Motto: "The science wouldn't be so good today, if yesterday we hadn't thought about today" Grigore C. Moisil

ECCENTRICITY, SPACE BENDING, DIMMENSION

Marian Niţu, Florentin Smarandache, Mircea Eugen Şelariu

0.1. ABSTRACT

This work's central idea is to present new transformations, previously non-existant in Ordinary mathematics, named centric mathematics (**CM**) but that became possible due to new born eccentric mathematics, and, implicit, to supermathematics.

As shown in this work, the new geometric transformations, named conversion or transfiguration, wipes the boundaries between discrete and continueous geometric forms, showing that the first ones are also continueous, being just apparently discontinueous.

0.2 ABBREVIATIONS AND ANNOTATIONS

C → Circular and Centric, E→ Eccentric and Eccentrics, F→ Function, M→ Mathematics, Circular Eccentric →CE, FCE → FCE, centric M → CM, eccentric M → EM, Super M → SM, F CM → FCM, F EM→FEM, F SM → FSM

1. INTRODUCTION: CONVERSION or TRANSFIGURATION

In <u>linguistics</u> a **word** is the fundamental unit to communicate a meaning. It can be composed by one or more <u>morphemes</u>. Usually, a word is composed by a basic part, named root, where one can attach affixes. To define some <u>concepts</u> and to express the domain where they are available, sometimes more words are needed; two, in our case.

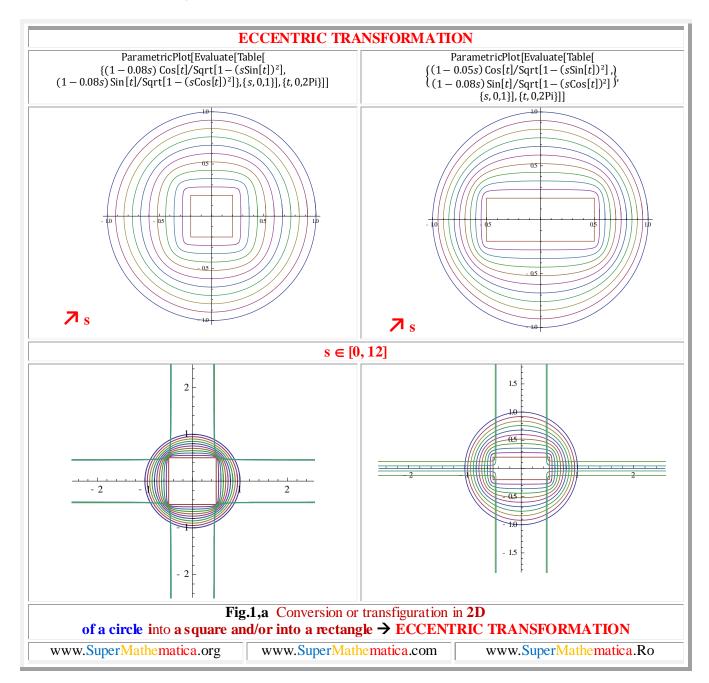
SUPERMATHEMATICAL CONVERSION

The concept is the easyest and methodical <u>idea</u> which reflect a finite of one or more/(a series) of attributes where these attributes are <u>essentials</u>.

The concept is a minimal coherent and usable information, relative to an object, action, property or a defined event.

According the Explicatory Dictionary, <u>THE CONVERSION</u> is, among many other definitions / meanings, defined as "changing the nature of an object". Next, we will talk about this thing, about transforming / changing / converting, previously impossible in the ordinary classic mathematics, now named also **CENTRIC** (**CM**), of some forms in others, and that became possible due to the new born mathematics, named **ECCENTRIC** (**EM**) and to the new built-in mathematical complements, named temporarly also **SUPERMATHEMATICS**

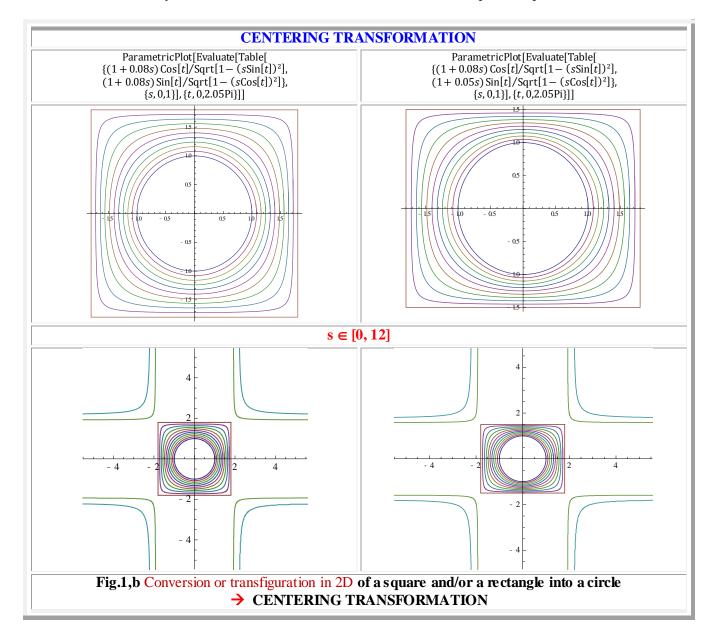
(SM). We talk about the <u>conversion</u> of a circle into a square, of a sphere into a cube, of a circle into a triangle, of a cone into a pyramid, of a cylinder into a prism, of a circular torus in section and shape into a square torus in section and/or form, etc. (**Fig. 1**).



SUPERMATHEMATICAL CONVERSION (SMC) is an internal pry for the mathematical dictionary enrichment, which consist in building-up of a new denomition, with one or more new terms, two in our case, by assimilating some words from the current language in a specialized domain, as Mathematics, with the intention to

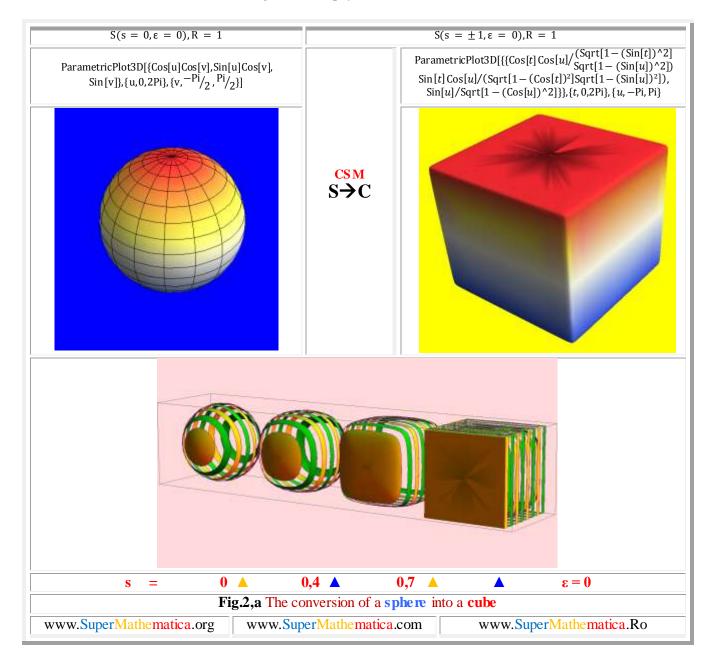
name, adequate, the new operations that became possible only due to the new born eccentric mathematics, and implicit, to supermathematics. Because previously mentioned conversions could not be made until today, in MC, but only in SM, we need to call them SUPERMATHEMATICAL conversion (SMC)

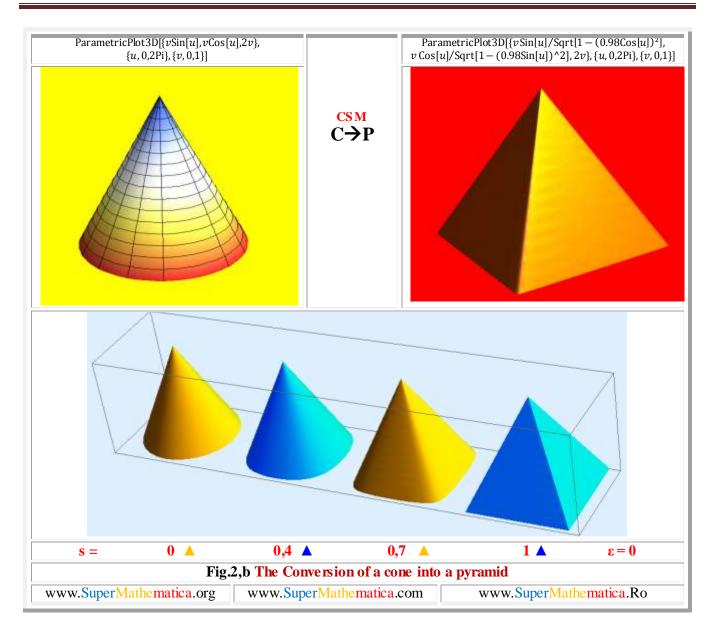
In [14] work, the continueous transformation of a circle into a square was named also **eccentric transformation**, because, in that case, the linear numeric eccentricity s varies/grows from 0 to 1, being a slide from centric mathematics domain $\mathbf{MC} \rightarrow \mathbf{s} = 0$ to the eccentric mathematics, $\mathbf{ME} (\mathbf{s} \neq 0) \rightarrow \mathbf{s} \in (0,1]$ where the circular form draws away more and more from the circular form until reach a perfect square ($\mathbf{s} = \pm 1$).



