The special theory of relativity: definition of an impulse and kinetic energy of the closed system of constantly cooperating bodies

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In article attempt to show on a concrete example becomes that application of the special theory of relativity by consideration of movement of the closed mechanical system of bodies in inertial systems of readout can lead to that the impulse and kinetic energy of the closed system will be time functions.

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1. The introduction

In the special theory of relativity of dependence of an impulse and kinetic energy of a dot body from speed of its movement are defined from a condition of compulsion of performance of laws of preservation of an impulse and energy for the closed system of the bodies which interaction has short-term character.

In article it is offered to consider the closed mechanical system of the bodies which interaction has constant character, for acknowledgement of applicability of laws of preservation of an impulse and energy in case of use of the special theory of relativity as an example.

2. Description of a closed mechanical system of bodies

For consideration we take the elementary closed mechanical system of the bodies having constant interaction.

Let's assume that there is the closed mechanical system of bodies shown on fig. 1 and consisting of dot bodies 1 and 2, having equal weight $M_0$ at rest, and thread 3.

Bodies 1 and 2 are connected by a thread 3 which at rest has weight $m_0$ in regular intervals distributed on length.

Bodies 1 and 2 (and a thread 3) rotate with angular speed $\omega$ round the general center of weights - point $O_c$.

The distance from a dot body 1 (body 2) to point $O_c$ is equal $R$.

Let's place the considered closed mechanical system of bodies 1 and 2 with
a thread 3 in inertial system of readout Oxyz so that point Oc would be motionless in this system of readout and coincided with the beginning of coordinates O, and rotation of bodies 1 and 2 round it would occur against an hour hand in plane Oxy, as is shown in fig. 2.

![Fig. 2](image)

Also we will admit that at the moment of time reference mark (t=0) in system of readout Oxyz a bodies 1 and 2 were on axes Ox, and a body 1 had positive coordinate, and a body 2 – negative.

In system of readout Oxyz:

- the body 1 has coordinates $x_1$ and $y_1$ and projections $v_{1x}$ and $v_{1y}$ of speed on axis Ox and Oy accordingly depending on time moment $t_1$, equal $t_1$:

\[
x_1 = R \cdot \cos(\omega \cdot t_1)
\]

\[
y_1 = R \cdot \sin(\omega \cdot t_1)
\]

\[
v_{1x} = -[\omega \cdot R \cdot \sin(\omega \cdot t_1)]
\]

\[
v_{1y} = [\omega \cdot R \cdot \cos(\omega \cdot t_1)]
\]

- the body 2 has coordinates $x_2$ and $y_2$ and projections $v_{2x}$ and $v_{2y}$ of speed on axis Ox and Oy accordingly depending on time moment $t_2$, equal $t_2$:

\[
x_2 = -[R \cdot \cos(\omega \cdot t_2)]
\]

\[
y_2 = -[R \cdot \sin(\omega \cdot t_2)]
\]

\[
v_{2x} = \omega \cdot R \cdot \sin(\omega \cdot t_2)
\]

\[
v_{2y} = -[\omega \cdot R \cdot \cos(\omega \cdot t_2)]
\]
Let's enter one more inertial systems of readout O'x'y'z', shown on fig. 3.

Let's admit that at inertial systems of readout Oxyz and O'x'y'z':
- similar axes of the Cartesian coordinates are in pairs parallel and equally directed;
- system O'x'y'z' moves concerning system Oxyz with constant speed V along axis Ox;
- as time reference mark (t=0 and t'=0) in both systems that moment when the beginnings of coordinates O and O' these systems coincided is chosen.

Leaning against Lorentz's transformations and transformations of speeds [1] it is possible to write down:

- communication between coordinates x'₁ and y'₁ of body 1 at the moment of time t', equal t'₁, in system of readout O'x'y'z' and coordinates x₁ and y₁ of body 1 in system of readout Oxyz at the moment of time t₁, corresponding to time moment t'₁ in system of readout O'x'y'z':

\[
x'₁ = \frac{x₁ - (V \cdot t₁)}{\sqrt{1 - \frac{V²}{c²}}}
\]

(9)

\[
y'₁ = y₁
\]

(10)

where: c - a constant in Lorentz's transformations (according to assumption
it is equal to a velocity of light in vacuum),

- communication between time moment \( t'_1 \) (event with a body 1) in system of readout \( O'x'y'z' \) and time moment \( t_1 \) (the same event with a body 1) in system of readout \( Oxyz \), corresponding to time moment \( t'_1 \) in system of readout \( O'x'y'z' \):

\[
t'_1 = t_1 - \frac{V \cdot x_1}{c^2} = t_1 - \frac{V \cdot R \cdot \cos(\omega \cdot t_1)}{c^2}
\]

