Local quantum measurement discrimination without assistance of classical communication

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Abstract.
The discrimination of quantum operations is an important subject of quantum information processes. For the local distinction, existing researches pointed out that, since any operation performed on a quantum system must be compatible with no-signaling constraint, local discrimination between quantum operations of two spacelike separated parties cannot be realized. We found that, however, local discrimination of quantum measurements may be not restricted by the no-signaling if more multi-qubit entanglement and selective measurements were employed. In this paper we report that local quantum measurement discrimination (LQMD) can be completed via selective projective measurements and numerous seven-qubit GHZ states without help of classical communication if both two observers agreed in advance that one of them should measure her/his qubits before an appointed time. As an application, it is shown that the teleportation can be completed via the LQMD without classical information. This means that the superluminal communication can be realized by using the LQMD.

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1. Introduction

Quantum state discrimination is an important subject in quantum information theory [1]. It is well known that two pure states cannot be perfectly discriminated unless they are orthogonal. An object closely related to quantum state discrimination is the discrimination of quantum operation, including unitary operations, quantum channels, and quantum measurements, etc. Several researches have shown that quantum measurements can be distinguished with certainty despite their uncertain nature [2−5]. For two spacelike separated parties, however, it has been shown theoretically [6−9] that since the operators at distance commute, the averages of the observable at distant site remain the same and do not depend on the operations employed by the other distant party, i.e., the no-signaling constraint holds that entanglement cannot be used for superluminal communication. For example, consider two observers, Alice and Bob, who have a bipartite quantum system in a known state ρ. They perform local quantum projection operators, with elements \( \sum_i A_{\mu i}^\dagger A_{\mu i} = I, \sum_j B_{\nu j}^\dagger B_{\nu j} = I \) and \([A_{\mu i}, B_{\nu j}] = 0\), on the subsystem respectively. If Bob is not informed that Alice got result \( \mu \), the
probability that he gets $\nu$ is $p_\nu = \text{tr}(\sum_j B_{\nu j} \rho B_{\nu j}^\dagger)$. This result does not depend on Alice’s operations, Bob cannot decide what measurements Alice did [10]. By a careful analysis, however, it may be found that, for multipartite entanglement systems shared by Alice and Bob, if Alice only announced publicly that she had completed her measurement and did not declare the result of her measurement after her operations, the local discrimination of quantum measurements can be completed. In this paper, we present a theoretical scheme for local quantum measurement discrimination (LQMD) by using selective projective measurement with numerous seven-qubit Greenberger-Horne-Zeilinger (GHZ) states. It is shown that, in this scheme, if both two observers (Alice and Bob) agreed in advance that one of them (e.g. Alice) should measure her qubits before an appointed time (it is equivalent that, after her measurement, Alice only announced publicly that she had completed the measurement, and did not declare the result of her measurement), the local discrimination of two different kinds of measurement can be completed by using a series of single-qubit correlative measuring basis without help of classical communication, that is to say, our LQMD may be not restricted by the no-signaling. As an application, we discuss the teleportation [11] of an unknown single-qubit state via the LQMD, and show that the unknown original state can be recovered without help of classical information. This means that the superluminal communication can be realized by using the LQMD.

The paper is organized as follows. In Sec. 2 two different kinds of projective quantum measurements with a seven-qubit GHZ state are described. In Sec. 3 we present an explicit scheme for local discrimination between two different kinds of quantum measurements. In Sec. 4 quantum teleportation via the LQMD is discussed. In Sec. 5 the obtained results are summarized.

2. Two different kinds of projective measurement

In order to present our ideas more clearly, let us first review the quantum measurement with entanglement system. Suppose Alice and Bob share an entangled pair of qubits in the state $(|01\rangle + |10\rangle)/\sqrt{2}$. Let Alice measure her qubit $A$ in the computational basis, the post-measurement states will be $|01\rangle$ with probability 1/2, and $|10\rangle$ with probability 1/2. We now consider two cases as follows. In the first case, after her measurement, Alice did not tell Bob anything. In this case, the reduced density operator of Bob’s system should be $\rho^B = I/2$, thus Bob cannot know what measurements Alice did, and he cannot even tell if she had measured or not. In the second case, after her measurement, Alice only told Bob she had completed the measurement by the classical channel, and did not tell the result of her measurement. In this case, after Alice’s measurement, Bob can measure his qubit $B$ under the computational basis and the result of his measurement must be in the state corresponded to Alice’s outcome of measurement. As mentioned above, the viewpoint we emphasized is that, in the second case, since Bob knows that Alice had completed the measurement by her announcement, he can affirm that the qubit $B$ must be collapsed into the state corresponded to Alice’s result of measurement,
although he did not know Alices result of measurement. Our scheme is just based on
the viewpoint.

