

D(H)-Cluster Langevin Code and Some Calculated Results

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[Abstract]

A PC code based on the quantum mechanical Langevin equation to simulate dynamic motion of deuterium (or hydrogen) cluster with three dimensional symmetry has been developed for studying very fast condensation or oscillation behavior in time-step of 0.001 as (1.0E-21 second) for overall time interval of several fs to 500 fs. Some numerical results are typically shown for two cases of condensation behavior; 1) reaching to ground state oscillations as for D(H)₂⁺ ion molecule, dμd muonic molecule, 3D⁺ ionic molecule, 6D/OSC and others, and 2) making fast collapse to get in the strong/weak nuclear interaction range of d-d (or p-p) inter-nuclear distance as for 4D(H)/TSC, 6D(H)/Rhombic-dodecahedron, 8D(H)/Rhombic-dodecahedron and 20D(H)/Rhombic-triacontahedron.

Keywords: PC code, D(H)-cluster dynamics, ground state oscillation, fast collapse, 4D(H)/TSC, 6D(H)-Rhombic-dodecahedron, larger clusters, nuclear interaction, simulation of cold fusion

1. Introduction

Time dependent motion of deuterium (or protium) cluster is calculable by a computer code based on the quantum-mechanical Langevin equation [1, 2]. Especially the dynamics analyses of a three body d-e-d or p-e-p, a 5-body d-e-d-e-d or p-e-p-e-p (namely D₃⁺ or H₃⁺ ionic molecule) and a 8-body d-e-d-e-d-e-d-e (4D) or p-e-p-e-p-e-p-e (4H) cluster under the Platonic symmetry (TSC: tetrahedral symmetric condensate) are important to understand the underlying mechanisms of condensed matter nuclear reactions aka cold fusion [3]. The dynamic analysis is quite applicable to investigate time-dependent behavior of the three body system of d-muon-d after sticking of muon onto a d-e-d molecule. The QM Langevin method is also applicable for much larger clusters under the Platonic symmetry, such as 6D(H), 8D(H), 12D(H) and 20D(H) clusters.

We have made a generalized D(H)-Cluster Langevin Code revised from the original crude one [1, 2]. We show some typical calculations of 1) dynamic motion going to the

ground state, for systems having ground state eigen-values (namely steady molecules), 2) collapsing motion going to several-tens or smaller fm size transitory condensates which may cause very enhanced multi-body nuclear interactions by strong (for D) or weak (for H) boson exchange (namely multi-body fusion), and 3) oscillation motion of EQPET clusters with electron Cooper pair and quadruplet [1, 2].

A muonic d- μ -d system converged in 8.3 fs to its ground state with the inter-nuclear d-d distance of 790 fm (0.79 pm) after approximately 80 oscillations from the time when a muon stuck onto a d-e-d state with 138 pm d-d distance of the electronic D₂⁺ molecule ground state. A 4D(H)/TSC cluster collapses to the “nuclear interaction size” (20 fm to 4 fm) in 1-4 fs depending on the adoption of different type of trapping potential functions (Vs2 or Vs1 potential, for instance), always. The Rhombic dodecahedron of 6D(2-) and the Rhombic triacontahedron 20D(8+) may collapse into the nuclear interaction size. Some other examples are also shown. A list of BASIC program of the Cluster Langevin code is given in Appendix.

2. Basic Methodology for QM-Langevin Calculation

The idea is based on the known QM electron wave-functions for d-e-d and d-e-e-d systems to form 3 dimensional volumetric symmetry to attain stable force-balance structure. These 3 dimensional symmetry systems are an elongated di-cone and ‘regular’ di-cone, respectively for 2D⁺ and D₂ molecule [2]. The ground state QM electron wave function for a d-e-d (or p-e-p) three body system is a linearly combined two 1S wave functions [2, 4], where each 1S wave function is for each D(H)-atom ground state of the d-e-d (or p-e-p) system. In [Fig.1](#), the feature of treatment for a d-e-d system is illustrated to apply to a QM Langevin equation for calculating its dynamic motion. The ground state orbit of electron QM center is a circular rotating one with $R_e = \text{Bohr radius}$ (52.9 pm) around the mid-point of inter-nuclear d-d distance. The electron kinetic energy of d-e-d (or p-e-p) ground state is 13.6 eV that is the same value with 13.6 eV of electron kinetic energy of a D(H)-atom ground state. The inter-nuclear distance R_{dd} (or R_{pp}) of d-e-d (or p-e-p) ground state is 138 pm. The Coulombic trapping potential Vs1(1,1) of the d-e-d (or p-e-p) three body system is given in Appendix of Reference-[3] and also in Reference [5] and graphic view is shown in [Fig.2](#). In the previous calculations [1, 2] for 4D/TSC, we have used the Vs2(1,1) potential for D₂ molecule or its approximate function Vs1(2,2) for a bosonized electron pair. In this paper, we will use Vs1(1,1) potential for every surface (regular triangle of d-d-d or p-p-p geometry) of various kind

of polyhedrons, as a unified potential component of polyhedral D(H)-cluster as 3D(H), 4D(H), 6D(H), 8D(H), 12D(H) and 20D(H) systems.

D₂⁺ (dde) Langevin Equation

$$m_d \frac{d^2 R_{dd}}{dt^2} = -2 \frac{e^2}{R_{de}^2} + \frac{e^2}{R_{dd}^2} + \frac{m_e v_e^2}{R_e} - \frac{\partial V_s(R_{dd}; 1, 1)}{\partial R_{dd}} + f(t)$$

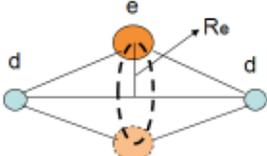
$$-e^2 \left\langle \frac{2}{R_{de}^2} - \frac{1}{R_{dd}^2} \right\rangle + \left\langle \frac{m_e v_e^2}{R_e} \right\rangle = 0$$

<R_{dd}> = 138 pm

<R_e> = 52.9 pm

Elongated Di-Cone

Electron Wave Function:
Linear combination of 1S wave function



$$m_d \frac{d^2 \langle R_{dd} \rangle}{dt^2} = - \frac{\partial V_s(R_{dd}; 1, 1)}{\partial \langle R_{dd} \rangle}$$

<R_{dd}>(∞) = R_{gs} = 138 pm

Electron KE = 13.6 eV



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Fig.1: Treatment of dynamic motion of a d-e-d three body system by a QM Langevin equation.

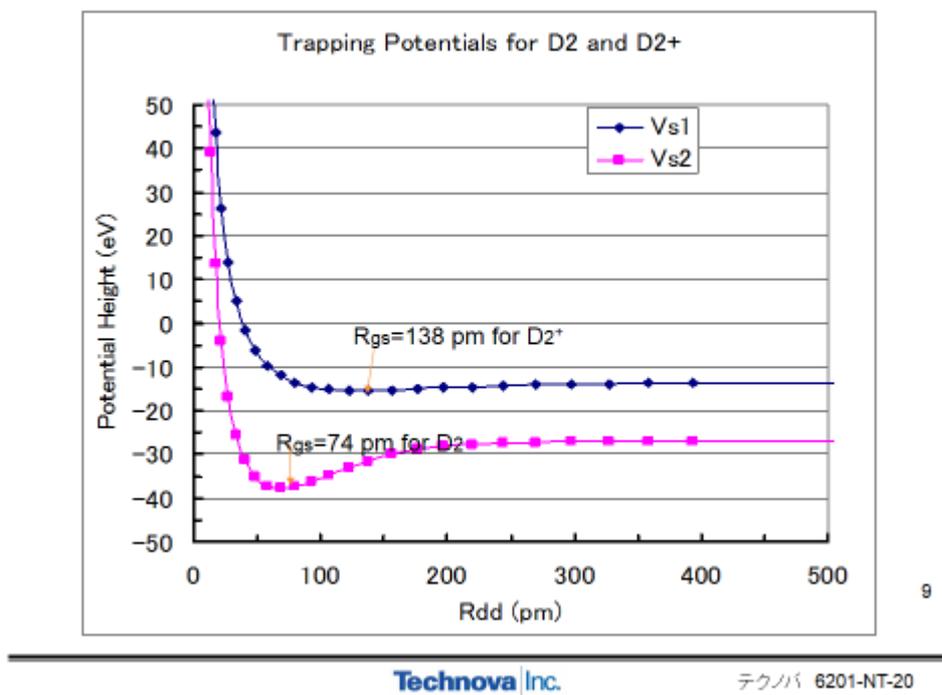


Fig.2: Coulombic trapping potential of a d-e-d system (D₂⁺), compared with D₂ one.

In this paper, all mathematical equations are only described in slide-figures. Derivations of equations for the QM Langevin method are fully given in References [2, 3]. This style of paper is chosen for aiming at easier explanation of physical processes employed for making program and computations, without getting into detail of mathematics derivations.

The case of TSC is special because of double octahedral symmetry for electron wave-function and deuteron wave-function of the TS (tetrahedral symmetry) configuration. This condition makes the usage of $Vs2$ potential (derived from a combined 1S product-wave-functions [4, 5]) possible for the confinement force by electrons which have much larger de Broglie wave-length than deuteron wave length. In this paper, we employ a new rule for evaluating the friction term by electron QM-clouds in the QM-Langevin equation, that is the adoption of $Vs1(1,1)$ potential always for a unit of d-d-d or p-p-p regular triangle surface configuration. We think, we have obtained similar results between the old rule (ACSLENR Vol.1 paper for 4D/TSC) and the new rule ($Nf=4$, $Ne=6$, $Vs1$ for 4D/TSC): the condensation time to collapse was 1.4fs and 3.6fs from 74pm to 20fm, respectively for the old and the new rule: So we may apply both rules for 4D/TSC.

When a 4D/TSC gets into the collapse region with less than about 20 fm d-d distance, strong nuclear interaction between 4 deuterons work significantly to form ${}^8\text{Be}^*$ intermediate compound nucleus by the 4D simultaneous fusion [2, 3] and time-dependent fusion rates have been calculated using the Fermi's golden rule with estimated Coulomb barrier penetration factors (time-dependent) by the HMEQPET method [2, 3]. In the case of 4H/TSC dynamic condensation, it can get into extremely collapsed state of TSC with very small inter-nuclear p-p distances as small as $R_{pp}=2\text{fm}$, and electron capture with a proton would induce weak-strong fusion reaction to form ${}^4\text{Li}^*$ intermediate compound state [1, 6, 7]. Nucleon halo models have been developed to study the final state interactions and ashes (nuclear products) [6, 7]. Major nuclear ashes are ${}^4\text{He}$ (2.0E+11 per joule) by the 4D/TSC fusion and ${}^3\text{He}$ and D (ca. 1.0E+12 per joule) by the 4H/TSC WS fusion, without significant hard radiations but low energy photons (BOLEP) and very weak secondary gamma-rays, respectively.

