

Two conjectures on the numbers obtained concatenating the integers of the form $6k+1$ with the digits 081

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Abstract. In this paper I conjecture that there exist an infinity of positive integers m of the form $6k + 1$ such that the numbers formed by concatenation $n = m081$ are primes or squares of primes, respectively semiprimes $p*q$ such that $q - p + 1$ is prime or power of prime.

Conjecture 1:

There exist an infinity of positive integers m of the form $6k + 1$ such that the numbers formed by concatenation $n = m081$ are primes or powers of primes.

Such pairs $[m, n]$ are:

: [19, 19081]; [31, 31081]; [97, 97081]; [49, 49081];
[85, 85081]; [91, 91081]; [121, 121081]; [127, 127081];
[157, 157081]; [175, 175081]; [181, 181081];
[187, 187081]; [199, 199081]; [205, 205081];
[217, 217081]; [229, 229081]; [241, 241081 = 491^2];
[253, 253081]; [259, 259081 = 509^2];
[295, 295081]; [313, 313081]; [325, 325081]; [331, 331081];
[337, 337081]; [343, 343081]; [349, 349081];
[379, 379081]; [385, 385081]; [409, 409081];
[421, 421081]; [427, 427081]; [439, 439081];
[475, 475081]; [517, 517081]; [559, 559081];
[577, 577081]; [563, 563081]; [569, 569081]; [595, 595081]; [607, 607081]...

Conjecture 2:

There exist an infinity of positive integers m of the form $6k + 1$ such that the numbers formed by concatenation $n = m081$ are semiprimes $p*q$ such that $q - p + 1$ is prime or power of prime.

Such pairs $[m, n]$ are:

: [1, 1081 = $23*47$ and $47 - 23 + 1 = 25 = 5^2$];
: [7, 7081 = $73*97$ and $97 - 73 + 1 = 25 = 5^2$];
: [13, 13081 = $103*127$ and $127 - 103 + 1 = 25 = 5^2$];
: [37, 37081 = $11*3371$ and $3371 - 11 + 1 = 3361$];
: [43, 43081 = $67*643$ and $643 - 67 + 1 = 577$];

: [73, 73081 = 107*683 and 683 - 107 + 1 = 577];
: [79, 79081 = 31*2551 and 2551 - 31 + 1 = 2521];
: [115, 115081 = 157*733 and 733 - 157 + 1 = 577];
: [145, 145081 = 59*2459 and 2459 - 59 + 1 = 2401 =
7^4];
: [247, 247081 = 211*1171 and 1171 - 211 + 1 = 961 =
31^2];
: [271, 271081 = 307*883 and 883 - 307 + 1 = 577];
: [463, 463081 = 571*811 and 811 - 571 + 1 = 241];
: [529, 529081 = 7*75583 and 75583 - 7 + 1 = 75577];
: [535, 535081 = 109*4909 and 4909 - 109 + 1 = 4801];
: [541, 541081 = 199*2719 and 2719 - 199 + 1 = 2521];
: [547, 547081 = 229*2389 and 2389 - 229 + 1 = 2161]
[...]