(11)

- communication between projections \( v'_{x1} \) and \( v'_{y1} \) on axis \( O'x' \) and \( O'y' \) of speed of movement \( v'_1 \) of body 1 at the moment of time \( t'_1 \) in system of readout \( O'x'y'z' \) and projections \( v_{x1} \) and \( v_{y1} \) on axis \( Ox \) and \( Oy \) of speed of movement \( v_1 \) of body 1 in system of readout \( Oxyz \) at the moment of time \( t_1 \), corresponding to time moment \( t'_1 \) in system of readout \( O'x'y'z' \):

\[
v'_{x1} = \frac{v_{x1} - V}{1 - \frac{V \cdot v_{x1}}{c^2}} = -\left[\frac{\omega \cdot R \cdot \sin(\omega \cdot t_1)}{1 + \frac{V \cdot \omega \cdot R \cdot \sin(\omega \cdot t_1)}{c^2}}\right] + V
\]

(12)

\[
v'_{y1} = \frac{v_{y1} \cdot \sqrt{1 - \frac{V^2}{c^2}}}{1 - \frac{V \cdot v_{x1}}{c^2}} = \frac{\omega \cdot R \cdot \cos(\omega \cdot t_1) \cdot \sqrt{1 - \frac{V^2}{c^2}}}{1 + \frac{V \cdot \omega \cdot R \cdot \sin(\omega \cdot t_1)}{c^2}}
\]

(13)

and besides:

\[
v'_1^2 = v'_{x1}^2 + v'_{y1}^2 = \frac{1 + \frac{V \cdot \omega \cdot R \cdot \sin(\omega \cdot t_1)}{c^2}}{\left[1 + \frac{V \cdot \omega \cdot R \cdot \sin(\omega \cdot t_1)}{c^2}\right]^2} \cdot c^2
\]

(14)

- communication between coordinates \( x'_2 \) and \( y'_2 \) of body 2 at the moment of time \( t'_2 \), equal \( t'_2 \), in system of readout \( O'x'y'z' \) and coordinates \( x_2 \) and \( y_2 \) of body 2 in system of readout \( Oxyz \) at the moment of time \( t_2 \), corresponding to time moment \( t'_2 \) in system of readout \( O'x'y'z' \):

\[
x'_2 = \frac{x_2 - (V \cdot t_2)}{\sqrt{1 - \frac{V^2}{c^2}}}
\]

\[
y'_2 = y_2
\]

(15)

(16)
- communication between time moment \( t'_2 \) (event with a body 2) in system of readout \( O'x'y'z' \) and time moment \( t_2 \) (the same event with a body 2) in system of readout \( Oxyz \), corresponding to time moment \( t'_2 \) in system of readout \( O'x'y'z' \):

\[
t'_2 = \frac{t_2 - \frac{V \cdot x_2}{c^2}}{\sqrt{1 - \frac{V^2}{c^2}}} = \frac{t_2 + \frac{V \cdot R \cdot \cos(\omega \cdot t_2)}{c^2}}{\sqrt{1 - \frac{V^2}{c^2}}}
\]

(17)

- communication between projections \( v'_x_2 \) and \( v'_y_2 \) on axis \( O'x' \) and \( O'y' \) of speed of movement \( v'_2 \) of body 2 at the moment of time \( t'_2 \) in system of readout \( O'x'y'z' \) and projections \( v_{x_2} \) and \( v_{y_2} \) on axis \( Ox \) and \( Oy \) of speed of movement \( v_2 \) of body 2 in system of readout \( Oxyz \) at the moment of time \( t_2 \), corresponding to time moment \( t'_2 \) in system of readout \( O'x'y'z' \):

\[
v'_x_2 = \frac{v_{x_2} - V}{1 - \frac{V \cdot v_{x_2}}{c^2}} = \frac{[\omega \cdot R \cdot \sin(\omega \cdot t_2)] - V}{1 - \frac{V \cdot \omega \cdot R \cdot \sin(\omega \cdot t_2)}{c^2}}
\]

\[
v'_y_2 = \frac{v_{y_2} \cdot \sqrt{1 - \frac{V^2}{c^2}}}{1 - \frac{V \cdot v_{x_2}}{c^2}} = \frac{\omega \cdot R \cdot \cos(\omega \cdot t_2) \cdot \sqrt{1 - \frac{V^2}{c^2}}}{1 - \frac{V \cdot \omega \cdot R \cdot \sin(\omega \cdot t_2)}{c^2}}
\]