For other combinations for 3D, 6D, 8D, 12D, 20D and so forth, we do not have the double symmetry as that of 4D/TSC. (The situation is same for any H-cluster.) So AT's idea (ACSLENRSB Vol.2 [3]) was to learn the QM electron behavior of 3D+ stable ionic molecule, for which we have experimental confirmation on 3D+ stable ion in plasma and some solutions of Schroedinger QM calculations were given [2]. The idea is to apply the confinement force of $Vs1(1,1)$ potential for a d-e-d (or p-e-p) three body

QM system, for a basic component per a regular triangle face of total confining potential of combined D(H) polyhedral system having many faces and edges.

It is an approximate way of QM for such complicated systems as 3D+, 6D(2-), 8D(2+), 12D(8-), 20D(8+), and so on. We need careful study by cross-checking so far if the approximate approach is rational.

Because of much larger QM wave length of electrons than d(p)'s, we need a free 'rotation space' of electron QM-orbit (to satisfy HUP: Heisenberg Uncertainty Principle) for 'expectation position' for every d-d (or p-p) dipole edge. The d-e-d (2D+) system makes stable (ground state) force-balanced system as a di-cone in 3-dimensional way: the force balance holds between the central attraction force (centripetal force to the center-of-mass point) and the centrifugal force by electron rotation (circular orbit) of expectation position around the center-of-mass point (mid-point of d-d "dipole" edge). Because of 2 electrons in 3D+ system, the circular rotation orbit can be shared for 3 d-d edges in 3-dimensional symmetric way to take balance within HUP (or electron de Broglie wave-length domain). It means, the balance is not possible in the view of classical mechanics, because only two d-d edges can share electron rotation simultaneously and the third deuteron will be kicked outside. **The HUP helps the balance for simultaneous electron sharing for 3 d-d edges and thus 3D+ can be stable quantum-mechanically.**

If we consider a 3D++ case, the regular triangle of 3d's cannot be sustained while electron is rotating around a d-d edge and therefore the third deuteron shall apart (by d-d repulsion force) from the system. Consequently, 3D++ breaks up to 2D+ (d-e-d) and deuteron. The helping force by HUP will not be enough. (We need more study here.)

Then, what will happen for 6D(2-) 3-dimensional symmetric system by 'orthogonal' combination of deuteron-octahedron and electron-cube (Rhombic Dodecahedron)?

This is our challenging problem. We think the solution by our new rule (8Nf and 12Ne) may be right. A triangle surface of deuteron-octahedron has no 'back-side' surface for an 'paired electrons' but has for an electron, so that 8 Nf will be OK as every d-d edge has sharing d-e-d type rotation orbit simultaneously to avoid break-up.

However, we are assuming that the same partial QM electron wave-function as that of the d-e-d system, namely Vs1(1,1) confining potential for a d-d pair, holds for every electron 'QM-center' on the triangle surface. The validity of this assumption shall be further studied.

For more complicated systems as 8D(2+), 12D(8-), 20D(8+), and their relative states as 'neutral' like 6D, 8D, 12D, 20D having 'fractional' net-charge of electron QM-center at a face, we do not know exactly whether the analogy of partial Vs1(1,1) friction may

hold or not.

The formulation of QM-Langevin equation for many-body polyhedral system has been derived in Reference [2]. The original form for 4D/TSC as used in Reference [3] is shown in Fig.3 with physical meaning of balance of forces between the Coulombic centripetal force, the friction by QM electron cloud and the deviation force from pure Platonic symmetry. The form of cluster trapping potential is shown accordingly.

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TSC Langevin Equation:

$$6m_d \frac{d^2 \langle R_{dd} \rangle}{dt^2} = - \frac{11.85}{\langle R_{dd} \rangle^2} - 6 \frac{\partial V_s(\langle R_{dd} \rangle; m, Z)}{\partial \langle R_{dd} \rangle} + 6.6 \left\langle \frac{(R' - R_{dd})^2}{R_{dd}^4} \right\rangle$$

Coulombic Centripetal Force Friction By electron Cloud Deviation From Platonic symmetry

TSC Trapping Potential:

$$V_{tsc}(R'; R_{dd}(t)) = - \frac{11.85}{R_{dd}(t)} + 6V_s(R_{dd}(t); m, Z) + 2.2 \frac{|R' - R_{dd}(t)|^3}{[R_{dd}(t)]^4}$$

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Fig.3: The QM-Langevin equation and trapping potential, originally used for Ref.[3] for 4D/TSC condensation motion.

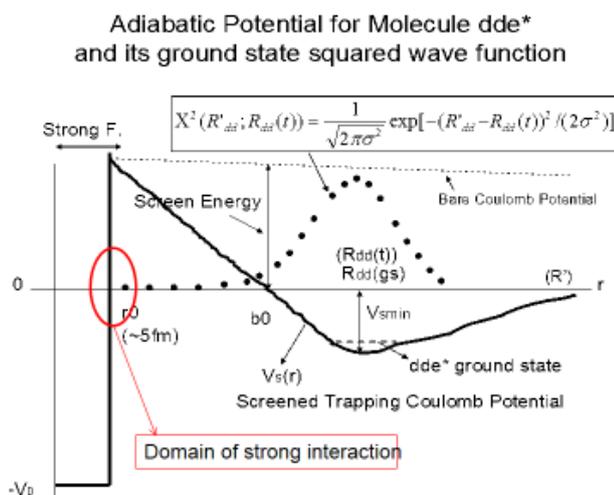


Fig.4: A d-d pair wave function, time-dependent, is approximated with Gaussian wave function

Time dependent d-d pair (for nearest d and d of polyhedron) wave function is approximated with a Gaussian wave function, adiabatically which pseudo-eigenvalue can be estimated by the HMEQPET method [2, 3]. The QM weight (barrier factor) of d-d wave function to getting into the range of strong interaction (See Fig.4) is also estimated by the WKB approximation in the HMEQPET method.

Now, our general formulas of new QM-Langevin code is shown in Fig.5 for many body polyhedral system.

QM Average of Langevin Equation for D(H) Cluster

$$N_e m_d \frac{d^2 R}{dt^2} = -\frac{k}{R^2} - N_f \frac{\partial V_s}{\partial R} + f(t)$$

Ne: Number of d-d edges

$$N_e m_d \left\langle \Psi(R, R') \left| \frac{d^2 R}{dt^2} \right| \Psi(R, R') \right\rangle = - \left\langle \Psi(R, R') \left| \frac{k}{R^2} \right| \Psi(R, R') \right\rangle$$

$$- N_f \left\langle \Psi(R, R') \left| \frac{\partial V_s}{\partial R} \right| \Psi(R, R') \right\rangle + \left\langle \Psi(R, R') | f(t) | \Psi(R, R') \right\rangle$$

$$\Psi(R, R') = \frac{1}{\sqrt{2\pi\sigma^2}} \exp(-(R'-R)^2 / (2\sigma^2))$$

Gaussian Wave Function

$$N_e m_d \frac{d^2 \langle R \rangle}{dt^2} = -\frac{k}{R^2} - N_f \frac{\partial V_s}{\partial R} + \langle f(t) \rangle$$

Equation for Expectation Value ³⁷

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Fig.5: general formulas of QM-Langevin method for Platonic polyhedral

3. Some Calculated Results

A PC code as given in Appendix has been developed using Basic programming. We show some typical results and discussions in the following for 1) D(H)-clusters getting to stable ground state oscillations, 2) D(H)-clusters getting to collapses in nuclear strong/weak interaction ranges, and 3) virtual EQPET molecules with bosonized electrons.

3.1 Results for Stable D(H)-Clusters

The 3D(H)+ ionic molecule exists stably in solar plasma and accelerator ion-source plasma. The solution of the 5-body Schroedinger equation [8] has been given and

discussed in our previous paper comparing with our QM-Langevin solution, in good agreement [3]. The polyhedral structure of the 5-body d-e-d-e-d system is illustrated in Fig.6.

