1 / 6\pi \cdot G\rho(t)]^{1/2} \\
\rho(t) &\sim a(t)^{-4}
\end{aligned} \tag{7}$$

Our starting point for the rest of the article will lie in making sense of the following inputs into the scale factor as the last part of Eq.(7) grouping of mathematical relations, namely we will look at time defined via [5] . of time $t = 1 / \sqrt{6\pi G\rho(t)}$

And the following for defining the density, via its scaled relationship to $(1/ a^4(t))$, with the minimum value of $a(t)$, as given by Camara [4] as, using a frequency ω , B_0 an initial E and M field given at the start of creation itself, and of course a cosmological 'constant' parameter Λ which will be defined later

$$\alpha_0 = \sqrt{\frac{4\pi G}{3\mu_0 c}} B_0$$

$$\hat{\lambda}(\text{defined}) = \Lambda c^2/3$$
(8)

$$a_{\min} = a_0 \cdot \left[\frac{\alpha_0}{2\hat{\lambda}(\text{defined})} \left(\sqrt{\alpha_0^2 + 32\hat{\lambda}(\text{defined}) \cdot \mu_0 \omega \cdot B_0^2} - \alpha_0 \right) \right]^{1/4}$$

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The linkage to graviton mass, and heavy gravitons will build upon this structure so built up via [6] , and will comprise the capstone as to what to look for in GW research. A topic which the author is involved with. I.e. consequences of working with the following graviton mass will be brought up, namely what if[6]

$$m_{\text{graviton}} = \frac{\hbar}{c} \cdot \sqrt{\frac{(2\Lambda)}{3}}$$
(9)

This above formula will de evolve, from a larger value, to having the mass of a graviton approximately as given about 10^{-62} grams in the present era [9]

Also, if the above graviton mass is accepted, we will be considering the value of N defined within the event horizon r_H , with

$$N = N_{\text{graviton}} \Big|_{r_H} = \frac{c^3}{G \cdot \hbar} \cdot \frac{1}{\Lambda}$$
(10)

A specified value of a_0 will also be ascertained, in this document. We set it equal to 1, and then calculated the other values from there.

From the above, we will specify a variance graviton mass, a minimum time, according to the above, and work out full consequences, with suggestions for finding exact values of the above parameters.

3. Filling in the parameters, what it says about initial cosmological conditions

First, now the treatment of entropy due to early universe Gravitons. In the beginning of this analysis, we start with Ali and Das's cosmology from Quantum potential article[10], where a derived

cosmological “constant is given by, if $l_{Planck}^2 \sim 10^{-70}$ meters squared, and $l_{Radius-Universe}^2 \sim 10^{52}$ meters squared, so that

$$\Lambda_{Einstein-Const.} = 1/l_{Radius-Universe}^2 \quad (11)$$

Eq.(11) should be compared to an expression given by T. Padmanabhan [11], if the $E_{Planck} \sim 10^{28} eV$, and $m_{graviton} \sim 10^{-32} eV$, and $E \sim N_{graviton} \cdot m_{graviton}$

$$\Lambda_{Einstein-Const.Padmanabhan} = 1/l_{Planck}^2 \cdot (E/E_{Planck})^6 \quad (12)$$

Then the entropy at the end of the electro weak era is, assuming this is commensurate with graviton production, with the value of the Horizon radius at the upper end of Eq. [3] above, namely about 1 meter

$$S_{graviton} \sim 10^{39} \quad (13)$$

Given this, we can now consider what would be the magnetic field, initially, and the other parameters as given in the end of the last section.

