

On the hierarchy of objects

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Abstract

The objects that occur in nature can be categorized in several levels. In this collection every level except the first level is built from lower level objects. This collection represents a simple model of nature. The model exploits the possibilities that mathematical concepts provide. Also typical physical ingredients will be used.

The paper splits the hierarchy of objects in a logic model and a geometric model. These two hierarchies partly overlap.

The underlying Hilbert Book Model is a simple self-consistent model of physics that is strictly based on quantum logic. This paper refines quantum logic to Hilbert logic such that it more directly resembles its lattice isomorphic companion, which is a separable Hilbert space. The HBM extends these sub-models into a dynamic model that consists of a sequence of the sub-models.

The paper is founded on three starting points: • A sub-model in the form of traditional quantum logic that represents a static status quo. • A correlation vehicle that establishes cohesion between subsequent members of a sequence of such sub-models. • The cosmological principle.

Further it uses a small set of hypotheses. It turns out that the cosmological principle is already a corollary of the first two points.

The paper explains or indicates the explanation of all features of fundamental physics that are encountered in the discussed hierarchy which ranges from propositions about physical objects until composites of elementary particles. Amongst them are the cosmological principle, the existence of quantum physics, the existence of a maximum speed of information transfer, the existence of physical fields, the origin of curvature, the origin of inertia, the dynamics of gravity, the existence of elementary particles, the existence of generations of elementary particles and the existence of the Pauli principle.

No model of physics can change physical reality.

Any view on physical reality involves a model

Drastically different models can still be consistent in themselves.

The Hilbert Book Model is a simple self-consistent model of physics.

This model steps with universe-wide progression steps from one sub-model to the next one. Each of these sub-models represents a static status quo of the universe.

The sub-models are strictly based on traditional quantum logic

The HBM is a pure quaternion based model. Conventional physics is spacetime based. When both models are compared, then the progression quantity (which represents the page number in the Hilbert Book model) corresponds to proper time in conventional physics.

The length of a smallest quaternionic space-progression step in the HBM corresponds with an "infinitesimal" coordinate time step in conventional physics.

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*The "secret" of physics is the way that it enumerates its countable sets,
such that these approach a corresponding continuum.*

1 Introduction

I present you my personal view on the hierarchy of objects that occur in nature. Only the lowest levels are extensively treated. Composite particle objects are treated in a more general way. Cosmology is touched.

The paper is founded on three starting points:

- A sub-model in the form of traditional quantum logic that represents a static status quo.
- A correlation vehicle that establishes cohesion between subsequent members of a sequence of such sub-models.
- The cosmological principle.

Further it uses a small set of hypotheses. It turns out that the cosmological principle is already a corollary of the first two points.

This hierarchy model is in concordance with the Hilbert Book Model¹. Since the HBM is strictly based on the axioms of traditional quantum logic, the same will be the case for the logic part of the object hierarchy model. The Hilbert Book Model gets its name from the fact that traditional quantum logic can only represent a static status quo and for that reason dynamics must be represented by an ordered sequence of these static models. The similarity with a sequence of pages and a book is obvious.

The object hierarchy model adds two fundamental starting points. First, a correlation vehicle must provide the cohesion between the subsequent members of the sequence. Second, the model must obey the cosmological principle.

The cosmological principle means that at large scales, universe looks the same for whomever and wherever you are. One of the consequences is that at larger scales universe possesses no preferred directions. It is *quasi-isotropic* (on average isotropic).

This paper is part of the ongoing HBM project. Many of the mathematical concepts that are touched here are treated in greater depth in Q-Formulæ: <http://vixra.org/abs/1210.0111>

The HBM refines quantum logic to Hilbert Logic. A Hilbert logic system resembles a separable Hilbert space much closer than quantum logic does. Hilbert logic is treated in more detail in a separate document <http://vixra.org/abs/1302.0149> .

¹ <http://vixra.org/abs/1209.0047>

The paper explains² all features of fundamental physics that are encountered in the discussed hierarchy which ranges from propositions about physical objects until elementary particles. Amongst them are the cosmological principle, the existence of quantum physics, the existence of a maximum speed of information transfer, the existence of physical fields, the origin of curvature, the origin of inertia, the dynamics of gravity, the existence of elementary particles, the existence of generations of elementary particles, the existence of the Pauli principle and the history of the universe.

² Or it indicates a possible explanation

2 General notes

2.1 Measurability and perceptibility

The first priority of the HBM is to understand how this model works and it is not her task to verify whether nature behaves that way. This is compensated by pursuing a strong degree of self-consistence of the model. At the same time the knowledge of how nature works is a guide in the development of the model.

For example the HBM uses proper time instead of coordinate time. The HBM does not bother about the fact that in general proper time cannot practicably be measured. The model includes lower level objects that cannot be observed as individuals. Only as groups these objects become noticeable.

The result of this target specification is that the HBM introduces its own methodology that often deviates considerably from the methodology of contemporary physics. As a consequence the HBM must be reluctant in comparing these methodologies and in using similar names. Confusions in discussion groups about these items have shown that great care is necessary. Otherwise, the author can easily be accused from stealing ideas from other theories that are not meant to be included in the HBM model.

This again will make it difficult to design measurements. Measuring methods are designed for measuring physical phenomena that are common in contemporary physics. This is best assured when is sought for phenomena that are similar between the model and contemporary physics. This action contradicts the caution not to use similar terms and concepts.

On the other hand, also contemporary physics contains items that cannot be measured. For example color charge is an item that cannot (yet) be measured. Proper time is a concept that also exists in contemporary physics, but in general it cannot be measured. Contemporary physics uses the field concept, but except for the cases that the fields are raised by properties of separate particles contemporary physics does not bother what causes the field.

2.2 Generators, spread and descriptors.

The generators produce a group of discrete objects that are spread over space. The density distribution and the current density distribution of these spreads are continuous functions that describe the spreads. A non-uniform spread of objects can influence space curvature. This holds when the objects are a kind of location pickets. Thus indirectly the generator may influence space curvature. The descriptors can only describe space curvature. The density distributions correspond to potential functions. The generator can be described by the convolution of a sharp continuous function and a low scale spread function. In this way, the spreading part can be seen as the activator of local space curvature, while the derivative of the sharp part defines a local metric that can be considered as the descriptor of the local curvature. The two parts must be in concordance. In this way two kinds of descriptors of local curvature exist. The first is the density distribution that describes the spread of the discrete objects. The second descriptor is the local metric.

The **origin of the local curvature** is the stochastic process that produces the low scale spread of the discrete objects. The HBM suggests the combination of a Poisson process that is coupled to a binomial process, where the attenuation of the binomial process is implemented by a 3D spread function³.

The stochastic generator process will generate according to a standard plan. Thus at each location where it is active it produces locally in principle the same kind of patterns. However, these patterns cause space curvature and due to the variance in space curvature, the center location of the pattern may move. Both effects disturb the natal state of the distributions that are generated by the generating process. Since the patterns are generated with a single element per progression step, the generation poses a large chance to not generate the target natal shape but instead a distorted shape that in addition is spread over the path that the center location decides to follow. The produced distribution can still be described by a continuous function, but that function will differ from the continuous function that describes the undisturbed natal state. So the generation process is characterized by two functions. The first one represents the characteristics of the local generation process. It describes the natal state of the intended distribution. It is more a prospector than a descriptor. The second one describes the actually produced distribution that is distorted by the local space curvature and spread out by the movement of the center location. Further the generation of the distribution may not be completely finished, because not enough elements were generated since the generation of the pattern was started. The generated element only lives during the current progression step. In the next step a newly generated element replaces the previous object. At any instant the generated distribution consists of only one element. Thus for its most part the distribution can be considered as a set of virtual elements that lived in the past or will live in the future. The virtual distribution together with its current non-virtual element represents a pattern. The local curvature is partly caused by the pattern itself, but for another part it is caused by neighbor patterns.

Nobody said that the undercrofts of physics behave in a simple way!

2.3 Coupling and events

The HBM introduces the notion of **coupling** of fields. It also means that a state of not being coupled exists. Coupling is described by a **coupling equation**, which is a special kind of **differential continuity equation**⁴.

Coupling takes place between **stochastic fields**. Stochastic fields describe **density distributions** and **current density distributions** of **lower order objects**. The distributions are generated by a local generation process that in each progression step produces ONE lower order object per stochastic field.

The generating process can chose to generate in configuration space or in the canonical conjugated momentum space. At the instant of an **event** the generator changes its **mode**. A change of mode means a switch between being coupled and not being coupled or vice versa. A **free** (non-coupled) stochastic field is generated in momentum space.

³ See: The enumeration process.

⁴ See: Differential equations

Being compactly generated in a given space does not mean that nothing will appear in the canonically conjugated space. However, the Fourier transform of the compact distribution is widely spread in the canonically conjugated space. The influence of the compact distribution on local curvature in the first space is far larger than the influence on local curvature in the second space where the corresponding distribution is spread over a large area⁵. Further, at every instant only a single element of the distribution exists. That element is a point-like. Its Fourier transform is flat. The information about the existence of the element will be transmitted over the full configuration space. That transmission has not finished after the disappearance of the generated element. This will happen with all elements of the distribution.

Coupling becomes complicated when it involves coupling dependencies that live in different dimensions. Such cases can no longer be solved by separating the problem per dimension. It also means that the problem is inherently quaternionic and cannot be solved by simple complex number based technology. This occurs in the coupling equation of elementary particles where two quaternionic functions are coupled that belong to different discrete symmetry sets. Dirac has solved this problem by applying spinors and Dirac matrices. The HBM solves this with quaternionic methodology.

⁵ See: Events

3 The logic model

3.1 Static status quo

3.1.1 Quantum logic

The most basic level of objects in nature is formed by the propositions that can be made about the objects that occur in nature. The relations between these propositions are restricted by the axioms of traditional quantum logic. This set of related propositions can only describe a static status quo.

In mathematical terminology the propositions whose relations are described by traditional quantum logic form a lattice. More particular, they form an orthomodular lattice that contains a countable infinite set of atomic (=mutually independent) propositions. Within the same quantum logic system multiple versions of sets of these mutually independent atoms exist. In this phase of the model the content of the propositions is totally unimportant. As a consequence these atoms form principally an unordered set⁶. Only the interrelations between the propositions count.

Traditional quantum logic shows narrow similarity with classical logic, however the modular law, which is one of the about 25 axioms that define the classical logic, is weakened in quantum logic. This is the cause of the fact that the structure of quantum logic is significantly more complicated than the structure of classical logic.

3.1.2 Hilbert logic

The set of propositions of traditional quantum logic is lattice isomorphic with the set of closed subspaces of a separable Hilbert space. However there exist still significant differences between this logic system and the Hilbert space. This gap can be closed by a small refinement of the quantum logic system.

Step 1: Define linear propositions (also called Hilbert propositions) as quantum logical propositions that are characterized by a number valued strength. This number is taken from a division ring.

Step 2: Require that linear combinations of atomic propositions also belong to the logic system. Call such propositions **linear propositions**.

Step 3: introduce the notion of **relational coupling** between two linear propositions. This measure has properties that are similar to the inner product of Hilbert space vectors.

Step 4: Close the subsets of the new logic system with respect to this relational coupling measure.

The relational coupling measure can have values that are taken from a suitable division ring. The resulting logic system will be called **Hilbert logic**.

The Hilbert logic is lattice isomorphic as well topological isomorphic with the corresponding Hilbert space.

⁶ This fact will prove to be the underpinning of the cosmologic principle.

Linear propositions are the equivalents of Hilbert vectors. General quantum logic propositions are the equivalents of (closed) subspaces of a Hilbert space.

The measure of the relational coupling between two linear propositions is the equivalent of the inner product between two Hilbert vectors.

Due to this similarity the Hilbert logic will also feature operators⁷.

In a Hilbert logic linear operators can be defined that have linear atoms as their eigenpropositions. Their eigenspace is countable.

In a Hilbert logic system the ***superposition principle*** holds. A linear combination of linear proposition is again a linear proposition.

Hilbert logic is treated in more detail in a separate document <http://vixra.org/abs/1302.0149> .

Dynamic model

A dynamic model can be constructed from an ordered sequence of the above static sub- models. Care must be taken to keep sufficient coherence between subsequent static models. However, some deviation must be tolerated, because otherwise, nothing dynamical will happen in this new dynamic model. The cohesion is established by a suitable correlation vehicle.

3.1.3 Correlation vehicle

The correlation vehicle uses a toolkit consisting of an enumerator generator, a reference continuum and a continuous function that maps the enumerators onto the continuum. The function is a continuous function of both the sequence number of the sub-models and the enumerators that are attached to a member of the selected set of atomic propositions. The enumeration is artificial and is not allowed to add extra characteristics or functionality to the attached proposition. For example, if the enumeration takes the form of a coordinate system, then this coordinate system cannot have a unique origin and it is not allowed to introduce preferred directions. These omissions lead to an affine space. The avoidance of preferred directions produces problems in multidimensional coordinate systems. In case of a multidimensional coordinate system the correlation vehicle must use a smooth touch. At very small scales the coordinate system must get blurred. This means that the guarantee for coherence between subsequent sub-models cannot be made super hard. Instead coherence is reached with an acceptable tolerance.

3.1.4 Isomorphic model

The natural form of the enumeration system can be derived from the lattice isomorphic companion of the quantum logic sub-model.

In the third and fourth decade of the twentieth century Garret Birkhoff and John von Neumann⁸ were able to prove that for the set of propositions in the traditional quantum logic model a mathematical

⁷ The Hilbert logic does not feature dynamic operators.

lattice isomorphic model exists in the form of the set of the closed subspaces of an infinite dimensional separable Hilbert space. The Hilbert space is a linear vector space that features an inner vector product. It offers a mathematical environment that is far better suited for the formulation of physical laws than what the purely logic model can provide.

Some decades later Constantin Piron⁹ proved that the only number systems that can be used to construct the inner products of the Hilbert vectors must be division rings. The only suitable division rings are the real numbers, the complex numbers and the quaternions¹⁰. Quaternions can be seen as combinations of a real scalar and a 3D (real) vector. The number system of the quaternions represent a dynamic 3D coordinate system. It can be shown that the eigenvalues of normal operators must also be taken from the same division ring.

Since the set of real numbers is multiple times contained in the set of complex numbers and the set of complex numbers is multiple times contained in the set of quaternions, the most extensive isomorphic model is contained in an infinite dimensional quaternionic separable Hilbert space. For our final model we will choose the quaternionic Hilbert space, but first we study what the real Hilbert space model and the complex Hilbert space model provide.