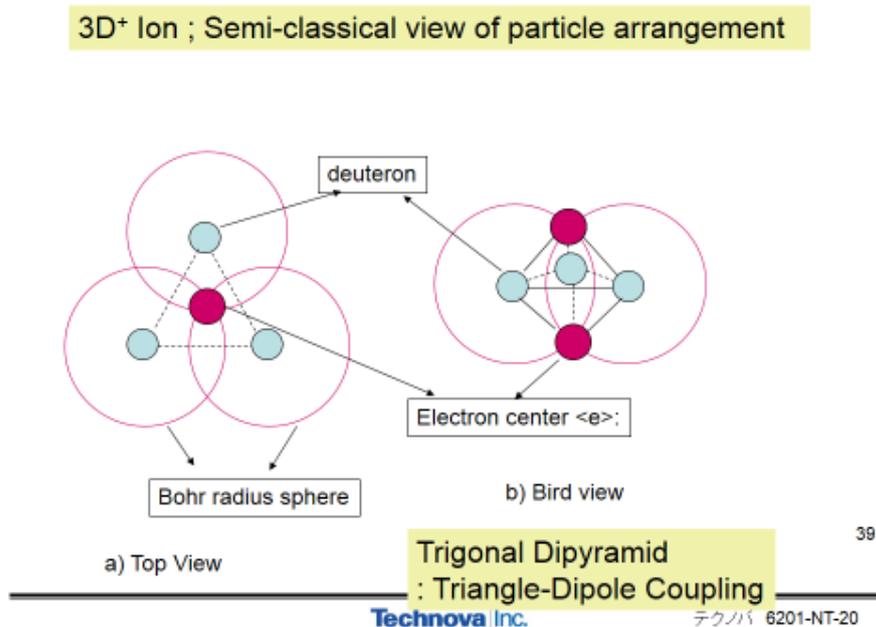


Fig.6: The polyhedral composition of 3D(H)⁺ ionic molecule

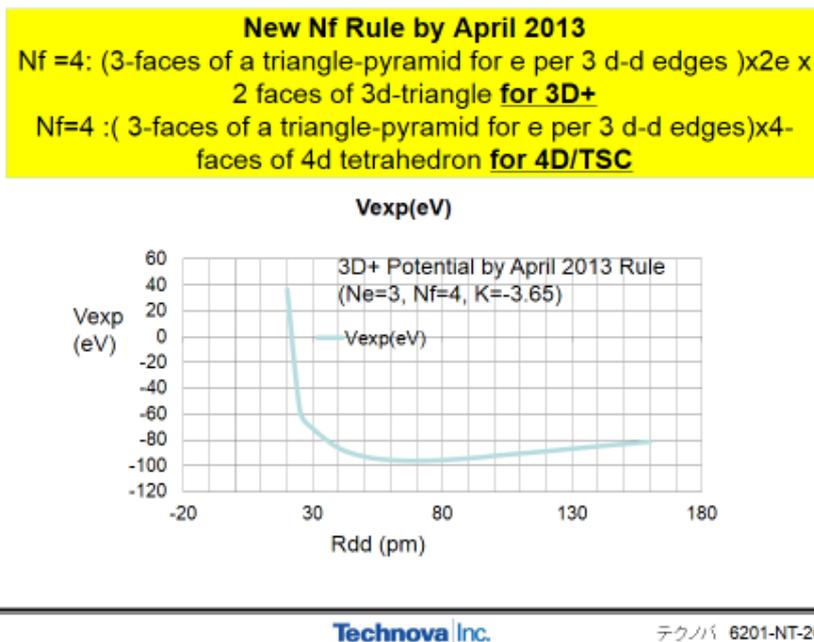
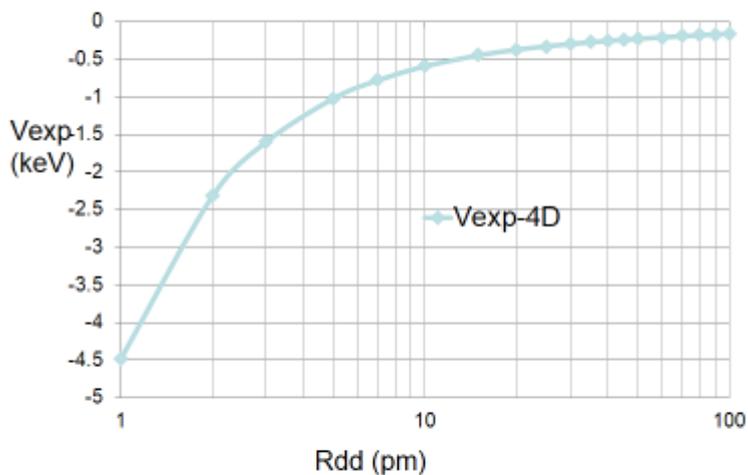


Fig.7: Trapping potential of 3D(H)⁺ ionic molecule, given by our new rule for QM-Langevin equation

4D/TS Cluster Trapping Potentials (expectation values) by April-2013 Rule



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Fig.8: Trapping potential of 4D(H)/TSC by our new rule with Vs1(1,1)

Table-1: Three key parameters for QM-Langevin calculations for D(H)-clusters

Parameters for Langevin Cal.: for Electron Friction of Vs1(1,1)

Cluster	k value (keVpm)	Ne	Nf
2D+: d-e-d	0	1	1
3D+	3.65	3	4
4D/TS	11.85	6	4
6D/RD	18.45	12	8
8D/RD	18.45	12	6
12D/RT	15.51	30	20
20D/RT	19.11	30	12

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Using our new rule based on components of triangle faces with $V_{s1}(1,1)$ trapping potential, the number of faces $N_f = 4$: (3-faces of a triangle-pyramid for e per 3 d-d edges) $\times 2e \times 2$ faces of 3d-triangle for $3D^+$: is concluded. Its trapping potential is shown in [Fig.7](#). The $3D(H)^+$ polyhedron has three d-d edges ($N_e = 3$). Interestingly, the $4D(H)/TSC$ has $N_f = 4$ (and $N_e = 6$) with its regular triangle surfaces, but the trapping potential shape is quite different, namely having no well-type minimum as shown in [Fig.8](#). In [Table-1](#), three key parameters, namely k-value of centripetal force, number of edges N_e and number of faces N_f are given for various polyhedrons. D. Rocha has calculated k-values for various configuration of polyhedral, using an excel sheet calculation by summing up all components of attractive and repulsive Coulombic potentials for possible d-d, d-e and e-e distances between QM charge centers.

The initial two oscillations of $3D^+$ cluster by the present D(H)-cluster Langevin code is shown in [Fig.9](#).

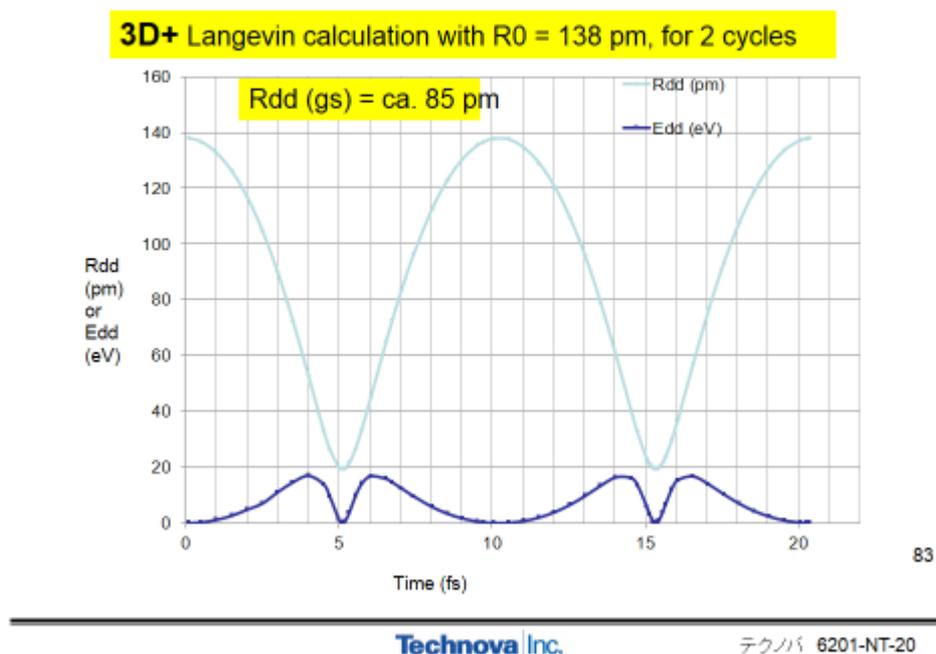


Fig.9: Initial two cycles of oscillation for $3D^+$ ionic molecule

Initial two cycles of simulated oscillation for $3D^+$ cluster is shown in [Fig.9](#). It has the ground state with $R_{dd}(gs) = 85$ pm which is in good agreement with the result of Schrodinger equation analysis [8]. When starting calculation with $R_0 = 138$ pm, complete steady oscillation with same amplitude was attained after about 500 oscillations. Changing R_0 value around 138 pm, we have found almost the same

converging oscillation mode that is regarded as ground state.

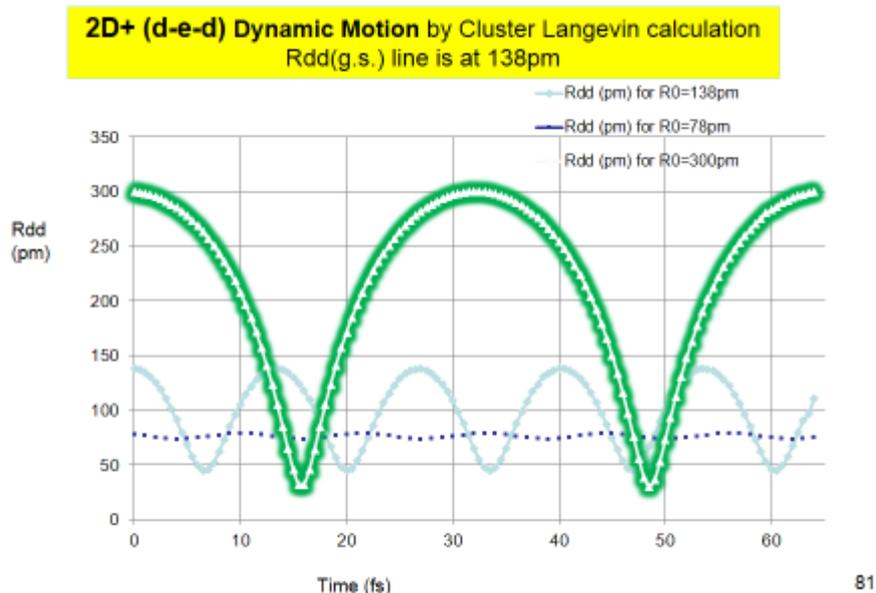


Fig.10: Initial two cycles of oscillation for 3D+ cluster started with R = 300 pm

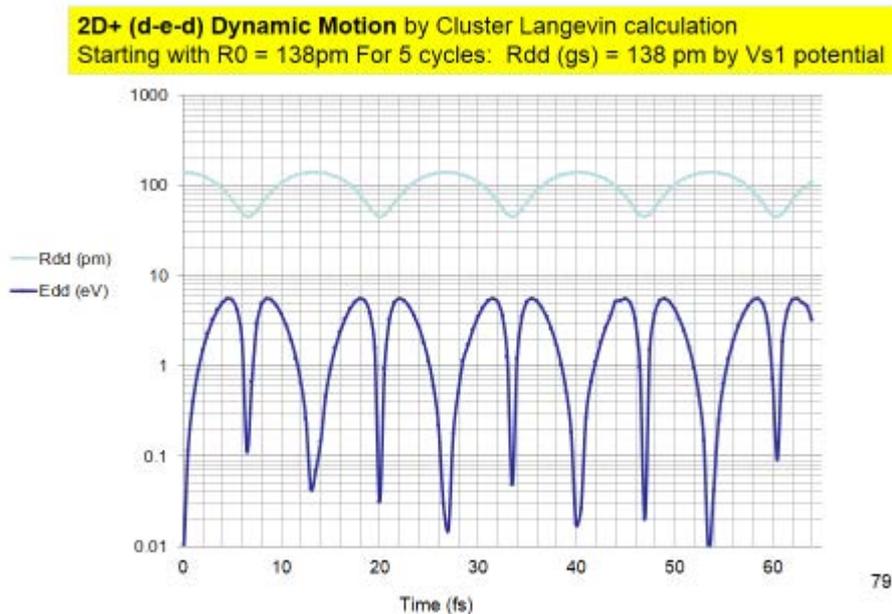


Fig.11: Initial 5 cycles of oscillation motion for 2D+(d-e-d) ionic molecule, started with R0 = 138 pm

The simplest cluster in the present paper is a d-e-d three body system. The first two cycles by starting with $R_0 = 300$ pm is shown in Fig.10. Comparison is made with starting conditions of $R_0 = 138$ pm and 78 pm. By random sampling of starting conditions we obtain corresponding oscillation curves. The ensemble average of curves will give the ground state solution. We know the ground state $R_{dd}(gs) = 138$ pm, as already discussed in Fig.1. Initial 5 cycles of oscillating motion of $2D^+$ (d-e-d) are plotted in Fig.11 for variation of $R_{dd}(t)$ and relative kinetic energy of d-d pair.

