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Abstract: We examine whether gravitational waves would be generated during the initial phase, \( \delta_0 \), of the universe when triggered by changes in spacetime geometry; i.e. We hope to find traces of the breakdown of the Entropy/QM spacetime regime during \( \delta_0 \). As well as proof, one way or another if several models of cosmology, giving different interpretations are verifiable.

Keywords: High-frequency Gravitational Waves (HFGW), symmetry, causal discontinuity

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1. Introduction

This paper examines geometric changes that may have occurred in the very earliest phase of the universe [1], or \( \delta_0 \), and explores how we might be able to gain insight into this epoch through gravitational wave research. The Planck epoch has remained mysterious, and may be invisible to all other kinds of detectors, but the universe’s gravity wave background radiation likely contains the imprint of even the very earliest events. Changes in the geometry of spacetime near the Planck scale could be revealed or studied in this manner. We discuss how to obtain insights into \( \delta_0 \), initially, while looking at the geometric considerations determining space and time development which would create relevant space-time geometry phase changes during the early universe. Each such phase change should produce gravitational waves.. Secondly, we review what are other candidate models which may have experimental verification if GW astronomy becomes a reality.

The topological transition is due to a change in basis / geometry from the regime of Renyi entropy to entropy in a particle count version of entropy, i.e. \( S \sim \langle n \rangle \) . This \( \rho_{\text{vacuum}} = [\Lambda/8\pi \cdot G] \) if stated correctly may enable tying in initial vacuum expectation value (VeV) behavior with the following diagram. Note that cosmology models have to be consistent with the following diagram.

![Diagram](image)

Figure 1, as supplied by L. Crowell, in correspondence to A. W. Beckwith, October 24, 2010 [2]
As stated by L. Crowell [8], in an email sent to A. Beckwith, the way to delineate the evolution of the VeV issue is to consider an initially huge VeV, due to initial inflationary geometry. As stated by L. Crowell [2]:

“The standard inflationary cosmology involves a scalar field \( \phi \) which obeys a standard wave equation. The potential is this function which I diagram ‘above’. The scalar field starts at the left and rolls down the slope until it reaches a value of \( \phi \) where the potential is \( V(\phi) \sim \phi^2 \). The enormous VeV at the start is about 14 orders of magnitude smaller than the Planck energy density \( (1/L_p)^4 \) on the long slope. The field then enters the quadratic region, where a lot of that large VeV energy is thermalized, with a tiny bit left that is the VeV and CC of the observable universe. The universe during this roll down the long small slope has a large cosmological constant, actually variable \( \lambda = \lambda(\phi, \partial \phi) \), which forces the exponential expansion. There are about 60-efolds of the universe through that period. Then at the low energy VeV the much smaller CC gives the universe with the configuration we see today.”

One of the ways to relate an energy density to cosmological parameters and a vacuum energy density may be using a relation as given by (1), as given by Poplawski [3]:

\[
\rho_\Lambda = H \lambda_{QCD}
\]

Where if \( \lambda_{QCD} \) is at least 200MeV and is similar to the QCD scale parameter of the SU(3) gauge coupling constant, and H a Hubble parameter. We can then equate vacuum potential with vacuum expectation values as follows:

\[
\rho_{\text{vacuum}} = \left[ \Lambda/8\pi \cdot G \right] \approx \rho_\Lambda \approx H \lambda_{QCD} \Leftrightarrow V \sim 3 \langle H \rangle^4 / 16\pi^2 \sim V_{\inf} \approx \phi^2
\]

Different models for the Hubble parameter, \( H \) exist, and can be directly linked to how one forms the inflaton. The authors presently explore what happens to the relations as given in Eq. (2) before, during, and after inflation. Table 1 below, is how to obtain inflation. In addition, in tandem to a suggestion made by Penrose, 2007 we investigate a dynamical systems mapping for recycling matter “caught” by millions of black holes, in the universe, to be recycled to the initial stages of a new big bang. The two mappings together may enable a description of how quantum gravity arises.

