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## Title: A Fundamental Model of Atomic Binding Energy

### Abstract

Reference 2 presents the author's attempt to "crack the information theory code" underlying nature. Once the energy components were understood, a model for the neutron and proton was developed. It is presented in Reference 2 and repeated below under the next heading. Using reference 1 for gravity, reference 2 also proposes an approach to unification of the four forces. The proton model shows that there is a 10.15 mev orbit that losses energy and is responsible for the binding energy curve. This paper contains the analysis.

Literature cites "water drop" models for binding energy that are admittedly empirical. Quantum physicists have suggested that there should be "electron like" shells inside atoms but to the author's knowledge they remain unclear. If there are shells the nucleons should fall into lower energy states releasing the remainder as binding energy. The author explored this possibility. Empirically, the model was successful but no explanation could be found for why a nucleon occupied a given shell.

The first part of the binding energy curve rises quickly and then levels off as saturation occurs. When the author compared the shape of the curve to a probability based model a fundamental relationship was discovered. The relationship is almost identical to the fundamentals presented in reference 2.

### Information contained in the proton mass table

Information from the proton mass model is used to understand fundamental interactions.

ll g228 mass ke	CALCULATION OF PROTON MASS				Mass and Kinetic Energy				Field Energies				
	Energy-mev	strong field grav field	Energy-mev	Mass mev	Difference ke mev	Strong residual ke mev	Neutrinos mev	Expansion ke mev	Strong & E/M field energy	Gravitation: spin Energy			
15.432	101.947	17.432	753.291	101.947	641.880				-753.29			0.5	
12.432	5.076	10.432	0.687										
13.432	13.797	15.432	101.947	13.797	78.685				-101.95			0.5	
12.432	5.076	10.432	0.687										
13.432	13.797	15.432	101.947	13.797	78.685				-101.95			-0.5	
12.432	5.076	10.432	0.687										
		-0.296	-2.72E-05				10.151		20.303 expansion ke				
large		equal and opposite charge	site charge						0.000 expansion pe				
10.408	0.67	0.075		0.000	0.000		-0.671 → 0.671 v neutrino						
-10.333	0												
↑													
↓													
↑													
↓													
10.136	0.51	10.333	0.62	129.541	799.251							0.5	
0.197	2.47E-05	0.296	2.72E-05	<b>0.511</b>	0.111				5.44E-05	-0.622		0.5	
				<b>ELECTRON</b>			→ 2.47E-05 e neutrino						
				130.052	0.111		0.671	20.303	-957.185	-2.683			
90.000		90.000						Total m+ke	Total fields				
								Total positive	Total negative				
								959.868	-959.868	0.00E+00	difference		

Values underlying four fundamental interactions come from the table above.

	Mass (m) (mev)	Ke (mev)	gamma (g)	R meters	Field (E (mev)
Gravity	129.541	10.151	0.9273	1.0584E-14	-2.683
Electromagn	0.511	1.36E-05	0.99997	5.2911E-11	-2.72E-05
Strong	129.541	799.251	0.1395	2.0928E-16	-957.18
Weak	939.565	10.151	0.9893	1.4211E-15	-20.303

## ***Orbital kinetic energy in the proton***

Physicists believe there are three quarks inside the proton and it is reasonable to model them as a small bundle of mass and kinetic energy contained by the strong interaction. The quark mass plus kinetic energy from the model is  $129.5 + 799.25 - .67 = 928.12$  mev. There is however, an additional kinetic energy of 10.15 mev that makes up the total mass of the proton (938.27 mev). This value changes during fusion.