The set of closed subspaces of the Hilbert space represents the set of propositions that forms the static quantum logic system. The set of mutually independent atoms in the logic model corresponds to a set of base vectors that together span the whole Hilbert space. Like the sets of mutually independent atoms in the quantum logic system, multiple sets of orthonormal base vectors exist in the Hilbert space. The base vectors do not form an ordered set. However, a so called normal operator will have a set of eigenvectors that form a complete orthonormal base. The corresponding eigenvalues may provide a means for enumeration and thus for ordering these base vectors. An arbitrary normal operator does not fit. Its eigenvalues introduce an origin and in the case of a multidimensional eigenspace they may produce preferred directions. The represented atoms do not have such properties. Still, many suitable enumeration operators exist. However, several things can already be said about the eigenspace of the enumeration operator. This space is countable. It has no origin. It does not show preferred directions. It can be embedded in a corresponding reference continuum.

As part of the corresponding Gelfand triple¹¹ the separable Hilbert space forms a sandwich that features uncountable orthonormal bases and (compact) normal operators with eigenspaces that form a continuum. The reference continuum can be taken as the eigenspace of the corresponding enumeration operator that resides in the Gelfand triple of a reference Hilbert space.

Together with the pure quantum logic model, we now have a dual model that is significantly better suited for use with calculable mathematics. Both models represent a static status quo.

⁸http://en.wikipedia.org/wiki/John_von_Neumann#Quantum_logics & Stanford Encyclopedia of Philosophy, *Quantum Logic and Probability Theory*, <http://plato.stanford.edu/entries/qt-quantlog/>

⁹ C. Piron 1964; *Axiomatique quantique*

¹⁰ Bi-quaternions have complex coordinate values and do not form a division ring.

¹¹ See <http://vixra.org/abs/1210.0111> for more details on the Hilbert space and the Gelfand triple. See the paragraph on the Gelfand triple.

The Hilbert space model suits as part of the toolkit that is used by the correlation vehicle.

As a consequence, ***an ordered sequence of infinite dimensional quaternionic separable Hilbert spaces forms the isomorphic model of the dynamic logical model.***

The refinement of quantum logic to Hilbert logic also can deliver an enumeration system. However, the fact that the separable Hilbert space offers a reference continuum via its Gelfand triple make the Hilbert space more suitable for implementing the Hilbert Book Model.

3.1.4.1 Correspondences

Several correspondences exist between the sub models:

Quantum logic	Hilbert logic	Hilbert space
Propositions: a, b	Linear propositions: a, b	Vectors: $ a\rangle, b\rangle$
atoms c, d	atoms c, d	Base vectors: $ c\rangle, d\rangle$
Relational complexity: $C_{complexity}(a \cap b)$	Relational coupling measure	Inner product: $\langle a b\rangle$
Inclusion: $(a \cup b)$	Linear combination	Linear combination: $\alpha a\rangle + \beta b\rangle$
For atoms c_i : $\bigcup_i c_i$	Subset $\left\{ \sum_i \alpha_i c_i \right\}$	Subspace $\left\{ \sum_i \alpha_i c_i\rangle \right\}_{\forall \alpha_i}$

The distribution

$$a(i) \equiv \{\langle a|c_i\rangle\}_{\forall i}$$

has no proper definition in quantum logic. It can be interpreted via the Hilbert logic and Hilbert space sub-models.

3.2 Affine space

The set of mutually independent atomic propositions is represented by an orthonormal set of base vectors in Hilbert space. Both sets span the whole of the corresponding structure. An arbitrary orthonormal base is not an ordered set. It has no start and no end. It is an affine space. However, all or a part of these base vectors can be enumerated. Enumeration introduces an artificial origin and may introduce artificially preferred directions. Thus, in general enumeration will apply to a part of the affine space.

The installation of the correlation vehicle requests the introduction of enumerators. The enumeration may introduce an ordering. In that case the attachment of the numerical values of the enumerators to the Hilbert base vectors defines a corresponding operator. It must be remembered that the selection of the enumerators and therefore the corresponding ordering is kind of artificial. The eigenspace of the

enumeration operator has *no unique origin* and is has *no natural preferred directions*. Thus it has no natural axes. It can only indicate the distance between two or more locations. For multidimensional enumerators the distance is not precise. The enumeration represents a blurred coordinate system. Both in the Hilbert space and in its Gelfand triple, the enumeration can be represented by a normal enumeration operator.

3.3 Continuity

3.3.1 Arranging dynamics

Embedding the enumerators in a continuum highlights the interspacing between the enumerators. Having a sequence of static sub-models is no guarantee that anything happens in the dynamic model. A fixed (everywhere equal) interspacing will effectively lame any dynamics. A more effective dynamics can be arranged by playing with the sizes of the interspacing. This is the task of *a continuous distance function*.

3.3.2 Establishing coherence

The coherence between subsequent static models can be established by embedding each of the countable sets in a single reference continuum. For example the Hilbert space can be embedded in its Gelfand triple. The enumerators of the base vectors of the separable Hilbert space can also be embedded in a corresponding continuum. That continuum is formed by the values of the enumerators that enumerate an orthonormal base of the Gelfand triple. We will reuse the same (reference) Gelfand triple for all members of the sequence of Hilbert spaces. The reference Gelfand triple is taken from a selected¹² member of the sequence. Next a correlation vehicle is established by introducing a continuous distance function that controls the coherence between subsequent members of the sequence of static models. It does that by defining the interspacing in the countable set of the enumerators that act in the separable Hilbert space by mapping them to the reference continuum. In fact the differential of the distance function is used to specify the “infinitesimal” interspacing¹³.

The equivalence of this action for the logic model is that the enumerators of the atomic propositions are embedded in a continuum that is used by an appropriate correlation vehicle.

The distance function uses a combination of progression and the enumerator id as its parameter value. The value of the progression might be included in the value of the id. Apart from their relation via the distance function, the enumerators and the embedding continuum are mutually independent¹⁴. For the selected correlation vehicle it is useful to use numbers as the value of the enumerators. The type of the numbers will be taken equal to the number type that is used for specifying the inner product of the corresponding Hilbert space and Gelfand triple. The danger is then that a direct relation between the value of the enumerator of the Hilbert base vectors and the embedding continuum is suggested. So, here a warning is at its place. Without the distance function there is no relation between the value of the enumerators and corresponding values in the embedding continuum. However, there is a well-defined

¹² A possible selection criterion is that around this member the scaling of the imaginary space is a symmetric function of progression. Another criterion is that the selected member represents the case of densest packaging.

¹³ The differential defines a local metric.

¹⁴ This is not the case for the reference Hilbert space in the sequence. There a direct relation exists.

relation between the images¹⁵ produced by the distance function and the embedding continuum that is formed by the corresponding enumerators in the Gelfand triple.¹⁶

The relation between the members of a countable set and the members of a continuum raises a serious one-to-many problem. That problem can easily be resolved for real Hilbert spaces and complex Hilbert spaces, but it requires a special solution for quaternionic Hilbert spaces.

Together with the reference continuum and the Hilbert base enumeration set the distance function defines the *evolution* of the model.

3.4 Hilbert spaces

3.4.1 Real Hilbert space model

When a real separable Hilbert space is used to represent the static quantum logic, then it is sensible to use a countable set of real numbers for the enumeration. A possible selection is formed by the natural numbers. Within the real numbers the natural numbers have a fixed interspacing. Since the rational number system has the same cardinality as the natural number system, the rational numbers can also be used as enumerators. In that case it is sensible to specify *a (fixed) smallest rational number* as the enumeration step size. In this way the notion of interspacing is preserved and can the distance function do its scaling task¹⁷. In the realm of the real Hilbert space model, the continuum that embeds the enumerators is formed by the real numbers. The values of the enumerators of the Hilbert base vectors are used as parameters for the distance function. The value that is produced by the distance function determines the target location for the corresponding enumerator in the embedding continuum. The interspacing freedom is used in order to introduce dynamics in which something happens.

In fact what we do is defining an enumeration operator that has the enumeration numbers as its eigenvalues. The corresponding eigenvectors of this operator are the target of the enumerator.

With respect to the logic model, what we do is enumerate a previously unordered set of atomic propositions that together span the quantum logic system and next we embed the numerators in a continuum. The correlation vehicle takes care of the cohesion between subsequent quantum logical systems.

While the progression step is fixed, the (otherwise fixed) space step might scale with progression.

Instead of using a fixed smallest rational number as the enumeration step size and a map into a reference continuum we could also have chosen for a model in which the rational numbered step size varies with the index of the enumerator.

3.4.2 Gelfand triple

The Gelfand triple of a real separable Hilbert space can be understood via the corresponding enumeration model of the real separable Hilbert space. Let the smallest enumeration value of the

¹⁵ Later these images will be called Qpatches

¹⁶ We will take the reference continuum from the Gelfand triple of the reference Hilbert space in the sequence. Thus, in the reference member of the sequence a clear relation between the two enumeration sets exist.

¹⁷ Later, in the quaternionic Hilbert space model, this freedom is used to introduce space curvature and it is used for resolving the one to many problem.

rational enumerators approach zero. Even when zero is reached, then still the set of enumerators is countable. Now add all limits of converging rows of rational enumerators to the enumeration set. After this operation the enumeration set has become a continuum and has the same cardinality as the set of the real numbers. It means that also every orthonormal base of the Gelfand triple has that cardinality. It also means that linear operators in this space have eigenspaces that are continuums and have the cardinality of the real numbers¹⁸.

3.4.3 Complex Hilbert space model

When a complex separable Hilbert space is used to represent quantum logic, then it is sensible to use rational complex numbers for the enumeration. Again a smallest enumeration step size is introduced. However, the imaginary fixed enumeration step size may differ from the real fixed enumeration step size. The otherwise fixed imaginary enumeration step may be scaled as a function of progression. In the complex Hilbert space model, the continuum that embeds the enumerators of the Hilbert base vectors is formed by the system of the complex numbers. This continuum belongs as eigenspace to the enumerator operator that resides in the Gelfand triple. It is sensible to let the real part of the Hilbert base enumerators represent progression. The same will happen to the real axis of the embedding continuum. On the real axis of the embedding continuum the interspacing can be kept fixed. Instead, it is possible to let the distance function control the interspacing in the imaginary axis of the embedding continuum. The values of the rational complex enumerators are used as parameters for the distance function. The complex value of the distance function determines the target location for the corresponding enumerator in the continuum. The distance function establishes the necessary coherence between the subsequent Hilbert spaces in the sequence. The difference with the real Hilbert space model is, that now the progression is included into the values of the enumerators. The result of these choices is that the whole model steps with (very small, say practically infinitesimal) fixed progression steps.

In the model that uses complex Hilbert spaces, the enumeration operator has rational complex numbers as its eigenvalues. In the complex Hilbert space model, the fixed enumeration real step size and the fixed enumeration imaginary step size define **a maximum speed**. The fixed imaginary step size may scale as a function of progression. The same will then happen with the maximum speed, defined as space step divided by progression step. However, if information steps one step per progression step, then the information transfer speed will be constant. Progression plays the role of proper time. Now define a new concept that takes the length of the complex path step as the step value. Call this concept the coordinate time step. Define a new speed as the space step divided by the coordinate time step. This new **maximum speed is a model constant**. Proper time is the time that ticks in the reference frame of the observed item. Coordinate time is the time that ticks in the reference frame of the observer¹⁹. Coordinate time is our conventional notion of time.

Again the eigenvectors of the (complex enumeration) operator are the targets of the enumerator whose value corresponds to the complex eigenvalue.

¹⁸ This story also applies to the complex and the quaternionic Hilbert spaces and their Gelfand triples.

¹⁹ In fact coordinate time is a mixture of progression and space. See paragraph on spacetime metric.

If we ignore the case of negative progression, then the complex Hilbert model exist in two forms, one in which the interspacing appears to expand and one in which the interspacing decreases with progression²⁰.

3.4.4 Quaternionic Hilbert space model

When a quaternionic separable Hilbert space is used to model the static quantum logic, then it is sensible to use rational quaternions for the enumeration. Again the fixed enumeration step sizes are applied for the real part of the enumerators and again the real parts of the enumerators represent progression. The continuum that embeds the enumerators is formed by the number system of the quaternions. The scaling distance function of the complex Hilbert space translates into an isotropic scaling function in the quaternionic Hilbert space. However, we may instead use a full 3D distance function that incorporates the isotropic scaling function. This new distance function may act differently in different spatial dimensions. However, when this happens at very large scales, then it conflicts with the cosmological principle. At those scales the distance function must be quasi isotropic. The distance function is not allowed to create preferred directions.

Now the enumeration operator of the Hilbert space has rational quaternions as its eigenvalues. The relation between eigenvalues, eigenvectors and enumerators is the same as in the case of the complex Hilbert space. Again the whole model steps with fixed progression steps.

3.4.4.1 Curvature and fundamental fuzziness

The spatially fixed interspacing that is used with complex Hilbert spaces poses problems with quaternionic Hilbert spaces. Any regular spatial interspacing pattern will introduce preferred directions. Preferred directions are not observed in nature²¹ and the model must not create them. A solution is formed by the **randomization of the interspacing**. Thus instead of a fixed imaginary interspacing we get an average interspacing. This problem does not play on the real axis. On the real axis we can still use a fixed interspacing. The result is an **average maximum speed**. This speed is measured as space step per coordinate time step, where the coordinate time step is given by the length of the 1+3D quaternionic path step. Further, the actual location of the enumerators in the embedding continuum will be determined by the combination of a sharp distance function and a Quaternionic Probability Amplitude Distribution (QPAD) that specifies the local blur. The form factor of the blur may differ in each direction and is set by the differential of the sharp distance function. The total effect is given by the convolution of the sharp distance function and a non-deformed QPAD. The result is a blurred distance function. A QPAD is a descriptor. It describes the distribution of a set of discrete objects.

The requirement that the cosmological principle must be obeyed is the cause of a fundamental fuzziness of the quaternionic Hilbert model. It is the reason of existence of quantum physics.

An important observation is that the blur mainly occurs locally.

²⁰ The situation that expands from the point of view of the countable enumeration set, will contract from the point of view of the embedding continuum of enumerators.

²¹ Preferred directions are in conflict with the cosmological principle.

At larger distances the freedom that is tolerated by the distance function causes **curvature of observed space**. However, as explained before, at very large scales the distance function must be quasi isotropic²². The local curvature is described by the differential of the sharp part of the distance function.

This picture only tells that space curvature might exist. It does not describe the origin of space curvature. For more detailed explanation, please see the paragraph on the enumeration process.

3.4.4.2 Discrete symmetry sets

Quaternionic number systems exist in 16 forms (sign flavors²³) that differ in their discrete symmetry sets. The same holds for sets of rational quaternionic enumerators. Four members of the set represent isotropic expansion or isotropic contraction of the imaginary interspacing. At large scales two of them are symmetric functions of progression. The other two are at large scales anti-symmetric functions of progression. We will take the symmetrical member that expands with positive progression as the **reference rational quaternionic enumerator set**. Each member of the set corresponds with a quaternionic Hilbert space model. Thus apart from a reference continuum we now have a reference rational quaternionic enumerator set. Both reference sets meet at the reference Hilbert space. Even at the instance of the reference Hilbert space, the distance function must be a continuous function of progression.