2.1 Re-casting the problem of GW / Graviton in a detector for “massive” Gravitons

We now turn to the problem of detection. The following discussion is based upon with the work of Dr. Li, Dr/ Beckwith, and other Institute of theoretical physics researchers in Chongquing University [4], [5]. For a cavity containing electromagnetic energy, if Q is the quality factor of a cavity, \( \xi \) is the total energy in a cavity, \( h\omega_e \) is the energy of a photon in the cavity, then the minimum sensitivity to a stochastic HFGW would need a metric ‘amplitude’ of at least

\[
\hbar_{\text{min}} \approx \frac{1}{\sqrt{Q}} \cdot \sqrt{\frac{h\omega_e}{\xi}}
\]

This can be a significant limitation in practice. For example, as quoted from a document being written up by F. Li et al, for publication [6] if \( Q = 10^{11}, E = 10^J, \) and \( \omega_e \) is a frequency \( = 10^{12} \) Hz, then one will obtain \( \hbar_{\text{min}} \sim 2.5 \times 10^{-17} \) for the stochastic HFGW. Therefore, we can conclude that advanced cavity detectors could be a promising way for the HFGW detection if much higher contained energies are developed. Similarly, if one has, instead, a coherent GW background,[6], [7],[8],[9] then

\[
\hbar_{\text{min}} \approx \frac{1}{Q} \cdot \sqrt{\frac{h\omega_e}{\xi}}
\]
It this case \( h_{\text{min}} \sim 8.1 \times 10^{-23} \) for the non-stochastic HFGW, even at a very low contained energy of 10 J. It is therefore quite plausible that such a detection cavity could be tuned over a range of HFGW frequencies to scan for detectible gravitational waves of either a coherent or stochastic nature. Given these figures, it is now time to consider what happens if one is looking for traces of gravitons which may have a small rest mass in four dimensions. What Li et al have shown in 2003 [10] which Beckwith commented [6] is to obtain a way to present first order perturbative electromagnetic power flux, i.e. what was called \( T_{\mu
u}^{(i)} \) in terms of a non zero graviton rest mass, in a detector, in an uniform magnetic field, i.e. [6], [10][23] what if we have curved space time with say an energy momentum tensor of the electro magnetic fields in GW fields as

\[
T_{\mu\nu} = \frac{1}{\mu_0} \left[ -F_{\mu\nu}^\alpha F_{\nu\alpha} + \frac{1}{4} \cdot g_{\mu\nu} F_{\alpha\beta} F_{\alpha\beta} \right]
\]  

(5)

Li et al [23] state that \( F_{\mu\nu} = F_{\mu\nu}^{(0)} + \tilde{F}_{\mu\nu}^{(i)} \), with \( \left| \tilde{F}_{\mu\nu}^{(i)} \right| \ll \left| F_{\mu\nu}^{(0)} \right| \) will lead to

\[
T_{\mu\nu}^{(i)} = T_{\mu\nu}^{(0)} + T_{\mu\nu}^{(i)}
\]

(6)

The 1st term to the right hand side of Eq. (6) is the energy – momentum tensor of the back ground electro magnetic field, and the 2nd term to the right hand side of Eq. (6) is the first order perturbation of an electro magnetic field due to gravitational waves. The above Eq.(5) and Eq. (6) will lead to Maxwell equations as

\[
\frac{1}{\sqrt{-g}} \cdot \frac{\partial}{\partial \bar{x}'^\nu} \left( \sqrt{-g} \cdot g^{\mu\nu} g_{\alpha\beta} F_{\alpha\beta} \right) = \mu_0 J^\mu
\]

(7)

as well as

\[
F_{[\mu\nu,\alpha]} = 0
\]

(8)

Eventually, with GW affecting the above two equations, we have a way to isolate \( T_{\mu\nu}^{(i)} \). If one looks at if a four dimensional graviton with a very small rest mass included [6], [10]we can write

\[
\frac{1}{\sqrt{-g}} \cdot \frac{\partial}{\partial \bar{x}'^\nu} \left( \sqrt{-g} \cdot g^{\mu\nu} g_{\alpha\beta} F_{\alpha\beta} \right) = \mu_0 J^\mu + J_{\text{effective}}
\]

(9)

where for \( \varepsilon^+ \neq 0 \) but very small

\[
F_{[\mu\nu,\alpha]} \sim \varepsilon^+
\]