In the same work, the reverse transformation, of a square into a circle, was named as **centering transformation**, by easy to understand means. Same remarks are valid also for transforming a circle into a rectangle and a rectangle into a circle (**Fig. 1**).

Most modern physicists and mathematicians consider that the <u>numbers</u> represent the reality's language. The truth is that <u>the forms</u> are those who generate all physical laws.





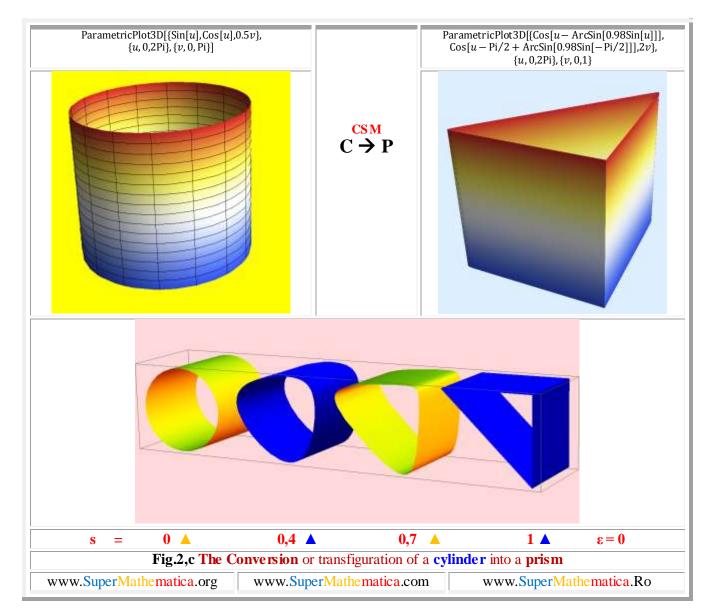
Look what the famous romanian physicist **Prof. Dr. Fiz. Liviu Sofonea** în "**REPRESENTATIVE GEOMETRIES AND PHYSICAL THEORIES**", Ed.Dacia, Cluj-Napoca, pag. 24, in 1984, in the chapter named "**MATHEMATICAL GEOMETRY AND PHYSICAL GEOMETRY**" wrote:

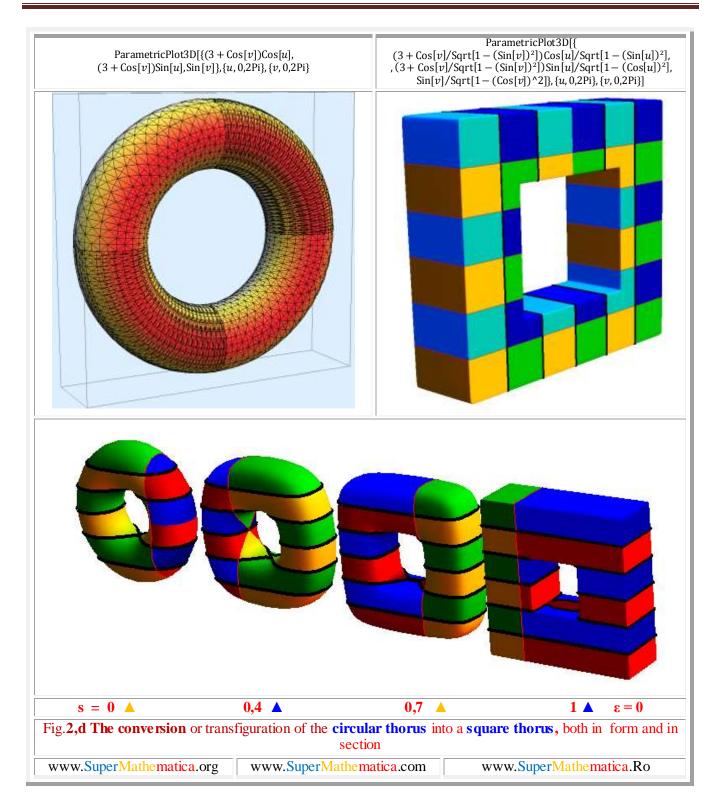
"Trough *geometrization* we look for (deliberately and by sui generis) exactly the ordering directions (detailed, fundamentals, even the supreme, the *unique-unifier*) thinking about the pre-established (relating to physical theory undertaking) from the "geometrical worlds" built and moved after disciplined canons in *more geometrico* style (logical derivability and structure, geometrically proved, where it's done), an extension with the purpose if "it works" also "*physicaly*", and as we see that we have reasons to say "it really works", we bargain on a methodological-operant gain, euristical, but even gnoseological. But never *geometrical* pre-norming can not be fully functional; it can be only (inherent) partial, limited, often a simple boundary marking, a suggestion, an

incitement, a scheme, sometimes too dummy, but we use it like a scaffold, to rise up, as we can, to a more adequate description or even more understanding"

In the **centric mathematical geometry** one is doing what can be done, how can be done, with what can be done, and in **supermathematical geometry** we can do what must be done, with what must be done, as we will proceed.

In the **supermathematical geometry**, between the elements of the "**CM** scaffold", one can introduce as many other constructive elements we want, which will give an infinitely denser scaffold structure, much more durable and, consequently, higher, able to offer an unseen high level and an extremely deep description and gravity.





<u>The fundamental principles</u> of the geometry are, according their topological dimmensions: the **corp** (3) the **line** (2) and the **point** (0)

<u>The elementary principles</u> of geometry are the point, the line, the space, the curve, the plane, geometrical figures (segment, triangle, square, rectangle, rhombus, the polygons, the polyhedrons, etc, the arcs, circle, ellipse, hyperbola, the scroll, the helix, etc) both in 2D and in 3D spaces.

With the fundamental geometrical elements are defined and built all the forms and geometrical structures of the objects:

- <u>Discrete forms</u>, or <u>discontinueous</u>, <u>statical</u>, <u>directly</u>, <u>starting</u> from a finite set (discrete) of points, statically bonded with lines and planes.
- <u>Continueous forms, or dynamical, mechanical, starting from a single point and considerring it's</u> motion, therefore the <u>time</u>, and obtaining in this way continueous forms of curves, as trajectories of points or curves traces, in the plane (2D) or in the space (3D)

Consequently, one has considered, and still is considerring, the existence of two geometries: the <u>geometry</u> of <u>discontinuum</u>, or discrete geometry, and the <u>geometry of the continuum</u>.

As, both the objects limited by plane surfaces (cube, pyramid, prism), <u>apparently discontinueous</u>, as those limited by different kinds of of <u>continueous surfaces</u> (sphere, cone, cylinder) can be described with the same parametric equations, the first ones for numerical eccentricity $\mathbf{s} = \pm 1$ and the last ones for $\mathbf{s}=0$, it results that in **SM** exists only one geometry, the geometry of the continuum.

In other words, the **SM** erases the boundaries between continueous and discontinueous, as **SM** erased the boundaries between <u>linear</u> and <u>nonlinear</u>, between <u>centric</u> and <u>eccentric</u>, between <u>ideal/perfection</u> and <u>real</u>, between <u>circular</u> and <u>hyperbolic</u>, between <u>circular</u> and <u>elliptic</u>, etc.

Between the values of numerical eccentricity of s=0 and $s = \pm 1$, exists an infinity of values, and for each value, an infinity of geometrical objects, which, all of them, has the right to a geometrical existence.

