

Square Number Theorem

$n=ab$, a, b in \mathbb{N} with 0

$$4ab = (a+b)^2 - (a-b)^2$$

\Leftrightarrow

$$(a+b)^2 = (a-b)^2 + 4ab$$

\Rightarrow Every $4n$ number is the difference of two perfect square numbers

\Rightarrow Every odd number is the difference of two perfect square numbers

\Rightarrow Every number is the difference of two squares

\Rightarrow Every number is the sum of two perfect square numbers, $0=0^2$, $n^2=n^2+0^2$

\Rightarrow Every perfect square number is the sum of two square numbers >0 if and only if $a*b$ is a square number

Remember a square divided by 4 is a square and a square factored by 4 is still a square

q.e.d.

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