

Raising our 4-dimensional uncurved space W to the power $1/2$.

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Abstract

The application of the (1402.0167, 1402.0170 viXra.org) to our 4 – dimensional vector space W when $M = 1, L = 2$. Cobasics are chosen so that V has simple algebraic and metric tensors.

Let the basis of W is $\overset{\mathbf{r}}{e}_\mu$. $W = V \otimes V$ (1)

$$V = W^{1/2} \quad (2)$$

The basis of V is $\overset{\mathbf{r}}{n}_\alpha$. $\overset{\mathbf{r}}{e}_\mu = e_\mu^{\alpha\beta} \cdot \overset{\mathbf{r}}{n}_\alpha \otimes \overset{\mathbf{r}}{n}_\beta$ (3)

Here $e_\mu^{\alpha\beta}$ are the cobasics. We choose the cobasics so :

$$\overset{\mathbf{r}}{e}_1 = 1 \cdot \overset{\mathbf{r}}{n}_1 \otimes \overset{\mathbf{r}}{n}_1 \quad (4)$$

$$\overset{\mathbf{r}}{e}_2 = i_1 \cdot \overset{\mathbf{r}}{n}_2 \otimes \overset{\mathbf{r}}{n}_1 \quad (5)$$

$$\overset{\mathbf{r}}{e}_3 = i_2 \cdot \overset{\mathbf{r}}{n}_1 \otimes \overset{\mathbf{r}}{n}_2 \quad (6)$$

$$\overset{\mathbf{r}}{e}_4 = i_1 \cdot i_2 \cdot \overset{\mathbf{r}}{n}_2 \otimes \overset{\mathbf{r}}{n}_2 \quad (7)$$

New hypercomplex numbers i_1 and i_2 are introduced here :

$$i_1 \cdot i_1 = -1 \quad (8) \quad i_2 \cdot i_2 = -1 \quad (9) \quad i_1 \cdot i_2 = -i_2 \cdot i_1 \quad (10)$$

$$i \cdot i = -1 \quad (11) \quad i \cdot i_1 = i_1 \cdot i \quad (12) \quad i \cdot i_2 = i_2 \cdot i \quad (13)$$

In order to $\overset{\mathbf{r}}{e}_\mu$ consist quaternion algebra, $\overset{\mathbf{r}}{n}_\alpha$ must satisfy such algebra :

$$[\overset{\mathbf{r}}{n}_1 \times \overset{\mathbf{r}}{n}_1] = \overset{\mathbf{r}}{n}_1 \quad (14) \quad [\overset{\mathbf{r}}{n}_1 \times \overset{\mathbf{r}}{n}_2] = \overset{\mathbf{r}}{n}_2 \quad (15)$$

$$[\overset{\mathbf{r}}{n}_2 \times \overset{\mathbf{r}}{n}_1] = \overset{\mathbf{r}}{n}_2 \quad (16) \quad [\overset{\mathbf{r}}{n}_2 \times \overset{\mathbf{r}}{n}_2] = \overset{\mathbf{r}}{n}_1 \quad (17)$$

And the same with the scalar product :

$$(\overset{\mathbf{r}}{n}_1, \overset{\mathbf{r}}{n}_1) = 1 \quad (18) \quad (\overset{\mathbf{r}}{n}_1, \overset{\mathbf{r}}{n}_2) = 0 \quad (19)$$

$$(\overset{\mathbf{r}}{n}_2, \overset{\mathbf{r}}{n}_1) = 0 \quad (20) \quad (\overset{\mathbf{r}}{n}_2, \overset{\mathbf{r}}{n}_2) = 1 \quad (21)$$

$$(\overset{\mathbf{r}}{n}_\alpha, \overset{\mathbf{r}}{n}_\beta) = q_{\alpha\beta} \quad (22) \quad [\overset{\mathbf{r}}{n}_\alpha \times \overset{\mathbf{r}}{n}_\beta] = \overset{\mathbf{r}}{n}_\gamma \cdot f^\gamma_{\alpha\beta} \quad (23)$$

So we have for V : $q_{\alpha\beta}$ - metric tensor, $f^\gamma_{\alpha\beta}$ - algebraic tensor.

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