If the geometrical mathematical objects for $s \in [0 \lor \pm 1]$ belongs to the centric ordinary mathematics (CM) (circle \rightarrow square, sphere \rightarrow cube, cylinder \rightarrow prism, etc), those for $s \in (0, \pm 1)$ has forms, equations and denominations unknown in this centric mathematics (CM)

They belongs to the new mathematics, the **eccentric mathematics** (EM), and, implicit, to the **supermathematics** (SM) which is a reunion of the two mathematics: centric and eccentric, that means $SM = MC \cup ME$

By erasing the boundaries between centric and eccentric, the **SM** implicitly dissolved the boundaries between **linear** and **nonlinear**, the <u>linear</u> being the appanage of **CM** and the nonlinear of the **EM** one, and introduced a disjunction between the centric geometrical entities and the eccentric ones. By this way, all the entities of **centric mathematics** in 2 D was named **centrics** (circular centrics, square centrics, triangular centrics, elliptical centrics, hyperbolic centrics, etc) and those of **eccentyric mathematics** was named as **eccentrics** (circular eccentrics, spiral eccentrics, cycloid eccentrics, etc)

If the 2D **centric** entrities can remain to the actual denominations (circle, square, ellypse, spiral, etc) at the **eccentric** ones one have to specify also the teh denomination of **eccentrics**. The same thing is available for 3D entities: **the centric** ones (sphere, ellypsoid, cube, paraboloid, etc) can carry, further, the old denominations, and for the new ones, the **eccentric** ones, it is necessaary to specify that they are **eccentric**. That means: eccentric sphere, eccentric ellypsoid, eccentric cube, eccentric paraboloid, etc

With the new SM functions, like eccentric amplitude $aex\theta$ și $Aex\alpha$, of eccentric variable θ and, respectively, centric α , beta eccentric $bex \theta$ și $Bex\alpha$, radial eccentric rex and REX, eccentric derived dex θ and $Dex\alpha$, etc, which having no equivalents in **centric** / (**CM**), doesn't need other denominations for determining the mathematical domain where they belongs.

By way of exception are the last two FSM-CE, rex α si dex α , ($\theta = \alpha$), to which ones are discovered, later, equivalents in **centrics**: the **centric radial** function rad α , which is the direction fazor α and the **centric derived** der α , which is the direction fazor $\alpha + \frac{\pi}{2}$, fazors reciprocal perpendiculars.

SUPERMATHEMATICAL HYBRIDIZATION AND METAMORPHOSIS THE CONSEQUENCES OF THE NEW SPACE DIMMENSIONS

The space is an abstract entity which reflects an objective form of matter's existance. It shows like a generalization and abstactization of the parameters assembly through which is achieved the **distinction between different systems** that forms a condition of the Universe.

It is an objective and universal form of matter's existency, inseparable from the matter, which has the aspect of a tri-dimmensional continuum and expresses the order of the real world's objects coexistance, their position, distance, size, form and extension.

In conclusion, one can say that the space appears like a synthesis, like a generalization and abstractization of the observations about a condition, in a certain moment, of the Universe.

Within the classical mechanics, the notion of space is that of the tridimmensional euclidian space (E3), homogenuos, isotropic, infinite.

When one discuss about the space, the first thought is directed to the position, that means the notion of position is directly associated with that of the notion of space. The **position** is expressed in terms of a reference system, or shortly, by a coordinate system.

A tridimmensional object has in the E^3 6 variances, made of the 3 translations, on X, Y and Z directions and of the 3 rotations, around the axis X, Y and Z, noted, respectively, by θ , ϕ , ψ in Mathematics and in Mechanics and with A, B and C in technology and in robotics.

An object can be "created", or more specifically, its image can be reproduced in the virtual space, when appears in the 3D space, on the display of a computer, by using some tecnical programs (CAD) or commercial mathematical programs (MATHEMATICA, MATLAB, MATHCAD, MAPLE, DERIVE, etc.), or special ones, which use **Eccentric-FSM, Elevated** and/or **Exotic** - for objects describing, as at **SM-CAD-CAM**.

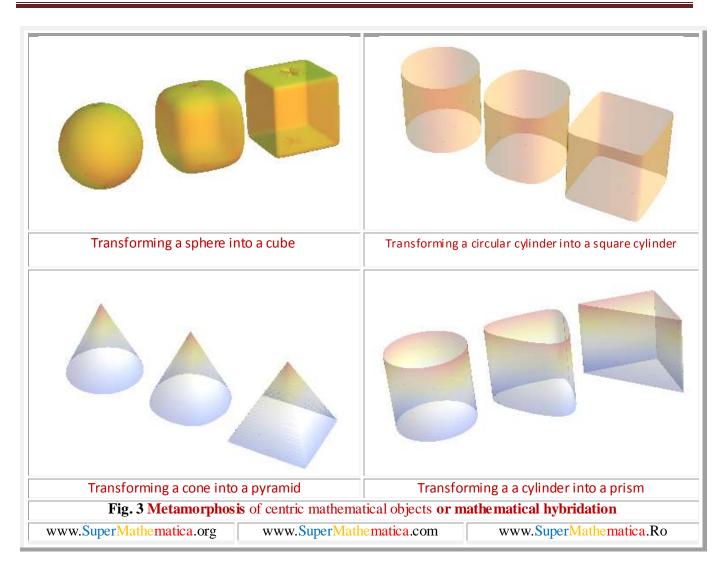
By modifying the eccentricity, the known and formed objects in the centric domain of the supermathematics (SM), that means, in centric mathematics (MC), can be deformed in the eccentric domain of the SM, therefore, in the eccentric mathematics (ME) and transformed, initially, in hybrid objects, proper to ME, and after that, to be re-transformed in other kind of objects, known in MC. As an example, by deforming a perfect **cone** ($\mathbf{s} = 0$) into a **cono-pyramid** [$\mathbf{s} \in (0, 1)$] with the base a perfect square and conical tip, which constitutes hybrid objects, placed between a cone and a pyramid, up to transforming it into a perfect **pyramid** ($\mathbf{s} = \pm 1$) with a perfect square base (Fig 3). In the fact, the object can be achieved by different machine works (see Mircea Şelariu, Cap.17 Dispozitive de prelucrare, PROIECTAREA DISPOZITIVELOR, EDP, București, 1982, coordonator Sanda-Vasii Roșculeț], by forming, (casting, syntering), deforming (at worm and cold), dislocation (cutting, chipping, erosion, grinding) and by aggregation (weldind and binding).

In both cases, **movements** of the tool and/or of the piece are needed, respectively, of the bright spot which delimitates a pixel on the screen and passes from a pixel to another.

The movement is strongly linked to space and time.

The mechanical movement can be of the:

- corps, and implicit, objects forming in time ;
- objects **position changing** in time, or of its parts, named corps, in relation to other corps, chosen as referentials.
- corps form changing in time, and implicit, of the objects form, by deforming them.



The Space reflects the coexistance relationship between objects and events, or parts of them, by indicating:

- their expansion/bigness, named gage dimmension;
- the objects **position**, through **linear coordinates X**, Y, Z, in 3D space, named **localization dimmensions**;
- the objects orientation, in 3D space, through the angular coordinates ψ , φ , θ , or A, B, C, named orientation dimmensions.
- the relative posititions or distances between the objects, named positioning dimmensions, if reffers to the absolute and/or relative orientation and localization of the objects, and if it reffers to parts of them, named corps, then they are named **coordination dimmensions**;
- the form of the objects and, respectively, the phenomena evolution, named forming dimmensions, which defines, at the same time, the objects defining equations;
- <u>the deformation</u> of the objects and phenomena evolution changing, named <u>dimmensions</u> <u>deformation</u> or <u>eccentricities</u>.

- The last space dimmension, eccentricity, by making possible the apparition of eccentric mathematics (EM) and by making the pass through from centric mathematics domain to the eccentric mathematics one, as well as the leap from a single mathematical entity, existant in Mathematics and in the centric domain, to an infinity of entities, of same kind, but more and more deformed, once the numerical's eccentricity value s is growing, up to their transformation in other kind of objects, also existent in the centric domain. An example, became already classical, is the continuous deforming of a sphere until it is transformed into a cube (Fig. 3), by using the same formation dimmensions (parametric equations), both for the sphere and for the cube, by changing only the eccentricity: being $\mathbf{s} = \mathbf{e} = 0$ for the sphere of radius R and $\mathbf{s} = \pm 1$, or $\mathbf{e} = \mathbf{R}$, for the cube of leg L = 2R.
- For $s \in [(-1, 1) \setminus 0]$ one obtain <u>hybrid objects</u>, proper for eccentric mathematics (EM), previously non-existant in mathematics, or, more specific, in Centric Mathematics (CM)
- As shown before, the straight line is an unidimmensional space, and, concurrently, in Supermathematics (SM), a bent of zero eccentricity [8].

