## The Connection between Gravitation and the Velocity of Light

D.T. Froedge

Formerly Auburn University Phys-dtfroedge@glasgow-ky.com

V101914 @ http://www.arxdtf.org

### ABSTRACT

It has long been known that a photon entering a gravitational potential follows a path identically to that of a photon in a variable speed of light defined by the Shapiro velocity for Minkowski flat space [1]. It is shown here that a particle having constant energy infalling a gravitational potential, and defined as a pair of trapped photons in a massless box, is accelerated by a gradient in the velocity of light exactly as a particle in a gravitational field [2], and thus, is asserted that gravitation is nothing more than a gradient in c produced by the presence of mass. It is also illustrated that QFT effects that define the total action path of trapped photons could induce an alteration in the velocity of light in the proximity of the photon paths [3], and could be the mechanism creating the effects of gravitation.

#### Introduction

This paper on the connection of gravity and the speed of light draws on components other papers by the author. Since there was an early postulation that the energy of a particle infalling gravitation was conserved, it was not clear how the mysterious effects of gravitation could effect this. By recently noting that an earlier paper postulation that particles are composed of opposite going photons, the mechanism of inducing the conservative effects of gravitation became apparent, the same gradient in c that bends the trajectory of photons can induce the energy in opposite going photons to transfer from one to the other effectuating an increased velocity of the center of mass without a change in energy. Blandford et.al [1], and others [4],[5], have shown that photons operating according to Fermat's principle, in a medium having a speed of light with an index of refraction defined by:

$$c = c_0 \left( 1 - 2\frac{\mu}{r} \right) , \qquad (1)$$

follow a trajectory identical to that of a particle in a gravitation field. It is argued then that; if gravitation is "only" a gradient in the velocity of light, the photon would behave exactly the same. There is no need to postulate that gravitation constitutes anything else for a photon.

Work done by this author on a particle model of two opposite going photons trapped in a massless box, shows that all the covariant relativistic dynamical properties of a particle are matched by this model for a particle[2]. If it is shown then that the same gradient in c as in Eq.(1), induces the same effect as gravitation on the center of mass of the two trapped photons, then it is indicative that gravitation is nothing more than a gradient in c.

#### **III Four Momentum**

A pair of photon with a mass as  $m = hv/c^2$ , (which has precedents in other publications on photon entrapments[7]), moving along vectors paths in the opposite direction can be defined by the null four-momentum in geometric algebra matrix as:

$$\vec{\mathbf{P}}_{1} = \mathbf{m}_{1} \left( \gamma^{k} \mathbf{c}_{k} + \gamma^{0} \mathbf{c} \right)$$
(2)

$$\overrightarrow{\mathbf{P}_{2}} = \mathbf{m}_{2} \left( -\gamma^{k} \mathbf{c}_{k} + \gamma^{0} \mathbf{c} \right)$$
(3)

Presuming these two photons are co-located, the square of the sum of the two null vectors is necessarily constant and is:

$$(m_1 + m_2)^2 - (m_1 - m_2)^2 = 4m_1m_2 = m_0^2$$
(4)

The magnitude of each of these null four-momentum is zero for covariance, and the sum of two such moments must be constant. Thus  $m_0$  must be invariant fixed quantity associated with the pair of opposite going photons. If this is defined as a rest mass then it is easy to identify:

$$\left(\mathbf{m}_{1}+\mathbf{m}_{2}\right), \tag{5}$$

as the total mass. Factoring the total mass from Eq.(4), gives:

$$\left(m_{1}+m_{2}\right)^{2}\left[1-\frac{\left(m_{1}-m_{2}\right)^{2}}{\left(m_{1}+m_{2}\right)^{2}}\right]=m_{0}^{2}$$
(6)

Noting that:

$$\frac{\left(\mathbf{m}_{1}-\mathbf{m}_{2}\right)}{\left(\mathbf{m}_{1}+\mathbf{m}_{2}\right)}\tag{7}$$

is the ratio of the velocity of each photon to the velocity of the center of mass then:

$$(m_1 - m_2)v_c = (m_1 + m_2)c$$
 (8)

This makes Eq.(6), the relativistic energy equation for a mass particle.

$$(m_1 + m_2)^2 \left[1 - \frac{v^2}{c^2}\right] = m_0^2$$
 (9)

From the relativistic Lagrangian for a particle in a gravitational field:

$$L = m_0 c^2 = \left( mc^2 + m_0 c^2 \frac{\mu}{r} - m \frac{1}{2} v^2 \right)$$

(10)

Rearranging and squaring we have:

$$m^{2}\left(1-\frac{v^{2}}{c^{2}}\right) = m_{0}^{2}\left(1-\frac{\mu}{r}\right)^{2}$$
(11)

The right side of this equation is the relativistic mass, and the left which is independent of velocity is the rest mass as a function of the distance from the gravitating body.

Putting in Eq.(1), into Eq.(11), gives:

$$(m_1 + m_2)^2 \left(1 - \frac{v^2}{c^2}\right) = m_0^2 \frac{c}{c_0}$$
 (12)

(Note that  $c/c_0 = (1 - \mu/r)^2$  is used instead of Eq.(1), since for the purpose here they are equivalent, and has been shown to be more accurate for a locally conserved system [6].)