*As an aside, based on the proton mass model the weak field energy does not result from a separate frequency transition. (In some literature this is called the strong residual force, but we are seeking the energy change responsible for binding energy). The proton and neutron mass models have a total energy of 959.86 mev, but the neutron only has only 939.56 mev. The total energy balance is zero if we consider the 20.3 deficit (959.86-939.56) as a field that surrounds the central mass (130.834 mev) similar to the manner in which the electromagnetic field surrounds the electron and proton. As quark bundles fall into the weak field, the released energy binds the neutrons and protons inside atoms.*

## **A top-down approach to fundamental release of atomic energy**

Reference 2 identifies  $1.5e78$  as the number of protons in the universe based on the results of WMAP [9]. This makes the probability (P) of one proton  $1/1.5e78$ . Nature uses Shannon [15] type information theory and makes  $N = -\ln(P)$  a fundamental number of nature (ln stands for natural logarithm). Reference 2 shows how nature's particles relate to  $N=180$ . Energy and N are related by the relationship  $E = e_0 \cdot \exp(N)$  and (for example) the number  $N=10.136$  represents the electron since  $E = 2.025e-5 \cdot \exp(10.136) = 0.511$  mev, the energy of the electron. In other words  $e_0/P$  is the electron energy where  $e_0 = 2.025e-5$  mev and  $P = 1/\exp(10.136)$ .

The fundamentals of atomic binding energy appear to be based on the same approach. First the probability of a proton in (for example) lithium 3 is given as  $P = 1/\exp(2/3)$ . The 2 means there are two types of particles (protons and neutrons) and 3 is of course the atomic number for lithium. Next  $N = -\ln(P) = 2/3$ . Note that in this case N is a number smaller than 1. Following a similar approach in the paragraph above, energy would be modified by P to give the binding energy of the proton at atomic number 3. The value  $e_0$  is 10.15 mev for binding energy, the value given above for "kinetic energy in the proton orbit". Binding energy for the proton contribution to atomic number 3 is  $10.15/\exp(2/3) = 5.21$ . In the table below the "Fundamentals of protons" is the approach that is used for "Fundamentals of atomic binding energy". Note that for the heaviest

atoms can have 110 protons which gives a potential release of 9.97 mev of atomic binding energy, indicating that the curve “saturates” at 10.15 mev.

Fundamentals of protons

protons	$P = 1/\text{protons}$	$N = -\ln P$	$E = e_0 \cdot \exp(N)$	$E = e_0 \cdot \exp(N)$
1.49E+78	6.71E-79	180	$e_0/P = 2e^{-5}/P$	$e_0/P = 2e^{-5}/P$
	$P = 1/\exp(180) = \exp(-N)$			
	3.96E-05	10.136	0.511	Electron

Fundamentals of atomic binding energy

protons	$P = 1/\exp(2/3) = \exp(-N)$	$N = -\ln(P)$	$e_0 \cdot P = 10.15 \cdot P$	$e_0 \cdot P = 10.15 \cdot P$
3	0.51	2/3	10.15 * P	10.15 * exp(-2/3)
110	0.98	0.02	5.21	5.21
			9.97	9.97

The values based on the fundamentals above will be called the “fundamental release” of atomic energy.

Consider now that neutrons are re-converted protons and also release energy as they fuse. The following calculations illustrate that the total fundamental release is the weighted contribution from the protons and neutrons. The weighted average is darkened in the table below.

protons p	$(10.15 \cdot \exp(-2/p))$	neutrons n	$(10.15 \cdot \exp(-2/n))$	$(p \cdot 10.15 \cdot \exp(-2/p) + n \cdot (10.15 \cdot \exp(-2/n) + E)) / (p+n)$ (weighted average)
1	1.374			1.374
2	3.734	2	3.734	3.734
3	5.211	4	6.156	5.751
4	6.156	5	6.804	6.516
5	6.804	6	7.273	7.060
6	7.273	7	7.627	7.464
7	7.627	8	7.905	7.775
8	7.905	9	8.127	8.023
9	8.127	10	8.310	8.224
10	8.310	11	8.463	8.390
110	9.967	272	10.076	10.044

This isotope of lithium has 4 neutrons and the calculation above gives a total binding energy of 5.751 mev. This is close to the NIST [8] value of 5.644 mev but the difference is significant and there are two corrections needed. The binding energy curve is based on two additional processes: retained energy and isotope number.