By increasing the eccentricity, from zero to one, it transforms the straight line into o broken line, both existing and known in Centric Mathematics, but not the rest of the bents, which are proper to Eccentric Mathematics, being generated by FSM-CE eccentric amplitude. In this way, the straight line with angular coefficient $m = tan \alpha = tan \frac{\pi}{4} = 1$ which pass through the point P(2, 3) has the equation -3 = x - 2,

(2)(3)

and the bents family, from the same family with the straight line, has the equation

$$y [x, S(s, \varepsilon)] - y_0 = m \{aex [\theta, S(s, \varepsilon)] - x_0\},\$$

 $y - y_0 = m\{\theta - \arcsin[s.\sin(\theta - \varepsilon)]\} - x_0$, $m = \tan \alpha$,

in eccentric coordinates θ and, in centric coordinates α , the equation is

 $y[x, S(s, \varepsilon)] - y_0 = m (Aex [\theta, S(s, \varepsilon)] - x_0),$ (4)

(5)
$$y - y_0 = m \{ \alpha + \arcsin \frac{s.\sin(\alpha - \varepsilon)}{Rex\alpha} - x_0 \}, m = \tan \alpha$$

(6)
$$y - y_0 = m \{ \propto + \arcsin \frac{s.\sin(\alpha - \varepsilon)}{\sqrt{1 + s^2 - 2s.\cos(\alpha - \varepsilon)}} - x_0 \}$$

- The difference, for the two types of bents, of θ and of α , is that the θ ones are continueous only for the numerical eccentricity from the domain $s \in [-1, 1]$, while the α ones are continuous for all the values possible for s, it means $s \in [-\infty, +\infty]$.
- The broken line in known in Centric Mathematics (CM), but without knowing their equations! That in not the case anymore in SM and, obviously, in EM where it is obtained for the value s = 1 of the numerical eccentricity s.
- A similar phenomenon of mathematical metamorphosis, through which from CM a known object pass through the eccentric mathematics (EM) taking hybrid forms and returns in the centric mathematics (CM), as another type of object (Fig.3), is considerred to take place also in physics: from vacuum continuously appears particles and they return back into to vacuum. Are they the same or are they other ones?
- The cosmology has a theory which applies to the whole universe, enounced by Einstein in 1916: the General Relativity. It says that the gravitational force, which acts on the objects, acts also on the structure of space, which loses its rigid and immutable frame, becoming flexible and curved, depending of the contained matter or energy. In other words, the space is deforming.

The space-time continuum, of general relativity, is not conceived without a content, so it not admits the vacuum! As Einstein said to the journalists that beg him to resume his theory: "Before, one believed that, if all the things would disappear from the Universe, the space and time will still be here, whatever. In the

theory of general relativity, the time and space disappears, together with the disappearance of the other things from the Universe."

- As one said before, $\mathbf{s} = \mathbf{e} = 0$ is the world of CM, of the liniarity, of perfect, ideal entities, as long as the infinite possible values referable to the eccentrities \mathbf{s} and \mathbf{e} , give birth to EM and, at the same time, to worlds that belongs to to the reality, to the imperfect world, which are farther of the ideal world as \mathbf{s} and \mathbf{e} are farther from zero.
- What happens if $\mathbf{e} = \mathbf{s} \rightarrow 0$? The real world, as **EM** too, disappears, and because an ideal world cannot exist, everything disappears!
- As shown in the author's theory from SUPERMATEMATICA. Fundamente, Vol. I, Editura POLITEHNICA, Timişoara, Cap. 1 INTRODUCERE [23], [24], the expansion of the Universe is a process of developing the order into absolute chaos, a progressive passing-through of the chaotic space in a more and more pronounced order.
- As a conclusion, the space, and also the time, is **forming and deforming**, it means that the space eccentricity, of a certain value, takes to a space **forming**, and than, by modifying it's value, the space **deforms**/modifies itself.
- The modified form of the the space is depending on the value of the eccentricity, which becomes o new space dimmension: the deformation dimmension.

Installing an object for machining in the working space of a modern machine tool, with computer numerical control (CNC) is very similar with "installing" a mathematical object in the R^3 tridimmensional euclidian space. Therefore, we will further use some notions from technological domain.

In technology, **installing** is the operation that precedes machining; only an installed object / piece can be machined. This involves the next phases or technological operations, in this sequence / order; only achieving one phase makes possible to pass to the next phase:

1. ORIENTATION, is the action or the operation where the object's geometrical elements, which are orientation technological referential bases, shortly, orientation bases (OB), accept a well determined direction, regarding to the directions of a referential. In technology, this is regarding to the main and/or secondary working movements, and/or regarding the directions of dimmensional arrangement movements of the technological system.

As orientation bases (OB) one can use:

a) A plane of the object, respectively a flat surface of the piece, if it exists; in that case, this surface, determined by three contact points between the object and the device, is named emplacement of orientation technological referential base (EOB), or shortly, emplacement base (EB), being theoretically determined by the three mutual contact points of the piece with the device, which has the task to achieve the piece installing on the working machine. As EB, virtually, the most extended surface of the piece is chosen, if other positioning restrictions are not imposed, or that one from where the resulting surface after machining has the highest imposed precision, or parallelism constraints with EB.

By imposing the condition of mutual piece/device contact on **EB**, the object/piece loses 3 degrees of freedom, among them, a translation on the direction, let's name it **Z**, perpendicular on **EB** (a plane) and two rotations: around the **X** axis, noted in technology with **A**, and around the **Y** axis, noted in technology with **B**.

The object/piece can also be rotated around the Z axis, totation noted with C and can be translated on EB on X and Y directions, by permanently keeping contact with EB.

From this surface is established, in technology, the z coordinate, by example, as a distance between **EOB** and the machining technological base (**MTB**), or shortly, machining base (**MB**), that means the plane generated on the piece by the machining tool. In a surface is totally machined (by milling, as example, with large milling machines, for a single passage), then the other coordinates y and x can be established with a very large approximation, because they did not influence the plane surface precision achievement, at z distance of **EB**,

resulted after piece machining and named MTP or shortly, MP, whose technological demand is to be parallel to **EOB** and to be located at z distance from it.

The z dimmension, being, in this case, a **forming dimmension** of the piece, on the one hand and on the other hand also a **coordinating dimmension** for tool/piece relative position, and from <u>technological</u> point of view, one of the **dimmensional alignment dimmensions** of the technological system **MDPT** (Machine-Device-Piece-Tool). Mathematically speaking, it's about two surfaces situated at z distance, it means parallel planes.

b) A straight line belonging to the object, if it exists, as axes on/or edges, as intersection of plane surfaces in Mathematics.

In Techology, the edges are avoided, because their irregularities, in other words because the deviations from semifabricates linear geometrical shape, ond of the pieces too, after machining their semifabricates.

In Technology, this straight line is determined by the two points from a piece surface, other than **EB**, common to the piece and the device, which achieve the piece and device orientation base, as heteronymous elements, a straight line named conducting orientation base (**COB**) or shortly, conducting base (**CB**), name derived from the fact that these two conducting elements, conducts/guides the movement of the object/piece for its localization, if the contact piece/device is permanently maintaned during the movement. In this way, the **CB** takes over two degrees of freedom of the object: the translation on a direction perpendicular on the straight line determined by the two contact points between piece/device that materializes **CB**, ytanslation on Y axis, as example, if **CB** is always parallel, with the **EB** from **XOY** pane, and the rotation around **Z** axis, noted in technology with **C**.

As **COB** is chosen, on principle, it's easy to understand why, by aiming the guiding precision, the longest surface of the piece, if other reasons are not imposed by the execution drawing.

From **COB** can be established/measured the level/dimmension y, parallel to **EOB** and perpendicular on **COB**, as example, perpendicular on **z**, because **COB** is parallel with **EOB**.

Therefore, if the two points belongs to a parallelipipedical object, so bounded by plane surfaces, and **COB** is parallel with **EOB**, by maintaining the contact between piece/device on the two bases, by a translation movement, the piece can only be translated, in the device, on **X** direction, until it comes into collision with a **localization element**.