A similar split in quaternionic sign flavors occurs with continuous quaternionic functions. For each discrete symmetry set of their parameter space, the function values of the continuous quaternionic distribution exist in 16 versions that differ in their discrete symmetry set. Within the target domain of the continuous quaternionic distribution the symmetry set will stay constant.

3.4.4.3 Generations and Qpatterns

The local generator of enumerators can depending on its characteristics generate a certain distribution of randomized enumerators. If generators with different characteristics exist, then several generations²⁴ of local QPAD's exist. At each progression step, all generators produce only a single element of the distribution. For a selected generation the following holds:

Apart from the adaptation of the form factor that is determined by the local curvature and apart from the discrete symmetry set of the QPAD, the natal QPAD's are everywhere in the model the same.

Therefore we will call the distribution of objects that is described by this basic form of the selected QPAD generation a **Qpattern**. For each generation, *Qpatterns exist in 16 versions that differ in their discrete symmetry set*.

A Qpattern corresponds with the statistic mechanical notion of a microstate. A microstate of a gas is defined as a set of numbers which specify in which cell each atom is located, that is, a number labeling the atom, an index for the cell in which atom *s* is located and a label for the microstate²⁵.

²² Quasi-isotropic = on average isoropic.

²³ See paragraph on Qpattern coupling

²⁴ See paragraph on generations

²⁵ <http://www.intechopen.com/books/theoretical-concepts-of-quantum-mechanics/quantum-mechanical-ensembles-and-the-h-theorem>

3.4.4.4 Optimal ordering

In the Hilbert space as well as in its isomorphic companion it is possible to select a base that has optimal ordering for the eigenvalues of a normal operator. In the quaternionic Hilbert space this optimally ordered base still contains sections that are in complete disorder. Optimally ordered means that these sections are uniformly distributed and that stochastic properties of these sections are the same. When the optimal ordering goes together with densest packaging, then all disordered sections are neighbors. A Poisson generator combined by a binomial process that is implemented by a suitable 3D isotropic spread function can implement such a section.

In the quantum logic system a similar selection is possible for the set of mutually independent atomic propositions. There the atoms are enumerated by the same set of rational quaternionic values.

3.5 The reference Hilbert space

The reference Hilbert space is taken as the member of the sequence of Hilbert spaces at the progression instance where the distance function is a symmetric function of progression that expands in directions that depart from the progression value of the reference Hilbert space.

At large and medium scales the reference member of the sequence of quaternionic Hilbert spaces is supposed to have a quasi-uniform²⁶ distribution of the enumerators in the embedding continuum. This is realized by requiring that the eigenspace of the enumeration operator that acts in the Gelfand triple of the zero progression value Hilbert space represents the reference embedding continuum. With other words, at this instance of progression, the rational quaternionic enumeration space is *flat*. This member of the sequence still features a stochastic interspacing in the imaginary part of the embedding quaternionic continuum. For the reference Hilbert space the isotropic scaling function is symmetric at zero progression value. Thus for the reference Hilbert space at the reference progression instance the distribution of the enumerators will realize a *densest packaging*²⁷.

For all subsequent Hilbert spaces the embedding continuum will be taken from the Gelfand triple of the reference Hilbert space.

²⁶ quasi-uniform = on average uniform.

²⁷ The densest packaging will also be realized locally when the geometry generates black regions.

3.6 The cosmological principle revisited

The enumeration process attaches an artificial content to the each of the members in the unordered set of atomic propositions. The unrestricted enumeration with rational quaternions generates an artificial origin and it generates artificial preferred directions that are not present in the original set of atomic propositions. The correlation vehicle is not allowed to attach this extra functionality to the original propositions. However, the vehicle must still perform its task to establish cohesion between subsequent sub-models. One measure is to turn the enumeration space into an affine space. An affine space has no origin. The next measure is to randomize the enumeration process sufficiently such that an acceptable degree of cohesion is reached and at the same time a quasi-isotropy of this affine space is established. This measure requires the freedom of some interspacing, which is obtained by assigning a lowest rational number. In principle, a lowest rational number can be chosen for the real part and a different smallest base number can be chosen for the imaginary part. This choice defines a basic notion of speed. The resulting (imaginary) space is on average isotropic. The randomization results in a local blur of the continuous function that regulates the enumeration process.

The result of these measures is that the cosmologic principle is installed. Thus, in fact ***the cosmological principle is a corollary of the other two starting points.***

However, according to this model, apart from the low scale randomization the universe was quite well ordered. After a myriad of progression steps this medium to large scale ordering is significantly disturbed.

Looking away from any point in universe is in fact looking back in time. Looking as far as is physically possible will open the view at a reference member of the Hilbert Book Model. This reference member represents a densest packaging. This will result in a uniform background at the horizon of the universe.

The well-known microwave background radiation is not fully uniform and is expelled by a member that is close to the densest packaged member.

4 The HBM picture

In the advance of quantum physics two views on quantum physics existed.

4.1 The Schrödinger picture

The Schrödinger picture describes a dynamic implementation in Hilbert space in which the quantum states carry the time dependence. The operators are static.

4.2 The Heisenberg picture

The Heisenberg picture describes a dynamic implementation in Hilbert space in which the operators (represented by matrices) carry the time dependence. The quantum states are static.

4.3 The Hilbert Book Model picture

In the HBM the whole Hilbert space carries the *proper time* dependence. Both the enumeration operator and the patterns that represent the quantum state functions depend on the progression parameter.

5 The enumeration process

It is not yet clear how Qpatterns will be shaped. This information can be derived from the requirements that are set for the correlation vehicle. We will start with a suggestion for the enumeration process that for this vehicle will lead to the wanted functionality.

Hypothesis I: At small scales the enumeration process is governed by a Poisson process.

The lateral spread that goes together with the low scale randomization of the interspacing plays the role of a binomial process. The combination of a Poisson process and a binomial process is again a Poisson process, but locally it has a lower efficiency than the original Poisson process. For a large number of enumerator generations the resulting Poisson distribution resembles a Gaussian distribution²⁸. If the generated enumerators are considered as charge carriers, then the corresponding potential has the shape of an Error function divided by r . Already at a short distance from its center location the potential function starts decreasing with distance r as a $1/r$ function²⁹.

If there is a static spherically symmetric Gaussian charge density

$$\rho_f(r) = \frac{Q}{\sigma^3 \sqrt{2\pi}} \exp\left(-\frac{r^2}{2\sigma^2}\right)$$

where Q is the total charge, then the solution $\varphi(r)$ of Poisson's equation,

$$\nabla^2 \varphi = -\frac{\rho_f}{\epsilon}$$

is given by

$$\varphi(r) = \frac{Q}{4\pi\epsilon r} \operatorname{erf}\left(\frac{r}{\sqrt{2}\sigma}\right) = \frac{1}{4\pi\epsilon} \int \frac{\rho_f(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d^3\mathbf{r}'$$

where $\operatorname{erf}(x)$ is the error function.

Note that, for r much greater than σ , the erf function approaches unity and the potential $\varphi(r)$ approaches the point charge potential

$$\varphi(r) \approx \frac{Q}{4\pi\epsilon r}$$

as one would expect. Furthermore the erf function approaches 1 extremely quickly as its argument increases; in practice for $r > 3\sigma$ the relative error is smaller than one part in a thousand.

²⁸ http://en.wikipedia.org/wiki/Poisson's_equation#Potential_of_a_Gaussian_charge_density

²⁹ <http://farside.ph.utexas.edu/teaching/em/lectures/node28.html> through node31

Now we remember Bertrand's theorem.³⁰ :

Bertrand's theorem states that only two types of central force potentials produce stable, closed orbits:

(1) an inverse-square central force such as the gravitational or electrostatic potential

$$V(r) = \frac{-k}{r} \quad (1)$$

and

(2) the radial harmonic oscillator potential

$$V(r) = \frac{1}{2} k r^2 \quad (2)$$

According to this investigation it becomes acceptable to assume that the undisturbed shape of the Qpatterns can be characterized as 3D Gaussian distributions³¹. Since this distribution produces the correct shape of the gravitation potential, ***it would explain the origin of curvature.***

However, this is one step too fast, because in the formulas above no explanation is given for the contribution of the members of the distribution that must add a term

$$\frac{Q}{|\mathbf{r} - \mathbf{r}'|}$$

to the integral. This is answered below in "Waves that shrink space".

5.1 The power of virtual distributions

A Qpattern is a mostly virtual distribution. At any instant it contains only a single actual element, the Qtarget. All other elements existed in the past or may exist in the future. The Qpattern corresponds to a plan of the generator of the Qpattern. The plan is determined by a set of characteristics. The plan also specifies its influence on the local curvature of space. Events may disturb the construction of the Qpattern. It is certainly a crux of mind that a virtual distribution can influence space curvature. However, if the Qpatch³² stays static, then the distribution is completely constructed at a single location. In that case the difference between the virtual and an actual distribution disappears. With that fact in mind it may become acceptable that one Qtarget per progression step can still cause the corresponding space curvature.

5.2 Qpatterns

Qpatterns of a given generation have a fixed shape.

³⁰ http://en.wikipedia.org/wiki/Bertrand's_theorem.

³¹ It might be clear that in this way an explanation is given for the effect of a Qpattern on local curvature.

³² A Qpatch is the center location of a Qpattern.

Not all enumerations that are required for generating a full Qpattern will be generated in a single progression step. In fact the generator creates only a single member of the Qpattern and that member is replaced in the next step by another member. Qpatterns contain one actual member and for the rest it consists of virtual members. The actual member is a location where an event can happen.

In order to stay at the same position a step in a given direction will on average be followed by a step in the reverse direction. Otherwise the average location will move away or the pattern will implode or explode.

Only when the Qpattern stays fixed at a single location, then that location will see the generation of a Qpattern that takes a shape that approaches a Gaussian distribution. It will take a huge number of progression steps to reach that condition.

A moving Qpattern will be spread out.

5.2.1 Fourier transform

A Qpattern that has the form of a Gaussian distribution has a Fourier transform that also has the form of a Gaussian distribution. However, the characteristics of the distributions will differ.

A coupled Qpattern is compact in configuration space and wide spread in canonical conjugated space.

A free Qpattern is compact in canonical conjugated space and wide spread in configuration space.

5.3 Waves that spread information

A Q_{target} exists during a single progression step. Even when they belong to the same Q_{pattern} will subsequent Q_{targets} be generated at different locations. If the distribution is generated in configuration space, then in the embedding continuum the Q_{target} corresponds to a flat distribution in momentum space. However, this distribution does not spread instantly. It corresponds in configuration space of the embedding continuum to a tsunami-like wave that has its source at the location of the Q_{target} . After the disappearance of the Q_{target} the wave keeps spreading out. The waves that belong to preceding Q_{targets} and the waves that belong to other Q_{patterns} will interfere with that wave. If an event occurs, then the generator stops generating Q_{targets} for this Q_{pattern} in the configuration space. However the waves that have been started will proceed spreading over configuration space.

When the local generator stops generating in configuration space then no new waves will be formed. The last wave and foregoing waves proceed spreading with light speed.

The fact that the waves keep spreading is a consequence of the characteristics of the correlation vehicle, which is implemented by the enumerator generation function.

5.4 Waves that shrink space

The tsunami-like waves appear to shrink space. The local shrinkage diminishes when the distance from the source increases. The integral shrinkage stays the same. As a consequence the influence diminishes as $1/r$. Also this fact is a consequence of the actions of the enumerator generation function.

All quantum state functions are fields (quaternionic probability amplitude distributions) that extend over the part of universe that falls within the information horizon of the corresponding particles. When a particle annihilates, then the information about its existence keeps spreading. However, no new information is generated.

The tsunami-like wave that spreads this information appears to shrink the space where it passes. However its influence diminishes with distance r as $1/r$.

As long as a particle lives, it keeps sending these tsunami-like waves. This might be the way that gravitation/ space curvature is implemented.

5.5 Spreading electric charge information

The Q_{target} also contains information about the electric charge of the corresponding particle. The process corresponds to the way that gravitational information is transmitted. In this case not the existence, but the charge is transmitted. The charge is determined by the discrete symmetry of the Q_{target} in comparison to the discrete symmetry of the corresponding RQE. Only the symmetries of the imaginary parts are relevant.

5.6 The tasks of the generator

The primary task of the generator is the generation of Q_{targets} that are part of Q_{patterns} . After the generation and vanishing of the Q_{target} the generator takes care of the transmission of the information about the generation incident over the space in which the Q_{target} was produced. This is done in the

form of the described tsunami-like waves. This is the second task of the generator. When the generator stops generating Q_{targets} for the current Q_{pattern} , then it does not transmit new information but the generator keeps supporting the transmission of existing information.

The transmission of incident information causes space curvature. The sharp part of the generator function describes the influence of space curvature. It does this via its differential which specifies a local metric.

6 Geometric model

The geometric model applies the quaternionic Hilbert space model. From now on the complex Hilbert space model and the real Hilbert space model are considered to be abstractions of the quaternionic model. It means that the special features of the quaternionic model bubble down to the complex and real models. For example both lower dimensional enumeration spaces will show blur at small enumeration scales. Further, both models will show a simulation of the discrete symmetry sets that quaternionic systems and functions possess. This can be achieved with spinors and Dirac matrices or with the combination of Clifford algebras, Grassmann algebras and Jordan algebras.

The real and complex models suit in situations where phenomena can be decoupled from the dimensions in which they appear.

At large scales the model can properly be described by the complex Hilbert space model. After a sufficient number of progression steps, at very large scales the quaternionic model is quasi isotropic.

We will place the reference Hilbert space at zero progression value. This reference Hilbert space can be a subspace of a much larger Hilbert space. However, in the reference Hilbert subspace a state of densest packaging must reside.

Quaternionic numbers exist in 16 discrete symmetry sets. When used as enumerators, half of this set corresponds with ***negative progression and will not be used in this geometric model.***

As a consequence we will call the Hilbert space at zero progression value the ***start*** of the model.

This model does not start with a Big Bang. Instead it starts in a state that is characterized by densest packaging of the Qpatches.

6.1 Quaternionic distributions

Quaternionic distributions consist of a real scalar distribution and an imaginary 3D vector distribution.

It is the sum of a symmetric distribution and an asymmetric distribution.

The complex Fourier transform of a symmetric (complex) function is a cosine transform. It is a real function.

The complex Fourier transform of an anti-symmetric (complex) function is a sine transform. It is an imaginary function.