Now let us consider two observers, Alice and Bob, who share a seven-qubit GHZ state
\[ |G\rangle = \frac{1}{\sqrt{2}} ((0000000) + |1111111\rangle)_{A_1A_2A_3A_4A_5A_6B}, \]
where qubits \( A_1, A_2, \ldots, A_6 \) belong to Alice and \( B \) to Bob, respectively. Assume that
Alice and Bob agreed in advance that Alice should measure her qubits before an
appointed time. Now, let Alice employ two different kinds of measurement on the state \( |G\rangle \). In the first kind of measurement, Alice performs in turn common projective
measurements (CPMs) on the qubits \( A_1, A_2, \ldots, A_6 \) and \( B \) under the basis \{\( |+\rangle, |-\rangle \},
where \( |+\rangle = \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle), \) \( |-\rangle = \frac{1}{\sqrt{2}} (|0\rangle - |1\rangle) \). It is easy found that, after Alice’s
measurements, 64 possible final collapsed states of the qubit \( B \) will always be \( \frac{1}{8}|+\rangle_B \) or
\( \frac{1}{8}|-\rangle_B \). Now let us turn to the second kind of measurement. To complete the LQMD,
Alice will employ a novel kind of projective measurements, which we refer to as selective
projective measurements (SPMs), with a series of single-qubit correlative measuring
basis, on her qubits. Firstly, Alice measures the qubit \( A_1 \) in the state \( |G\rangle \) under the
basis \{\( |\nu\rangle, |\nu^\perp\rangle \}, \) where \( |\nu\rangle = x|0\rangle + y|1\rangle, \) \( |\nu^\perp\rangle = y|0\rangle - x|1\rangle \) \( x \) and \( y \) are real, \( x^2 + y^2 = 1, \) \( x \) and \( y \) are best.
Assume that Bob knows the coefficients \( x \) and \( y \). If the result of Alice’s measurement is \( |\nu\rangle_{A_1}, \) the qubits \( A_2, A_3, \cdots, A_6 \) and \( B \) will be collapsed into the state
\[ |\phi_1\rangle = \frac{1}{\sqrt{2}}(x|000000\rangle + y|111111\rangle)_{A_2A_3A_4A_5A_6B}. \]
she can measure the qubits \( A_2, A_3, \cdots, A_6 \) under the basis \{\( |+\rangle, |-\rangle \}, \) successively. After
that, the qubit \( B \) will be in the state \( \frac{1}{\sqrt{2}}|\mu^+\rangle_B \) or \( \frac{1}{\sqrt{2}}|\mu^-\rangle_B \), here \( |\mu^+\rangle = \frac{1}{\sqrt{2}}(x|0\rangle + y|1\rangle) \)
and \( |\mu^-\rangle = \frac{1}{\sqrt{2}}(x|0\rangle - y|1\rangle) \). If Alice’s measurement outcome is \( |\nu^\perp\rangle_{A_1}, \) the state of
qubits \( A_2, A_3, \cdots, A_6 \) and \( B \) will be collapsed into the state
\[ |\phi_2\rangle = \frac{1}{\sqrt{2}F_2}(y|000000\rangle - x|111111\rangle)_{A_2A_3A_4A_5A_6B}. \]
Then Alice measures the qubit \( A_2 \) under the basis \{\( |\lambda_1\rangle, |\lambda_1^\perp\rangle \}, \) which is given by
\[ |\lambda_1\rangle = \frac{1}{F_2}(\frac{x}{y}|0\rangle + \frac{y}{x}|1\rangle), \quad |\lambda_1^\perp\rangle = \frac{1}{F_2}(\frac{y}{x}|0\rangle - \frac{x}{y}|1\rangle), \]
where \( F_2 = [(x/y)^2 + (y/x)^2]^{1/2} \). Corresponding to Alice’s measurement outcome \( |\lambda_1\rangle_{A_2} \)
or \( |\lambda_1^\perp\rangle_{A_2}, \) the qubits \( A_3, \cdots, A_6 \) and \( B \) will be collapsed into the state \( |\phi_2\rangle \) or \( |\phi_2^\perp\rangle \) with
probability 1/2 each, which are given by
\[ |\phi_2\rangle = 1 \frac{1}{\sqrt{2}F_2}(x|000000\rangle - y|111111\rangle)_{A_3A_4A_5A_6B}, \]
\[ |\phi_2^\perp\rangle = \frac{1}{\sqrt{2}F_2}(\frac{y}{x}|000000\rangle + \frac{x}{y}|111111\rangle)_{A_3A_4A_5A_6B}. \]
As mentioned above, one can easily see that the goal of our SPMs is as much as
possible to make the qubit \( B \) collapsed into the state \( \frac{1}{R}|\mu^+\rangle \) or \( \frac{1}{R}|\mu^-\rangle \) after all, where \( R \)
is a constant or a coefficient related to \( x \) and \( y \). To present the SPMs more clearly, by described above, we can generalize the general approach of the SPMs as follows:

If the qubits \( A_{n+1}, A_{n+2}, \ldots, A_m \) and \( B \) are collapsed into the state

\[
|\phi'_\nu\rangle = \frac{1}{\sqrt{2T_n}} \left( \frac{y^{p_n}}{x^{p_n-1}}|00\cdots00\rangle + \frac{x^{p_n}}{y^{p_n-1}}|11\cdots11\rangle \right)_{A_{n+1}A_{n+2}A_{n+3}A_{n+4}B},
\]

(6)

where \( n = 1, 2, \ldots, m \), \( T_n = F_1 F_2 \cdots F_n \), \( p_n = 2^{n-1} \), \( F_n = [(x/y)^{p_n} + (y/x)^{p_n}]^\frac{1}{2} \), and let \( F_1 = 1 \), Alice should employ a new single-qubit projective measurement on the qubit \( A_{n+1} \) under the basis \( \{|\lambda_n\rangle, |\lambda'_n\rangle\} \), which is given by

\[
|\lambda_n\rangle = \frac{1}{F_{n+1}} \left[ (\frac{x}{y})^{p_n}|0\rangle + (\frac{y}{x})^{p_n}|1\rangle \right], \quad |\lambda'_n\rangle = \frac{1}{F_{n+1}} \left[ (\frac{y}{x})^{p_n}|0\rangle - (\frac{x}{y})^{p_n}|1\rangle \right].
\]

(7)

If the result of Alice’s measurement is \( |\lambda_n\rangle \), the qubits \( A_{n+2}, A_{n+3}, \ldots, A_m \) and \( B \) will be collapsed into the state \( |\phi_{n+1}\rangle \), which is given by

\[
|\phi_{n+1}\rangle = \frac{1}{\sqrt{2T_{n+1}}} \left( x|00\cdots00\rangle + y|11\cdots11\rangle \right)_{A_{n+2}A_{n+3}A_{n+4}A_{n+5}B},
\]

(8)

she can measure the qubits \( A_{n+2}, A_{n+3}, \ldots, A_m \) under the basis \( \{|+\rangle, |-\rangle\} \) successively, the qubit \( B \) will be collapsed into the state \( \frac{1}{2^n T_n} |\mu^+\rangle \) or \( \frac{1}{2^n T_n} |\mu^-\rangle \), here \( d = (m - n - 1)/2 \). If the outcome of Alice’s measurement is \( |\lambda^\perp_n\rangle \), the qubits \( A_{n+2}, A_{n+3}, \ldots, A_m \) and \( B \) will be collapsed into the state \( |\phi'_{n+1}\rangle \), which is given by

\[
|\phi'_{n+1}\rangle = \frac{1}{\sqrt{2T_{n+1}}} \left( \frac{y^{p_{n+1}}}{x^{p_{n+1}-1}}|00\cdots00\rangle - \frac{x^{p_{n+1}}}{y^{p_{n+1}-1}}|11\cdots11\rangle \right)_{A_{n+2}A_{n+3}A_{n+4}A_{n+5}B},
\]