The next interesting three body system is a muonic d-d molecule. When a muon sticks to a D_2 molecule, how does the time-dependent motion of $d\mu d$ system look like? We used trapping potential of $V_{s1}(50,2)$ that is known to be almost equivalent to $V_{s1}(207,1)$ [3]. Using the starting value $R_0 = 74$ pm, simulation by the present code has given an interesting first oscillation cycle curves as shown in Fig.12. After about 2.7 fs, there happens very sharp valley of $R_{dd}(t)$ curve and local maximum of relative d-d kinetic energy curve, the extended figure of which is drawn in Fig.13. The local minimum d-d distance there is $R_{dd} = 0.2$ pm and the local maximum relative d-d kinetic energy is ca. 3.0 keV. Next local maximum d-d distance after the first oscillation cycle is $R_{dd} =$ ca. 52 pm which is smaller than the starting value of 74 pm; namely the system is condensing.

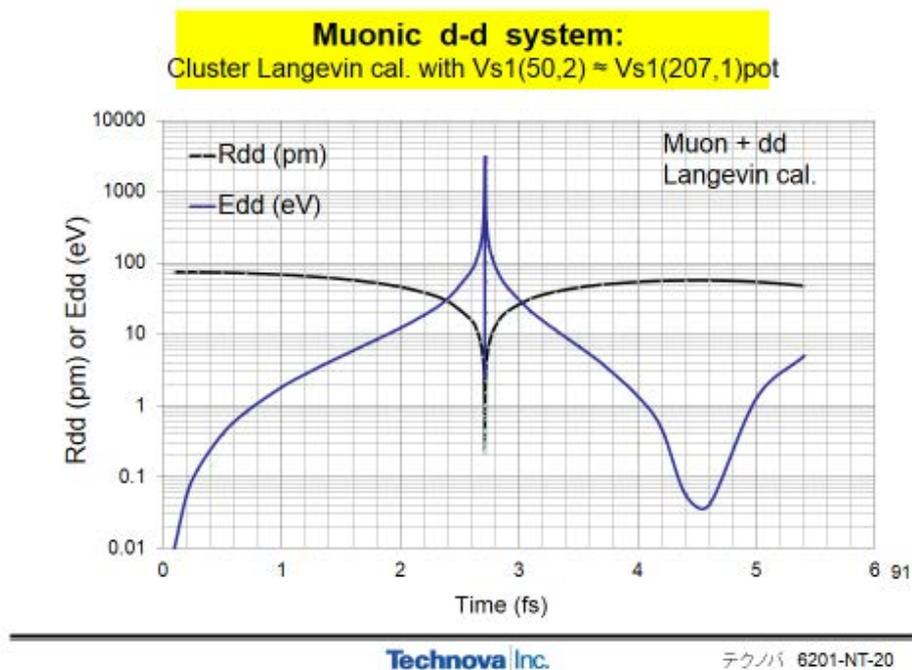


Fig.12: The initial one cycle of oscillation motion of muonic d-d molecule after sticking of muon onto a D_2 molecule.

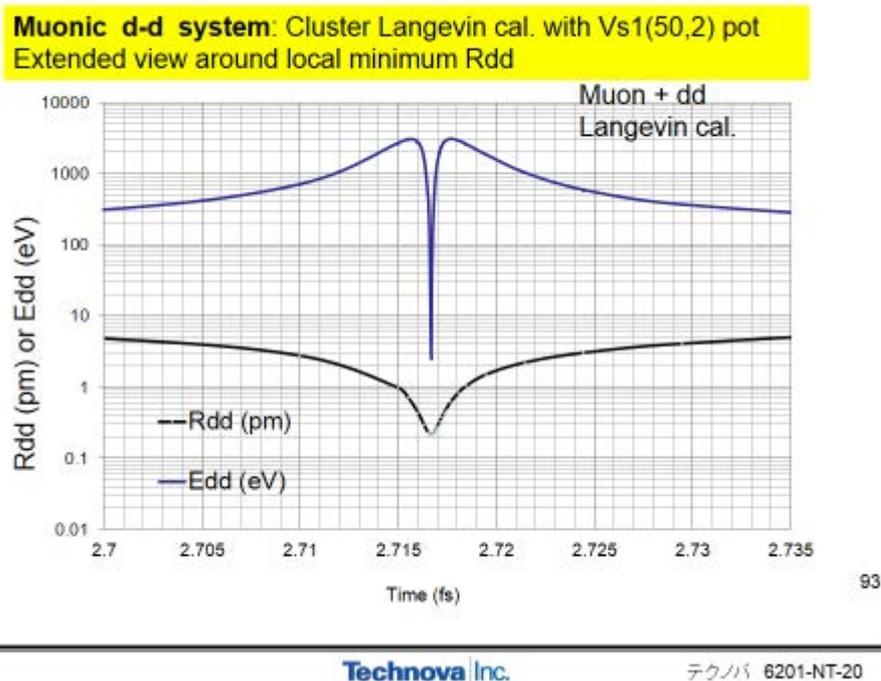


Fig. 13: Extended graph of Fig.12, for time interval around 2.7 fs

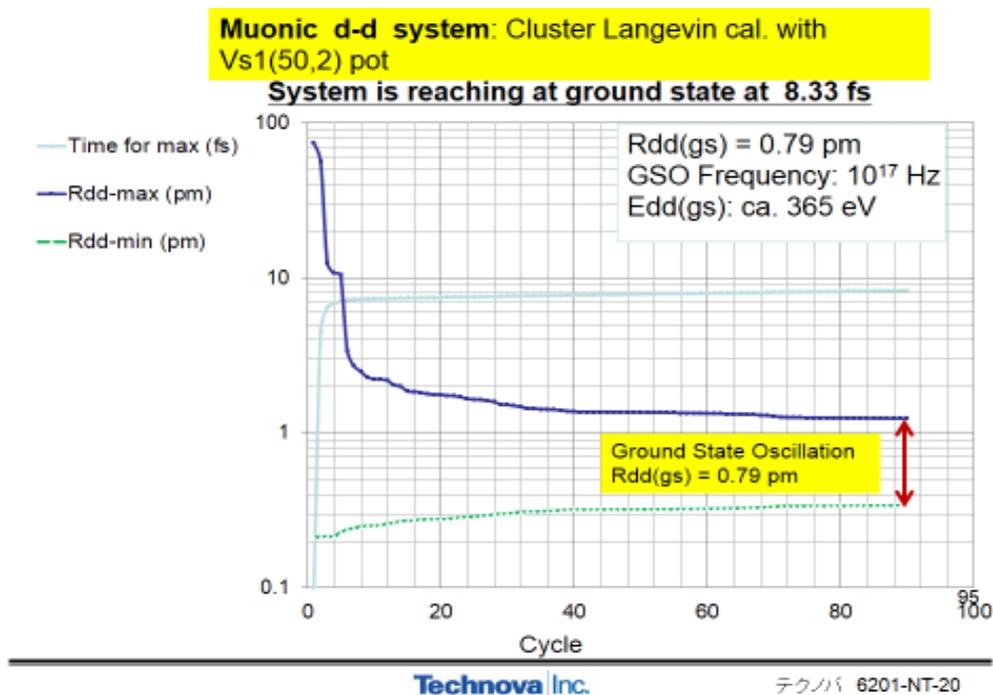


Fig.14: Condensing behavior of muonic d-d molecule after sticking of muon onto D₂ molecule. Changing starting R0 values around 100-50 pm does not effect on the converging 'ground' state.

For succeeding cycles of simulation, local maximum values of $R_{dd}(t)$ decrease and local minimum values of $R_{dd}(t)$ slowly increases as shown in [Fig.14](#). After about 80 cycles of oscillation, it looks converging to an asymptotic oscillation that is regarded as the ground state of muonic d-d molecule with $R_{dd}(gs) = 0.79\text{pm}$. The ground state oscillation frequency is ca. $1.0\text{E}+17$ Hz and the ground state relative d-d kinetic energy is estimated as ca. 365 eV which is a double score of the previously estimated value 180 eV by the QM variational calculation with Gaussian wave function ($R_{dd}(gs)$ was 0.805 pm in that case) [9]. In the QM variational calculation [3, 9], we used a reduced mass for a d-d pair to be 1.0, while the mass of d in the present QM Langevin code is 2.0. Therefore the double score is understandable as the difference in conversion from the center-of-mass system to the laboratory system.

Now we come back to a known standard case of D_2 molecule. We know the mathematical functions [4, 5] in $V_{s2}(1,1)$ potential for trapping D_2 molecule have difficulty in numerical calculation of its derivative (field-force form) to apply to QM Langevin calculation. However, we find that $V_{s1}(1,1.41)$ potential has very close curve to that of $V_{s2}(1,1)$ as compared in [Fig.15](#). Therefore, we can simulate an approximate dynamic motion of D_2 molecule by the present code with use of $V_{s1}(1, 1.41)$ potential. The initial two cycles of oscillation motion are drawn in [Fig.16](#).