This cannot directly be translated to quaternionic functions. The simplest solution is to consider the symmetric parts and asymmetric parts separately.

6.2 RQE's

RQE stands for Rational Quaternionic Enumerator. This lowest geometrical level is formed by the enumerators of a selected base of a selected member of the sequence of Hilbert spaces. The selected

base vectors represent the atoms of the Hilbert logic system. In this level, the embedding continuum is not included. The sequence number corresponds with the progression value in the real part of the value of the RQE. In principle the enumerators enumerate a previously unordered set. For the considered subspace the selected member represents a state of densest packaging of the RQE's.

The ordering and the corresponding origin of space become relevant when an observer object considers one or more observed objects. The real parts of the enumerators define progression. In physics progression conforms to proper time. As a consequence according to our model, the equivalent of proper time steps with a fixed step.

HYPOTHESIS II : At the start of the considered subspace the HBM used only one discrete symmetry set for its lowest level of geometrical objects. This discrete symmetry set is the same set that characterizes the reference continuum. This situation stays throughout the history of the model. This set corresponds with the set of eigenvalues of an RQE operator that resides in the reference quaternionic Hilbert space model.

Due to this restriction the RQE-space is not afflicted with splits and ramifications³³.

In the reference continuum the RQE's are surrounded by a Qpattern. In fact they act as the Qpatch of that Qpattern. In this occasion the Qpatch is also the Qtarget.

6.3 Palestra

The second geometric level is a curved space, called Palestra. As ingredients, it consists of an embedding continuum, the embedded RQE set and a sharp continuous quaternionic distance function. The local curvature is defined via the differential of the continuous (sharp) quaternionic distance function. The parameter space of the distance function embeds the RQE-set. Thus since the RQE-set is countable, the Palestra contains a countable set of images of the sharp distance function. We will call these images "Qpatches". The distance function may include an isotropic scaling function. The differential of the distance function defines an infinitesimal quaternionic step. In physical terms the length of this step is the infinitesimal coordinate time interval. The differential is a linear combination of sixteen partial derivatives. It defines a quaternionic metric³⁴. The enumeration process adds a coordinate system. The selection of the coordinate system is arbitrary. The origin and the axes of this coordinate system only become relevant when the distance between locations must be handled. The origin is taken at the location of the current observer. The underlying space is an affine space. It does not have a unique origin. We only consider a compartment of the affine space.

Like all continuous quaternionic functions, for each discrete symmetry set of its parameter space, the distance function exists in 16 different discrete symmetry sets for its function values. This means that also 16 different embedding continuums exist. The symmetry set of the distance function values may differ from the symmetry set of the parameter space of the distance function. The distance function keeps its discrete symmetry set throughout its life.

³³ http://en.wikipedia.org/wiki/Quaternion_algebra#Quaternion_algebras_over_the_rational_numbers

³⁴ See the paragraph on the spacetime metric.

6.4 Qpatches

The third level of geometrical objects consists of a countable set of space patches that occupy the Palestra. We already called them Qpatches. They are images of the RQE's that house in the first geometric object level. The set of RQE's is used as parameter set for the distance function. Apart from the rational quaternionic value of the corresponding RQE, their charge is formed by the discrete symmetry set of the distance function. The curvature of the second level space relates to the density distribution of the Qpatches. The Qpatches represent the centers of the locations of the *regions*³⁵ where next level objects can be detected. The name Qpatch stands for space patches with a quaternionic value. The charge of the Qpatches can be named Qsymm, Qsymm stands for discrete symmetry set of a quaternion. However, we already established that the value of the enumerator is also contained in the property set that forms the Qsymm charge.

The enumeration problems that come with the quaternionic Hilbert space model indicate that the Qpatches are in fact centers of a fuzzy environment that houses the potential locations where the actual RQE image can be found. ***A Qpatch is a non-blurred image of a RQE.***

6.5 QPAD's and Qtargets

The fuzziness in the sampling of the enumerators and their images in the reference continuum is described by a ***quaternionic probability amplitude distribution*** (QPAD). The squared modulus of the QPAD represents the probability that an image of an RQE will be detected on the exact location that is specified by the value of the parameter of the blurred distance function.

The ***QPAD's that describe Qpatterns have a flat parameter space in the form of a quaternionic continuum.*** This QPAD adds blur to the sharp distance function. The blurred distance function is formed by the ***convolution*** of the sharp distance function with the QPAD that describes the Qpattern. In this way the local form of the total QPAD describes a deformed Qpattern. The adaptation concerns the form factor of the deformed QPAD. The form factor may differ in each direction. It is determined by the differential of the sharp distance function.

The image of an RQE that is produced by the *blurred distance function* is a ***Qtarget. Qtargets only live during a single progression step.*** Qtargets mark the location where (higher level) objects may be detected. In this way QPAD's exist in two types. The first QPAD type describes the undisturbed Qpattern. The second QPAD type describes the potential Qtargets that are ***locally*** generated by the total distance function. That is why this second QPAD type is also called a local QPAD.

The fact that Qtargets only exist during a single progression step is related to the fact that a Qpattern is not generated in one progression step. It is more likely that for each RQE and thus for each Qpatch location only one enumerator is generated at each progression step. It means that on the instant of an event the generation of the Qpattern stops or proceeds in a different mode. Only if the Qpattern stays untouched, a rather complete Qpattern will be generated at that location. When the Qpatch moves, then the corresponding Qpattern smears out. With other words the first type QPAD is a plan rather than reality.

³⁵ Not the exact locations.

An event means that a Qpattern couples or decouples. In that case the pattern generation changes its mode. For example when a Qpattern couples, the generator will create a relatively small pattern in configuration space. However, when it decouples, then the generator will create a relatively small pattern in the canonical conjugated space of the configuration space. Coupling means that the generated Qpattern is coupled via its Qpatch to a corresponding RQE. This RQE is Qpatch of a historical Qpattern. Thus the current Qpattern is coupled to a historical Qpattern.

The parameter space of the blurred distance function is a flat quaternionic continuum. The RQE's form points in that continuum.

Local QPAD's are quaternionic distributions that contain a scalar potential in their real part that describes a density distribution of **potential** Qtargets. Further they contain a 3D vector potential in their imaginary part that describes the associated current density distribution of potential Qtargets. Continuous quaternionic distributions exist in eight different discrete spatial symmetry sets. However, the QPAD's inherit the discrete symmetry of their connected sharp distance function. The QPAD's superpose. Together they form a global QPAD.

The QPAD's are continuous functions. The objects that are described by these distributions form countable discrete sets.

6.5.1 Inner products of QPAD's

Each QPAD is a representative of a Hilbert vector and indirectly the QPAD represents a linear proposition.

Two QPAD's a and b have an inner product defined by

$$\langle a|b \rangle = \int_V a b dV \quad (1)$$

Since the Fourier transform \mathcal{F} preserves inner products, the Parseval equation holds for the inner product:

$$\langle a|b \rangle = \langle \mathcal{F}a|\mathcal{F}b \rangle = \langle \tilde{a}|\tilde{b} \rangle = \int_{\tilde{V}} \tilde{a} \tilde{b} d\tilde{V} \quad (2)$$

QPAD's have a norm

$$|a| = \sqrt{\langle a|a \rangle} \quad (3)$$

6.6 Blurred distance functions

The blurred distance function \mathcal{P} has a flat parameter space that is formed by rational quaternions. It is the convolution of the sharp distance function \wp with a QPAD ψ that describes a Qpattern.

$$\mathcal{P} = \wp \circ \psi \quad (1)$$

\wp describes the long range variation and ψ describes the short range variation. Due to this separation it is possible to describe the effect of the convolution on the local QPAD as a deformed QPAD that on its turn describes a Qpattern, where the form factor is controlled by the differential $d\wp$ of the sharp distance function. The spread function is implemented by a stochastic process. This second part influences the local curvature. The differential of first part defines a quaternionic **metric** that describes the **local spatial curvature**. This means that the two parts must be in concordance with each other.

Fourier transforms cannot be defined properly for functions with a curved parameter space, however, the blurred distance function \mathcal{P} has a well-defined Fourier transform $\tilde{\mathcal{P}}$, which is the product of the Fourier transform $\tilde{\wp}$ of the sharp distance function and the Fourier transform $\tilde{\psi}$ of the Qpattern.

$$\tilde{\mathcal{P}} = \tilde{\wp} \times \tilde{\psi} \quad (2)$$

The Fourier transform pairs and the corresponding canonical conjugated parameter spaces form a double-hierarchy model.

The Fourier transform $\tilde{\mathcal{P}}$ of the blurred distance function \mathcal{P} equals the product of the Fourier transform $\tilde{\wp}$ of the sharp distance function \wp and the Fourier transform $\tilde{\psi}$ of the Qpattern QPAD ψ .

16 blurred distance function exist that together cover all Qpatches. One of the 16 blurred distance functions acts as reference. The corresponding sharp distance function and thus the corresponding QPAD have the same discrete symmetry set as the lowest level space.

The fact that the blur ψ mainly has a local effect makes it possible to treat \wp and ψ seperately³⁶.

6.7 Local and global QPAD's

The model uses Qpatterns in order to implement the fuzziness of the local interspacing. After adaptation of the form factor to the differential of the sharp distance function a local QPAD is generated. The non-deformed local QPAD describes a Qpattern. Each Qpattern possess a private inertial reference frame³⁷. The superposition of all deformed local QPAD's, including the (deformed) descriptors of the higher generations of the Qpatterns, forms a global QPAD. Each of the 16 blurred distance functions corresponds to a global QPAD. The global QPAD is the image of the corresponding distance function.

Each of the Qpatterns extends over the whole RQE-set. However, the probability amplitude of the elements of these Qpatterns diminishes with the distance from their center point³⁸.

6.8 Generations

Photons and gluons correspond to a special kind of Qpatterns. They are generated in momentum space rather than in configuration space. Two photon Qpatterns and six³⁹ gluon Qpatterns exist⁴⁰.

³⁶ ψ concerns quantum physics. \wp concerns general relativity.

³⁷ See the paragraph on inertial reference frames.

³⁸ See the paragraph on the enumeration process.

³⁹ In the Standard Model gluons appear as eight superpositions of the six base gluons.

For fermions, three generations of Qpatterns exist that have non-zero extension and that differ in their basic form factor.

Generations may differ in the frequency at which they oscillate and/or in the number of objects that take part in the Qpattern.

The generator of enumerators is for a part a random number generator. That part is responsible for the generation of the Poisson distribution. Generations correspond to different characteristics of the enumerator generator.

6.9 Elementary particles

Elementary particles are constituted by the coupling of two Qpatterns that belong to the same generation. One of the Qpatterns is the quantum state function of the particle. The other Qpattern can be interpreted to implement inertia. Apart from their sign flavors these constituting Qpatterns form the same quaternionic distribution. However, the sign flavor may differ and their progression must have the same direction. It means that the density distribution is the same, but the signs of the flows of the concerned objects differ between the two distributions.

Coupling occurs because the two Qpatterns that constitute the coupling take the same location. Because they differ in their discrete symmetry they take part in a local oscillation where an outbound move is followed by an inbound move and vice versa⁴¹. Coupling occurs with the RQE, with the historic Qpattern that belongs to this RQE and with the tails of all historic Qpatterns.

If the first Qpattern oscillates, then the second Qpattern oscillates in synchrony or asynchronous. This situation may differ per dimension. This results in 32 elementary particle types, 32 anti-particle types and 8 non-particle (=uncoupled) types. The coupling has a small set of observable properties: coupling strength, electric charge, color charge and spin. Due to the fact that the enumerator generation stays in configuration space, the coupling affects the local curvature of the involved Palestras.

Qpatterns that belong to the same generation have the same shape. This is explained in the paragraph on the enumeration process. The difference between the coupling partners resides in the discrete symmetry sets. ***Thus the properties of the coupled pair are completely determined by the sign flavors of the partners.***

HYPOTHESIS III: If the quaternionic quantum state function of an elementary particle couples to a local piece of the reference blurred distance function, then the particle is a ***fermion***, otherwise it is a ***boson***. For anti-particles the quaternionic conjugate of the reference blurred distance function must be used. Non-coupled Qpatterns are bosons.

The fact that for fermions the reference continuum and the reference enumerator set play a crucial role may indicate ***that the Pauli principle is based on this fact.***

⁴⁰ Bertrand's theorem indicates that under some conditions, the Qpatterns of photons and gluons might be described as radial harmonic oscillators.

⁴¹ See: Coupling Qpatterns.

This paper does not give an explanation for the influence on the spin by the fact that the quantum state function is connected to an isotropic or an anisotropic Qpattern.

6.9.1 Differential equations

Locally, the coupling of two Qpatterns is controlled by a coupling equation

$$\nabla\psi = \phi = m \varphi \quad (1)$$

$$\phi = \nabla\psi; \text{ differential equation; holds for continuous quaternionic distributions} \quad (1a)$$

$$\nabla\psi = \phi; \text{ continuity equation; holds for QPAD's} \quad (1b)$$

$$\nabla\psi = m \varphi; \text{ coupling equation; holds for coupled field pairs } \{\psi, \varphi\} \quad (1c)$$

Here ∇ is the quaternionic nabla. ψ and φ are normalized Qpatterns that belong to the same generation. ψ plays the role of quantum state function. The coupling factor m is a global characteristic of the particle. The equation ignores the influence of the sharp distance function \wp . For elementary particles ψ and φ are different sign flavors of the same Qpattern:

$$\psi_0 = \varphi_0 \quad (2)$$

$$|\boldsymbol{\psi}| = |\boldsymbol{\varphi}| \quad (3)$$

$$\langle\psi|\psi\rangle = \int_V |\psi|^2 dV = \langle\varphi|\varphi\rangle = \int_V |\varphi|^2 dV = 1 \quad (4)$$

$$\langle\phi|\phi\rangle = \int_V |\phi|^2 dV = m^2 \quad (5)$$

$$\langle\nabla\psi|\varphi\rangle = \int_V (\nabla\psi) \varphi dV = m \quad (6)$$

This makes $|\phi|$ to the distribution of ***the local energy*** and m to the ***total energy*** of the quantum state function. The coupling equation can be split in a real equation and an imaginary equation.

$$\nabla_0\psi_0 - \langle\nabla, \boldsymbol{\psi}\rangle = m \varphi_0 \quad (6)$$

$$\nabla_0\boldsymbol{\psi} + \nabla\psi_0 + \nabla \times \boldsymbol{\psi} = m \boldsymbol{\varphi} \quad (7)$$

Bold characters indicate imaginary quaternionic distributions and operators. Zero subscripts indicate real distributions and operators.

The quantum state function of a particle moving with uniform speed \boldsymbol{v} is given by

$$\boldsymbol{\psi} = \chi + \chi_0 \boldsymbol{v} \quad (8)$$

$$\chi_0 = \psi_0 \quad (9)$$

Here χ stands for quantum state function of the particle at rest.