(9)

she should repeat above similar approach, until the result of measurement \( |\lambda_{m-1}\rangle_{A_m} \) or \( |\lambda^\perp_{m-1}\rangle_{A_m} \) in the basis \( \{|\lambda_{m-1}\rangle, |\lambda^\perp_{m-1}\rangle\} \) has been obtained, and the qubit \( B \) has been collapsed into the state \( \frac{1}{T_m} |\mu^+\rangle_B \) or \( \frac{1}{\sqrt{2T_m}} (\frac{y^{p_m}}{x^{p_m}}|0\rangle - \frac{x^{p_m}}{y^{p_m}}|1\rangle) \) after all.

By above general approach, after Alice’s measurements, 64 possible final collapsed states of the qubit \( B \) can be obtained. The relation of the results of Alice’s measurement and the possible final collapsed states of the qubit \( B \) can be expressed as follows:

\[
|\nu\rangle_{A_1} \rightarrow |\psi^\perp\rangle = \frac{1}{4\sqrt{2}} |\mu^\perp\rangle_B \quad (32 \text{ terms})
\]

\[
|\lambda_1\rangle_{A_2} \rightarrow |\psi^\perp\rangle = \frac{1}{4T_2} |\mu^\perp\rangle_B \quad (16 \text{ terms})
\]

\[
|\lambda_2\rangle_{A_3} \rightarrow |\psi^\perp\rangle = \frac{1}{2\sqrt{2T_3}} |\mu^\perp\rangle_B \quad (8 \text{ terms})
\]

\[
|\lambda_3\rangle_{A_4} \rightarrow |\psi^\perp\rangle = \frac{1}{2T_4} |\mu^\perp\rangle_B \quad (4 \text{ terms})
\]

\[
|\lambda_4\rangle_{A_5} \rightarrow |\psi^\perp\rangle = \frac{1}{\sqrt{2T_5}} |\mu^\perp\rangle_B \quad (2 \text{ terms})
\]

\[
|\lambda_5\rangle_{A_6} \rightarrow \left\{ \begin{array}{ll}
|\psi^\perp\rangle = \frac{1}{\sqrt{2T_6}} (\frac{2^2}{x^2} |0\rangle + \frac{2^2}{y^2} |1\rangle) \quad (1 \text{ term})
\end{array} \right.
\]

Thus much Alice’s selective measurements have been completed. From Eq.(10), it is easy found that, after Alice performing the SPMs on her all qubits, the probability of
the qubit $B$ being in the state $\frac{1}{\sqrt{3}}|\mu^\pm\rangle$ ($g_n = 2^{(6-n)/2}$, $n = 1, 2, \cdots, 6$) is \(\frac{63}{64}\). Clearly, after Alice performing the CPMs or SPMs on her qubits respectively, the final collapsed states of the qubit $B$ are obvious different. It must be emphasized that, whether Alice’s measurements are the CPMs or SPMs, since Alice and Bob agreed in advance that Alice should measure her qubits before an appointed time, Bob can know that the qubit $B$ must be collapsed into the state corresponded to one of Alice’s 64 results of measurement after Alice’s measurements.

3. Local discrimination of two different kinds of measurement

Now let us turn to depict the LQMD. Suppose that two observers, Alice and Bob, share 30 seven-qubit GHZ states, which are given by

$$|G^{(k)}\rangle = \frac{1}{\sqrt{2}}((|0000000\rangle + |1111111\rangle)|A_1^{(k)}A_2^{(k)}A_3^{(k)}A_4^{(k)}A_5^{(k)}A_6^{(k)}B^{(k)}\rangle,$$