Doing so, if so, we can have frequency as high as

$$\omega_{initial} \Big|_{r_H \sim 1meter} \sim 10^{21} Hz \quad (14)$$

Using inflation, this would be redshifted at a minimum of 11 orders of magnitude, down to about 10^{10} Hz today, at the highest end. The nature of the E and B fields, also as fill in would have to be commensurate with what was given in [12]

Still though, as a rule of thumb, we would have that the MINIMUM value of the magnetic field, in question would have to be [4]. I.e. for high frequencies, the minimum value of the magnetic field would actually be very low!

$$B > \frac{1}{2 \cdot \sqrt{10 \mu_0 \cdot \omega}} \quad (15)$$

4. Conclusions; Why we have a non zero initial entropy

Why we pursued this datum of an initial non zero entropy ? In a word, to preserve the fidelity of physical law from cosmological cycle to cycle. I.e. the bits we calculated with, came from Seth Lloyd [13], and also from Giovanni [14], with the upper end to graviton frequencies calculated as follows [14]

$$\begin{aligned}
S_{\text{gravitons-present.era}} &= V(\text{volume}) \times \int_{v_0}^{v_1} r(v) dv \\
&\approx (10^{29})^3 \times (H_1 / M_p)^3 \sim (10^{29})^3 \sim 10^{87} \\
&\Leftrightarrow v_0 \sim 10^{-18} \text{ Hz} \ \& \ v_1 \sim 10^{11} \text{ Hz}
\end{aligned} \tag{16}$$

S.Lloyd, sets, in [13]

$$\begin{aligned}
I(\text{number} - \text{bits}) &\sim (\#)^{3/4} \sim 10^{90} (\text{present} - \text{era}) \\
&\Leftrightarrow \# \leq (1 / 2\pi) \cdot (r / l_p) \cdot (t / t_p) \sim 10^{122} (\text{present} - \text{era})
\end{aligned} \tag{16}$$

The first part of Eq.(16) in terms of ‘bits’ is approximately similar to Eq.(15), and even more tellingly,

$$\begin{aligned}
I(\text{number} - \text{bits}) &\sim (\#)^{3/4} \sim 10^{37} (\text{EW} - \text{era}) \\
&\Leftrightarrow \# \leq (1 / 2\pi) \cdot (r / l_p) \cdot (t / t_p) \sim 10^{49} (\text{EW} - \text{era})
\end{aligned} \tag{17}$$

The upper part of Eq.(17) overlaps, a bit with Eq.(3) and Eq. (14), whereas Eq.(16) is only a few orders of magnitude higher than the formal numerical count for the number of operations, # of Eq. (13), i.e. the number of bits, given in Eq.(16) is similar to the graviton entropy count given in Eq. (15), which in turn is within several orders of magnitude of the baryon count used to fix the fine structure constant, as given in Eq. (13). Note that Eq. (13), in the baryon number count is within several orders of magnitude of the graviton count, in Eq. (16). However, most tellingly, the initial non zero graviton count, given when the universe is 1 meter in diameter, or so, is initiated by negative pressure, which we recount, below

We state, first of all, that with we use Lloyd [13], and also Corda, et.al [15]

$$\begin{aligned}
\# \text{operations} &\sim \rho_{\text{crit}} \times t^4 \sim (t / t_p)^2 \\
&\Leftrightarrow \rho_{\text{crit}} \sim 1 / t^2 \propto \rho_\gamma = \frac{16}{3} \cdot c_1 \cdot B^4 \\
&\Leftrightarrow \# \text{operations} \sim (t / t_p)^2 / B^8 \\
&\sim 1 / (t_p B^4) \sim 1 / B^4
\end{aligned} \tag{18}$$

The upshot is that the entropy, at the close of the Inflationary era, would be dominated by Graviton production as of about the electroweak era, and this would have consequences as far as information, as can be seen by the approximation given by Seth Lloyd [13] on page 14 of the article, as to the number of operations # being roughly about

$$\# \leq (1 / 2\pi) \cdot (r / l_p) \cdot (t / t_p) \tag{19}$$

In the electro-weak era, we would be having Eq. (19) as giving a number of ‘computational steps’ many times larger (10 orders of magnitude) than the entropy of the Electro-weak,

$$\#(\text{Electro-weak}) \sim 10^{49} \tag{20}$$

In addition, making use of the above calculations, if we do so, we obtained that the minimum time step would be of the order of Planck time, i.e. of about 10^{-44} seconds, using [5] and Eq. (7) above, which is very small, but not zero, whereas, again, assuming a 1 meter radii, which we obtain at the end of inflation, with a time step the, at the end of inflation of 10^{-20} seconds. This is significant, when the universe had a radii of 1 meter, is about when we would expect to have the value of Eq.(20). This set of number of operations would be about when we would expect Planck's constant to be set, with the values as given in [16]. In addition, there is no way that the initial entropy would be zero, largely on account of Eq. (5) and Eq. (10) above. As to Stoica's work, we will say that the removal of a chance for a non zero pathological singularity, as he mentioned, would be altered to cover a non zero bounce, but one which was nearly zero. I.e. the initial graviton count would be immeasurably lower than the present day era value, as given in Eq. (16) above.