We introduce new symbols. In order to indicate the difference with Maxwell's equations we use Gothic capitals:

$$\mathfrak{E} = \nabla_0 \boldsymbol{\psi} + \nabla \psi_0 \quad (10)$$

$$\mathfrak{B} = \nabla \times \boldsymbol{\psi} \quad (11)$$

The local field energy E is given by:

$$E = |\phi| = \sqrt{\phi_0 \phi_0 + \langle \boldsymbol{\phi}, \boldsymbol{\phi} \rangle} = \sqrt{\phi_0 \phi_0 + \langle \mathfrak{E}, \mathfrak{E} \rangle + \langle \mathfrak{B}, \mathfrak{B} \rangle + 2\langle \mathfrak{E}, \mathfrak{B} \rangle} \quad (12)$$

The total energy is given by the volume integral

$$E_{total} = \sqrt{\int_V |\phi|^2 dV} \quad (13)$$

In a static situation the local energy E reduces to

$$E_{static} = \sqrt{\langle \nabla, \boldsymbol{\psi} \rangle^2 + \langle \mathfrak{E}, \mathfrak{E} \rangle + \langle \mathfrak{B}, \mathfrak{B} \rangle} \quad (14)$$

Photons and gluons are not coupled.

In the standard model the eight gluons are constructed from superpositions of these six base gluons.

6.9.2 Fourier transform

In a region of little or no space curvature the Fourier transform of the local QPAD can be taken.

$$\nabla \psi = \phi = m \varphi \quad (1)$$

$$\mathcal{M} \tilde{\psi} = \tilde{\phi} = m \tilde{\varphi} \quad (2)$$

$$\langle \tilde{\psi} | \mathcal{M} \tilde{\psi} \rangle = m \langle \tilde{\psi} | \tilde{\varphi} \rangle \quad (3)$$

$$\mathcal{M} = \mathcal{M}_0 + \mathbf{M} \quad (4)$$

$$\mathcal{M}_0 \tilde{\psi}_0 - \langle \mathbf{M}, \tilde{\boldsymbol{\psi}} \rangle = m \tilde{\varphi}_0 \quad (5)$$

$$\mathcal{M}_0 \boldsymbol{\psi} + \mathbf{M} \tilde{\psi}_0 + \mathbf{M} \times \tilde{\boldsymbol{\psi}} = m \tilde{\boldsymbol{\varphi}} \quad (6)$$

$$\int_{\tilde{V}} \tilde{\phi}^2 d\tilde{V} = \int_{\tilde{V}} (\overline{\mathcal{M} \tilde{\psi}})^2 d\tilde{V} = m^2 \quad (7)$$

In general $|\tilde{\psi}\rangle$ is not an eigenfunction of operator \mathcal{M} . That is only true when $|\tilde{\psi}\rangle$ and $|\tilde{\varphi}\rangle$ are equal. For elementary particles they are equal apart from their difference in discrete symmetry.

6.9.3 Inertial reference frames

Each Qpattern possesses an inertial reference frame that represents its current location, its orientation and its discrete symmetry. The reference frame corresponds with a Cartesian coordinate system that has

a well-defined origin. Reference frames of different Qpatterns have a relative position. A Qpattern does not move with respect to its own reference frame. However, reference frames of different Qpatterns may move relative to each other. The reference frames reside in an affine space. Interaction can take place between reference frames that reside in different HBM pages and that are within the range of the interaction speed. Within the same HBM page no interaction is possible. Interaction runs from a reference frame to a frame that lays in the future of the sender.

Coupling into elementary particles puts the origins of the reference frames of the coupled Qpatterns at the same location. At the same location reference frames are parallel. That does not mean that the axes have the same sign.

6.9.4 Coupling Qpatterns

Qpatterns are not static. Instead they oscillate. In the light of the fact that Qpatterns are mostly virtual and have only one actual element, the Qtarget, the oscillation is an odd concept. The interpretation of this oscillation is that on the average the Qpattern keeps its location and it keeps its form. Thus an outbound move of a Qtarget must be followed by an inbound move of the next Qtarget. The zero order temporal frequency of this oscillation is set by the progression step. In this light coupling means the synchronization of the involved Qpatterns. For fermions the oscillation can occur in three, two or one dimensions. Bosons may oscillate differently in different dimensions. The sharp distance function takes care of the stickier part of the dynamics. The synchronization can involve oscillations that are in-phase and oscillations that are in anti-phase. These criterions may act isotropic or they may hold in one or two dimensions.

The coupling uses pairs $\{\psi^x, \psi^y\}$ of two sign flavors. Thus the coupling equation runs:

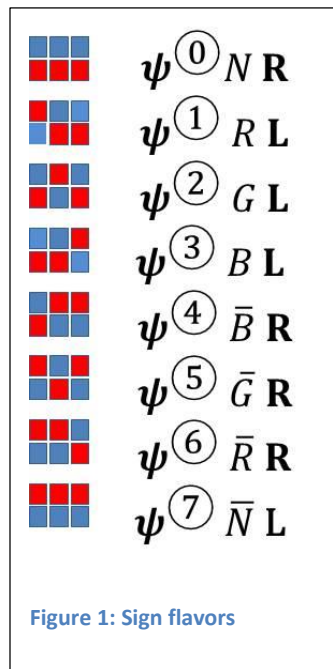
$$\nabla\psi^x = m \psi^y \quad (1)$$

Corresponding anti-particles obey

$$(\nabla\psi^x)^* = m (\psi^y)^* \quad (2)$$

The anti-phase couplings must use different sign flavors. In the figure below $\psi^{(0)}$ acts as the reference sign flavor.

The coupling and its effect on local curvature is treated in the section on the enumeration process.



Eight sign flavors
 (discrete symmetries)
 Colors N, R, G, B, \bar{R} , \bar{G} , \bar{B} , W
 Right or Left handedness **R,L**

6.9.5 Elementary particle properties

Elementary particles retain their properties when they are contained in composite particles.

6.9.5.1 Spin

HYPOTHESIS IV: The size of the spin relates to the fact whether the coupled Qpattern is the reference Qpattern.

Each generation has its own reference Qpattern. Fermions couple to the reference Qpattern. Fermions have half integer spin. Bosons have integer spin.

The spin of a composite equals the sum of the spins of its components.

6.9.5.2 Electric charge

HYPOTHESIS V: Electric charge depends on the difference and direction of the imaginary base vectors for the Qpattern pair. Each sign difference stands for one third of a full electric charge. Further it depends on the fact whether the handedness differs. If the handedness differs then the sign of the count is changed as well.

The electric charge of a composite is the sum of the electric charge of its components.

6.9.5.3 Color charge

HYPOTHESIS VI: Color charge is related to the direction of the anisotropy of the considered Qpattern with respect to the reference Qpattern. The anisotropy lays in the discrete symmetry of the imaginary part. The color charge of the reference Qpattern is white. The corresponding anti-color is black. The color charge of the coupled pair is determined by the colors of its members.

All composite particles are black or white. The neutral colors black and white correspond to isotropic Qpatterns.

Currently, color charge cannot be measured. In the Standard Model the existence of color charge is derived via the Pauli principle.

6.9.5.4 Mass

Mass is related to the number of involved Qpatches. It is more directly related to the square root of the volume integral of the square of the local field energy E . Any internal kinetic energy is included in E .

The same mass rule holds for composite particles. The fields of the composite particles are dynamic superpositions of the fields of their components.

6.9.6 Elementary object samples

With these ingredients we can look for agreements with the standard model. It appears that the coverage is complete. But the diversity of the HBM table appears to be not (yet) discernible.

For the same generation, the real parts of the Qpatterns (that contain the static scalar distribution) are all born the same way! When the Qpattern holds position and oscillates there, the imaginary part changes sign at each oscillation cycle. In this way the Qpatterns become vibrating micro states. The vibration mode may vary per dimension. (The parameter space acts as a reference).

Elementary particles are couplings of two Qpatterns that may vary in their vibration modes. The vibration modes determine the properties of the particle.

6.9.6.1 Photons and gluons

Photons and gluons are not coupled. In the standard model the eight gluons are constructed from superpositions of these six base gluons.

type	s-type	e-charge	c-charge	Handedness	SM Name
$\{\psi^{\textcircled{7}}\}$	boson	0	N	R	photon
$\{\psi^{\textcircled{0}}\}$	boson	0	W	L	photon
$\{\psi^{\textcircled{6}}\}$	boson	0	\bar{R}	R	gluon
$\{\psi^{\textcircled{1}}\}$	boson	0	R	L	gluon
$\{\psi^{\textcircled{5}}\}$	boson	0	\bar{G}	R	gluon
$\{\psi^{\textcircled{2}}\}$	boson	0	G	L	gluon
$\{\psi^{\textcircled{4}}\}$	boson	0	\bar{B}	R	gluon
$\{\psi^{\textcircled{3}}\}$	boson	0	B	L	gluon

Photons and gluons are better interpreted as Qpatterns in Fourier space. During their lifetime they do not couple. Only at the instance of generation or annihilation they couple to the emitter or absorber.

Two types of photons exist. One fades away from its point of generation. The other concentrates until it reaches the absorber. The act of interaction can be interpreted as a Fourier transform. The Fourier transforms converts a distribution in configuration space into a distribution in its canonical conjugated space or vice versa.

For gluons similar things occur, but they happen in fewer than three dimensions.

6.9.6.2 Leptons and quarks

According to the Standard Model both leptons and quarks comprise three generations. They form 22 particles. Neutrinos will be treated separately.

6.9.6.2.1 Neutrinos

Neutrinos are boson-fermions and have zero electric charge. They are leptons, but they seem to belong to a separate low-weight family of (three) generations. They couple to a Qpattern that has the same sign-flavor. The Qpatterns oscillate synchronous. The lowest generation has a very small rest mass.

type	s-type	e-charge	c-charge	Handedness	SM Name
$\{\psi^7, \psi^7\}$	fermion	0	NN	RR	neutrino
$\{\psi^0, \psi^0\}$	Anti-fermion	0	WW	LL	neutrino
$\{\psi^6, \psi^6\}$	boson?	0	\overline{RR}	RR	neutrino
$\{\psi^1, \psi^1\}$	Anti- boson?	0	RR	LL	neutrino
$\{\psi^5, \psi^5\}$	boson?	0	\overline{GG}	RR	neutrino
$\{\psi^2, \psi^2\}$	Anti- boson?	0	GG	LL	neutrino
$\{\psi^4, \psi^4\}$	boson?	0	\overline{BB}	RR	neutrino
$\{\psi^3, \psi^3\}$	Anti- boson?	0	BB	LL	neutrino

6.9.6.2.2 Leptons

Pair	s-type	e-charge	c-charge	Handedness	SM Name
$\{\psi^7, \psi^0\}$	fermion	-1	N	LR	electron
$\{\psi^0, \psi^7\}$	Anti-fermion	+1	W	RL	positron

The generations contain the muon and tau generations of the electrons. The Qpatterns oscillate asynchronous in three dimensions.

6.9.6.2.3 Quarks

Pair	s-type	e-charge	c-charge	Handedness	SM Name
$\{\psi^{\textcircled{1}}, \psi^{\textcircled{0}}\}$	fermion	-1/3	R	LR	down-quark
$\{\psi^{\textcircled{6}}, \psi^{\textcircled{7}}\}$	Anti-fermion	+1/3	\bar{R}	RL	Anti-down-quark
$\{\psi^{\textcircled{2}}, \psi^{\textcircled{0}}\}$	fermion	-1/3	G	LR	down-quark
$\{\psi^{\textcircled{5}}, \psi^{\textcircled{7}}\}$	Anti-fermion	+1/3	\bar{G}	RL	Anti-down-quark
$\{\psi^{\textcircled{3}}, \psi^{\textcircled{0}}\}$	fermion	-1/3	B	LR	down-quark
$\{\psi^{\textcircled{4}}, \psi^{\textcircled{7}}\}$	Anti-fermion	+1/3	\bar{B}	RL	Anti-down-quark
$\{\psi^{\textcircled{4}}, \psi^{\textcircled{0}}\}$	fermion	+2/3	\bar{B}	RR	up-quark
$\{\psi^{\textcircled{3}}, \psi^{\textcircled{7}}\}$	Anti-fermion	-2/3	B	LL	Anti-up-quark
$\{\psi^{\textcircled{5}}, \psi^{\textcircled{0}}\}$	fermion	+2/3	\bar{G}	RR	up-quark
$\{\psi^{\textcircled{2}}, \psi^{\textcircled{7}}\}$	Anti-fermion	-2/3	G	LL	Anti-up-quark
$\{\psi^{\textcircled{6}}, \psi^{\textcircled{0}}\}$	fermion	+2/3	\bar{R}	RR	up-quark
$\{\psi^{\textcircled{1}}, \psi^{\textcircled{7}}\}$	Anti-fermion	-2/3	R	LL	Anti-up-quark

The generations contain the charm and top versions of the up-quark and the strange and bottom versions of the down-quark. The Qpatterns oscillate asynchronous in one or two dimensions.

6.9.6.2.4 Reverse quarks

Pair	s-type	e-charge	c-charge	Handedness	SM Name
$\{\psi^{\textcircled{0}}, \psi^{\textcircled{1}}\}$	fermion	+1/3	R	RL	down-r-quark
$\{\psi^{\textcircled{7}}, \psi^{\textcircled{6}}\}$	Anti-fermion	-1/3	\bar{R}	LR	Anti-down-r-quark
$\{\psi^{\textcircled{0}}, \psi^{\textcircled{2}}\}$	fermion	+1/3	G	RL	down-r-quark
$\{\psi^{\textcircled{7}}, \psi^{\textcircled{5}}\}$	Anti-fermion	-1/3	\bar{G}	LR	Anti-down-r-quark
$\{\psi^{\textcircled{0}}, \psi^{\textcircled{3}}\}$	fermion	+1/3	B	RL	down-r-quark
$\{\psi^{\textcircled{7}}, \psi^{\textcircled{4}}\}$	Anti-fermion	-1/3	\bar{B}	LR	Anti-down-r-quark
$\{\psi^{\textcircled{0}}, \psi^{\textcircled{4}}\}$	fermion	-2/3	\bar{B}	RR	up-r-quark
$\{\psi^{\textcircled{7}}, \psi^{\textcircled{3}}\}$	Anti-fermion	+2/3	B	LL	Anti-up-r-quark
$\{\psi^{\textcircled{0}}, \psi^{\textcircled{5}}\}$	fermion	-2/3	\bar{G}	RR	up-r-quark
$\{\psi^{\textcircled{7}}, \psi^{\textcircled{2}}\}$	Anti-fermion	+2/3	G	LL	Anti-up-r-quark
$\{\psi^{\textcircled{0}}, \psi^{\textcircled{6}}\}$	fermion	-2/3	\bar{R}	RR	up-r-quark
$\{\psi^{\textcircled{7}}, \psi^{\textcircled{1}}\}$	Anti-fermion	+2/3	R	LL	Anti-up-r-quark

The generations contain the charm and top versions of the up-r-quark and the strange and bottom versions of the down-r-quark. The Qpatterns oscillate asynchronous in one or two dimensions.