1) from this one, named localization element, namely localization technological base (LTB), or shortly, localization base (LB) can be established the x coordinate/dimmension perpendicular simultaneously on y and z. But without being coordinates/dimmensions/concurrent segments in a common point O(x,y,z) as in mathematics, only if COB and LTB drops to the level EOB, and, in addition, LTB moves toward COB and will be contained in it, both going to be contained in EOB, so the point O(x, y, z), as LTB will be a tip of the parallelipipedical piece, contained simultaneously in the EOB plane, the CB straight line in LB point, resulting, in this case, that $O(x,y,z) \equiv BL$

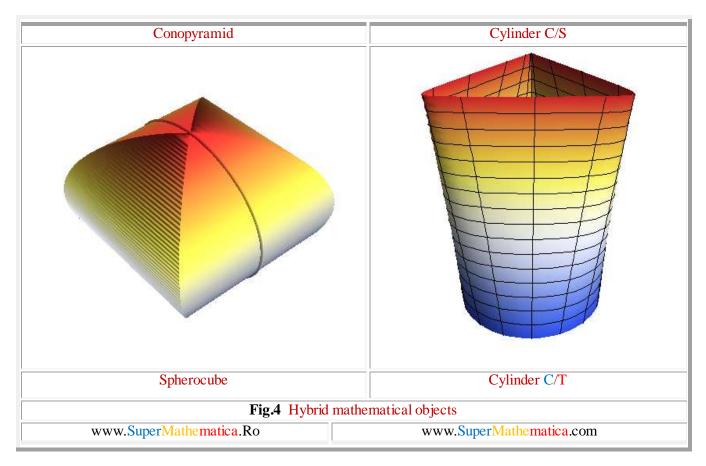
If the localization is achieved by a translation movement, as previously assumed, it is also named **translation localization (TL).**

If the localization is achieved through a rotational movement of the object, it is named **rotational localization (RL).** In this case, **CB** can be, or is, usually, a symmetry plane of the piece, by example a cylindric one, a plane named **semicentering orientation base (SCOB)**, in the case of a semicentering, or an axis of a rotational surface (cylindrical or spherical) of the object, named **Centering orientation base (COB)**, around whom the object rotates antil another corp of the piece come into collision with the rotation localization element. Or, until a locator gets into a muzzle perpendicular on **COB** or into a channel parallel with **COB**.

The objects which did not bring out **elements/orientation bases**, like the sphere in mathematics or the balls for ball bearings in technology, as example, are <u>non-orientational objects</u>.

<u>1.</u> <u>LOCALIZATION</u> is the operation or the action to establish the place, in E^3 tridimmensional euclidian space, of an O(x,y,z) point, characteristic for the object, which belongs to a orientating referential element

of this one, from whic one are established the coordinates/linear dimmensions x,y,z regarding a given referential system, or in technology, regarding the machining tool.



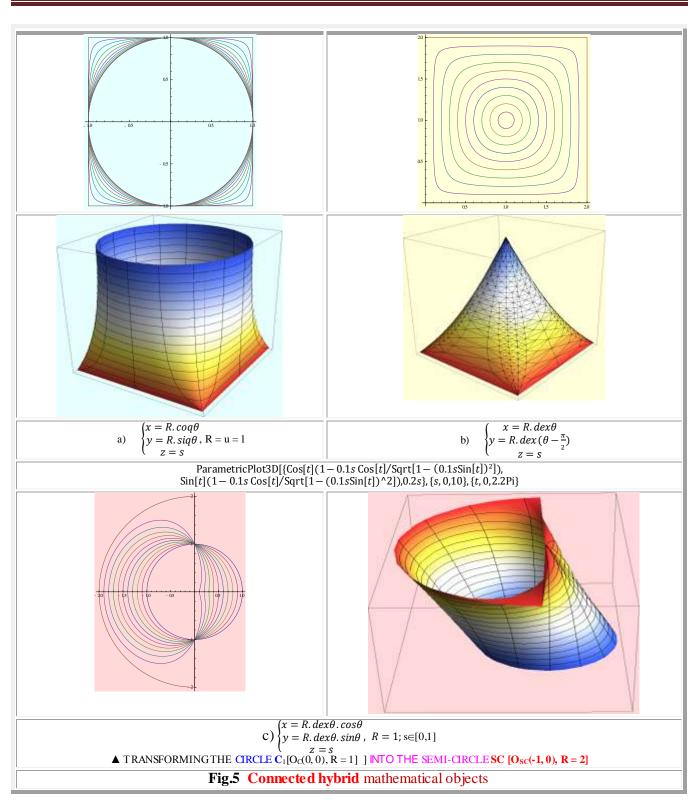
The O(x,y,z) point of the **non-orientational** objects is the symmetry center of them, and of the **orientational** objects, like the parallelipipedical ones, in Technology, as example, the O(x,y,z) point is disseminated in three distinctive points, for each coordinate apart, $Ox \subset LB$ for x, $Oy \subset CB$ for y si $Oz \subset EB$ for z, as explained before.

In the Technology, the succession orientation \rightarrow localization is compulsory; only an oriented object can be then located. Beside this, as in mathematics. First, one chose a reference system unitive with the **O(x,y,z)** object, and after that, an invariant one (**O**, **X**, **Y**, **Z**) which one, initially, coincide with the other one, in 3D space or in the E³ tridimmensional one, and then are operated various translation and/or rotation transformations.

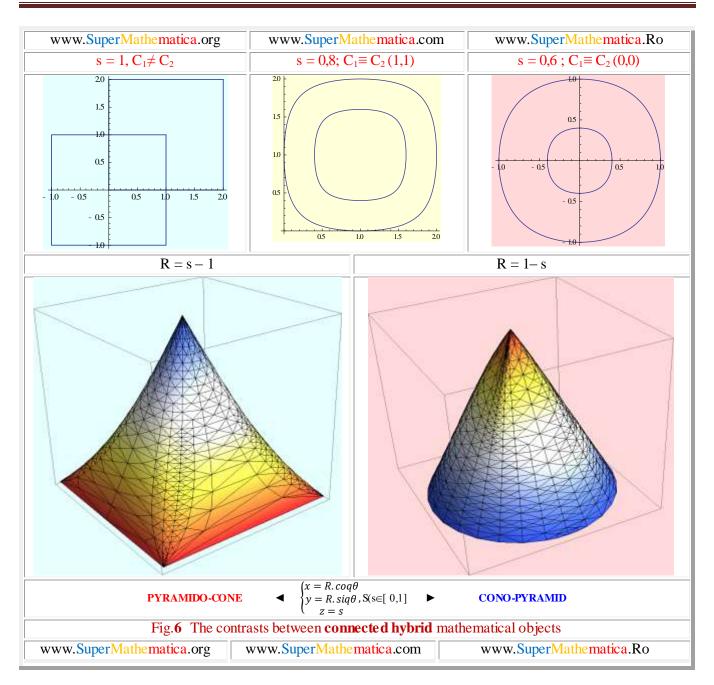
The union between orientation and localization represents the most important technological action/operation, named **pozitioning**, namely **orientation** \cup **localization** = **pozitioning**

If the object **pozitioning** is achieved/ finished/ fulfilled, then the relative position piece/device can be maintained by the operation of **anchorage** of the piece in the device.

Further, one can establish the distances/dimmensions between the tool and the piece, so one can obtain the piece of dimmensions and precizions imposed by the piece work drawing. This technological operation is named **dimmensional adjustment**. With this, the installing process is finished, and the machining of the piece can be started



Marian Niţu, Florentin Smarandache, Mircea Eugen Şelariu ECCENTRICITY, SPACE BENDING, DIMMENSION



Reductively, installing an object is an union of positioning with anchorage and dimmensional adjustment of the technological system, namely:

installing = pozitioning \cup anchorage \cup adjustment (dimmensional)

In Technology, **the adjustment** can be achieved by (fixing) **force** or by **form** (which blocks the piece displacement during the machining). In Mathematics, the anchorage is "achieved" by **convention.**

By telling that the (O, x,y,z) system is linked to the piece, it cannot move anymore relative to the piece, but only together with the object, so they are "bonded" each other. Therefore, in Mathematics, the anchorage of

the elements relative to the reference systems, is a matter of course, it doesn't exist anymore, because in mathematics doesn't exist "mathematical forces". These belonging to the Mechanics, namely it's dynamics, also in mathematics doesn't exist machining tools, neither various coordinating dimmensions, dimmensional adjustments, dimmensional machining, etc.