(18)

and besides:

\[
v'_2^2 = v'_{x_2}^2 + v'_{y_2}^2 = \left\{1 - \frac{V \cdot \omega \cdot R \cdot \sin(\omega \cdot t_2)}{c^2}\right\}^2 - \left[\left(1 - \frac{V^2}{c^2}\right) \cdot \left(1 - \frac{\omega^2 \cdot R^2}{c^2}\right)\right] \cdot c^2
\]

(19)

\[
\]

(20)

For consideration a thread 3 at rest we will conditionally divide on \( 2 \cdot n \) equal parts with placing in the center of each part of a dot body with weight of rest \( m_0n \), equal:

\[
m_0n = \frac{m_0}{2 \cdot n}
\]

(21)

The points of a thread 3 which are on a piece from point \( O_c \) to a body 1, we will designate as \( i \)-points \((i = 0, 1, 2, 3, \ldots n)\), and the points of a thread 3 located on a piece from point \( O_c \) to a body 2, we will designate as \( j \) points \((j = 0, 1, 2, 3, \ldots n)\).
Thus distance $R_i$ from point $O_c$ to $i$-points of a thread 3 is equal:

$$R_i = R \cdot \left( \frac{1}{2} \cdot \frac{i}{n} + \frac{i-1}{n} \right) \quad (22)$$

And distance $R_j$ from point $O_c$ to $j$-points of a thread 3 will be defined as:

$$R_j = R \cdot \left( \frac{1}{2} \cdot \frac{j}{n} + \frac{j-1}{n} \right) \quad (23)$$

In system of readout $Oxyz$:

- $i$-point of a thread 3 has coordinates $x_{1i}$ and $y_{1i}$ and projections $v_{1xi}$ and $v_{1yi}$ of speed on axis Ox and Oy accordingly depending on time moment $t$, equal $t_{1i}$:

$$x_{1i} = R_i \cdot \cos(\omega \cdot t_{1i}) \quad (24)$$

$$y_{1i} = R_i \cdot \sin(\omega \cdot t_{1i}) \quad (25)$$

$$v_{1xi} = -[\omega \cdot R_i \cdot \sin(\omega \cdot t_{1i})] \quad (26)$$

$$v_{1yi} = [\omega \cdot R_i \cdot \cos(\omega \cdot t_{1i})] \quad (27)$$

- $j$-point of a thread 3 has coordinates $x_{2j}$ and $y_{2j}$ and projections $v_{2xj}$ and $v_{2yj}$ of speed on axis Ox and Oy accordingly depending on time moment $t$, equal $t_{2j}$:

$$x_{2j} = -R_j \cdot \cos(\omega \cdot t_{2j}) \quad (28)$$

$$y_{2j} = -R_j \cdot \sin(\omega \cdot t_{2j}) \quad (29)$$

$$v_{2xj} = \omega \cdot R_j \cdot \sin(\omega \cdot t_{2j}) \quad (30)$$

$$v_{2yj} = -[\omega \cdot R_j \cdot \cos(\omega \cdot t_{2j})] \quad (31)$$

Similarly using Lorentz's transformations and transformation of speeds [1] it is possible to write down:

- communication between coordinates $x'_{1i}$ and $y'_{1i}$ of $i$-point of a thread 3 at the moment of time $t'$, equal $t'_{1i}$, in system of readout $O'x'y'z'$ and coordinates $x_{1i}$ and $y_{1i}$ of $i$-point of a thread 3 in system of readout $Oxy$ at the moment of time $t_{1i}$, corresponding to time moment $t'_{1i}$ in system of readout $O'x'y'z'$:

$$x'_{1i} = \frac{x_{1i} - (V \cdot t_{1i})}{\sqrt{1 - \frac{V^2}{c^2}}} \quad (32)$$

$$y'_{1i} = y_{1i} \quad (33)$$

- communication between time moment $t'_{1i}$ (event from $i$-point of a thread
3) in system of readout O'x'y'z' and time moment $t_{1i}$ (the same event from $i$-point of a thread) 3) in system of readout Oxyz, corresponding to time moment $t'_{1i}$ in system of readout O'x'y'z':

$$t'_{1i} = \frac{t_{1i} - \frac{V \cdot x_{1i}}{c^2}}{\sqrt{1 - \frac{V^2}{c^2}}} = \frac{t_{1i} - \frac{V \cdot R_i \cdot \cos(\omega \cdot t_{1i})}{c^2}}{\sqrt{1 - \frac{V^2}{c^2}}}$$ (34)