6.9.6.3 W-particles

The 18 W-particles have indiscernible color mix. W_+ and W_- are each other's anti-particle.

Pair	s-type	e-charge	c-charge	Handedness	SM Name
$\{\psi^6, \psi^1\}$	boson	-1	$\bar{R}R$	RL	W_-
$\{\psi^1, \psi^6\}$	Anti-boson	+1	$R\bar{R}$	LR	W_+
$\{\psi^6, \psi^2\}$	boson	-1	$\bar{R}G$	RL	W_-
$\{\psi^2, \psi^6\}$	Anti-boson	+1	$G\bar{R}$	LR	W_+
$\{\psi^6, \psi^3\}$	boson	-1	$\bar{R}B$	RL	W_-
$\{\psi^3, \psi^6\}$	Anti-boson	+1	$B\bar{R}$	LR	W_+
$\{\psi^5, \psi^1\}$	boson	-1	$\bar{G}G$	RL	W_-
$\{\psi^1, \psi^5\}$	Anti-boson	+1	$G\bar{G}$	LR	W_+
$\{\psi^5, \psi^2\}$	boson	-1	$\bar{G}G$	RL	W_-
$\{\psi^2, \psi^5\}$	Anti-boson	+1	$G\bar{G}$	LR	W_+
$\{\psi^5, \psi^3\}$	boson	-1	$\bar{G}B$	RL	W_-
$\{\psi^3, \psi^5\}$	Anti-boson	+1	$B\bar{G}$	LR	W_+
$\{\psi^4, \psi^1\}$	boson	-1	$\bar{B}R$	RL	W_-
$\{\psi^1, \psi^4\}$	Anti-boson	+1	$R\bar{B}$	LR	W_+
$\{\psi^4, \psi^2\}$	boson	-1	$\bar{B}G$	RL	W_-
$\{\psi^2, \psi^4\}$	Anti-boson	+1	$G\bar{B}$	LR	W_+
$\{\psi^4, \psi^3\}$	boson	-1	$\bar{B}B$	RL	W_-
$\{\psi^3, \psi^4\}$	Anti-boson	+1	$B\bar{B}$	LR	W_+

The Qpatterns oscillate differently in multiple dimensions.

6.9.6.4 Z-candidates

The 12 Z-particles have indiscernible color mix.

Pair	s-type	e-charge	c-charge	Handedness	SM Name
$\{\psi^2, \psi^1\}$	boson	0	GR	LL	Z
$\{\psi^5, \psi^6\}$	Anti-boson	0	$\bar{G}R$	RR	Z
$\{\psi^3, \psi^1\}$	boson	0	BR	LL	Z
$\{\psi^4, \psi^6\}$	Anti-boson	0	$\bar{R}B$	RR	Z
$\{\psi^3, \psi^2\}$	boson	0	BR	LL	Z
$\{\psi^4, \psi^5\}$	Anti-boson	0	$\bar{R}B$	RR	Z
$\{\psi^1, \psi^2\}$	boson	0	RG	LL	Z
$\{\psi^6, \psi^5\}$	Anti-boson	0	$\bar{R}G$	RR	Z
$\{\psi^1, \psi^3\}$	boson	0	RB	LL	Z
$\{\psi^6, \psi^4\}$	Anti-boson	0	$\bar{R}B$	RR	Z
$\{\psi^2, \psi^3\}$	boson	0	RB	LL	Z
$\{\psi^5, \psi^4\}$	Anti-boson	0	$\bar{R}B$	RR	Z

The Qpatterns oscillate differently in multiple dimensions.

6.10 Physical fields

Elementary particles conserve their properties in higher level bindings. These properties are sources to new fields. Besides the photons and the gluons these fields are the physical fields that we know. These new fields can be described by quaternionic distributions and when they cover large numbers of particles they can be described with quaternionic distributions that contain a scalar potential and a vector potential like the QPAD's described above. However, if they contain multiple charge carriers, then these charge carriers are particles and not Qpatches and the charge is a property of the corresponding particle.

6.11 Gravitation field

One of the physical fields, the gravitation field describes the local curvature of the reference Palestra. It equals the scalar potential field that corresponds to the real part of the quantum state function.

The gravitation field has much in common with the right term in the coupling equation.

$$\nabla\psi = \phi = m \varphi \quad (1)$$

Both ψ and φ are normalized. So, ϕ can represent the gravitation potential field of the considered particle.

Now let ϕ represent the quaternionic potential of a set of massive particles. It is a superposition of single charge potentials.

$$\phi = \phi_0 + \Phi = \sum_i \phi_i = \sum_i m_i \varphi_i \quad (2)$$

The particles may represent composites. In that case the mass m_i includes the internal kinetic energy of the corresponding particle. Here ϕ and ϕ_i are not considered as a QPAD, but as quaternionic distribution. All massive particles attract each other. In superpositions, gravitational fields tend to enforce each other.

6.12 Electromagnetic fields

The electric charge e_i is represented similarly as m_i , but where m_i is always positive, the electric charge e_i can be either positive or negative. Equal signs repel, opposite signs attract each other. Superposition of the fields must include the sign. In superpositions, arbitrary electronic fields tend to neutralize each other. Moving electric charges correspond to a vector potential and the curl of this vector potential corresponds to a magnetic field.

$$\phi = \phi_0 + \Phi = \sum_i e_i \varphi_i \quad (1)$$

Here ϕ is the quaternionic electro potential. It is a superposition of single charge potentials ϕ_i . ϕ_0 is the scalar potential. $\boldsymbol{\phi}$ is the vector potential. The values of the electric charge sources e_i are included in ϕ .

$$\mathbf{E} = \nabla_0 \phi + \nabla \phi_0 \quad (2)$$

$$\mathbf{B} = \nabla \times \boldsymbol{\phi} \quad (3)$$

6.13 Photons and gluons

Photons and gluons are QPAD's.

In configuration space they obey

$$\nabla \psi = 0 \quad (1)$$

$$\nabla^2 \psi = 0 \quad (2)$$

Photons and gluons are better considered as QPAD's in the canonical conjugated space of the configuration space.

The Fourier transform of a Qpattern has the same shape as its Fourier transform. Both approach the shape of a 3D Gaussian distribution.

7 Continuity equation

7.1 From coupling equation to continuity equation

Locally, the coupling of two Qpatterns is controlled by a coupling equation

$$\nabla\psi = m \varphi \quad (1)$$

The coupling equation is equivalent to a quaternionic differential equation.

$$\phi = \nabla\psi \quad (2)$$

The coupling equation is also equivalent to a quaternionic differential continuity equation.

$$\nabla\psi = \phi \quad (3)$$

This is best comprehended when the corresponding integral equation is investigated.

7.2 The differential and integral continuity equations

Let us approach the balance equation from the integral variety of the balance equation.

When $\rho_0(q)$ is interpreted as a charge density distribution, then the conservation of the corresponding charge⁴² is given by the continuity equation:

$$\text{Total change within } V = \text{flow into } V + \text{production inside } V \quad (1)$$

In formula this means:

$$\frac{d}{d\tau} \int_V \rho_0 dV = \oint_S \hat{\mathbf{n}} \rho_0 \frac{\mathbf{v}}{c} dS + \int_V s_0 dV \quad (2)$$

$$\int_V \nabla_0 \rho_0 dV = \int_V \langle \nabla, \boldsymbol{\rho} \rangle dV + \int_V s_0 dV \quad (3)$$

The conversion from formula (2) to formula (3) uses the Gauss theorem⁴³. Here $\hat{\mathbf{n}}$ is the normal vector pointing outward the surrounding surface S , $\mathbf{v}(\tau, \mathbf{q})$ is the velocity at which the charge density $\rho_0(\tau, \mathbf{q})$ enters volume V and s_0 is the source density inside V . In the above formula $\boldsymbol{\rho}$ stands for

⁴² Also see Noether's laws: http://en.wikipedia.org/wiki/Noether%27s_theorem

$$\boldsymbol{\rho} = \rho_0 \mathbf{v}/c \quad (4)$$

It is the flux (flow per unit area and unit time) of ρ_0 .

The combination of $\rho_0(\boldsymbol{\tau}, \mathbf{q})$ and $\boldsymbol{\rho}(\boldsymbol{\tau}, \mathbf{q})$ is a quaternionic skew field $\rho(\boldsymbol{\tau}, \mathbf{q})$ and can be seen as a probability amplitude distribution (QPAD).

$$\rho \stackrel{\text{def}}{=} \rho_0 + \boldsymbol{\rho} \quad (5)$$

$\rho(\boldsymbol{\tau}, \mathbf{q})\rho^*(\boldsymbol{\tau}, \mathbf{q})$ can be seen as an overall probability density distribution of the presence of the carrier of the charge. $\rho_0(\boldsymbol{\tau}, \mathbf{q})$ is a charge density distribution. $\boldsymbol{\rho}(\boldsymbol{\tau}, \mathbf{q})$ is the current density distribution.

This results in the law of charge conservation:

$$\begin{aligned} s_0(\boldsymbol{\tau}, \mathbf{q}) &= \nabla_0 \rho_0(\boldsymbol{\tau}, \mathbf{q}) \mp \langle \nabla, (\rho_0(\boldsymbol{\tau}, \mathbf{q})\mathbf{v}(\boldsymbol{\tau}, \mathbf{q}) + \nabla \times \mathbf{a}(\boldsymbol{\tau}, \mathbf{q})) \rangle \\ &= \nabla_0 \rho_0(\boldsymbol{\tau}, \mathbf{q}) \mp \langle \nabla, \rho(\boldsymbol{\tau}, \mathbf{q}) + \mathbf{A}(\boldsymbol{\tau}, \mathbf{q}) \rangle \\ &= \nabla_0 \rho_0(\boldsymbol{\tau}, \mathbf{q}) \mp \langle \mathbf{v}(\boldsymbol{\tau}, \mathbf{q}), \nabla \rho_0(\boldsymbol{\tau}, \mathbf{q}) \rangle \mp \langle \nabla, \mathbf{v}(\boldsymbol{\tau}, \mathbf{q}) \rangle \rho_0(\boldsymbol{\tau}, \mathbf{q}) \\ &\quad \mp \langle \nabla, \mathbf{A}(\boldsymbol{\tau}, \mathbf{q}) \rangle \end{aligned} \quad (6)$$

The blue colored \pm indicates quaternionic sign selection through conjugation of the field $\rho(\boldsymbol{\tau}, \mathbf{q})$. The field $\mathbf{a}(\boldsymbol{\tau}, \mathbf{q})$ is an arbitrary differentiable vector function.

$$\langle \nabla, \nabla \times \mathbf{a}(\boldsymbol{\tau}, \mathbf{q}) \rangle = 0 \quad (7)$$

⁴³ http://en.wikipedia.org/wiki/Divergence_theorem

$\mathbf{A}(\tau, \mathbf{q}) \stackrel{\text{def}}{=} \nabla \times \mathbf{a}(\tau, \mathbf{q})$ is always divergence free. In the following we will neglect $\mathbf{A}(\tau, \mathbf{q})$.

Equation (6) represents a balance equation for charge density. What this charge actually is, will be left in the middle. It can be one of the properties of the carrier or it can represent the full ensemble of the properties of the carrier.

Up to this point the investigation only treats the real part of the full equation. The full continuity equation runs:

$$s(\tau, \mathbf{q}) = \nabla \rho(\tau, \mathbf{q}) = s_0(\tau, \mathbf{q}) + \mathbf{s}(\tau, \mathbf{q}) \quad (8)$$

$$= \nabla_0 \rho_0(\tau, \mathbf{q}) \mp \langle \nabla, \rho(\tau, \mathbf{q}) \rangle \pm \nabla_0 \rho(\tau, \mathbf{q}) + \nabla \rho_0(\tau, \mathbf{q}) \pm (\pm \nabla \times \rho(\tau, \mathbf{q}))$$

$$= \nabla_0 \rho_0(\tau, \mathbf{q}) \mp \langle \mathbf{v}(\tau, \mathbf{q}), \nabla \rho_0(\tau, \mathbf{q}) \rangle \mp \langle \nabla, \mathbf{v}(\tau, \mathbf{q}) \rangle \rho_0(\tau, \mathbf{q})$$

$$\pm \nabla_0 \mathbf{v}(\tau, \mathbf{q}) + \nabla_0 \rho_0(\tau, \mathbf{q}) + \nabla \rho_0(\tau, \mathbf{q})$$

$$\pm (\pm (\rho_0(\tau, \mathbf{q}) \nabla \times \mathbf{v}(\tau, \mathbf{q}) - \mathbf{v}(\tau, \mathbf{q}) \times \nabla \rho_0(\tau, \mathbf{q})))$$

$$s_0(\tau, \mathbf{q}) = 2 \nabla_0 \rho_0(\tau, \mathbf{q}) \mp \langle \mathbf{v}(\tau, \mathbf{q}), \nabla \rho_0(\tau, \mathbf{q}) \rangle \mp \langle \nabla, \mathbf{v}(\tau, \mathbf{q}) \rangle \rho_0(\tau, \mathbf{q}) \quad (9)$$

$$\mathbf{s}(\tau, \mathbf{q}) = \pm \nabla_0 \mathbf{v}(\tau, \mathbf{q}) \pm \nabla \rho_0(\tau, \mathbf{q}) \quad (10)$$

$$\pm (\pm (\rho_0(\tau, \mathbf{q}) \nabla \times \mathbf{v}(\tau, \mathbf{q}) - \mathbf{v}(\tau, \mathbf{q}) \times \nabla \rho_0(\tau, \mathbf{q})))$$

The red sign selection indicates a change of handedness by changing the sign of one of the imaginary base vectors. Conjugation also causes a switch of handedness. It changes the sign of all three imaginary base vectors.

In its simplest form the full continuity equation runs:

$$s(\mathbf{q}, \tau) = \nabla \rho(\mathbf{q}, \tau)$$

Thus the full continuity equation specifies a quaternionic distribution s as a flat differential $\nabla \rho$.