**The re-conversion process**

Reference 2 reviewed the neutron to proton decay (conversion) process  $N \rightarrow P + e^- + \bar{\nu}_e + KE$  (e-,  $\bar{\nu}_e$  and KE refer to the electron, the anti-neutrino and kinetic energy required to balance the process). The electron quad table (reproduced below) indicates that the electron initially has 0.111 mev of kinetic energy (explained in reference 2).

As a proton, the electron quad of the proton mass model contains these energies:

-(0+1)			-0.296	-2.72E-05	20.303 expansion ke		
Total proton charge			equal and opposite charge		0.000 expansion pe		
	10.408	0.67	0.075	0.000	0.000	-0.671 → 0.671 v neutrino	
-10.33	-10.333	0					
Neutron separates here to form proton and electron					<b>938.272013</b> PROTON MASS		
10.33	10.136	0.51	10.333	0.62	<b>0.511</b>	0.111	5.44E-05
	0.197	2.47E-05	0.296	2.72E-05	<b>ELECTRON</b>		
	90.000		90.000		130.052	0.111	-2.683
					0.671	20.303	-957.185
					Total m+ke		Total fields
					Total positive		Total negative
					959.868	-959.868	0.00E+00

But as a neutron, the electron quad of the mass model contains these energies:

10.408	0.67	0.075	0.000	0.000		
-10.333						
10.333	0.6224	0	2.02E-05	0.6224	0.000	2.02E-05
0	2.02E-05	10.333	0.6224			
90.000 sum		90.000		130.163	799.251	<b>939.5653531</b>
				<b>NEUTRON MASS</b>		
				2.02E-05	20.303	-957.185
				Total m+ke		Total fields
				Total positive		Total negative
				959.868	-959.868	0.000E+00

130.16

The decay energy balance can be written  $N(939.565) \rightarrow P(938.272) + e^-(0.511 + 0.111) + \nu(0.671)$ . (This accounts for the neutron/proton mass difference of 1.293 mev). This process is reversed during fusion. The neutrino energy of 0.671 mev is ejected according to the binding energy model, but regained. At high temperature and pressure there is a chance that the electron/proton can regain the 0.111 ke lost from the decay. The reverse process for the proton to neutron re-conversion is as follows:  $P(938.272) + e^-(0.511) + ke(0.111) \rightarrow N(938.27) + \nu(0.622)$ . The re-converted neutron undergoes a properties re-conversion and reverts to a neutron from the standpoint of charge, etc. The kinetic energy it absorbs is the “difference kinetic energy”  $(0.111 = 27.2e-6 + 0.622 - 0.511 - 2.4e-5)$ . Since it is a subtraction of four values linked with the electron quad, some of the values may contain properties (spin and charge) that balance the re-conversion. The proton actually gains the two neutrinos lost in the decay process from a neutron to a proton (energy  $0.6709 + 0.6224 = 1.293$  mev. The electron is absent after the conversion to a neutron. It is converted to energy  $0.622$  mev energy  $0.511$  mev +  $0.111$  mev absorption. Re-conversion and a gain of energy on the order of 0.111 are pre-requisites for fusion. The process involves new-neutrons and protons falling into weak field energy. More than half of the incoming protons become neutrons because neutrons can lose more energy. (See the paragraph below entitled “Prediction of excess neutrons over protons...”). The other portion of the incoming protons is accepted without conversion.

Summarizing, the requirement for fusion is that the environment must provide energy. In this model, if the electrons and protons gain 0.111 mev and are in contact they fuse. This amount of energy is large compared to the kinetic energy available from even a very hot environment. For example the sun’s core temperature of  $1.5e7$  degrees K provides 0.0022 mev. (A probabilistic process appears to limit the reaction rate. A simplified way to think about this is a Boltzmann type calculation like  $P = \exp(-0.009/0.002)$ , where -0.009 mev is a barrier energy and 0.002 mev is kinetic energy from the environment). The low

probability that the value 0.111 mev will be achieved helps determines the low reaction rate at this temperature (a description of solar fusion is contained in reference 14).