Therefore, in Centric mathematics (CM), only 3 \mathbf{x} , \mathbf{y} and \mathbf{z} linear dimmensions exists, which are, at the same time, forming dimmensions of the 3D objects, by their parametric equations, by example.

Reductively, in this Centric mathematics (CM), entities as straight line, the square, the circle, the sphere, the cube e.a., are uniques, while in the Eccentric Mathematics (EM), and implicit, in Supermathematics (SM), they are infinitely multiplied through hybridation, a hybridation possible by introducing of a new space dimmension, the eccentricity.

The supermathematical Hybridation can be defined as the mathematical process of "cross-breeding" of two mathematical entities from CM (the circle, and the square, the sphere and the cube, the cone and the pyramid) and obtaining of a supermathematical <u>new entity</u> in EM, which is unknown/non-existant in CM (by example: cono-pyramid).

Through <u>metamorphosis</u> one understand a continuous passing from from a certain entity, existing in CM, to another entity, also existing in CM, through an infinity of hybrid entities, appropriates only to EM. In other words, transforming a centric mathematical entity into another centric mathematical entity, an action that became possible inside the Eccentric mathematics (EM), by using supermathematical functions.

By <u>metamorphosis</u> one obtain new entities, previously non-existant in **CM**, named **hybrid entities**, and also **eccentric** entities, or **supermathematical (SM**), to differ the centric ones, also by name, because **by form**, they are essentially different.

The first object obtained through **mathematical hybridation** was the **cono-pyramid**: a supermathematical corp with the square base of a pyramid and the tip of a circular cone, resulting from the transformation of the unity square of L=2 into the unity circle of R=1 and/or viceversa (Fig. 4). The parametric equations of the cono-pyramid are obtained from the parametric equations of right circular cone, where the FCC are changed/converted with the corresponding quadrilobe supermathematical functions (FSM-Q).

$$\begin{cases} x = u. \cos \theta = u. \frac{\cos \theta}{\sqrt{1 - s^2. \sin^2 \theta}} \\ y = u. \sin \theta = u. \frac{\sin \theta}{\sqrt{1 - s^2. \cos^2 \theta}} \\ z = u \end{cases} \quad for \quad \begin{cases} u = 1 - s, \quad s \in [0, \quad 1] \triangleright CONO - PIRAMIDĂ \\ u = s - 1, \quad s \in [0, \quad 1] \triangleright PIRAMIDO - CON \\ u = 1; \quad s = 1 \triangleright PĂTRAT; \quad L = 2 \\ u = 1; \quad s = 0 \quad \triangleright CERC; \quad R = 1 \\ u = 1; \quad s \in [0, \quad 1] \triangleright CILINDRU \quad C/P \end{cases}$$

(Fig. 1, Fig. 3 și Fig. 5,a), because FSM-Q can achieve the continuous transformation of the circle into a square and viceversa, also as FSM-CE eccentric derivate $dex_{1,2}\theta$

(7)
$$\begin{cases} x = u. \, dex\theta = u\left[1 - \frac{s.\cos(\theta - \varepsilon)}{\sqrt{1 - s^2 sin^2(\theta - \varepsilon)}}\right] \\ y = u. \, dex\left(\theta - \frac{\pi}{2}\right) = u\left[1 - \frac{s.\cos(\theta - \varepsilon - \frac{\pi}{2})}{\sqrt{1 - s^2 sin^2(\theta - \varepsilon - \frac{\pi}{2})}}\right]^p entru \begin{cases} u = 1; \ s = 0 \triangleright CON \\ u = 1, \ s = 1 \triangleright PIRAMIDĂ \\ u = s \in [0, 1] \triangleright CONOPIRAMIDĂ \\ u = 1; \ s \in [0, 1] \triangleright Fig \mathbf{5}, \mathbf{c} \end{cases}$$

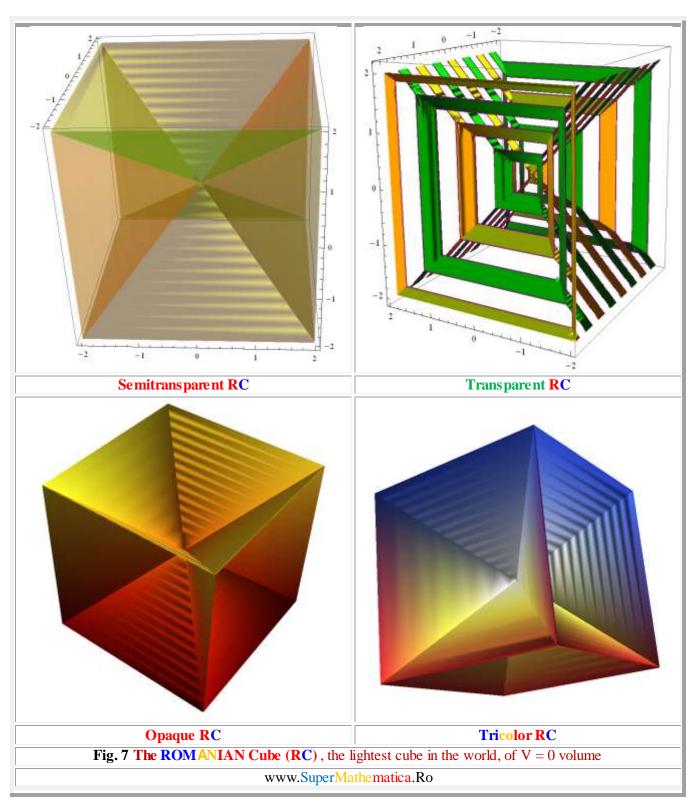
(**Fig. 4** și **Fig. 5,b și Fig. 5,c**).

The relations (7) are expressed with the help of quadrilobes **FSM-Q**, introduced in Mathematics since 2005, in the work [19], quadrilobe cosine $coq\theta$ and quadrilobe sine $siq\theta$.

The (7) and (8) equations express the same forms, but with following remarks:

- Of a circle only for an eccenter $S(s = 0, \varepsilon = 0)$, with the difference that the first one (7) has the radius R = 1, and the other one (8) has the radius R = 0, Fig. 6, up \blacktriangle ;
- Of a square for an eccenter S (s = 1, ε = 0), of the same dimmensions L = 2R, as one can see in the figure **6**, but centered in different points; one is centered in the origin O(0, 0), the one expressed by the

Marian Niţu,Florentin Smarandache,Mircea Eugen ŞelariuECCENTRICITY, SPACE BENDING, DIMMENSION



- relations (7), and the other one is ex-centered, centered eccentrical relative to the origin O(0, 0)- in the point C(1,1);
- Of a quadrilobe (neither circle and neither square, namely an infinity of hybrid forms, between circle and square). For the same numarical eccentricity s ∈ (0, 1), which caracterizes the matematical excenter (ME) domain, they has the same forms, but are of different dimmensions; the first one, having higher dimmensions then those expressed with dexθ function, what can be concluded also from the figure 5,b from 2D.

One can see that the dimmension of the quadrilobes expressed by the relation (8) by dex θ decrease as eccentricity increase.

The romanian cube from the **Fig 7**, "**the lightest cube of the world**", is the cube with zero volume, obtained from 6 pyramids, without their square base surfaces, with the common tip in the cube's symmetry center.

In this case, the pyramid was expressed through the relations (7), by quadrilobe functions of s=1. As a conclusion, **supermatematics** offer multiple possibilities to express different mathematical entities from **center mathematics** (**CM**), and, at the same time, an infinity of hybrid entities from the **eccentric mathematics** (**EM**).