- communication between projections $v'_{x1i}$ and $v'_{y1i}$ on axis O'x' and O'y' of speed of movement $v'_{1i}$ of $i$-point of a thread 3 at the moment of time $t'_{1i}$ in system of readout O'x'y'z' and projections $v_{x1i}$ and $v_{y1i}$ on axis Ox and Oy of speed of movement $v_{1i}$ of $i$-point of a thread 3 in system of readout Oxyz at the moment of time $t_{1i}$, corresponding to time moment $t'_{1i}$ in system of readout O'x'y'z':

$$v'_{x1i} = \frac{v_{x1i} - V}{1 - \frac{V \cdot v_{x1i}}{c^2}} = \frac{-\left[\omega \cdot R_i \cdot \sin(\omega \cdot t_{1i})\right] + V}{1 + \frac{V \cdot \omega \cdot R_i \cdot \sin(\omega \cdot t_{1i})}{c^2}}$$ (35)

$$v'_{y1i} = \frac{v_{y1i} \cdot \sqrt{1 - \frac{V^2}{c^2}}}{1 - \frac{V \cdot v_{x1i}}{c^2}} = \frac{\omega \cdot R_i \cdot \cos(\omega \cdot t_{1i}) \cdot \sqrt{1 - \frac{V^2}{c^2}}}{1 + \frac{V \cdot \omega \cdot R_i \cdot \sin(\omega \cdot t_{1i})}{c^2}}$$ (36)

and besides:

$$v'_{1i}^2 = v'_{x1i}^2 + v'_{y1i}^2 = \left\{1 + \frac{V \cdot \omega \cdot R_i \cdot \sin(\omega \cdot t_{1i})}{c^2}\right\}^2 - \left[\left(1 - \frac{V^2}{c^2}\right) \cdot \left(1 - \frac{\omega^2 \cdot R_i^2}{c^2}\right)\right]$$

$$= \frac{\left\{1 + \frac{V \cdot \omega \cdot R_i \cdot \sin(\omega \cdot t_{1i})}{c^2}\right\}^2}{1 + \frac{V \cdot \omega \cdot R_i \cdot \sin(\omega \cdot t_{1i})}{c^2}} \cdot c^2$$ (37)

- communication between coordinates $x'_{2j}$ and $y'_{2j}$ of $j$-point of a thread 3 at the moment of time $t'$, equal $t'_{2j}$, in system of readout O'x'y'z' and coordinates $x_{2j}$ and $y_{2j}$ of $j$-point of a thread 3 in system of readout Oxy at the moment of time $t_{2j}$, corresponding to time moment $t'_{2j}$ in system of readout O'x'y'z':

$$x'_{2j} = \frac{x_{2j} - \left(V \cdot t_{2j}\right)}{\sqrt{1 - \frac{V^2}{c^2}}}$$ (38)

$$y'_{2j} = y_{2j}$$ (39)

- communication between time moment $t'_{2j}$ (event from $j$-point of a thread 3) in system of readout O'x'y'z' and time moment $t_{2j}$ (the same event from $j$-point
of a thread 3) in system of readout \( Oxyz \), corresponding to time moment \( t'_{2j} \) in system of readout \( O'x'y'z' \):

\[
\frac{t'_{2j}}{c^2} = \frac{t_{2j} - \frac{V \cdot x_{2j}}{c^2}}{\sqrt{1 - \frac{V^2}{c^2}}} = \frac{t_{2j} + \frac{V \cdot R_j \cdot \cos(\omega \cdot t_{2j})}{c^2}}{\sqrt{1 - \frac{V^2}{c^2}}} \tag{40}
\]

- communication between projections \( v'_{x2j} \) and \( v'_{y2j} \) on axis \( O'x' \) and \( O'y' \) of speed of movement \( v'_{2j} \) of \( j \)-point of a thread 3 at the moment of time \( t'_{2j} \) in system of readout \( O'x'y'z' \) and projections \( v_{x2j} \) and \( v_{y2j} \) on axis \( Ox \) and \( Oy \) of speed of movement \( v_{2j} \) of \( j \)-point of a thread 3 in system of readout \( Oxyz \) at the moment of time \( t_{2j} \), corresponding to time moment \( t'_{2j} \) in system of readout \( O'x'y'z' \):

\[
v'_{x2j} = \frac{v_{x2j} - V}{1 - \frac{V \cdot v_{x2j}}{c^2}} = \frac{\left[ \omega \cdot R_j \cdot \sin(\omega \cdot t_{2j}) \right] - V}{1 - \frac{V \cdot \omega \cdot R_j \cdot \sin(\omega \cdot t_{2j})}{c^2}} \tag{41}
\]