## **Retained kinetic energy**

The incoming protons gain energy from their environment (i.e., the core of the sun). When energy conditions allow, protons are accepted into the developing atom and they retain part of the supplied energy. After considering the fundamental release, the binding energy falls with increasing atomic number (and is quite evident for large atomic number) as more energy is retained inside the atom. The atom retains energy of  $-0.1/4$  mev for each proton. This is close to the value 0.111 given in the proton mass model as the kinetic energy of the electron. This energy may be related to compressing the charges (literature refers to a coulomb barrier since protons resist bringing more positive charge into the nucleus). The overall retained energy is the number of protons times the retained energy per proton pair.

## **Correction for isotope number**

Without a second correction, the difference between the published and predicted value *cycles* within one atomic number for the several isotopes of that atom. The cycle was characterized by the retained energy of  $-0.004 * \text{isotope number (n)}$  and n was assigned as follows. The first isotope was normally given the value  $n=1$  and incrementally increased (neutrons minus protons) as isotopes became more massive. The correction could be considered empirical but with more work might be fundamental.

## **Binding energy results**

The following data is a combination of NIST [8] data for published binding energy compared against the author's binding energy model. Two corrections were made to the fundamental release. First the retained energy and second the small retention for isotope number.

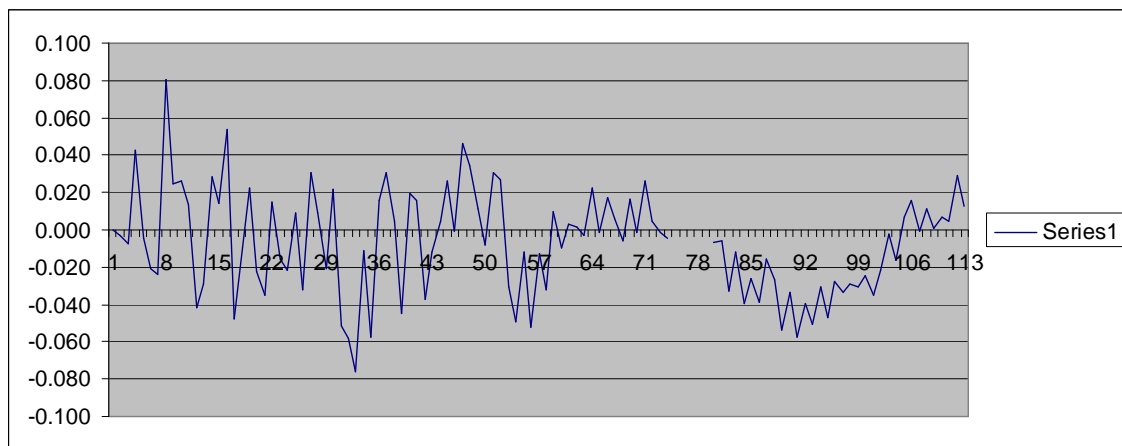
There was another correction sometimes required that the author believes can be easily identified. Some of the predicted values are multiples of 0.111 mev higher or lower (this is the energy associated with the electron kinetic energy that initiates fusion) and were subtracted out. This correction only appears in the steeply rising portion of the curve. In addition, there were two atoms that were obviously different. The fundamental release from Helium (2,2) was exactly doubled. Secondly, it appears that Carbon (6,6) retains an extra 0.622 mev (a neutrino like energy) for some reason.