(10)

The claim which A. Beckwith made [16], [22] is that

\[
J_{\text{effective}} \propto n_{\text{count}} \cdot m_{4-D-Graviton}
\]

(11)

As stated by Beckwith, in [6], [11], [12] \( m_{4-D-Graviton} \sim 10^{-65} \) grams \( , n_{\text{count}} \) is the number of gravitons which are in the detector. What Beckwith, and Li, intend to do is to try to isolate out an appropriate \( T_{\mu\nu}^{(i)} \) assuming non zero graviton rest mass, and using Eq. (9), Eq. (10) and Eq. (11) . From there, the energy density contributions of \( T_{\mu\nu}^{(i)} \), i.e. \( T_{\mu\nu}^{(0)} \) can be isolated, and reviewed in order to obtain traces of \( \tilde{\beta} \), which can be used to interpret Eq. (15) . application of the Gauss mapping of [13],[14]. With the LHS being degrees of freedom, in Eq. (12b) [1], [15]

\[
E_{\text{thermal}} \approx \frac{1}{2} k_b T_{\text{temperature}} \propto \Omega_\gamma \tilde{T} \sim \tilde{\beta}
\]

(12a)

\[
x_{i+1} = \exp\left[ -\tilde{\alpha} \cdot x_i^2 \right] + \tilde{\beta}
\]

(12b)
I.e. use $\bar{\beta} \equiv |F|$ and make a linkage of sorts with $\mathcal{T}^{(i)}_{G00}$. The term $\mathcal{T}^{(i)}_{G00}$ isolated out from $\mathcal{T}^{(i)}_{G\nu \nu}$ present day data. The point here that the detected GW would help constrain and validate Eq. 14. Then, the next step will be making sense out of different GW measurement protocols.

2.2 : NOTE TO TAME THE INCOMMENSURATE METRICS, THE APPROXIMATION given below is used as a START to come up with how to make measurements. [1]

$$h_0^2 \Omega_{GW} \sim 10^{-6} \quad (13a)$$

Next, we will commence to note the difference and the variances from using $h_0^2 \Omega_{GW} \sim 10^{-6}$ as a unified measurement which will be in the different models discussed right afterwards

2.3 Wavelength, sensitivity and other such constructions from Maggiore, with our adaptations and comments

We will next give several of our considerations as to early universe geometry which we think are appropriate as to Maggiore’s [1],[16] treatment of both wavelength, strain, and $\Omega_{GW}$. To begin with, look at Maggiore’s [1] [16] $\Omega_{GW}$ formulation, strain, and what we did with observations as from L. Crowell [17] which ties in with the ten to the tenth power increase as to wave length from pre Planckian physics to 1-10 GHz inflationary GW frequencies. We will proceed to look at how the conclusions factor in with information exchange between different universes. We begin with the following, Table 1 and Table 2. What we have stated below in Table 2 and Table 3 will have consequences of information flow from a prior to present universe, and fine tuning GW variance

Table 1: Managing GW generation from Pre Planckian physics [1], [16]

<table>
<thead>
<tr>
<th>$h_c \leq 2.82 \times 10^{-33}$</th>
<th>$f_{GW} \sim 10^{12}$ Hertz</th>
<th>$\lambda_{GW} \sim 10^{-8}$ meters</th>
</tr>
</thead>
<tbody>
<tr>
<td>$h_c \leq 2.82 \times 10^{-31}$</td>
<td>$f_{GW} \sim 10^{10}$ Hertz</td>
<td>$\lambda_{GW} \sim 10^{-2}$ meters</td>
</tr>
<tr>
<td>$h_c \leq 2.82 \times 10^{-29}$</td>
<td>$f_{GW} \sim 10^{8}$ Hertz</td>
<td>$\lambda_{GW} \sim 10^{0}$ meters</td>
</tr>
<tr>
<td>$h_c \leq 2.82 \times 10^{-27}$</td>
<td>$f_{GW} \sim 10^{6}$ Hertz</td>
<td>$\lambda_{GW} \sim 10^{2}$ meters</td>
</tr>
<tr>
<td>$h_c \leq 2.82 \times 10^{-25}$</td>
<td>$f_{GW} \sim 10^{4}$ Hertz</td>
<td>$\lambda_{GW} \sim 10^{4}$ kilometer</td>
</tr>
<tr>
<td>$h_c \leq 2.82 \times 10^{-23}$</td>
<td>$f_{GW} \sim 10^{2}$ Hertz</td>
<td>$\lambda_{GW} \sim 10^{6}$ kilometer</td>
</tr>
</tbody>
</table>