\[
v'_{y2j} = \frac{v_{y2j} \cdot \sqrt{1 - \frac{V^2}{c^2}}}{1 - \frac{V \cdot v_{x2j}}{c^2}} = -\frac{\omega \cdot R_j \cdot \cos(\omega \cdot t_{2j}) \cdot \sqrt{1 - \frac{V^2}{c^2}}}{1 - \frac{V \cdot \omega \cdot R_j \cdot \sin(\omega \cdot t_{2j})}{c^2}} \tag{42}
\]

and besides:

\[
v'_{2j}^2 = v'_{x2j}^2 + v'_{y2j}^2 = \left\{ 1 - \frac{V \cdot \omega \cdot R_j \cdot \sin(\omega \cdot t_{2j})}{c^2} \right\}^2 - \left[ 1 - \frac{V^2}{c^2} \right] \cdot \left( 1 - \frac{\omega^2 \cdot R_j^2}{c^2} \right) \cdot c^2 \tag{43}
\]

3. Reception of the equations of an impulse and kinetic energy of system

Using dependences of an impulse and kinetic energy of a moving body on its speed of movement [1], we can write down following formulas:

- formulas for impulse \( P' \) of body 1 and its projections \( P'_{x1} \) and \( P'_{y1} \) on axis \( O'x' \) and \( O'y' \) in system of readout \( O'x'y'z' \) at the moment of time \( t' \), corresponding to time moment \( t \) in system of readout \( Oxyz \) (using formulas (12)
\[ P'_x_1 = \frac{v'_x_1 \cdot M_0}{\sqrt{1 - \frac{v'^2_1}{c^2}}} = - \frac{M_0 \cdot \{[\omega \cdot R \cdot \sin(\omega \cdot t_1)] + V\}}{\sqrt{1 - \frac{V^2}{c^2}} \cdot \sqrt{1 - \frac{\omega^2 \cdot R^2}{c^2}}} \]  

\[ P'_y_1 = \frac{v'_y_1 \cdot M_0}{\sqrt{1 - \frac{v'^2_1}{c^2}}} = \frac{M_0 \cdot \omega \cdot R \cdot \cos(\omega \cdot t_1)}{\sqrt{1 - \frac{\omega^2 \cdot R^2}{c^2}}} \]  

\[ P'_1 = \frac{v'_1 \cdot M_0}{\sqrt{1 - \frac{v'^2_1}{c^2}}} = M_0 \cdot c \cdot \left[ \left\{ \frac{1 + \frac{V \cdot \omega \cdot R \cdot \sin(\omega \cdot t_1)}{c^2}}{\sqrt{\left(1 - \frac{V^2}{c^2}\right) \cdot \left(1 - \frac{\omega^2 \cdot R^2}{c^2}\right)}} \right\} - 1 \right] \]  

- formula for kinetic energy \( E'_1 \) of body 1 in system of readout \( O'x'y'z' \) at the moment of time \( t'_1 \), corresponding to time moment \( t_1 \) in system of readout \( Oxyz \) (using the formula (14)):  

\[ E'_1 = M_0 \cdot c^2 \cdot \left( \frac{1}{\sqrt{1 - \frac{v'^2_1}{c^2}}} - 1 \right) = M_0 \cdot c^2 \cdot \left\{ \left[ \frac{1 + \frac{V \cdot \omega \cdot R \cdot \sin(\omega \cdot t_1)}{c^2}}{\sqrt{\left(1 - \frac{V^2}{c^2}\right) \cdot \left(1 - \frac{\omega^2 \cdot R^2}{c^2}\right)}} \right] - 1 \right\} \]  

- formulas for impulse \( P'_2 \) of body 2 and its projections \( P'_{x2} \) and \( P'_{y2} \) on axis \( O'x' \) and \( O'y' \) in system of readout \( O'x'y'z' \) at the moment of time \( t'_2 \), corresponding to time moment \( t_2 \) in system of readout \( Oxyz \) (using formulas (18) - (20)):  

\[ P'_{x2} = \frac{v'_{x2} \cdot M_0}{\sqrt{1 - \frac{v'^2_2}{c^2}}} = - \frac{M_0 \cdot \{[\omega \cdot R \cdot \sin(\omega \cdot t_2)] - V\}}{\sqrt{1 - \frac{V^2}{c^2}} \cdot \sqrt{1 - \frac{\omega^2 \cdot R^2}{c^2}}} \]  

\[ P'_{y2} = \frac{v'_{y2} \cdot M_0}{\sqrt{1 - \frac{v'^2_2}{c^2}}} = - \frac{M_0 \cdot \omega \cdot R \cdot \cos(\omega \cdot t_2)}{\sqrt{1 - \frac{\omega^2 \cdot R^2}{c^2}}} \]
\[ P'_2 = \frac{v'_2 \cdot M_0}{\sqrt{1 - \frac{v'_2^2}{c^2}}} = M_0 \cdot c \cdot \sqrt{\left\{ \frac{1 - V \cdot \omega \cdot R \cdot \sin(\omega \cdot t_2)}{c^2} \right\}^2 - \left( \frac{1 - \frac{V^2}{c^2}}{1 - \frac{\omega^2 \cdot R^2}{c^2}} \right) - 1} \]  