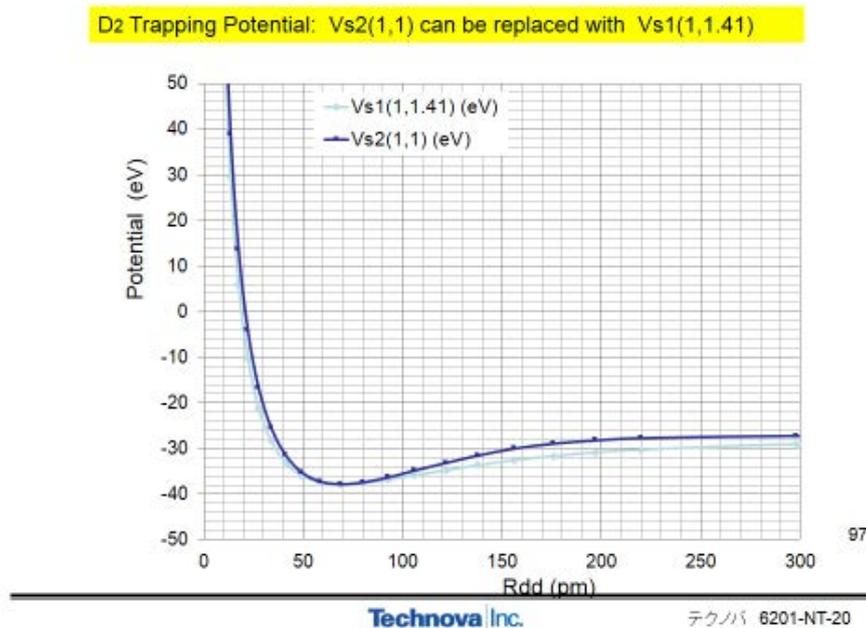


Fig.15: $V_{s1}(1, 1.41)$ potential behaves closely to that of $V_{s2}(1,1)$ potential of D_2 molecule

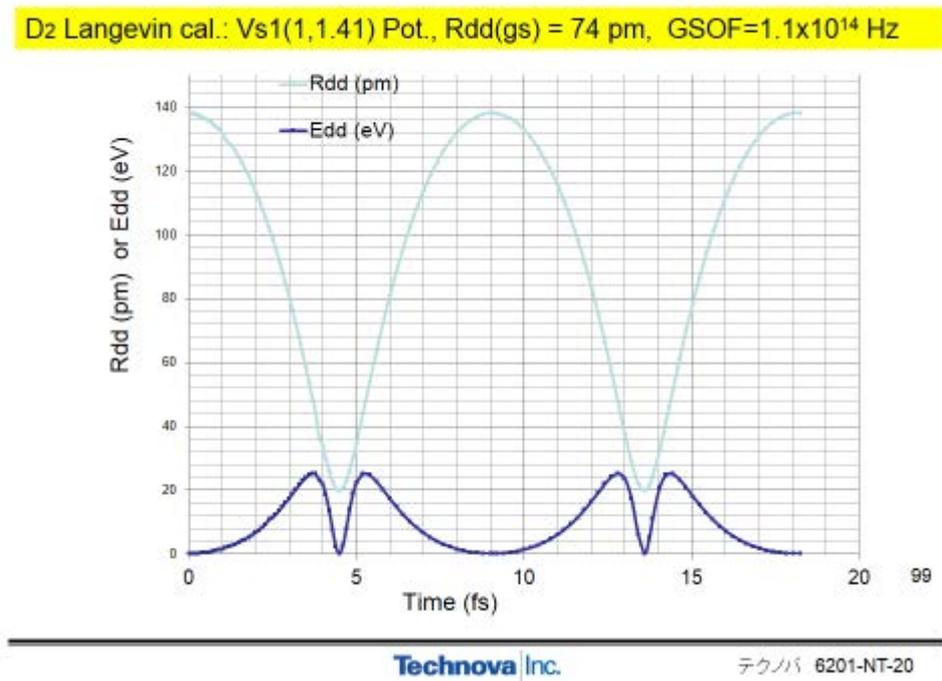


Fig.16: Initial two cycles of oscillation motion for D₂ molecule

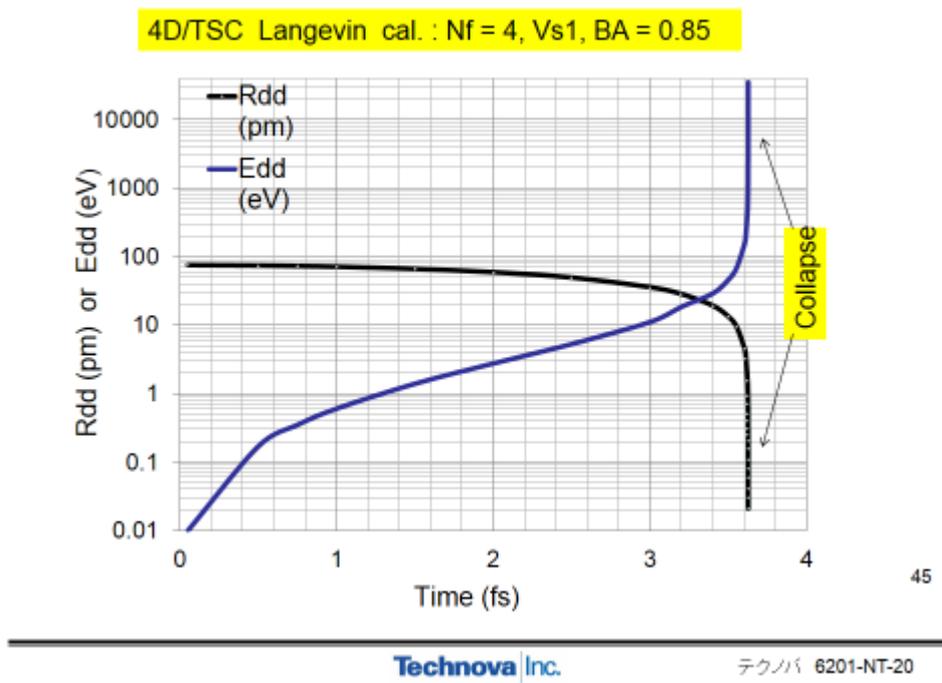


Fig.17: Condensation and collapse of 4D/TSC as simulated by the present code with the new rule for face trapping potential component

3.2 Condensation Collapse of D(H)-Cluster Polyhedron

Now we argue on the results for larger D(H)-clusters than 3D under 3 dimensional symmetry (Platonic symmetry). We have already given three key parameters for various D(H)-clusters in [Table-1](#). The result for 4D/TSC by the new rule of usage of Vs1(1,1) potential for its unit face of triangle d-d-d is shown in [Fig. 17](#). The 4D-cluster collapses at around 3.6 fs after the TS formation, while it was after 1.4 fs by using the old rule in References [2, 3] which used Vs1(2,2) potential of ‘bosonized electron pair’ on d-e-e-d surface of cubic TSC configuration.

[Fig.18](#) illustrates the feature of 6D(2-) Rhombic dodecahedron. It has 12 d-d edges (Ne = 12) and 8 triangle d-d-d faces (Nf = 8). The value of k is estimated by D. Rocha to be 18.45 keVpm. The results of simulation by the present code are shown in [Figs. 19 and 20](#). It has given collapse after ca. 4.1 fs. Near collapsing time-interval, we had to use very fine time meshes as 0.000001 fs (1.0E-21 s) as shown in [Fig.20](#). Such very small time meshes would have not been tried in the past molecular dynamics codes conventionally available: usually as (1.0E-18 s) would have been the smallest time mesh as far as tried. Therefore, usual molecular dynamics codes (or static Schroedinger equation analyses) should have missed the collapsing states of D(H)-clusters which have no static ground state eigen-values but transient condensing and collapse evolution.