where $k = 1, 2, \cdots, 30$, and the qubits $A_1^{(k)}, A_2^{(k)}, \cdots, A_6^{(k)}$ belong to Alice and $B^{(k)}$ to Bob, respectively. Different from previous quantum operation discrimination schemes, we assume that there is no classical channel between Alice and Bob. In this case, before the agreed time $t$, Alice randomly performs two different kinds of measurements, CPMs or SPMs, on her qubits in the state $|G^{(k)}\rangle$ ($k = 1, 2, \cdots, 30$) respectively. If Alice employs the CPMs on her qubits, after Alice’s measurements, all qubits $B^{(k)}$ will be in the states $\frac{1}{8}|+\rangle_{B^{(k)}}$ or $\frac{1}{8}|-\rangle_{B^{(k)}}$. At the appointed time $t$, Bob measures his qubits $B^{(k)}$ all in the basis $\{|0\rangle, |1\rangle\}$. After Bob’s measurements, by statistics theory, the probability of all qubits $B^{(k)}$ in the state $|0\rangle$ or $|1\rangle$ will be in the ratio of one to one. If Alice’s measurements are the SPMs, by described above, after Alice’s selective measurements, the probability of all qubits $B^{(k)}$ in the states $\frac{1}{\sqrt{3}}|\mu^+\rangle$ or $\frac{1}{\sqrt{3}}|\mu^-\rangle$ ($g_n = 2^{(6-n)/2}$, $n = 1, 2, \cdots, 6$) is $\left(\frac{63}{64}\right)^{30} \approx 0.62$, i.e., the probability of at least one qubit $B^{(k)}$ in the state $|\psi^+_6\rangle$ is $1 - \left(\frac{63}{64}\right)^{30} \approx 0.38$. At the appointed time $t$, Bob measures the qubits $B^{(k)}$ all in the basis $\{|0\rangle, |1\rangle\}$. One can see that, after measurements of Bob, in the 38% cases, the probability of the qubits $B^{(k)}$ in the state $|0\rangle$ or $|1\rangle$ will be different from the case Alice employed the CPMs. To illustrate this clearly, without loss of generality, we first discuss the case in which only one qubit $B^{(k)}$ in the state $|\psi^+_6\rangle$ after Alice’s measurements. From the state $|\psi^+_6\rangle$ in Eq. (10), it is easily found that, after Bob’s measurements, the probability of the qubit $B^{(k)}$ in the state $|0\rangle$ or $|1\rangle$ will be in the ratio of one to $u$ ($u = (\frac{2^2}{31^2})^2/(\frac{2^2}{31^2})^2 \approx 1.45 \times 10^{29}$), that is, the qubit $B^{(k)}$ will be always collapsed into the state $|1\rangle$. As a special case, we also assume that all the other 29 qubits $B^{(k)}$ are in the states $|\psi^+_6\rangle$ after Alice’s measurements and then all the 29 qubits are in the state $|0\rangle$ after Bob’s measurement. In this situation, one can easily find that the probability of the 30 qubits $B^{(k)}$ in the state $|0\rangle$ or $|1\rangle$ will be in the ratio of 1 to 2.5 after Bob’s measurement. For general case in which the qubit $B^{(k)}$ in the state $|\psi^+_6\rangle$ and other 29 qubits $B^{(k)}$ collapsed randomly into the states $\frac{1}{\sqrt{6}}|\mu^\pm\rangle$ ($g_n = 2^{(6-n)/2}$, $n = 1, 2, \cdots, 6$) after Alice’s measurement, it is easily found that the probability of the 30 qubits $B^{(k)}$ in the state $|0\rangle$ or $|1\rangle$ will be in the ratio of one to $w(1)$. 

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Bob should make three agreements beforehand as follows: Belong to Alice and states, which are given by EDS is composed of 40 ESGs and each ESG consisting of 30 seven-qubit GHZ informing quantum channel (IQC), which consists of two encoding-decoding sets (EDSs), is no classical channel between Alice and Bob, instead, another quantum channel, called Pauli matrix. Different from previous protocols of teleportation, we suppose that there qubit 2 belongs to Alice and 3 to Bob. The state of whole system can be expressed as

\[
|\psi_6^+\rangle = \frac{1}{\sqrt{2}}(|0000000\rangle + |1111111\rangle),
\]

where \(|\Phi^\pm\rangle = (|00\rangle \pm |11\rangle)/\sqrt{2}, |\Psi^\pm\rangle = (|01\rangle \pm |10\rangle)/\sqrt{2}, and \sigma_i (i = x, y, z) is the Pauli matrix. Different from previous protocols of teleportation, we suppose that there is no classical channel between Alice and Bob, instead, another quantum channel, called informing quantum channel (IQC), which consists of two encoding-decoding sets (EDSs), either EDS is composed of 40 ESGs and each ESG consisting of 30 seven-qubit GHZ states, which are given by