	Simple probability model										
				average	0.007	-0.100 electrostatic retention					
				stand dev	0.025	-0.004 isotope n correction					
	Published			Binding Energy	Pub BE-pred Energy	Isotope N		Fundamenta		Release P*(1)	
protons	neutrons	isotope n	mev	.11 correctio	mev	retention	correction	prediction			
H	1	0	1	0.000		0.000	0	0	0.000	0.000	
D	1	1	2	1.115	-1	-0.003	-0.025065	-0.008	1.118	1.151	
T	1	2	1	2.915	1	-0.004	-0.025065	-0.004	2.919	2.948	
He	2	1	1	2.490	-3	0.042	-0.05013	-0.004	2.448	2.502	
	2	2	1	7.075	-2	-0.005	-0.05013	-0.004	7.080	7.134	
Li	3	3	1	5.334	3	-0.021	-0.075195	-0.004	5.355	5.434	
	3	4	2	5.644	1	-0.024	-0.075195	-0.008	5.668	5.752	
Be	4	5	1	6.492	1	0.080	-0.10026	-0.004	6.412	6.516	
B	5	5	1	6.476	-1	0.024	-0.125325	-0.004	6.452	6.581	
0	5	6	2	6.952		0.137	-0.125325	-0.008	6.815	6.949	
C	6	6	3	7.681		-0.051	-0.15039	-0.012	7.732	7.895	
	6	7	1	7.491	3	-0.042	-0.15039	-0.004	7.533	7.687	
	6	8	2	7.558	2	-0.030	-0.15039	-0.008	7.587	7.746	
N	7	7	1	7.477	1	0.028	-0.175455	-0.004	7.448	7.628	
	7	8	2	7.717	2	0.014	-0.175455	-0.008	7.704	7.887	
O	8	8	1	7.977	3	0.054	-0.20052	-0.004	7.924	8.128	
	8	9	2	7.767		0.064	-0.20052	-0.008	7.703	7.912	
	8	10	3	7.796		-0.010	-0.20052	-0.012	7.806	8.019	
F	9	10	1	7.793	-1	0.022	-0.225585	-0.004	7.772	8.001	
Ne	10	10	1	8.033	1	-0.023	-0.25065	-0.004	8.056	8.311	
	10	11	2	7.985		-0.036	-0.25065	-0.008	8.020	8.279	
	10	12	3	8.105		0.014	-0.25065	-0.012	8.090	8.353	
Na	11	12	1	8.123		-0.016	-0.275715	-0.004	8.139	8.419	
Mg	12	12	2	8.262		0.089	-0.30078	-0.008	8.172	8.481	
	12	13	3	8.235		0.009	-0.30078	-0.012	8.226	8.538	
	12	14	4	8.354		0.079	-0.30078	-0.016	8.275	8.592	
Al	13	14	1	8.342		0.030	-0.325845	-0.004	8.312	8.642	
Si	14	14	2	8.448		0.120	-0.35091	-0.008	8.329	8.688	
	14	15	3	8.458		0.090	-0.35091	-0.012	8.368	8.731	
	14	16	4	8.538		0.133	-0.35091	-0.016	8.405	8.772	
P	15	16	1	8.490		0.060	-0.375975	-0.004	8.430	8.810	
S	16	16	1	8.494		0.053	-0.40104	-0.004	8.441	8.846	
	16	17	2	8.506		0.035	-0.40104	-0.008	8.471	8.880	
	16	18	3	8.599	1	-0.012	-0.40104	-0.012	8.611	9.024	
	16	20	5	8.604		0.053	-0.40104	-0.02	8.551	8.972	
Cl	17	18	1	8.528		0.016	-0.426105	-0.004	8.513	8.943	
	17	20	3	8.592		0.031	-0.426105	-0.012	8.561	8.999	
Ar	18	18	1	8.521		0.004	-0.45117	-0.004	8.516	8.972	
	18	20	3	8.628		0.067	-0.45117	-0.012	8.562	9.025	
	18	22	5	8.622		0.019	-0.45117	-0.02	8.602	9.074	
K	19	20	6	8.564		0.015	-0.476235	-0.024	8.549	9.050	
	19	21	2	8.552		-0.037	-0.476235	-0.008	8.589	9.073	
	19	22	3	8.595		-0.012	-0.476235	-0.012	8.608	9.096	
Ca	20	20	6	8.552		0.004	-0.5013	-0.024	8.548	9.073	
	20	22	3	8.629		0.026	-0.5013	-0.012	8.604	9.117	
	20	23	4	8.619		-0.001	-0.5013	-0.016	8.620	9.138	
	20	24	5	8.682		0.046	-0.5013	-0.02	8.636	9.157	
	20	26	6	8.703		0.034	-0.5013	-0.024	8.669	9.194	
	20	28	7	8.710		0.011	-0.5013	-0.028	8.699	9.228	
Sc	21	24	1	8.637		-0.009	-0.526365	-0.004	8.646	9.176	
Ti	22	24	1	8.668		0.030	-0.55143	-0.004	8.638	9.194	
	22	25	2	8.678		0.026	-0.55143	-0.008	8.652	9.211	
	22	26	3	8.745		-0.030	-0.55143	-0.012	8.775	9.339	
	22	27	4	8.738		-0.049	-0.55143	-0.016	8.787	9.355	
	22	28	5	8.787		-0.012	-0.55143	-0.02	8.799	9.370	
V	23	27	6	8.717		-0.052	-0.576495	-0.024	8.769	9.370	
	23	28	7	8.768		-0.012	-0.576495	-0.028	8.780	9.385	
Cr	24	26	6	8.712		-0.032	-0.60156	-0.024	8.744	9.370	
	24	28	3	8.795		0.009	-0.60156	-0.012	8.785	9.399	
	24	29	4	8.785		-0.010	-0.60156	-0.016	8.795	9.412	
	24	30	5	8.807		0.003	-0.60156	-0.02	8.804	9.426	
Mn	25	30	6	8.789		0.001	-0.626625	-0.024	8.788	9.438	
Fe	26	28	6	8.746		-0.003	-0.65169	-0.024	8.750	9.425	
	26	30	3	8.809		0.023	-0.65169	-0.012	8.787	9.450	
	26	31	4	8.793		-0.001	-0.65169	-0.016	8.795	9.462	
	26	32	5	8.819		0.017	-0.65169	-0.02	8.802	9.474	
Co	27	32	6	8.790		0.006	-0.676755	-0.024	8.784	9.485	
Ni	28	30	6	8.742		-0.006	-0.70182	-0.024	8.748	9.474	
	28	32	3	8.798		0.017	-0.70182	-0.012	8.782	9.495	
	28	33	4	8.787		-0.001	-0.70182	-0.016	8.788	9.506	
	28	34	5	8.820		0.026	-0.70182	-0.02	8.794	9.516	
	28	36	7	8.810		0.005	-0.70182	-0.028	8.806	9.535	