(50)

- formula for kinetic energy \( E'_2 \) of body 2 in system of readout \( O'x'y'z' \) at the moment of time \( t'_2 \), corresponding to time moment \( t_2 \) in system of readout \( Oxyz \) (using the formula (20)):

\[ E'_2 = M_0 \cdot c^2 \cdot \left( \frac{1}{\sqrt{1 - \frac{v'_2^2}{c^2}}} - 1 \right) = M_0 \cdot c^2 \cdot \left\{ \frac{1 - \frac{V \cdot \omega \cdot R \cdot \sin(\omega \cdot t_2)}{c^2}}{\sqrt{\left( \frac{1 - \frac{V^2}{c^2}}{1 - \frac{\omega^2 \cdot R^2}{c^2}} \right) - 1}} \right\} \]  

(51)

- formulas for impulse \( P'_{x1i} \) of \( i \)-point of a thread 3 and its projections \( P'_{x1i} \) and \( P'_{y1i} \) on axis \( O'x' \) and \( O'y' \) in system of readout \( O'x'y'z' \) at the moment of time \( t'_1i \), corresponding to time moment \( t_1i \) in system of readout \( Oxyz \) (using formulas (35) - (37)):

\[ p'_{x1i} = \frac{v'_{x1i} \cdot m_{0n}}{\sqrt{1 - \frac{v'_{1i}^2}{c^2}}} = - \frac{m_{0n} \cdot \{ \omega \cdot R_i \cdot \sin(\omega \cdot t_{1i}) \} + V}{\sqrt{1 - \frac{V^2}{c^2}} \cdot \sqrt{1 - \frac{\omega^2 \cdot R_i^2}{c^2}}} \]  

(52)

\[ p'_{y1i} = \frac{v'_{y1i} \cdot m_{0n}}{\sqrt{1 - \frac{v'_{1i}^2}{c^2}}} = \frac{m_{0n} \cdot \omega \cdot R_i \cdot \cos(\omega \cdot t_{1i})}{\sqrt{1 - \frac{\omega^2 \cdot R_i^2}{c^2}}} \]  

(53)

\[ p'_{1i} = \frac{v'_{1i} \cdot m_{0n}}{\sqrt{1 - \frac{v'_{1i}^2}{c^2}}} = m_{0n} \cdot c \cdot \frac{\left\{ \frac{1 + \frac{V \cdot \omega \cdot R_i \cdot \sin(\omega \cdot t_{1i})}{c^2}}{\sqrt{\left( \frac{1 - \frac{V^2}{c^2}}{1 - \frac{\omega^2 \cdot R_i^2}{c^2}} \right) - 1}} \right\}} \]  

(54)

- formula for kinetic energy \( E'_{1i} \) of \( i \)-point of a thread 3 in system of readout \( O'x'y'z' \) at the moment of time \( t'_1i \), corresponding to time moment \( t_{1i} \) in system of readout \( Oxyz \) (using the formula (37)): 

\[ E'_{1i} = M_0 \cdot c^2 \cdot \left( \frac{1}{\sqrt{1 - \frac{v'_{1i}^2}{c^2}}} - 1 \right) = M_0 \cdot c^2 \cdot \left\{ \frac{1 - \frac{V \cdot \omega \cdot R_i \cdot \sin(\omega \cdot t_{1i})}{c^2}}{\sqrt{\left( \frac{1 - \frac{V^2}{c^2}}{1 - \frac{\omega^2 \cdot R_i^2}{c^2}} \right) - 1}} \right\} \]  

(55)
\[ E'_{1i} = m_{0n} \cdot c^2 \cdot \left( \frac{1}{\sqrt{1 - \frac{v'_{1i}^2}{c^2}}} - 1 \right) = \]

\[ = m_{0n} \cdot c^2 \cdot \left\{ \frac{1 + \frac{V \cdot \omega \cdot R_i \cdot \sin(\omega \cdot t_{1i})}{c^2}}{\left( 1 - \frac{V^2}{c^2} \right) \left( 1 - \frac{\omega^2 \cdot R_i^2}{c^2} \right)} - 1 \right\} \quad (55) \]