\[
|G^{(k)}_{i,j}\rangle = \frac{1}{\sqrt{2}}(|0000000\rangle + |1111111\rangle)A_{1(i,j)}^{(k)}A_{2(i,j)}^{(k)}A_{3(i,j)}^{(k)}A_{4(i,j)}^{(k)}A_{5(i,j)}^{(k)}A_{6(i,j)}^{(k)}B_{(i,j)}^{(k)},
\]

where \(i = 1, 2, j = 1, 2, \cdots, 40, and k = 1, 2, \cdots, 30, and qubits A_{1(i,j)}^{(k)}, A_{2(i,j)}^{(k)}, \cdots, A_{6(i,j)}^{(k)}\) belong to Alice and \(B_{(i,j)}^{(k)}\) to Bob, respectively. To complete the teleportation, Alice and Bob should make three agreements beforehand as follows:

\[w(1) > 2.5\] after Bob’s measurement. Now we consider the case in which there are two qubits \(B_{(k)}^{(i)}\) and \(B_{(k')}^{(i')}\) in the state \(|\psi_6^+\rangle\) after Alice’s measurement. Similar to the above described, one can find that there is no classical channel between Alice and Bob, instead, another quantum channel, called Pauli matrix. Different from previous protocols of teleportation, we suppose that there qubit 2 belongs to Alice and 3 to Bob. The state of whole system can be expressed as

\[
|\psi_6^+\rangle = \frac{1}{\sqrt{2}}(|0000000\rangle + |1111111\rangle).
\]

To ensure the result of Bob’s measurement more reliable, it can be further supposed that Alice and Bob share 40 entangled states groups (ESGs), each consisting of 30 seven-qubit GHZ states \(|G^{(k)}\rangle\) (see Eq. (11)). If Alice’s measurements are the CPMs, it is easy found that, after Alice’s and Bob’s measurements, the probability of all qubits \(B_{(k)}^{(i)}\) of each ESG in the state \(|0\rangle\) or \(|1\rangle\) will be in the ratio of one to one. If Alice’s measurements are the SPMs, by statistics theory, after Alice’s and Bob’s measurements, in 15 ESGs the probability of the qubits \(B_{(k)}^{(i)}\) of each ESG in the state \(|0\rangle\) or \(|1\rangle\) will be in the ratio of one to \(W\) \((W \geq 2.5)\) after Bob’s measurements.

4. Applications: quantum teleportation via the LQMD

As an example of application, we present a quantum teleportation protocol (QTP) by using the LQMD. Suppose that Alice wants to teleport an unknown arbitrary single-qubit state \(|\xi_1\rangle = \alpha|0\rangle + \beta|1\rangle\) to Bob, with \(|\alpha|^2 + |\beta|^2 = 1\), and the state shared by Alice and Bob as the quantum channel is an EPR pair \(|\psi_23\rangle = \frac{1}{\sqrt{2}}(|00\rangle + |11\rangle)|_{23}\), where qubit 2 belongs to Alice and 3 to Bob. The state of whole system can be expressed as

\[
|\Xi\rangle = \frac{1}{2}(|\Phi^+\rangle_2|\xi_3\rangle_3 + |\Phi^-\rangle_2|\xi_3\rangle_3 + |\Psi^+\rangle_2|\sigma_x\rangle_3|\xi_3\rangle_3 + |\Psi^-\rangle_2(-i\sigma_y)|\xi_3\rangle_3,
\]

where \(|\Phi^\pm\rangle = (|00\rangle \pm |11\rangle)/\sqrt{2}, |\Psi^\pm\rangle = (|01\rangle \pm |10\rangle)/\sqrt{2}, and \sigma_i (i = x, y, z) is the Pauli matrix. Different from previous protocols of teleportation, we suppose that there is no classical channel between Alice and Bob, instead, another quantum channel, called informing quantum channel (IQC), which consists of two encoding-decoding sets (EDSs), either EDS is composed of 40 ESGs and each ESG consisting of 30 seven-qubit GHZ states, which are given by

\[
|G^{(k)}_{i,j}\rangle = \frac{1}{\sqrt{2}}(|0000000\rangle + |1111111\rangle)A_{1(i,j)}^{(k)}A_{2(i,j)}^{(k)}A_{3(i,j)}^{(k)}A_{4(i,j)}^{(k)}A_{5(i,j)}^{(k)}A_{6(i,j)}^{(k)}B_{(i,j)}^{(k)},
\]