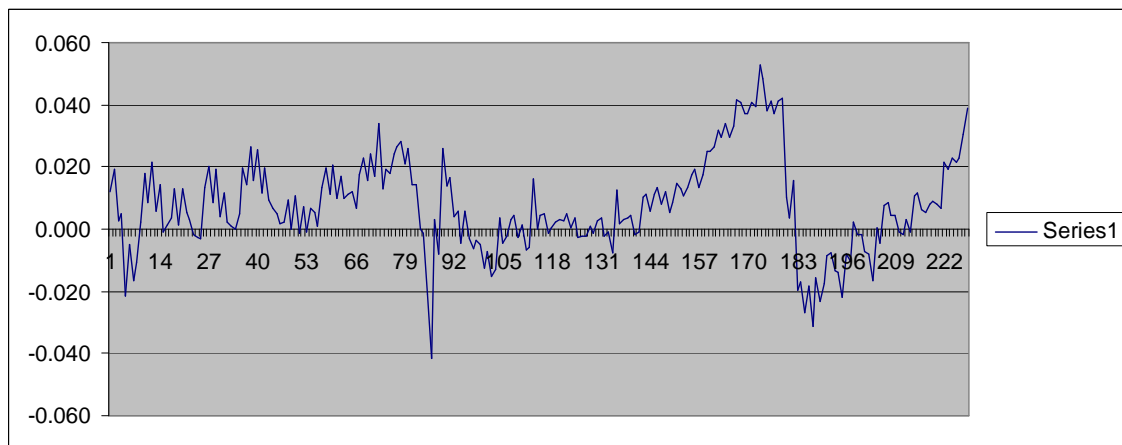
The fundamental release in yellow contains an extra retention of 0.111 mev. All the others are normal.

The remainder of the atoms were calculated but not presented here for brevity. For all 345 atoms, the standard deviation was 0.021 and the average from zero was 0.003 mev.