When we go back to the integral balance equation, then holds for the imaginary parts:

$$\frac{d}{d\tau} \int_V \boldsymbol{\rho} dV = - \oint_S \hat{\mathbf{n}} \rho_0 dS - \oint_S \hat{\mathbf{n}} \times \boldsymbol{\rho} dS + \int_V \mathbf{s} dV \quad (4)$$

$$\int_V \nabla_0 \boldsymbol{\rho} dV = - \int_V \nabla \rho_0 dV - \int_V \nabla \times \boldsymbol{\rho} dV + \int_V \mathbf{s} dV \quad (5)$$

For the full integral equation holds:

$$\frac{d}{d\tau} \int_V \rho dV + \oint_S \hat{\mathbf{n}} \rho dS = \int_V s dV \quad (6)$$

$$\int_V \nabla \rho dV = \int_V s dV \quad (7)$$

Here $\hat{\mathbf{n}}$ is the normal vector pointing outward the surrounding surface S , $\mathbf{v}(\tau, \mathbf{q})$ is the velocity at which the charge density $\rho_0(\tau, \mathbf{q})$ enters volume V and s_0 is the source density inside V . In the above formula ρ stands for

$$\rho = \rho_0 + \boldsymbol{\rho} = \rho_0 + \frac{\rho_0 \boldsymbol{v}}{c} \quad (8)$$

It is the flux (flow per unit of area and per unit of progression) of ρ_0 . t stands for progression (not coordinate time).

8 Inertia

We use the ideas of Denis Sciama⁴⁴⁴⁵⁴⁶.

8.1 Inertia from coupling equation

In order to discuss inertia we must reformulate the coupling equation.

$$\nabla\psi = m \varphi \quad (1)$$

$$\nabla_0\psi_0 - \langle \nabla, \psi \rangle = m \varphi_0 \quad (2)$$

$$\nabla_0\psi + \nabla\psi_0 + \nabla \times \psi = \mathfrak{E} + \mathfrak{B} = m \varphi \quad (3)$$

We will write ψ as a superposition

$$\psi = \chi + \chi_0 \mathbf{v} \quad (4)$$

$$\psi_0 = \chi_0 \quad (5)$$

$$\boldsymbol{\psi} = \boldsymbol{\chi} + \chi_0 \mathbf{v}$$

χ represents the rest state of the object. With respect to progression, it is a constant.

$$\nabla_0\chi = 0 \quad (6)$$

For the elementary particles the coupled distributions $\{ \psi, \varphi \}$ have the same real part.

$$\psi_0 = \varphi_0 \quad (7)$$

$$\nabla_0\boldsymbol{\psi} = \chi_0 \dot{\mathbf{v}} \quad (8)$$

Remember

$$\mathfrak{E} = \nabla_0\boldsymbol{\psi} + \nabla\psi_0 \quad (9)$$

$$\chi_0 \dot{\mathbf{v}} = \mathfrak{E} - \nabla\psi_0 \quad (10)$$

In static conditions \mathbf{v} represents a uniform speed of linear movement. However, if the uniform speed turns into acceleration $\dot{\mathbf{v}} \neq \mathbf{0}$, then an extra field of size $\chi_0 \dot{\mathbf{v}}$ is generated that counteracts the acceleration. The Qpattern does not change, thus $\nabla\psi_0$ does not change. Also \mathfrak{B} does not change. This means that the acceleration of the particle corresponds to an extra \mathfrak{E} field that counteracts the acceleration. On its turn it corresponds with a change of the coupling partner φ . That change involves the coupling strength m . The counteraction is felt as inertia.

⁴⁴ <http://arxiv.org/abs/physics/0609026v4.pdf>

⁴⁵ <http://www.adsabs.harvard.edu/abs/1953MNRAS.113...345>

⁴⁶ http://rmp.aps.org/abstract/RMP/v36/i1/p463_1

8.2 Background potential

The superposition of all real parts of Qpatterns of a given generation produces a uniform background potential. At a somewhat larger distance r these real Qpattern parts diminish in their amplitude as $1/r$. However, the number of involved Qpatterns increases with the covered volume. Further, on average the distribution of the Qpatterns is isotropic and uniform. The result is a huge (real) local potential Φ

$$\Phi = - \int_V \frac{\bar{\rho}_0}{r} dV = -\bar{\rho}_0 \int_V \frac{dV}{r} = 2\pi R^2 \bar{\rho}_0 \quad (1)$$

After averaging the Qpatterns reduce to their real parts.

$$\bar{\rho} = \bar{\rho}_0; \bar{\mathbf{p}} = \mathbf{0} \quad (2)$$

Apart from its dependence on the average value of $\bar{\rho}_0$, Φ is a huge constant. Sciama relates Φ to the gravitational constant G .

$$G = (-c^2) / \Phi \quad (3)$$

If the considered local particle moves relative to the universe with a uniform speed \mathbf{v} , then a vector potential \mathbf{A} is generated.

$$\mathbf{A} = - \int_V \frac{\mathbf{v} \bar{\rho}_0}{c r} dV \quad (4)$$

Both $\bar{\rho}_0$ and \mathbf{v} are independent of r . The product $\mathbf{v} \bar{\rho}_0$ represents a current. Together with the constant c they can be taken out of the integral. Thus

$$\mathbf{A} = \Phi \mathbf{v} / c \quad (5)$$

$$\mathfrak{E} = -\nabla\Phi - \frac{1}{c} \cdot \dot{\mathbf{A}} \quad (6)$$

If we exclude the first term because it is negligible small, we get:

$$\mathfrak{E} = -\frac{\Phi}{c^2} \dot{\mathbf{v}} = G \dot{\mathbf{v}} \quad (7)$$

Like χ_0 and χ forms a QPAD χ , the fields Φ and \mathbf{A} together form a QPAD. However, this time the fields Φ and \mathbf{A} do not represent parts of a Qpattern. The χ Qpattern differs fundamentally from the QPAD that is formed by Φ and \mathbf{A} . Instead these fields represent the distribution of the averages of the quantum state functions of distant particles and the distribution of the currents of these patterns.

8.3 Interpretation

As soon as an acceleration of the local item occurs, an extra component $\dot{\mathbf{A}}$ of field \mathfrak{E} appears that corresponds to acceleration $\dot{\mathbf{v}}$.

In our setting the component $\nabla\Phi$ of the field \mathfrak{E} is negligible. With respect to this component the items compensate each other's influence. This means that if the influenced subject moves with uniform speed

\mathbf{v} , then $\mathfrak{E} \approx 0$. However, a vector potential \mathbf{A} is present due to the movement of the considered item. Any acceleration of the considered local item goes together with an extra non-zero \mathfrak{E} field. In this way the universe of particles causes inertia in the form of a force that acts upon the χ_0 distribution of the accelerating item.

If we compare this result with the previous analysis of inertia, then it becomes sensible to ***interpret the coupling partner of the quantum state function as the representation of the superposition of the tails of the quantum state functions of distant particles.***

The amplitude of Φ says something about the number of coupled Qpatterns of the selected generation that exist in universe. If it is constant and the average interspacing grows with progression, then the universe dilutes with increasing progression. Also the volume of the reference continuum over which the integration must be done will increase with progression. The total energy of these coupled Qpatterns that is contained in universe equals:

$$E_{total} = \sqrt{\int_V \left| \frac{\bar{\rho}_0}{r} \right|^2 dV}$$

8.4 Isotropic vector potential

The scalar background potential is accompanied by a similar background vector potential that is caused by the fact that the considered volume that was investigated in order to calculate the scalar background potential is enveloped by a surface that delivers a non-zero surface integral. The isotropic background potential corresponds to an isotropic scaling factor. This factor was already introduced in the first phases of the model.

8.5 Information horizon

The terms in the integral continuity equation

$$\Phi = \int_V \nabla \psi dV = \int_V \phi dV$$

can be interpreted as representing the influence of a local object onto the rest of the universe or as the influence of the rest of the universe onto a local object. In the second case the influence diminishes with distance and the number of influencers increases such that the most distant contributors together poses the largest influence. These influencers sit at the information horizon. In the history of the model they are part of the birth state of the current episode of the universe. This was a state of densest packaging.

The local Qpattern that is described by ψ couples to the historic Qpattern ϕ for which the RQE acts as a Qpatch and as a Qtarget. This historic Qpattern resided in the reference page of the HBM.

9 Gravitation

The sharp distance function can act as the base of a quaternionic gravitation theory. The sharp distance function has sixteen partial derivatives that combine in a differential.

9.1 Palestra

All quantum state functions share their parameter space as affine spaces. Due to the fact that the coupling of Qpatterns affects this parameter space, the Palestra is curved. The curvature is not static. With other words the Qpatches in the parameter space move and densities in the distribution of these patches change. For potential observers, the Palestra is the place where everything classically happens. The Palestra comprises the whole universe.

9.1.1 Spacetime metric

The Palestra is defined with respect to a flat parameter space, which is spanned by the **rational** quaternions⁴⁷. We already introduced the existence of a smallest rational number, which is used to arrange interspace freedom. The specification of the set of Qpatches is performed by a continuous quaternionic distribution $\wp(x)$ that acts as a distance function. This distance function defines a quaternionic infinitesimal interval ds . On its turn this definition defines a metric⁴⁸.

$$\begin{aligned}
 ds(x) &= ds^v(x)e_v = d\wp = \sum_{\mu=0\dots3} \frac{\partial \wp}{\partial x_\mu} dx_\mu = q^\mu(x)dx_\mu & (1) \\
 &= \sum_{\mu=0\dots3} \sum_{v=0,\dots,3} e_v \frac{\partial \wp_v}{\partial x_\mu} dx_\mu = \sum_{\mu=0\dots3} \sum_{v=0,\dots,3} e_v q_v^\mu dx_\mu
 \end{aligned}$$

The base e_v and the coordinates x_μ are taken from the **flat** parameter space of $\wp(x)$. That parameter space is spanned by the quaternions. The definition of the quaternionic metric uses a full derivative $d\wp$ of the distance function $\wp(x)$. This full derivative differs from the quaternionic nabla ∇ , which ignores the curvature of the parameter space. On its turn $d\wp$ ignores the blur of \mathcal{P} .

The distance function $\wp(x)$ may include an isotropic scaling function $a(\tau)$ that only depends on progression τ . It defines the expansion/compression of the Palestra.

ds is the infinitesimal quaternionic step that results from the combined real valued infinitesimal dx_μ steps that are taken along the e_μ base axes in the (flat) parameter space of $\wp(x)$.

⁴⁷ http://en.wikipedia.org/wiki/Quaternion_algebra#Quaternion_algebras_over_the_rational_numbers

⁴⁸ The intervals that are constituted by the smallest rational numbers represent the infinitesimal steps. Probably the hair of mathematicians are raised when we treat the interspacing as an infinitesimal steps. I apologize for that.

$dx_0 = c dt$ plays the role of the infinitesimal space time interval ds_{st} ⁴⁹. It is a physical invariant. $d\tau$ plays the role of the proper time interval and it equals the infinitesimal progression interval. The progression step is an HBM invariant. Without curvature, dt in $\|ds\| = c dt$ plays the role of the infinitesimal coordinate time interval.

$$c^2 dt^2 = ds ds^* = dx_0^2 + dx_1^2 + dx_2^2 + dx_3^2 \quad (2)$$

$$dx_0^2 = ds_{st}^2 = c^2 dt^2 - dx_1^2 - dx_2^2 - dx_3^2 \quad (3)$$

dx_0^2 is used to define the local spacetime metric tensor. With that metric the Palestra is a pseudo-Riemannian manifold that has a Minkowski signature. When the metric is based on ds^2 , then the Palestra is a Riemannian manifold with a Euclidean signature. The Palestra comprises the whole universe. It is the arena where everything happens.

For the distance function holds

$$\frac{\partial^2 \wp}{\partial x_\mu \partial x_\nu} = \frac{\partial^2 \wp}{\partial x_\nu \partial x_\mu} \quad (4)$$

And similarly for higher-order derivatives. Due to the spatial continuity of the distance function $\wp(x)$, the quaternionic metric as it is defined above is far more restrictive than the metric tensor that is used in General Relativity:

$$ds^2 = g_{ik} dx^i dx^k \quad (5)$$

Still

$$g_{ik} = g_{ki} \quad (6)$$

9.1.2 The Palestra step

When nature steps with universe (Palestra) wide steps during a progression step Δx_0 , then in the Palestra a quaternionic step Δs_\wp will be taken that differs from the corresponding flat step Δs_f

$$\Delta s_f = \Delta x_0 + \mathbf{i} \Delta x_1 + \mathbf{j} \Delta x_2 + \mathbf{k} \Delta x_3 \quad (1)$$

$$\Delta s_\wp = q^0 \Delta x_0 + q^1 \Delta x_1 + q^2 \Delta x_2 + q^3 \Delta x_3 \quad (2)$$

The coefficients q^μ are quaternions. The Δx_μ are steps taken in the (flat) parameter space of the distance function $\wp(x)$.

⁴⁹ Notice the difference between the quaternionic interval ds and the spacetime interval ds_{st}

9.1.3 Pacific space and black regions.

If we treat the Palestra as a continuum, then the parameter space of the distance function is a flat space that it is spanned by the number system of the quaternions. This parameter space gets the name “**Pacific space**”. This is the space where the RQE’s live. If in a certain region of the Palestra no matter is present, then in that region the Palestra is hardly curved. It means that in this region the Palestra is nearly equal to the parameter space of the distance function.

The Pacific space has the advantage that when distributions are converted to this parameter space the Fourier transform of the converted distributions is not affected by curvature.

In a region where the curvature is high, the Palestra step comes close to zero. At the end where the Palestra step reaches the smallest rational value, an information horizon is established. For a distant observer, nothing can pass that horizon. The information horizon encloses a **black region**. Inside that region the quantum state functions are so densely packed that they lose their identity. However, they do not lose their sign flavor. The result is the formation of a single quantum state function that consists of the superposition of all contributing quantum state functions. The resulting black body has mass, electric charge and angular momentum. The quantum state function of a black region is quantized. Due to the fact that no information can escape through the information horizon, the inside of the horizon is obscure. No experiment can reveal its content. It does not contain a singularity at its center. All characteristics of the black region are contained in its quantum state function⁵⁰.

The distance function $\wp(x)$ is a continuous quaternionic distribution. Like all continuous quaternionic distributions it contains two fields. It is NOT a QPAD. It does not contain density distributions.

9.1.4 Start of the universe.

At the start of the universe the package density was so high that also in that condition only one mixed QPAD can exist. That QPAD was a superposition of QPAD’s that have different sign flavors. Only when the universe expands enough, multiple individual Qpatterns may have been generated. In the beginning, these QPAD’s were uncoupled.

⁵⁰ See Cosmological history

10 Modularization

A very powerful influencer is modularization. Together with the corresponding **encapsulation** it has a very healthy influence on the **relational complexity** of the ensemble of objects on which modularization works. The encapsulation takes care of the fact that most relations are kept internal to the module. When relations between modules are reduced to a few types, then the module becomes **reusable**. The most Influential kind of modularization is achieved when modules can be **configured from lower order modules**.