- formulas for impulse \( P'_{2j} \) of \( j \)-point of a thread 3 and its projections \( P'_{x2j} \) and \( P'_{y2j} \) on axis \( O'x' \) and \( O'y' \) in system of readout \( O'x'y'z' \) at the moment of time \( t'_{2j} \), corresponding to time moment \( t_{2j} \) in system of readout \( Oxyz \) (using formulas (41) - (43)):

\[ P'_{x2j} = \frac{v'_{x2j} \cdot m_{0n}}{\sqrt{1 - \frac{v'_{x2j}^2}{c^2}}} = \frac{m_{0n} \cdot \left\{ \left[ \omega \cdot R_j \cdot \sin(\omega \cdot t_{2j}) \right] - V \right\}}{\sqrt{1 - \frac{V^2}{c^2}} \cdot \sqrt{1 - \frac{\omega^2 \cdot R_j^2}{c^2}}} \quad (56) \]

\[ P'_{y2j} = \frac{v'_{y2j} \cdot m_{0n}}{\sqrt{1 - \frac{v'_{y2j}^2}{c^2}}} = - \frac{m_{0n} \cdot \omega \cdot R_j \cdot \cos(\omega \cdot t_{2j})}{\sqrt{1 - \frac{\omega^2 \cdot R_j^2}{c^2}}} \quad (57) \]

\[ P'_{z2j} = \frac{v'_{z2j} \cdot m_{0n}}{\sqrt{1 - \frac{v'_{z2j}^2}{c^2}}} = m_{0n} \cdot c \cdot \left\{ \frac{1 - \frac{V \cdot \omega \cdot R_j \cdot \sin(\omega \cdot t_{2j})}{c^2}}{\left( 1 - \frac{V^2}{c^2} \right) \left( 1 - \frac{\omega^2 \cdot R_j^2}{c^2} \right)} \right\} - 1 \quad (58) \]

- formula for kinetic energy \( E'_{2j} \) of \( j \)-point of a thread 3 in system of readout \( O'x'y'z' \) at the moment of time \( t'_{2j} \), corresponding to time moment \( t_{2j} \) in system of readout \( Oxyz \) (using the formula (43)): 
\[ E'_{2j} = m_0 n \cdot c^2 \cdot \left( \frac{1}{\sqrt{1 - \frac{v'_{2j}^2}{c^2}}} - 1 \right) = \]

\[ = m_0 n \cdot c^2 \cdot \left\{ \left[ 1 - \frac{V \cdot \omega \cdot R_j \cdot \sin(\omega \cdot t_{2j})}{c^2} \right] \sqrt{1 - \frac{V^2}{c^2}} \right\} - 1 \] (59)

For definition of sizes of an impulse and kinetic energy of system of bodies 1 and 2 and thread 3 in system of readout \( O'x'y'z' \) at the moment of time \( t' \) it is necessary, that time moments \( t'_1, t'_2, t'_{1i}, \) and \( t'_{2j} \) (formulas (11), (17), (34) and (40)) were equal among themselves and equal \( t' \), i.e.:

\[ t' = t'_1 = t'_2 = t'_{1i} = t'_{2j} = \frac{t_1 - \frac{V \cdot R \cdot \cos(\omega \cdot t_1)}{c^2}}{\sqrt{1 - \frac{V^2}{c^2}}} \]

\[ = \frac{t_2 + \frac{V \cdot R \cdot \cos(\omega \cdot t_2)}{c^2}}{\sqrt{1 - \frac{V^2}{c^2}}} = \frac{t_{1i} - \frac{V \cdot R_i \cdot \cos(\omega \cdot t_{1i})}{c^2}}{\sqrt{1 - \frac{V^2}{c^2}}} = \]

\[ = \frac{t_{2j} + \frac{V \cdot R_j \cdot \cos(\omega \cdot t_{2j})}{c^2}}{\sqrt{1 - \frac{V^2}{c^2}}} \] (60)

Considering that the system of readout \( O'x'y'z' \) is inertial, it is possible to write down following formulas for kinetic energy \( E' \) and projections \( P'_x \) and \( P'_y \) on axis \( O'x' \) and \( O'y' \) of impulse \( P' \) of the closed mechanical system consisting of bodies 1 and 2 and thread 3, for time moment \( t' \) in system of readout \( O'x'y'z' \):

\[ P'_{x} = P'_{x1} + P'_{x2} + \sum_{i=1}^{i=n} P'_{x1i} + \sum_{j=1}^{j=n} P'_{x2j} \] (61)

\[ P'_{y} = P'_{y1} + P'_{y2} + \sum_{i=1}^{i=n} P'_{y1i} + \sum_{j=1}^{j=n} P'_{y2j} \] (62)
\[ P' = \sqrt{P'_{x}^2 + P'_{y}^2} \]  
\[ E' = E'_{1} + E'_{2} + \sum_{i=n} E'_{1i} + \sum_{j=n} E'_{2j} \]