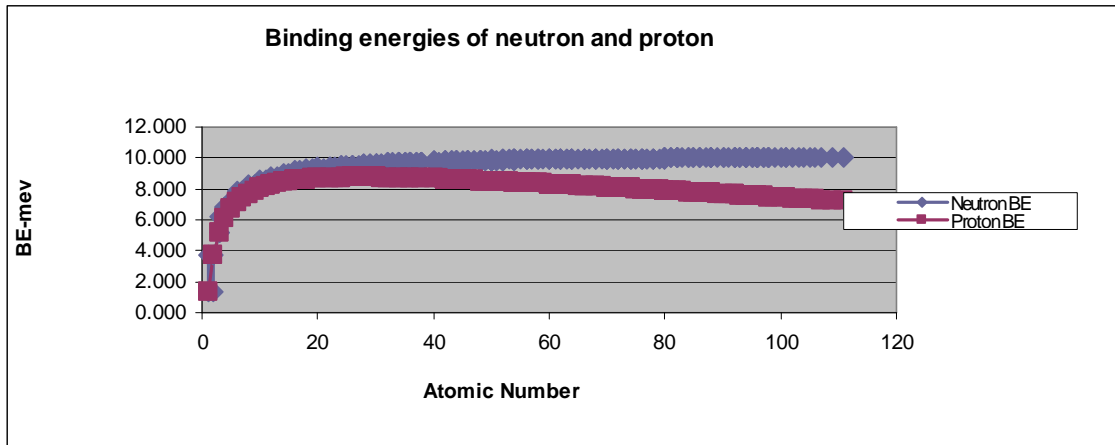
Since the predicted values are very close to the published binding energy, the points overlie each other and there was no need to present the predicted curve. The more meaningful graph is the following deviation for the first 113 atoms (including the isotopes). The vertical axis is published binding energy minus predicted binding energy in mev.



And for the remaining atoms and isotopes, the following graph shows the deviations. The vertical axis is mev, indicating that the predictions are within standard deviation 0.021 mev overall.



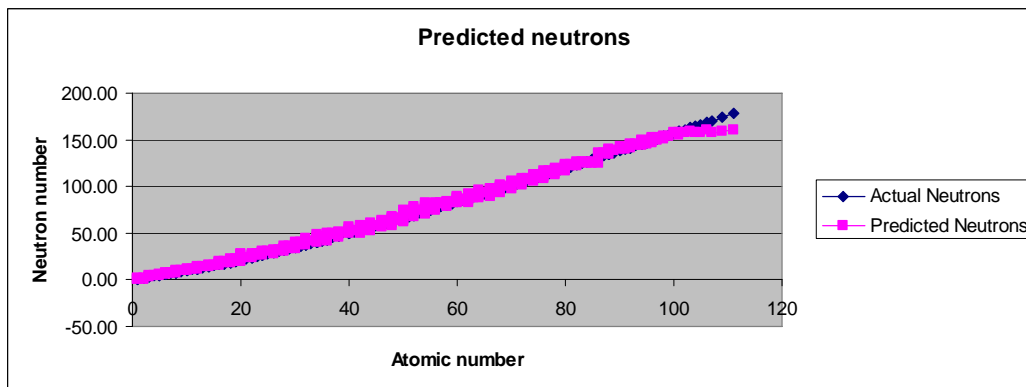
It is instructive to show the binding energy for the proton and neutron separately.



### Prediction of neutron excess over protons with increasing atomic number

Excess neutrons are produced because they can give up more energy. Prediction of the excess neutrons is simply a result of the energy that the protons retain. Based solely on this parameter, the number of neutrons can be predicted from the number of protons.

$$\text{Neutrons} = \text{protons} + \text{protons} / (\text{EXP}(1.32 / (\text{Eretained})))$$



### Summary

A proposal regarding how nature releases binding energy is offered as verification of the proton kinetic energy value 10.15 meV. This value appears in the proton mass model



presented in reference 2. Reference 2 offers an internally consistent approach to the four forces of nature and this paper extends the basic approach to binding energy.

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