Elementary particles can be considered as the lowest level of modules. All composites are higher level modules.

When **sufficient resources** in the form of reusable modules are present, then modularization can reach enormous heights. On earth it was capable to generate **intelligent species**.

10.1 Complexity

Potential complexity of a set of objects is a measure that is defined by the number of potential relations that exist between the members of that set.

If there are n elements in the set, then there exist $n*(n-1)$ potential relations.

Actual complexity of a set of objects is a measure that is defined by the number of relevant relations that exist between the members of the set.

In human affairs and with intelligent design it takes time and other resources to determine whether a relation is relevant or not. Only an expert has the knowledge that a given relation is relevant. Thus it is advantageous to have as little irrelevant potential relations as is possible, such that mainly relevant and preferably usable relations result.

Physics is based on relations. Quantum logic is a set of axioms that restrict the relations that exist between quantum logical propositions. Via its isomorphism with Hilbert spaces quantum logic forms a fundament for quantum physics. Classical logic is a similar set of restrictions that define how we can communicate logically. Like classical logic, quantum logic only describes static relations. Traditional quantum logic does not treat physical fields and it does not touch dynamics. However, the model that is based on traditional quantum logic can be extended such that physical fields are included as well and by assuming that dynamics is the travel along subsequent versions of extended quantum logics, also dynamics will be treated. The set of propositions of traditional quantum logic is isomorphic with the set of closed subspaces of a Hilbert space. This is a mathematical construct in which quantum physicists do their investigations and calculations. In this way fundamental physics can be constructed. Here holds very strongly that only relevant relations have significance.

10.2 Relationalcomplexity

We define **relational complexity** as the ratio of the number of actual relations divided by the number of potential relations.

10.3 Interfaces

Modules connect via interfaces. Interfaces are used by interactions. Interactions run via (relevant) relations. Relations that act within modules are lost to the outside world of the module. Thus interfaces

are collections of relations that are used by interactions. Inbound interactions come from the past. Outbound interactions go to the future. Two-sided interactions are cyclic. They are either oscillations or rotations of the inter-actor.

10.4 Interface types

Apart from the fact that they are inbound, outbound or cyclic the interfaces can be categorized with respect to the type of relations that they represent. Each category corresponds to an interface type. An interface that possesses a type and that installs the possibility to couple the corresponding module to other modules is called a standard interface.

10.5 Modular subsystems

Modular subsystems consist of connected modules. They need not be modules. They become modules when they are encapsulated and offer standard interfaces that makes the encapsulated system a reusable object.

The cyclic interactions bind the corresponding modules together. Like the coupling factor of elementary particles characterizes the binding of the pair of Qpatterns will a similar characteristic characterize the binding of modules.

This binding characteristic directly relates to the total energy of the constituted sub-system. Let ψ represent the renormalized superposition of the involved distributions.

$$\nabla\psi = \phi = m \varphi \tag{1}$$

$$\int_V |\psi|^2 dV = \int_V |\varphi|^2 dV = 1 \tag{2}$$

$$\int_V |\phi|^2 dV = m^2 \tag{3}$$

Here again m represents total energy.

The binding factor is the total energy of the sub-system minus the sum of the total energies of the separate constituents.

10.6 Relational complexity indicators

The inner product of two Hilbert vectors is a measure of the relational complexity of the combination.

A Hilbert vector represents a linear combination of atoms. When all coefficients are equal, then the vector represents an assembly of atoms. When the coefficients are not equal, then the vector represents a **weighted assembly** of atoms.

For two normalized vectors $|a\rangle$ and $|b\rangle$:

$$\langle a|a\rangle = 1 \tag{1}$$

$$\langle b|b\rangle = 1 \tag{2}$$

$$\langle a|b\rangle = 0 \text{ means } |a\rangle \text{ and } |b\rangle \text{ are not related.} \tag{3}$$

$$\langle a|b\rangle \neq 0 \text{ means } |a\rangle \text{ and } |b\rangle \text{ are related.} \tag{4}$$

$$|\langle a|b\rangle| = 1 \text{ means } |a\rangle \text{ and } |b\rangle \text{ are optimally related.} \tag{5}$$

10.7 Modular actions

Subsystems that have the ability to choose their activity can choose to organize their actions in a modular way. As with static relational modularization the modular actions reduce complexity and for the decision maker it eases control.

10.8 Random design versus intelligent design

At lower levels of modularization nature design modular structures in a stochastic way. This renders the modularization process rather slow. It takes a huge amount of progression steps in order to achieve a relatively complicated structure. Still the complexity of that structure can be orders of magnitude less than the complexity of an equivalent monolith.

As soon as more intelligent sub-systems arrive, then these systems can design and construct modular systems in a more intelligent way. They use resources efficiently. This speeds the modularization process in an enormous way.

11 Functions that are invariant under Fourier transformation.

A subset of the (quaternionic) distributions have the same shape in configuration space and in the linear canonical conjugated space.

We call them dual space distributions. It are functions that are invariant under Fourier transformation⁵¹. These functions are not eigenfunctions.

The Qpatterns and the harmonic and spherical oscillations belong to this class.

Fourier-invariant functions show iso-resolution, that is, $\Delta_p = \Delta_q$ in the Heisenberg's uncertainty relation.

11.1 Natures preference

Nature seems to have a preference for quaternionic distributions that are invariant under Fourier transformation.

A possible explanation is the two-step generation process, where the first step is realized in configuration space and the second step is realized in canonical conjugated space. The whole pattern is generated two-step by two-step.

The only way to keep coherence between a distribution and its Fourier transform that are both generated step by step is to generate them in pairs.

12 Events

12.1 Generations and annihilations

At the instant of generation or annihilation, the enumerator generator will change its mode and the Qpattern that will be generated changes its mode as well.

If the number of enumerator generations per step that contributes to a Qpattern is left open and if this number is larger than one, then it is difficult to understand that at a given instant the whole Qpattern changes its mode. The Qpattern has no knowledge of the mode that its members are in. The individual members might have that knowledge. In that case it is part of their charge.

So, from now on we suppose that the Qpatterns will be generated such that one member, the Qtarget, is generated per progression step. An event then indicates that the enumeration generator changes its generation mode.

For example, when a particle is annihilated the generator switches from generating a Qpattern in configuration space to generating an equivalent pattern in the canonical conjugated space. The result is that the pattern is no longer coupled and becomes a photon or a gluon. Of course the reverse procedure occurs at the generation of a particle.

⁵¹ Q-Formulæ contains a section about functions that are invariant under Fourier transformation.

In the original space, the object that corresponds to the Qpattern is annihilated while in the new space the transformed object is generated. Since the Qpattern is generated with a Qtarget at each progression step the event has immediate consequences.

Conservation laws govern the annihilation and creation processes.

12.2 Emissions and absorptions

When only a part of a composite annihilates, then a similar process can take place. A sub-module is annihilated and either the whole energy is emitted in the form of radiation or only part of the energy is emitted and the rest is used to constitute a new particle at a lower energy level.

It is also possible that a complete sub-module is emitted. This can be done in a two-step mode, where first the sub-module or part of it is converted into radiation and subsequently the sub-module is regenerated.

Absorption is described as the reverse process.

12.3 Oscillating interactions

Oscillating interactions are implemented by cyclic interfaces. They consist of a sequence of annihilations and generations, where the locations alternate.

12.4 Movements

The fact that a particle moves, and the fact that a Qpattern is generated with only one Qtarget per progression step means that during a movement the Qpattern is spread along the path of movement.

12.5 Curvature

When the generator operates in one space and produces there a compact distribution then it affects the curvature of that space. It also has consequences in the canonical conjugated space. However, there the corresponding distribution will be spread out. Its effect on space curvature will also be spread. As a result the effect on space curvature in this canonical conjugated space will be negligible.

12.6 Tsunami

After annihilation in configuration space the new generation in the canonical conjugated space looks like the build-up of a tsunami wave in configuration space. It races with light speed away from the point of annihilation. The process is described in the section on the enumeration process. This lasts until a new generated Qtarget is captured and the generation mode switches again. This happens most probably somewhere at a high amplitude of the tsunami wave. The next Qtarget is generated in configuration space.

13 Cosmology

13.1 Cosmological view

Even when space was fully densely packed with matter (or another substance) then nothing dynamic would happen. Only when sufficient interspacing comes available dynamics becomes possible.

The Hilbert Book Model exploits this possibility. It sees black regions as local returns to the original condition.

13.2 The cosmological equations

The integral equations that describe cosmology are:

$$\frac{d}{d\tau} \int_V \rho dV + \oint_S \hat{\mathbf{n}} \rho dS = \int_V s dV \quad (1)$$

$$\int_V \nabla \rho dV = \int_V s dV \quad (2)$$

Here $\hat{\mathbf{n}}$ is the normal vector pointing outward the surrounding surface S , $\mathbf{v}(\tau, \mathbf{q})$ is the velocity at which the charge density $\rho_0(\tau, \mathbf{q})$ enters volume V and s_0 is the source density inside V . In the above formula ρ stands for

$$\rho = \rho_0 + \boldsymbol{\rho} = \rho_0 + \frac{\rho_0 \mathbf{v}}{c} \quad (3)$$

It is the flux (flow per unit of area and per unit of progression) of ρ_0 . t stands for progression (not coordinate time).

13.3 Inversion surfaces

An inversion surface S is characterized by:

$$\oint_S \hat{\mathbf{n}} \rho dS = 0 \quad (1)$$

13.4 Cosmological history

The inversion surfaces divide universe into compartments. Think that these universe pockets contain matter that is on its way back to its natal state. If there is enough matter in the pocket this state forms a black region. The rest of the pocket is cleared from its mass content. Still the size of the pocket may increase. This represents the expansion of the universe. Inside the pocket the holographic principle governs. The black region represents the densest packaging mode of entropy.

The pockets may merge. Thus at last a very large part of the universe may return to its birth state, which is a state of densest packaging of entropy.

Then the resulting mass which is positioned at a huge distance will enforce a uniform attraction. This uniform attraction will install an isotropic extension of the central package. This will disturb the densest

packaging quality of that package. The motor behind this is formed by the combination of the attraction through distant massive particles, which installs an isotropic expansion and the influence of the small scale random localization which is present even in the state of densest packaging.

This describes an eternal process that takes place in and between the pockets of an affine space.

13.5 Entropy

As a whole, universe expands. Locally regions exist where contraction overwhelms the global expansion. These regions are separated by inversion surfaces. The regions are characterized by their inversion surface. Within these regions the holographic principle resides. The fact that the universe as a whole expands means that the average size of the encapsulated regions increases.

The ***holographic principle*** says that the total entropy of the region equals the entropy of a black region that would contain all matter in the region. Black regions represent regions where entropy is optimally packed.

Thus entropy is directly related to the interspacing between enumerators. With other words, local entropy is related to local curvature.

14 Recapitulation

The model starts by taking quantum logic as its foundation. It could as well have started by taking an infinite dimensional separable Hilbert space as its foundation. However, in that case the special role of base vectors would not so easily have been brought to the front. It appears that the atoms of the logic system and the base vectors of the Hilbert space play a very crucial role in the model. They represent the lowest level of objects in nature that play the theater of our observation.

The atoms are only principally unordered at very small “distances”. They have content. The Hilbert space offers built-in enumerator machinery that defines the distances and that specifies the content of the represented atoms. The same can be achieved in a refined version of quantum logic that we call Hilbert logic.

In fact we focus on a compartment of universe, where universe is an affine space. The isotropic scaling factor that was assumed in the early phases of the model appears to relate to mass carrying particles that exist at huge distances. In the considered compartment an enumeration process establishes a kind of coordinate system. The master of the enumeration process is the distance function \mathcal{P} . This function has a flat parameter space.

$$\mathcal{P} = \wp \circ \psi \tag{1}$$

At small scales this function becomes a spread function ψ that governs the quantum physics of the model. The whole function \mathcal{P} is a convolution of a sharp part \wp and the spread function ψ . The differential of \wp delivers a local metric. The spread function appears to be generated by a Poisson generator which produces Qpatterns.

After a myriad of progression steps the original ordering of the natal state of the model is disturbed so much that the natal large and medium scale ordering is largely lost. However, this natal ordering is returning in the black regions that constitute pockets that surround them in universe. When the pockets merge into a huge black region, the history might restart enforced by the still existing low scale randomization and by the isotropic expansion factor, which is the consequence of the existence of massive particles at huge distances in the affine space.

The model uses a first part where elementary particles are formed by the representatives of the atomic propositions of the logic.

In a second part the formation of composites is described by a process called modularization. In that stage, in places where sufficient resources are present, the modularization process is capable of forming intelligent species.

This is the start of a new phase of evolution in which the intelligent species get involved in the modularization process and shift the mode from random design to intelligent design. Intelligent design runs much faster and uses its resources in a more efficient and conscientious way.

15 Conclusion

With respect to conventional physics, this simple model contains extra layers of individual objects. The most interesting addition is formed by the RQE's, the Qpatches, the Qtargets and the Qpatterns. They represent the atoms of the quantum logic sub-model.

The model gives an acceptable explanation for the existence of an (average) maximum velocity of information transfer. The two prepositions:

- Atomic quantum logic fundament
- Correlation vehicle

Lead to the existence of fuzzy interspacing of enumerators of the Hilbert space base vectors and to dynamically varying space curvature when compared to a flat reference continuum.

Without the freedom that is introduced by the interspacing fuzziness and which is used by the dynamic curvature, no dynamic behavior would be observable in the Palestra.

In the generation of the model the enumeration process plays a crucial role, but we must keep in mind that the choice of the enumerators and therefore the choice of the type of correlation vehicle is to a large degree arbitrary. It means that the Palestra has no natural origin. It is an affine space. The choice for quaternions as enumerators seems to be justified by the fact that the sign flavors of the quaternions explain the diversity of elementary particles.

Physicist that base their model of physics on an equivalent of the Gelfand triple which lacks a mechanism that creates the freedom that flexible interspaces provide, are using a model in which no natural curvature and fuzziness can occur. Such a model cannot feature dynamics.

Attaching a progression parameter to that model can only create the illusion of dynamics. However, that model cannot give a proper explanation of the existence of space curvature, space expansion, quantum physics or even the existence of a maximum speed of information transfer.

Physics made its greatest misstep after the nineteen thirties when it turned away from the fundamental work of Garret Birkhoff and John von Neumann. This deviation did not prohibit pragmatic use of the new methodology. However, it did prevent deep understanding of that technology because the methodology is ill founded.

Doing quantum physics in continuous function spaces is possible, but it makes it impossible to find the origins of dynamics, curvature and inertia. Most importantly it makes it impossible to find the reason of existence of quantum physics.

Only the acceptance of the fact that ***physics is fundamentally countable*** can solve this dilemma.

Please attack these statements with your criticism.