In a locally conservative system the energy of the particle is constant, thus as the particle infalls from infinity the rest mass is equal to the total mass. i.e.

$$\left(\mathbf{m}_{1}+\mathbf{m}_{2}\right)=\mathbf{m}_{0} \tag{13}$$

From Eq.(4), the rest mass in terms of the masses of the individual photons is:

$$4m_{1}m_{2} = m_{0}^{2} \frac{c}{c_{0}}$$
(14)

Eliminating  $m_2$  in Eq.(14), by use of Eq.(13), gives:

$$4m_{1}(m_{0}-m_{1})=m_{0}^{2}\frac{c}{c_{0}}$$
(15)

Solving for the mass of the mass of one of the single photons,  $m_1$  gives:

$$m_1^2 - m_1 m_0 + \frac{1}{4} m_0^2 \frac{c}{c_0} = 0, \qquad (16)$$

The quadratic solution of this is:

$$m_{1} = \frac{1}{2} m_{01} \left( 1 \pm \sqrt{1 - \frac{c}{c_{0}}} \right)$$
(17)

Since the initial mass of the total particle  $m_{01}$ , is twice the initial mass of the  $m_1$  photon then the mass change in the internal photon is:

$$\frac{\mathbf{m}_{01} - \mathbf{m}_{1}}{\mathbf{m}_{01}} = \pm \sqrt{\frac{\mathbf{c}_{0} - \mathbf{c}}{\mathbf{c}_{0}}},$$
(18)

or:

$$\frac{\Delta m_{1,2}}{m_{01}} = \pm \sqrt{\frac{\Delta c}{c_0}}$$
(19)

Eq.(13), is the relation between the constant total mass, which is the same as the rest mass. Eq.(19), is the change of the mass from one internal photon to another inside the particle as a function of the change in the speed of light. It represents a change in the velocity of the particle without a change in energy. The in-going photon has the + sign and the outgoing is the – sign.

#### Origin of Gravitation

The above expression, Eq.(19), may not seem all that impressive, but does have profound implications, the change in the kinetic energy of a particle is effectuated by the gradient of the velocity of light the same as if the particle was in a gravitational potential.

Conceptually, this seems simple accept that there is no work done on the particle as the particle enters the potential, and thus no energy exchanged, thus gravity is properly not a force, conveys no energy, and does no work. The kinetic mass has increased at the expense of the rest mass. The change in c provides the mechanism by which a conservative gravitational potential effectuates a change in the velocity of a particle without contributing energy.

The effect of gravitation on a particle is thus, induced in the particle by the gradient in the speed of light. Newton's apple falls not because of a decrease in energy, but because the speed of light at the branch is higher than the speed of light at the ground.

It has long been known that a photon obeying Fermat's principle, with a speed defined by Eq.(1), exhibits the proper trajectory [1], and from this development the same change in c induces the proper gravitational motion in particles. The concept of gravitation thus reduces to the presence of a gravitating mass, altering the local velocity of light in its vicinity.

It is asserted that Eq.(19), represents a cause-effect relation between particle motion and the speed of light **and is the mechanism that effects gravitation.** 

# **QFT Origin of Gravitation?**

This section is a bit of speculation, but well indicated by the state of the art.

Consider an apparatus having a cavity with opposing mirror and having photons trapped between the mirrors. From conservation of energy the apparatus has more mass and thus more gravitational attraction than the cavity without the photons. There is not asserted to be interaction between the photons, so the photons that are bouncing back and forth generates the gravitation. (Note that it is not without precedent that photons oscillating in a cavity are ascribed to have with mass  $(m = hv / c^2)[7]$ .

It has been shown by the mechanisms of Quantum Electrodynamics that an intense photon beam induces a change in the velocity of light in the vicinity of the beam. From the work of D. Kharzeeva, et.al, [3] it is shown that for an intense laser beam the QFT effects related to electron–positron loops induce vacuum "self-focusing" which is a vacuum alteration of the index of refraction in the speed of light in the vicinity of the beam. A model of particles being trapped, opposite going photons, as asserted here, consisting of photons reciprocating in the interior, which constitutes an intense, highly energetic back and forth beam of photons. This is orders of magnitude greater than a laser, and should by methods of QFT induce a change in c outside the particle itself. The repeating path action from one reflection to another has path probability well outside the classical path of the oscillating photons [8], and could induce the change in c near the particle equivalent to the effect of gravitation.

If gravitation is nothing more than a gradient in c. and QFT can induce a vacuum gradient in c then there is a direct connection.

"If" the induced value of c in the vicinity of oscillating photons can be found by methods of QFT to be:

$$c = c_0 \left( 1 - G \frac{\hbar \omega}{c^4 r} \right)^2$$
(20)

then the gravitational constant is calculated, and the riddle of gravitation would be solved.

References:

- 1. Roger Blandford, Kip S. Thorne, in Applications of Classical Physics, (in preparation, 2004), Chapter 26 http://www.pma.caltech.edu/Courses/ph136/yr2002/chap26/0226.1.pdf
- DT Froedge, The Concept of Mass as Interfering Photons, and the Originating Mechanism of Gravitation, V020914, <u>http://www.arxdtf.org/</u>
- 3. D. Kharzeeva, K. Tuchinb, Vacuum Self–Focussing of Very Intense Laser Beams, arXiv:hep-ph/0611133v2
- 4. F. Karimi, S. Khorasani, Ray-tracing and Interferometry in Schwarzschild Geometry, arXiv:1001.2177 [gr-qc]
- 5. Khorasani, Defections of Light and Shapiro Delay: An Equivalent Medium Theory Approach, arXiv:1206.1947v1 [gr-qc] 9 Jun 2012
- 6. DT Froedge, The Velocity of Light in a Locally Conserved Gravitational Field, ,V020914, <u>http://www.arxdtf.org/</u>
- 7. Alex KruchkovBose-Einstein condensation of light in a cavity http://arxiv.org/pdf/1401.0520v2.pdf

8. Feynman, Hibbs, 1965, Quantum Mechanics and Path Integrals McGraw-Hill.