where \(i = 1, 2, j = 1, 2, \cdots, 40, and k = 1, 2, \cdots, 30, and qubits A_{1(i,j)}^{(k)}, A_{2(i,j)}^{(k)}, \cdots, A_{6(i,j)}^{(k)}\) belong to Alice and \(B_{(i,j)}^{(k)}\) to Bob, respectively. To complete the teleportation, Alice and Bob should make three agreements beforehand as follows:
The informing messages 0 and 1 are represented by two different kinds of measurement CPMs and SPMs respectively.

The four Bell states $|\Phi^+\rangle$, $|\Psi^+\rangle$, $|\Psi^-\rangle$ and $|\Phi^-\rangle$ are represented by the informing messages 00, 01, 10 and 11 respectively.

Before an agreed time $T$, Alice can perform a Bell-state measurement on her qubits 1 and 2, and then according to her result of measurement, she should encode the messages of her result of measurement on the IQC. At the agreed time $T$, Bob should check Alice’s informing messages in the IQC.

Our QTP can be expressed as follows. Before the agreed time $T$, Alice performs a Bell-state measure on her qubits 1 and 2. Without loss of generality, assume her result of measurement is $|\Psi^+\rangle_{12}$. Then Alice encodes her informing messages 01 on the IQC, i.e., she makes the CPMs on the set $|G^{(k)}_{1,j}\rangle$ and the SPMs on the set $|G^{(k)}_{2,j}\rangle$, successively. At the agreed time $T$, Bob should check the states of qubits $B^{(k)}_{(1,j)}$ and $B^{(k)}_{(2,j)}$ all in the basis $\{|0\rangle, |1\rangle\}$. As described above, after that, Bob can extract that Alice employed the CPMs on the set $|G^{(k)}_{1,j}\rangle$ and the SPMs on the set $|G^{(k)}_{2,j}\rangle$, this means that Alice’s informing massages are 01 and the result of Bell-state measurement is $|\Psi^+\rangle_{12}$. By Eq. (12), Bob knows that the qubit 3 has been collapsed into the state $\frac{1}{2}(\beta|0\rangle + \alpha|1\rangle)_3$, then he can perform $\sigma_x$ on his qubit 3 and the original state $|\xi\rangle$ can be recovered. Thus, the teleportation is completed successfully.

Compared with precious teleportation protocols, the advantage in our QTP is that there is no classical channel. It is just because of this, the speed of teleporting quantum information is no longer limited by the speed of light, but it depends on the speed of quantum state collapse (or speed of quantum information) [12]. In recent years, the results of some EPR experiments [12-15] set a lower bound on this speed of $10^4 \sim 10^7$ times the speed of light. Obviously, in our QTP, if Alice and Bob are spaced far enough, the required time completing the quantum information transmission (including the time completed all measurements by Alice and Bob) will be less than the required time by the classical communication. In other words, the speed of teleporting an unknown quantum state in the QTP will be faster than the speed of light. It must be pointed out that, however, our QTP is not in contradiction with the special relativity, because, in the present scheme of LQMD, only multipartite entanglement systems were used and none of real material objects were transmitted between Alice and Bob.

5. Conclusions

In conclusion, we have proposed a theoretical scheme for local discrimination of two different kinds of measurement by using selective measurement and numerous seven-qubit GHZ states. To realize the scheme, a series of single-qubit correlative measuring basis has been employed. It is shown that, in this scheme, if both two observers agreed in advance that one of them (e.g. Alice) should measure her qubits before an appointed time, the perfect discrimination of local quantum measurement can be
completed successfully without help of classical communication, that is to say, our LQMD may be not restricted by the no-signaling. As an application, we have shown that the teleportation of an arbitrary single-qubit state can be completed via the LQMD without classical information. This means that the superluminal communication can be realized by using the LQMD. Furthermore, we should emphasize that our work has been completed in the framework of standard quantum mechanics. So far there has been experiment implementing the eight-qubit GHZ state [16], hence, we hope our work can be experimentally realized in the near future and stimulate further research on quantum communication and quantum information processing.

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References

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