BIBLIOGRAFIE

IN DOMENIUL SUPERMATEMATICII

1	Şelariu Mircea Eugen	FUNCȚII CIRCULARE EXCENTRICE	Com. I Conferință Națională de Vibrații în Construcția de Mașini, Timișoara, 1978, pag.101108.
2	Şelariu Mircea Eugen	FUNCȚII CIRCULARE EXCENTRICE ȘI EXTENSIA LOR.	Bul .Şt.şi Tehn. al I.P. "TV" Timişoara, Seria Mecanică, Tomul 25(39), Fasc. 1-1980, pag. 189196
3	Şelariu Mircea Eugen	STUDIUL VIBRAȚIILOR LIBERE ALE UNUI SISTEM NELINIAR, CONSERVATIV CU AJUTORUL FUNCȚIILOR CIRCULARE EXCENTRICE	Com. I Conf. Naț. Vibr.în C.M. Timișoara,1978, pag. 95100
4	Şelariu Mircea Eugen	APLICAȚII TEHNICE ALE FUNCȚIILOR CIRCULARE EXCENTRICE	Coma IV-a Conf. PUPR, Timişoara, 1981, Vol.1. pag. 142150 A V-a
5	Şelariu Mircea Eugen	THE DEFINITION of the ELLIPTIC ECCENTRIC with FIXED ECCENTER	Conf. Naț. de Vibr. în Constr. de Mașini,Timișoara, 1985, pag. 175 182
6	Şelariu Mircea Eugen	ELLIPTIC ECCENTRICS with MOBILE ECCENTER	Com.a IV-a Conf. PUPR, Timişoara, 1981, Vol.1. pag. 183188
7 8	Şelariu Mircea Eugen Şelariu Mircea	CIRCULAR ECCENTRICS and HYPERBOLICS ECCENTRICS ECCENTRIC LISSAJOUS FIGURES	Com. a V-a Conf. Naţ. V. C. M. Timişoara, 1985, pag. 189194. Com.a IV-a Conf. PUPR, Timişoara,
9	Eugen Şelariu Mircea Eugen	FUNCȚIILE SUPERMATEMATICE cex ȘI sex- SOLUȚIILE UNOR SISTEME MECANICE NELINIARE	1981, Vol.1. pag. 195202 Com. a VII-a Conf.Nat. V.C.M., Timişoara,1993, pag. 275284.
10	Şelariu Mircea Eugen	<u>SUPERMATEMATICA</u>	Com.VII Conf. Internaţ. de Ing. Manag. şi Tehn.,TEHNO'95 Timişoara, 1995, Vol. 9: Matematicπ Aplicată, pag.4164

11	Şelariu Mircea Eugen	FORMA TRIGONOMETRICĂ A SUMEI SI A DIFERENȚEI NUMERELOR COMPLEX E	Com.VII Conf. Internat. de Ing. Manag. și Tehn., TEHNO'95 Timișoara, 1995, Vol. 9: Matematică Aplicată, pag. 6572 Com.VII Conf. Internaț. de Ing.
12	Şelariu Mircea Eugen	MIȘ CAREA CIRCULARĂ EXCENTRICĂ	Manag. și Tehn. TEHNO'95., Timișoara, 1995 Vol.7: Mecatronică, Dispozitive și Rob.Ind.,pag. 85102 Com.VII Conf. Internaț. de Ing.
13	Şelariu Mircea Eugen	RIGIDITATEA DINAMICĂ EXPRIMATĂ CU FUNCȚII SUPERMATEMATICE DETERMINAREA ORICÂT DE EXACTĂ	Manag. și Tehn., TEHNO'95 Timișoara, 1995 Vol.7: Mecatronică, Dispoz. și Rob.Ind., pag. 185194 Bul. VIII-a Conf. de Vibr. Mec.,
14	Şelariu Mircea Eugen	A RELAȚIEI DE CALCUL A INTEGRALEI ELIPTICE COMPLETE DE SPETA ÎNTÂIA K(k)	Timișoara,1996, Vol III, pag.15 24
15	Şelariu Mircea Eugen	FUNCȚII SUPERMATEMATICE CIRCULARE EXCENTRICE DE VARIABILĂ CENTRICĂ	TEHNO ' 98. A VIII-a Conferință de inginerie menagerială și tehnologică, Timișoara 1998, pag 531548
16	Şelariu Mircea Eugen	FUNCȚII DE TRANZIȚIE INFORMAȚIONALĂ	TEHNO ' 98. A VIII-a Conferință de inginerie menagerială și tehnologică , Timișoara 1998, pag 549 556
17	Şelariu Mircea Eugen	FUNCȚIILE SUPERMATEMATICE CIRCULARE EXCENTRICE DE VARIABILA CENTRICA CA SOLUȚII ALE UNOR SISTEME OSCILANTE NELINIARE	TEHNO ' 98. A VIII-a Conferință de inginerie menagerială și tehnologică , Timișoara 1998, pag 557572
18	Şelariu Mircea Eugen	INTRODUCEREA STRÂMBEI ÎN MATEMATICĂ	Lucr. Simp. Național "Zilele Universității Gh. Anghel" Ed. II-a, Drobeta Turnu Severin, 16-17 mai 2003, pag. 171 178 The 11 –th International Conference on
19	Şelariu Mircea Eugen	QUADRILOBIC VIBRATION SYSTEMS	Vibration Engineering, Timişoara, Sept. 27-30, 2005 pag. 77 82
20	Şelariu Mircea Eugen	SMARANDACHE STEPPED FUNCTIONS	International Journal "Scientia Magna" Vol.3, Nr.1, 2007, ISSN 1556-6706
21	Şelariu Mircea Eugen	TEHNO-ART OF ȘELARIU SUPERMATHEMATICS FUNCTIONS	(ISBN-10):1-59973-037-5 (ISBN-13):974-1-59973-037-0 (EAN): 9781599730370
22	Şelariu Mircea Eugen	PROIECTAREA DISPOZITIVELOR DE PRELUCRARE, Cap. 17 din PROIECTAREA DISPOZITIVELOR	Editura Didactică și Pedagogică, București, 1982, pag. 474 543 Coord onator Vasii Roșculeț Sanda
23	Şelariu Mircea Eugen	SUPERMATEMATICA. FUNDAMENTE	Editura "POLITEHNICA", Timişoara, 2007
24	Şelariu Mircea Eugen	<u>SUPERMATEMATICA.</u> <u>FUNDAMENTE VOL.I EDIȚIA A II-A</u>	Editura "POLITEHNICA", Timișoara, 2012
25	Şelariu Mircea Eugen	SUPERMATEMATICA. FUNDAMENTE VOL.II	Editura "POLITEHNICA", Timişoara, 2012
26	Şelariu Mircea Eugen	TRANSFORMAREA RIGUROASA IN CERC A DIAGRAMEI POLARE A COMPLIANȚEI	Buletiul celei de a X-a Conf. de Vibr. Mec.cu participare interatională, Bul. Șt. al Univ. "Politehnica" din Timșoara,

			Seria Mec. Tom 47(61), mai 2002, Vol II, pag.247260.
27	Şelariu Mircea Eugen	UN SISTEM SUPERMATEMATIC CU BAZĂ CONTINUĂ DE APROXIMARE A FUNCȚIILOR	www.CartiAZ.ro
28	Şelariu Mircea Eugen	DE LA REZOLVAREA TRIUNGHIURILOR LA FUNCȚII SUPERMATEMATICE (SM)	www.CartiAZ.ro
29	Şelariu Mircea Eugen	FUNCȚIILE SUPERMATEMATICE CIRCULARE COSINUS ȘI SINUS EXCENTRICE (FSM-CE cexθ	www.CartiAZ.ro
	Lugon	SI sexθ) DE VARIABLĂ EXCENTRICĂ θ, DERIVATELE ȘI	
30	Şelariu Mircea	INTEGRALELE LOR LOBE EXTERIOARE ȘI CVAZILOBE	www.CartiAZ.ro
50	Eugen	INTERIOARE CERCULUI UNITATE	www.carthitz.io
31	Şelariu Mircea Eugen	METODĂ DE INTEGRARE PRIN DIVIZAREA DIFERENȚIALEI	www.CartiAZ.ro
32	Şelariu Mircea	FUNCȚII COMPUSE AUTOINDUSE (FAI) ȘI	www.CartiAZ.ro
33	Eugen Şelariu Mircea	FUNCȚII INDUSE (FI) FUNCȚII SUPERMATEMATICE	www.CartiAZ.ro
55	Eugen	CIRCULARE EXCENTRICE INVERSE (FSM-CEI)	www.cattinz.io
34	Şelariu Mircea Eugen	FUNCȚII HIPERBOLICE EXCENTRICE	www.CartiAZ.ro
35	Şelariu Mircea Eugen	ELEMENTE NELINIARE LEGATE ÎN SERIE	www.CartiAZ.ro
36	Şelariu Mircea Eugen	I NTERSECȚII ÎN PLAN	www.CartiAZ.ro
37	Şelariu Mircea Eugen	LINIILE CONCURENTE ȘI PUNCTELE LOR DE INTERSECȚIE ÎNTR-UN TRIUNGHI	www.CartiAZ.ro
38	Şelariu Mircea Eugen	MIȘ CAREA CIRCULARĂ EXCENTRICĂ DE EXCENTRU PUNCT MOBIL	www.CartiAZ.ro
39	Şelariu Mircea	TEOREMELE POLIGOANELOR	www.CartiAZ.ro
	Eugen	PĂTRĂTE, DREPTUNGHIURI ȘI TRAPEZE ISOSCELE <mark>Ș</mark>	
40	Şelariu Mircea Eugen	UN SISTEM SUPERMATEMATIC CU BAZĂ CONTINUĂ DE APROXIMARE A FUNCȚIILOR	www.CartiAZ.ro
41	Şelariu Mircea Eugen	FUNCȚIILE SM– CE rex _{1,2} θ CA SOLUȚII ALE ECUAȚIILOR ALGEBRICE	www.CartiAZ.ro
	Lugen	DE GRADUL AL DOILEA CU O SINGURĂ NECUNOSCUTĂ	
42	Şelariu Mircea	TEOREMA § A BISECTOARELOR UNUI	www.CartiAZ.ro
	Eugen	PATRULATER INSCRIPTIBIL ȘI TEOREMELE Ș ALE TRIUNGHIULUI	
43	Petrișor	ON THE DYNAMICS OF THE DEFORMED	Workshop Dynamicas Days'94, Budapest, și Analele Univ.d in
	Emilia	STANDARD MAP	Timişoara, Vol.XXXIII, Fasc.1-1995, Seria MatInf.,pag. 91105
44	Petrișor Emilia	SISTEME DINAMICE HAOTICE	Seria Monografii matematice, Tipografia Univ. de Vest din Timişoara, 1992
		RECONECTION SCENARIOS AND THE	1 miş0ala, 1772