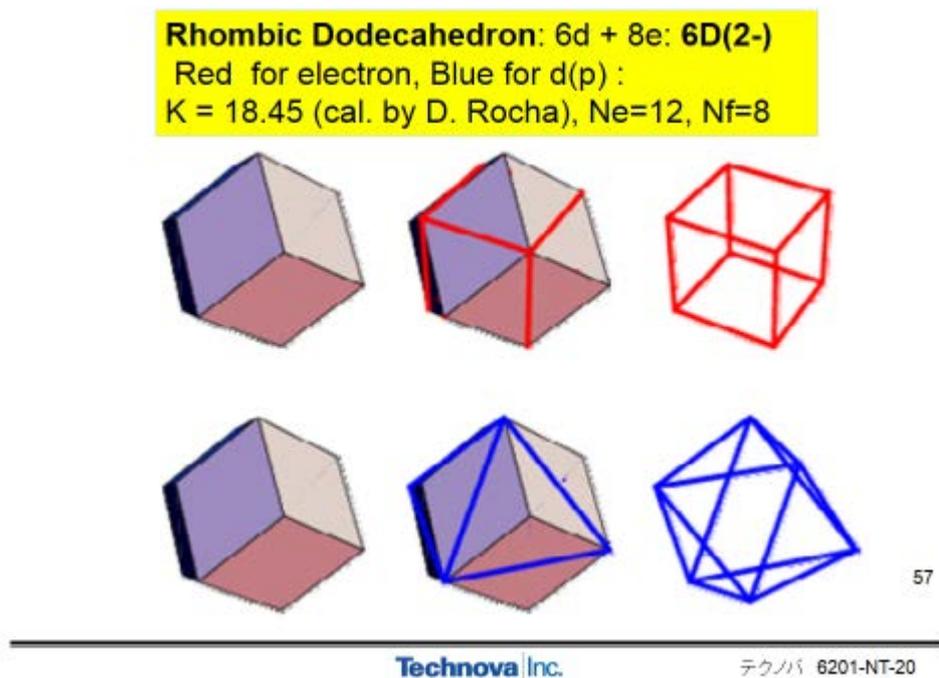


Fig.18: Rhombic dodecahedron is the polyhedron of 6D(2-)-cluster

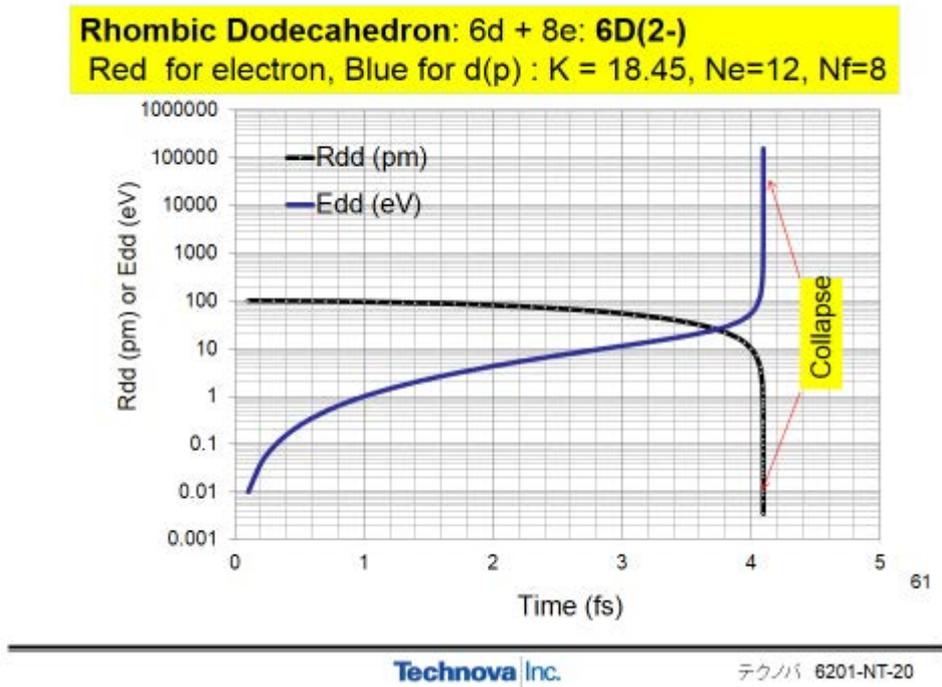


Fig.19: Simulated results of condensation motion of 6D(2-) Rhombic dodecahedron, getting to collapse after ca. 4.1 fs and maybe inducing 6D multi-body fusion

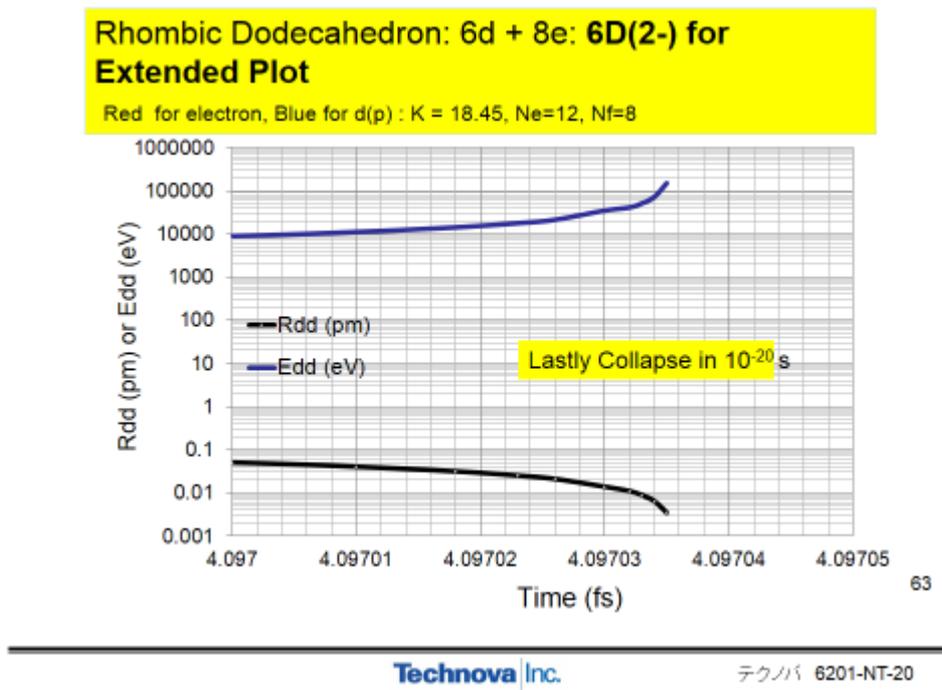


Fig.20: Extended graph of condensing evolution before collapse at around 4.097035 fs

When we exchange QM centers between electrons (red) and deuterons (blue) in Fig.18, we get 8D(2+) cluster of Rhombic dodecahedron. The result of simulation by the present code is shown in Fig.21. This 8D(2+) cluster may also collapse at ca. 3 fs after the cluster polyhedron formation.

Example for more larger D(H)-cluster is for the case of 20D(8+) cluster of Rhombic triacontahedron as its geometrical feature is illustrated in Fig.22. This 20D(8+) cluster may also collapse at around 6.5 fs after the cluster formation. What kind of strong interactions (so many body fusion?) will happen is the remained problem of nuclear physics consideration.

When we exchange QM centers between electrons (red) and deuterons (blue) of Fig.22, we get 12D(8-) cluster of Rhombic triacontahedron. The simulation calculation for the system, as shown in Fig.24, does not make collapse but converges to steady oscillation of ground state, interestingly. We tried to find that some other polyhedral cluster as 6D(2-)/OSC does not collapse either.

To summarize the results of simulation for various clusters, in the view of collapse and possible multi-body nuclear interactions, Table-2 is conclusively obtained.