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References

- [1] R. Mueller, C. O. Lousto, “**Entanglement entropy in curved spacetimes with event horizons**”, **Phys.Rev. D52 (1995) 4512-4517**, <http://arxiv.org/abs/gr-qc/9504049>
- [2] R-C. Cai, “Some Remarks on Constant Curvature Spaces”, pp. 234-250, in Superstring Theory, K. Liu, and S-T. Yau, (Advanced Lectures in Mathematics,) Higher Education Press, Beijing, PRC (2005)
- [3] Y. Jack Ng, “Holographic foam, dark energy and infinite statistics,” Phys. Lett. B, 657, (2007), pp. 10-14
Y.Jack Ng,”Article: Spacetime Foam: From Entropy and Holography to Infinite Statistics and Nonlocality” Entropy 2008, 10(4), 441-461; DOI: 10.3390/e10040441
- [4] C.S. Camara, M.R. de Garcia Maia, J.C. Carvalho, and J.A.S. Lima, “ Nonsingular FRW cosmology and Non Linear dynamics”, Arxiv astro-ph/0402311 version 1, Feb 12, 2004
- [5] J. D. Walecka, *Introduction to Modern Physics, Theoretical Foundations*, World press scientific Co, Pte. Ltd. 5 Tok Link, Singapore, Republic of Singapore, 596224
- [6] I. Haranas and I. Gkigkitzis, “The Mass of Graviton and Its Relation to the Number of Information according to the Holographic Principle”, International Scholarly Research Notices, Volume 2014 (2014), Article ID 718251, 8 pages, <http://www.hindawi.com/journals/isrn/2014/718251/>
- [7] Ovidiu Cristinel Stoica *Singular General Relativity Ph.D. Thesis*; <http://arxiv.org/pdf/1301.2231v4.pdf>
- [8] L Bombelli, R. K. Koul, J. Lee, and R. D. Sorkin, PRD 34, 373(1986)
- [9] **A. Goldhaber, M. Nieto, “Photon and Graviton Mass Limits”, Rev.Mod.Phys.82:939-979,2010**, <http://arxiv.org/abs/0809.1003>
- [10] A. F. Ali, S. Das “Cosmology from Quantum Potential”, Physics Letters B 741, (2015), 276-279
- [11] T. Padmanabhan, http://ned.ipac.caltech.edu/level5/Sept02/Padmanabhan/Pad1_2.html
- [12] **H. Wen, F.Y. Li, Z.Y. Fang, A. Beckwith, “Impulsive cylindrical gravitational wave: one possible radiative form emitted from cosmic strings and corresponding electromagnetic response”, <http://arxiv.org/abs/1403.7277>**
- [13] S. Lloyd, “Computational Capacity of the Universe”, <http://arxiv.org/abs/quant-ph/0110141>

and [10.1103/PhysRevLett.88.237901](https://doi.org/10.1103/PhysRevLett.88.237901)

- [14] M. Giovannini “A primer on the Physics of the Cosmic Microwave Background”, World Scientific, Singapore, Republic of Singapore, 2008
- [15] C. Corda, H. Cuesta “Removing Black Hole singularities with Non Linear Electrodynamics”, Modern Physics A, Volume 25, No. 28 (2010), PP 2423-2429
- [16] P.J. Mohr, B.N. Taylor, and D.B. Newell (2011), "The 2010 CODATA Recommended Values of the Fundamental Physical Constants" (Web Version 6.0). This database was developed by J. Baker, M. Douma, and S. Kotochigova. Available: <http://physics.nist.gov> [Thursday, 02-Jun-2011