4. The results of the calculation of the numerical example

For reception of the evident image of dependence of impulse \( P' \) and kinetic energy \( E' \) of the closed mechanical system consisting of bodies 1 and 2 and thread 3, from time \( t' \) in inertial system of readout \( O'x'y'z' \) it is possible to consider a numerical example, having entered the following any way chosen initial data:

\[ \frac{V}{c} = 0,9 \]  
\[ \frac{\omega \cdot R}{c} = 0,8 \]  
\[ \frac{m_{0}}{M_{0}} = 0,1 \]  
\[ n = 10 \]

Calculation can be spent under the following scheme:
- setting values of the moment of time \( t' \) (we will admit that \( t' \) has values:
  - \(-2R/c, -R/c, 0, R/c \ldots 21R/c\) and using the formula (60), we define values of the moments of time \( t_{1}, t_{2}, t_{i1} \) and \( t_{2j} \);
- further we define values of kinetic energy \( E'_{1} \) and projections \( P'_{x1} \) and \( P'_{y1} \) impulse \( P'_{1} \) of body 1 (formulas (44), (45) and (47)), kinetic energy \( E'_{2} \) and projections \( P'_{x2} \) and \( P'_{y2} \) of impulse \( P'_{2} \) of body 2 (formulas (48), (49) and (51)), kinetic energies \( E'_{1i} \) and projections \( P'_{x1i} \) and \( P'_{y1i} \) of impulses \( P'_{1i} \) of \( i \)-points of a thread 3 (formulas (52), (53) and (55)), kinetic energies \( E'_{2j} \) and projections \( P'_{x2j} \) and \( P'_{y2j} \) of impulses \( P'_{2j} \) of \( j \)-points of a thread 3 (formulas (56), (57) and (59)) for the various moments of time \( t' \) in inertial system of readout \( O'x'y'z' \);
- then for the various moments of time \( t' \) in inertial system of readout \( O'x'y'z' \) we define values of kinetic energy \( E' \) (the formula (64)), projections \( P'_{x} \)
and $P'_y$ of impulse $P'$ of system of bodies 1 and 2 and thread 3 (formulas (61) and (62)), absolute size $|P'|$ of impulse $P'$, using the formula (63), and also values of a corner $\alpha'$ between a direction of a vector of impulse $P'$ and axis $O'x'$, defined under the formula:

$$\alpha' = \arctg \left( \frac{P'_y}{P'_x} \right) \quad (69)$$

Results of calculation are resulted in schedules:

- the schedule of dependence of absolute size $|P'|$ of impulse $P'$ of system of bodies 1 and 2 and thread 3 from time size $t'$ (with the account and without weight of a thread 3), represented on fig. 4;

- the schedule of dependence of size of a corner $\alpha'$ between a direction of a vector of impulse $P'$ of system of bodies 1 and 2 and thread 3 and axis $O'x'$ from time size $t'$ (with the account and without weight of a thread 3), represented on fig. 5;
the schedule of dependence of kinetic energy $E'$ of system of bodies 1 and 2 and thread 3 from time size $t'$ (with the account and without weight of a thread 3), represented on fig. 6;

In article [2] doctor Michael H. Brill dependences of kinetic energy $E'$ and
projections of impulse $P'$ on an axis of coordinates $x$ and $y$ systems of bodies 1 and 2 from time size $t'$ are represented.

As a result of calculation it has been received that use of the special theory of relativity leads to that in inertial system of readout $O'x'y'z'$ the closed mechanical system of bodies 1 and 2 and thread 3 has variable in time $t'$ on absolute size and a direction a vector of impulse $P'$ and variable in time $t'$ value of kinetic energy $E'$ (i.e. kinetic energy $E'$ and impulse $P'$ this closed system are time functions of time $t'$) that contradicts the law of preservation of an impulse and the law of conservation of energy (if the assumption is true that if in one inertial system of readout at the closed mechanical system and its components do not occur change of size of potential energy and in any other inertial system of readout at the same closed mechanical system and its components will not occur change of size of potential energy).

As a result it is possible to draw a conclusion that in inertial system of readout $O'x'y'z'$ application of the special theory of relativity at the description of movement of the closed mechanical system of the bodies considered in the given example, leads to default of the law of preservation of an impulse and the law of conservation of energy (since in the closed mechanical system there is a change of size of kinetic energy without change of size of potential energy).

5. Conclusion

In summary it is possible to notice that use of the special theory of relativity by consideration of separate examples can lead to default of laws of preservation of an impulse and energy of the closed mechanical system in inertial systems of readout.

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