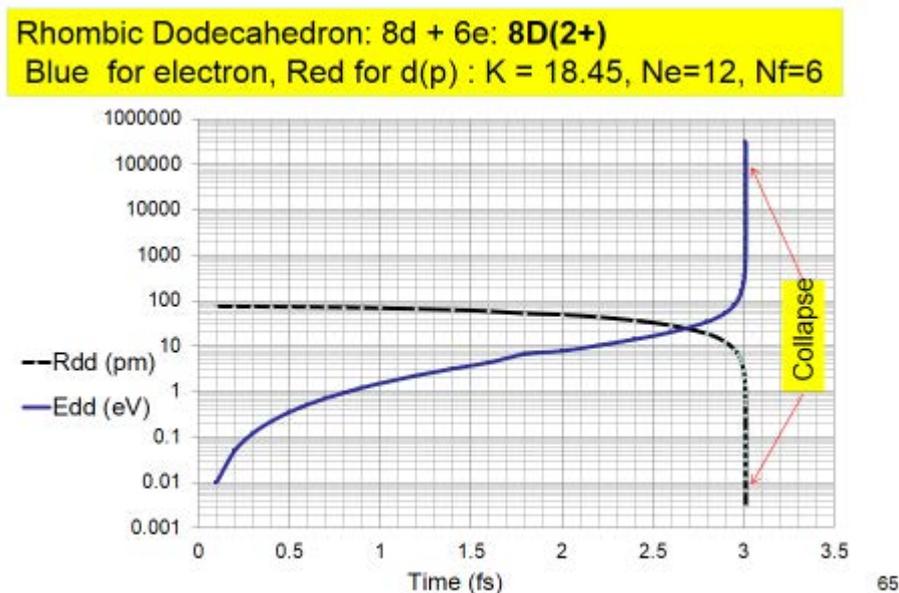


Fig.21: Results of simulation for condensation motion of 8D(2+) cluster

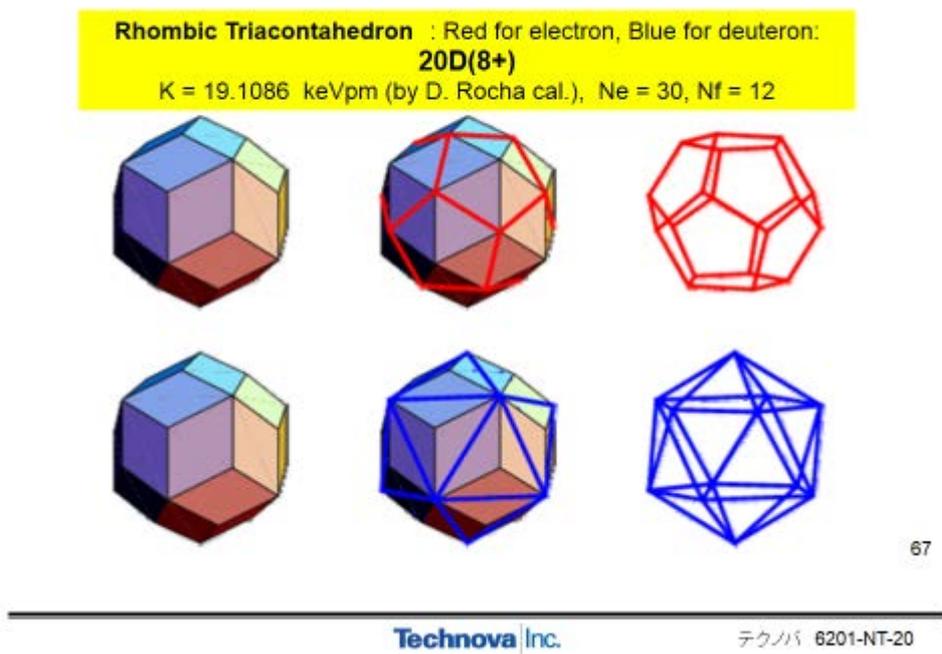


Fig.22: Geometrical feature of 20D(8+) cluster of Rhombic triacontahedron

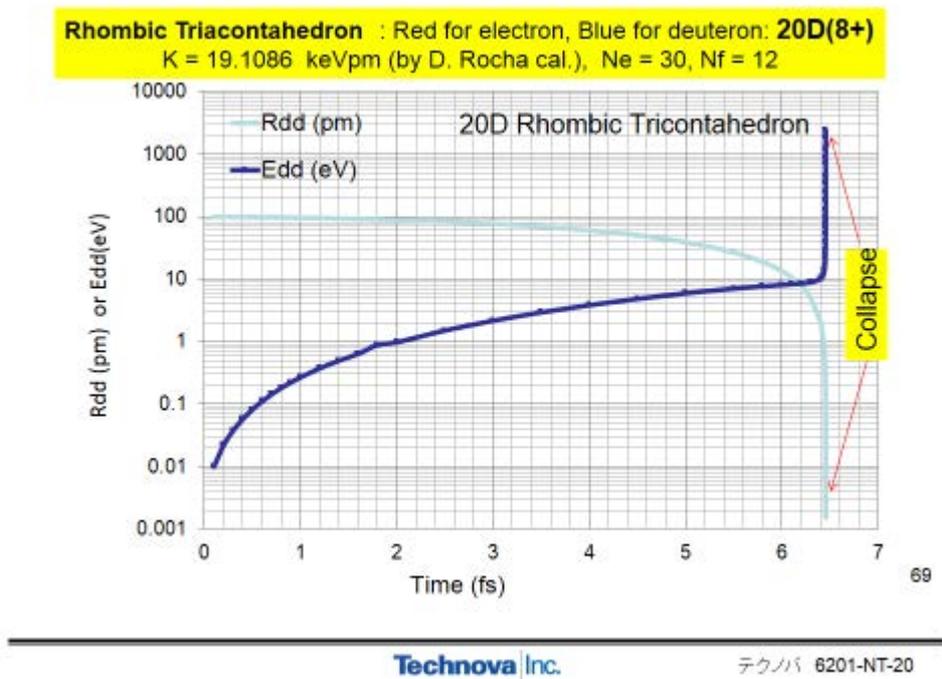
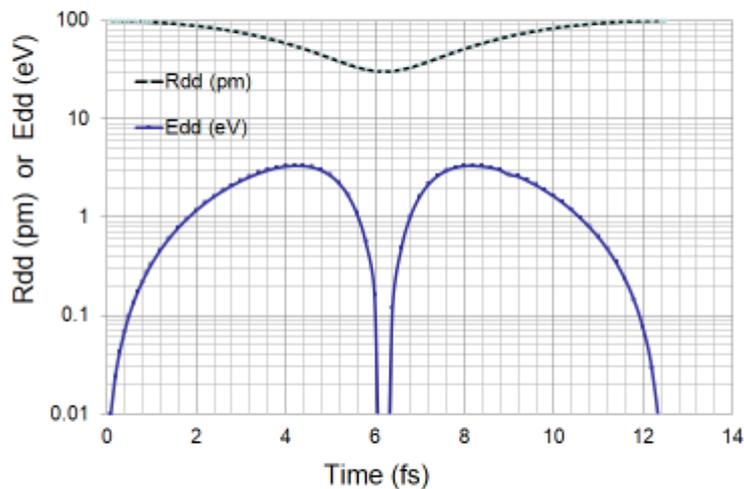


Fig.23: Results of simulation for 20D(8+) cluster of Rhombic triacontahedron

Rhombic Tricontahedron : Red for deuteron, Blue for electron: **12D(8-)**
 K = 15.51 keVpm (by D. Rocha cal.), Ne = 30, Nf = 20: For one cycle



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Fig.24: Results of simulation for 12D(8-) cluster of Rhombic tricontahedron

Table-2: Summary of condensation and collapse states for D-clusters;

Here RD denotes Rhombic dodecahedron and RT does Rhombic tricontahedron.

Summary of Results

Cluster Type	Collapse? (Rdd-min ≤ 10 fm)	Rdd (gs)	Remarks
d-e-d (2D+)	N	138 pm	
d- μ -d	N	0.79 pm	DD fusion in 0.1ns
3D+	N	85 pm	
4D/TS	Y		100% 4D fusion
6D/RD	Y		100% 6D fusion
8D/RD	Y		100% 8D fusion or 4D fusion?
12D/RT	N	ca. 80 pm	
20D/RT	Y		What kind of fusion?

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3.3 Simulation of EQPET D(H)-Clusters

Because of the spin arrangement of electrons in D(H)-clusters of polyhedra, condensation motion may be somewhat different from above results for which the spin effect was not treated.

The anti-parallel arrangement of spins for counter-part electrons in polyhedron of D(H)-cluster, bosonized pseudo-particle state of coupled electrons were assumed in our previous study on D(H)-cluster condensation [5]. The typical bosonized pseudo-particle states of oriented electrons as assumed in reference [5] are illustrated in Fig.25.

Results of simulation calculations for EQPET clusters by the present code are shown in Figs. 26 through 29. In many cases, EQPET clusters have very diminished size ground states as summarized in Table-3. Since these diminished size states as ground states have infinite life time and very close d-d (or p-p) inter-nuclear distances, reaction rates by strong (even weak) interactions may become significantly large to be able to argue on the possibility of condensed matter nuclear reactions aka cold fusion.

In this paper, example figures for H-systems are not specifically shown. However condensation speed is inversely proportional to mass and all figures may be rescaled for the case of H-clusters.