45	Petrișor Emilia	THRESHOLD OF RECONNECTION IN THE DYNAMICS OF NONTWIST MAPS NON TWIST AREA PRESERVING MAPS WITH	Chaos, Solitons and Fractals, 14 (2002) 117-127 International Journal of Bifurcation and
46	Petrișor Emilia	REVERSING SYMMETRY GROUP	Chaos, Vol.11, no 2(2001) 497-511 Proceedings of the Scientific
47	Cioara Romeo	FORME CLASICE PENTRU FUNCȚII CIRCULARE EXCENTRICE	Communications Meetings of "Aurel Vlaicu" University, Third Edition, Arad, 1996, pg.61 65
48	Preda Horea	REPREZENTAREA ASISTATĂ A TRAIECTORILOR ÎN PLANUL FAZELORA VIBRAȚIILOR NELINIARE	Com. VI-a Conf.Naţ.Vibr. în C.M. Timișoara, 1993, pag.
49	Filipescu Avram	APLICAREA FUNCȚIILOR EXCENTRICE PSEUDOHIPERBOLICE (EXPH) ÎN TEHNICĂ	Com.VII-a Conf. Internat.de Ing. Manag. și Tehn. TEHNO'95, Timișoara, Vol. 9. Matematică aplicată, pag. 181 185
50	Drago mir Lucian	UTILIZAREA FUNCȚIILOR SUPERMATEMATICE IN CAD / CAM : SM-CAD / CAM. Nota I-a: REPREZENTARE ÎN 2D	Com. VII-a Conf. Internaț.de Ing. Manag. și Tehn. TEHNO'95, Timișoara, Vol. 9. Matematică aplicată, pag. 83 90
51	Şelariu Şerban	UTILIZAREA FUNCȚIILOR SUPERMATEMATICE IN CAD / CAM : SM-CAD / CAM. Nota I I -a: REPREZENTARE ÎN 3D	Com. VII-a Conf. Internaţ.de Ing. Manag. şi Tehn. TEHNO'95, Timişoara, Vol. 9. Matematică aplicată., pag. 91 96
52	Staicu Florențiu	DISPOZITIVE UNIVERSALE de PRELUCRARE a SUPRAFEȚELOR COMPLEXE de TIPUL EXCENTRICELOR ELIPTICE THE ECCENTRIC TRIGONOMETRIC	Com. Ses. anuale de com.şt. Oradea ,1994 The University of Western Ontario,
53	George LeMac	FUNCTIONS: AN EXTENTION OF CLASSICAL TRIGONOMETRIC FUNCTIONS.	London, Ontario, Canada Depertment of Applied Mathematics May 18, 2001
54	Şelariu Mircea Ajiduah Cristoph Bozântan Emil Filipescu Avram	INTEGRALELE UNOR FUNCȚII SUPERMATEMATICE	Com. VII Conf.Internaţ. de Ing.Manag. şi Tehn. TEHNO'95 Timişoara. 1995, Vol.IX: Matem. Aplic. pag.7382
55	Şelariu Mircea Fritz Georg Meszaros A.	ANALIZA CALITĂȚII MIȘ CARILOR PROGRAMATE cu FUNCȚII S UPERMATEMATICE	IDEM, Vol.7: Mecatronică, Dispozitive și Rob.Ind., pag. 163184
56	Şelariu Mircea Szekely Barna	ALTALANOS SIKMECHANIZMUSOK FORDULATSZAMAINAK ATVITELI FUGGVENYEI MAGASFOKU MATEMATIKAVAL	Bul.Șt al Lucr. Premiate, Universitatea din Budapesta, nov. 1992
57	Şelariu Mircea Popovici Maria	A FELSOFOKU MATEMATIKA ALKALMAZASAI	Bul.Șt al Lucr. Premiate, Universitatea din Budapesta, nov. 1994
58	Smarandache Florentin Şelariu Mircea Eugen	IMMEDIATE CALCULATION OF SOME POISSON TYPE INTEGRALS USING SUPERMATHEMATICS CIRCULAR EX-CENTRIC FUNCTIONS	arXiv:0706.4238, 2007

59	Konig Mariana Şelariu Mircea	PROGRAMAREA MIȘ CARII DE CONTURARE A ROBOȚILOR INDUSTRIALI cu AJUTORUL FUNCȚIILOR TRIGONOMETRICE CIRCULARE EXCENTRICE	MEROTEHNICA, Al V-lea Simp. Naț.de Rob.Ind.cu Part .Internaț. Bucuresti, 1985 pag.419425
60	Konig Mariana Şelariu Mircea	PROGRAMAREA MIȘCĂRII de CONTURARE ale R. I. cu AJUTORUL FUNCȚIILOR TRIGONOMETRICE CIRCULARE EXCENTRICE	Merotehnica, V-lea Simp. Naţ.de RI cu participare internatională, Buc.,1985, pag. 419 425.
61	Konig Mariana Selariu Mircea	THE STUDY OF THE UNIVERSAL PLUNGER IN CONSOLE USING THE ECCENTRIC CIRCULAR FUNCTIONS	pag. 419 425. Com. V-a Conf. PUPR, Timişoara, 1986, pag. 3742
62	Staicu Florentiu Şelariu Mircea	CICLOIDELE EXPRIMATE CU AJUTORUL FUNCȚIEI SUPERMATEMATICE rexθ	Com. VII Conf. Internatională de Ing.Manag. și Tehn ,Timișoara "TEHNO'95''pag.195-204
62	Gheorghiu Em. Octav Şelariu Mircea	FUNCȚII CIRCULARE EXCENTRICE DE SUMĂ DE ARCE	Ses.de com.șt.stud.,Secția Matematică,Timișoara, Premiul II la Secția Matematică, 1983
64	Bozântan Emil Gheorghiu Emilian Octav Şelariu Mircea Cojerean	FUNCȚII CIRCULARE EXCENTRICE. DEFINIȚII, PROPRIETĂȚI, APLICAȚII TEHNICE	Ses. de com. șt.stud. Secția Matematică, premiul II la Secția Matematică, pe anul 1985.
65	Ovidiu Şelariu Mircea Eugen, Bălă Dumitru	WAYS OF PRESENTING THE DELTA FUNCTION AND AMPLITUDE FUNCTION JACOBI	Proceedings of the2nd World Congress on Science, Economics and Culture, 25-29 August 2008 New York, paper published in Denbridge Journals, p.42 55
66	Du mit ru Bă lă	SUPERMATHEMATICAL – ŞELARIU FUNCTIONS BETA ECCENTRIC bex θ SOLUTIONS OF SOME OSCILATORY NON-LINIAR SYSTEMS (SO β)	Proceedings of the2nd World Congress on Science, Economics and Culture, 25-29 August 2008 New York, paper published in Denbridge Journals, p.27 41
67	Şelariu Mircea Eugen Smarandache Florentin	CARDINAL FUNCTIONS AND INTEGRAL FUNCTIONS	International Journal of Geometry Vol.1 (2012), NO. 1, 5-14

Florentin Niţu Marian