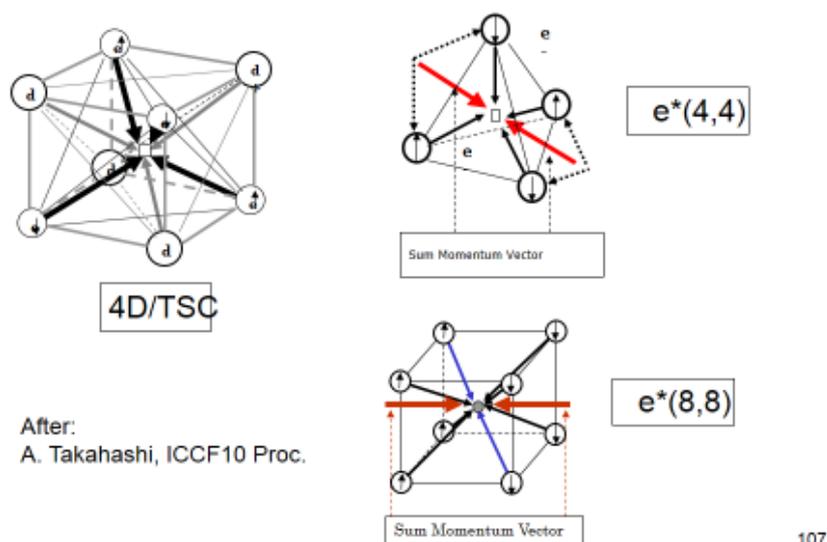


Fig.25: Assumed bosonized quasi-particles of oriented electrons

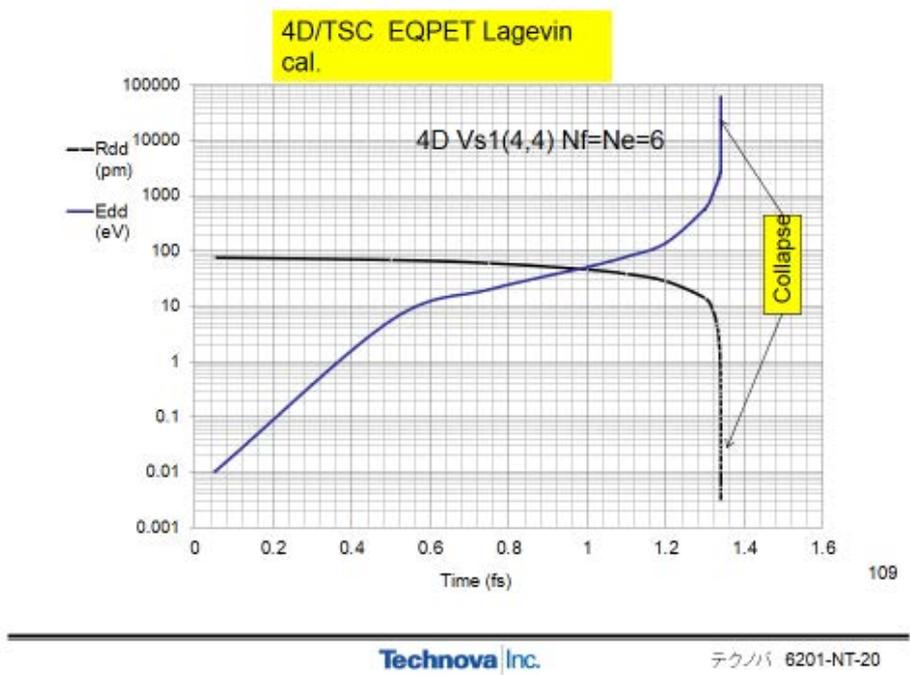


Fig.26: Results of simulation for 4D/TSC cluster with Vs1(4,4) EQPET potential

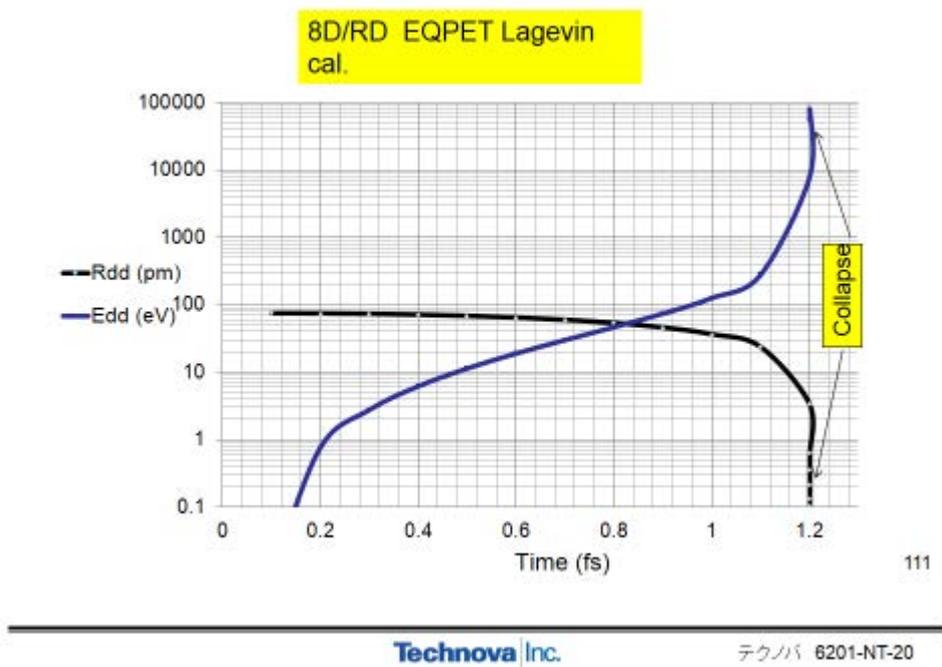


Fig.27: Results of simulation for EQPET 8D/RD cluster

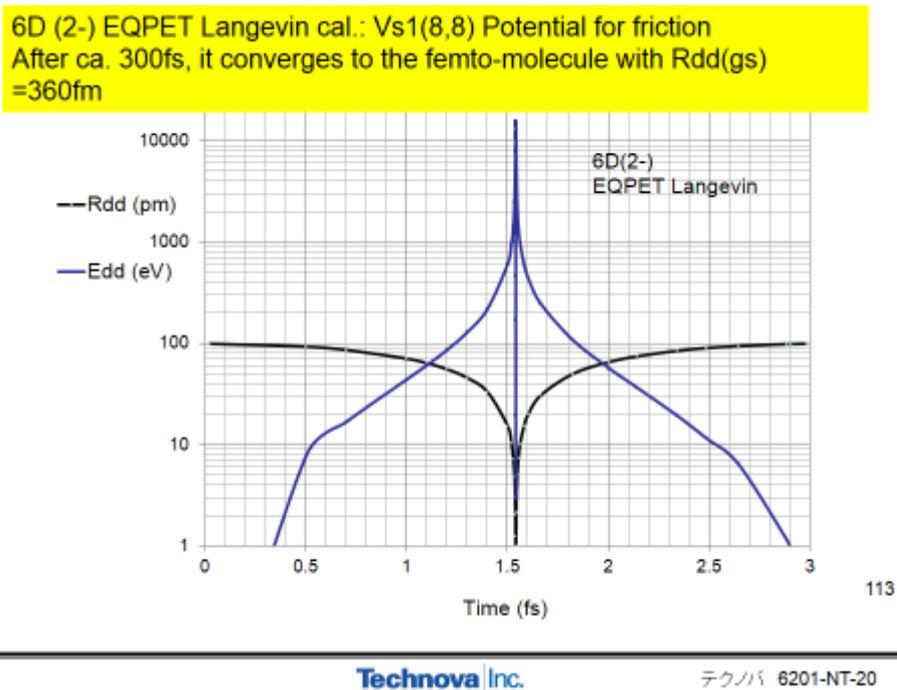


Fig.28: Results of simulation for EQPET 6D(2-) cluster with Vs1(8,8) potential, having no collapse but converged ground state of diminished size cluster (Rdd(gs) = 125 fm)

Table-3: Summary of converged ‘ground’ sates for EQPET clusters

Calculated convergence-to-Femto-Molecule
 by EQPET Langevin mode (Use dim 200000): by
 D.R.

Cluster Type	e* (m, Z)	Rdd (gs) (fm)
4D/TSC	(4,4)	None (collapse)
6D(2-)/OSC	(8,8)	360
6D(2-)/RD	(8,8)	125
6D(n)/RD	(6,6)	300 (Nf=12)
12D(8-)/RT	(20,20)	42
20D(8+)/RT	(12,12)	150

A typical example of simulation for such EQPET clusters is the cases of 4D/TSC with $V_{s1}(4,4)$ trapping potential and 8D/RD neutral-cluster with $V_{s1}(8,8)$ trapping potential. Results of simulation on condensation/collapse motion by the present code are shown in [Figs. 26 and 27](#).

4. Concluding Remarks

A generalized PC computer code written by Basic language has been developed for making simulation calculations on very time-sensitive dynamics behavior of polyhedral D(H) clusters which transient behavior is recognized very important according to the physical mechanisms of condensed matter nuclear reactions aka cold fusion.

For realizing the frictional/constraint force components caused by the quantum mechanical motion of electrons in D(H)-cluster, the well-studied Coulombic trapping potential $V_{s1}(1,1)$ of three body system (d-e-d or p-e-p) was used as a unit of particle trapping force per a regular triangle d-d-d (or p-p-p) surface of D(H)-cluster polyhedron assuming the 3 dimensional symmetry (Platonic symmetry). Evaluating three key parameters as k-value of centripetal Coulombic force of cluster, number of d-d (or p-p) edges N_e and number of regular triangle surfaces for individual D(H)-cluster, the programmed D(H)-cluster Langevin code can be run for simulation of very precise time-dependent behavior of condensation and sometimes collapsing states.

Time steps of numerical Verlet run must be very fine as $1.0E-21$ s to find very rapidly collapsing states. Such extremely small time mesh dynamics may be new in molecular/cluster-forming dynamics codes as given conventionally. Usual time mesh calculations with a few fs or even few as time mesh should miss easily the collapse states due to the time-averaging or error accumulation in time-step sequences of numerical calculation. Of course, the eigenvalue approach by the static Schroedinger equations cannot resolve such very fast transient behavior. The developed QM-Langevin method is a unique tool that should be very usable in studying underlying dynamic mechanisms of condensed matter nuclear reactions aka cold fusion.

Summary of most important consequences in this respect of cold fusion is given in Table-2. We may conclude the polyhedral D(H) cluster such as 4D(H)/TS, 6D/RD, 8D/RD, 20D/RT have something to do with inducing dreamy cold fusion events.

Acknowledgment: Kind support to this work by Technova colleagues (A. Kitamura, R.

Seto and Y. Fujita) is appreciated.

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Appendix: D(H)-Cluster Langevin Program

- 1 ! Cluster Langevin Code (written by Akito Takahashi, revised on April 11 2013)
- 2 ! Instruction: Time-dependent motion of d-d (or p-p) distance for a polyhedral deuteron(d) or proton(p) cluster is calculated.
- 3 ! Source Literature: Akito Takahashi: The Basics of Deuteron-Cluster Dynamics as Shown by a Langevin Equation, ACSLENRSB Vol.2, Chapter 11, pp.193-217, 2009
- 4 ! the second literature: A. Takahashi, N. Yabuuchi, Study on 4D/TSC Condensation Motion by Non-Linear Langevin Equation, ACSLENRSB Vol.1, pp.57-83, 2008
- 5 ! Correction in the second literature: In Appendix, (A-4) minus is missing for K, (A-9) minus should be removed for K'

```

11 ! ms: mass number (cf. electron) of electronic quasi-particle, Z: relative charge (cf. electron)
of EQ
12 ! BA: bias factor by <f(t)> for the main centripetal Coulombic force: BA=0.91 is
recommended for most cases.
16 input BA
17 print using "BA=% .#####" :BA
20 input ms
30 print using "ms=% .#####" :ms
40 input Z
50 print using "Z=% .#####" :Z
55 ! EK is k-value (keVpm) for centripetal force, EK=3.65 for 3D+, EK=11.85 for 4D/TSC,
EK=10.97 for 6D(2-)
56 ! FNf is the number of effective faces of d(or p)-polyhedron: FNf=4 for 3D+, FNf=4(for
Vs1(1,1)) or 6(for Vs1(2,2) or Vs1(4,4)) for 4D, Nf=8 (for Vs1(1,1)) for 6D
57 ! FNe is the number of nearest d-d edges: FNe=3 for 3D+, FNe=6 for 4D, FNe=12 for 6D
58 ! fmrev is the inverse of d (or p)-mass: 4.77E4 for deuteron, 2*4.77E4 for proton (See the
second literature).
59 ! R0 is the starting d-d distance in pm unit.
60 ! Please write-in the following parameters in line 62-66
62 LET EK=11.85
63 LET FNf=6
64 LET FNe=6
65 LET fmrev = 4.77E4
66 LET R0=74.0
69 input TDT
70 print using "DT=% .#####" :TDT
100 DIM RDD(2000), R(2000), T(2000), V(2000), VS1(2000), FCOND(2000),
BALANCE(2000), G(2000), ED(2000), DT(2000)
110 ! T is in (fs), R and RDD are in (pm), V is in (pm/fs), VS1 and ED are in (keV), FCOND
and BALANCE are in (pm/fs/fs)
210 LET V(1)=1.0
215 LET T(1)=0.0
218 LET R(1)=V(1)*TDT
220 LET IMAX=2000
230 LET I=1
300 do while I<IMAX

```

```

305 LET DT(I)=TDT
320 LET RDD(I)=R0-R(I)
321 if RDD(I)<=20 then LET DT(I)=0.1*TDT
322 if RDD(I)<=5 then LET DT(I)=0.01*TDT
323 if RDD(I)<=1 then LET DT(I)=0.001*TDT
324 if RDD(I)<=0.5 then LET DT(I)=0.0001*TDT
325 if RDD(I)<=0.05 then LET DT(I)=0.00001*TDT
315 if RDD(I)<=0.001 then LET RDD(I)=0.001
330 LET y=ms*Z*RDD(I)/52.9
340 LET FJ=0.0272*Z^2*ms*(-1/y+(1+1/y)*exp(-2*y))
350 LET FK=-0.0272*Z^2*ms*(1+y)*exp(-y)
360 LET FD=(1+y+y^2/3)*exp(-y)
365 LET VS1(I)=-0.0136*Z^2*ms+1.44/RDD(I)+(FJ+FK)/(1+FD)
370 LET FJD=(5.14E-4)*Z^3*ms^2*((1.0-exp(-2*y))/y^2-2*(1.0+1/y)*exp(-2*y))
380 LET FKD=(5.14E-4)*Z^3*ms^2*y*exp(-y)
390 LET FDD=-0.0063*(y+y^3)*exp(-y)
400 LET DVS=-1.44/RDD(I)^2+((FJD+FKD)*(1+FD)+(FJ+FK)*FDD)/(1+FD)^2
410 LET BALANCE(I)=(FNf*fmrev/FNe)*DVS
420 LET FCOND(I)=(EK*fmrev/FNe)/RDD(I)^2
430 LET G(I)=BA*FCOND(I)+BALANCE(I)
500 ! Verlet Solution
510 LET R(I+1)=R(I)+V(I)*DT(I)+0.5*G(I)*DT(I)^2
512 LET RDD(I+1)=R0-R(I+1)
513 if RDD(I+1)<=0.001 then LET RDD(I+1)=0.001
515 LET y=ms*Z*RDD(I+1)/52.9
516 LET FJ=0.0272*Z^2*ms*(-1/y+(1+1/y)*exp(-2*y))
517 LET FK=-0.0272*Z^2*ms*(1+y)*exp(-y)
518 LET FD=(1+y+y^2/3)*exp(-y)
519 LET FJD=(5.14E-4)*Z^3*ms^2*((1.0-exp(-2*y))/y^2-2*(1.0+1/y)*exp(-2*y))
520 LET FKD=(5.14E-4)*Z^3*ms^2*y*exp(-y)
521 LET FDD=-0.0063*(y+y^3)*exp(-y)
522 LET DVS=-1.44/RDD(I+1)^2+((FJD+FKD)*(1+FD)+(FJ+FK)*FDD)/(1+FD)^2
523 LET G(I+1)=BA*(fmrev*EK/FNe)/RDD(I+1)^2+(fmrev*FNf/FNe)*DVS
530 LET V(I+1)=V(I)+(DT(I)/2)*(G(I+1)+G(I))
540 LET ED(I)=(0.5/fmrev)*V(I)^2
590 if RDD(I)<=0.001 then LET IMAX=I

```