What we are expecting, as given to us by L. Crowell,[17] is that initial waves, synthesized in the initial part of the Planckian regime would have about $\lambda_{GW} \sim 10^{-14}$ meters for $f_{GW} \sim 10^{22}$ Hertz which would turn into $\lambda_{GW} \sim 10^{-1}$ meters for $f_{GW} \sim 10^{9}$ Hertz, and sensitivity of $h_c \leq 2.82 \times 10^{-30}$. This is assuming that $h_0^2 \Omega_{GW} \sim 10^{-6}$, using Maggiorie’s [16]$h_0^2 \Omega_{GW}$ analytical expression.[1]

It is important to note in all of this, that when we discuss the different models that the $h_0^2 \Omega_{GW} \sim 10^{-6}$ is the first measurement metric which is drastically altered. $h_c$ should be also noted to be an upper bound. In reality, only the 2nd and 3rd columns in table 1 above escape being seriously off and very different. So for table 1, the first column is meant to be an upper bound which, even if using Eq. (15.c) may be off by an order of
magnitude. More seriously, the number of gravitons per unit volume of phase space as estimated, is heavily
dependent upon $h_0^2\Omega_{GW} \sim 10^{-6}$. If that is changed, which shows up in the models discussed right afterwards,
the degree of fidelity with Eq. (13.b) drops

Table 2: Managing GW count from Planckian physics/unit-phase-space[1],[16]

<table>
<thead>
<tr>
<th>$\lambda_{GW}$</th>
<th>$n_f$</th>
<th>phase space</th>
</tr>
</thead>
<tbody>
<tr>
<td>$10^{-4}$ meters</td>
<td>$10^{-6}$</td>
<td>$n_f \propto 10^{-6}$ graviton/phase space</td>
</tr>
<tr>
<td>$10^{-2}$ meters</td>
<td>$10^{2}$</td>
<td>$n_f \propto 10^{2}$ graviton/phase space</td>
</tr>
<tr>
<td>$10^{0}$ meters</td>
<td>$10^{10}$</td>
<td>$n_f \propto 10^{10}$ graviton/phase space</td>
</tr>
<tr>
<td>$10^{2}$ meters</td>
<td>$10^{18}$</td>
<td>$n_f \propto 10^{18}$ graviton/phase space</td>
</tr>
<tr>
<td>$10^{1}$ kilometer</td>
<td>$10^{26}$</td>
<td>$n_f \propto 10^{26}$ graviton/phase space</td>
</tr>
<tr>
<td>$10^{3}$ kilometer</td>
<td>$10^{34}$</td>
<td>$n_f \propto 10^{34}$ graviton/phase space</td>
</tr>
</tbody>
</table>

The particle per phase state count will be given as, if $h_0^2\Omega_{GW} \sim 10^{-6}$ [1], [16]

$$n_f \sim h_0^2\Omega_{GW} \cdot \frac{10^{37}}{3.6} \cdot \left[\frac{1000 \text{Hz}}{f}\right]^{-4}$$

(13.b)

Secondly we have that a detector strain for device physics is given by [1],[16]

$$h_C \lesssim \left(2.82 \times 10^{-21}\right) \cdot \left(\frac{1 \text{Hz}}{f}\right)$$

(13.c)

These values of strain, the numerical count, and also of $n_f$ give a bit count and entropy which will lead to
possible limits as to how much information is transferred. Note that per unit space, if we have an entropy count
of , after the start of inflation with having the following , namely at the beginning of relic inflation.

$$\lambda_{GW} \sim 10^{-14}\text{ meters} \Rightarrow n_f \propto 10^{15} \text{ graviton/unit space}$$

for $f_{GW} \sim 10^{9} \text{ Hertz}$ This is to have, say a
starting point in pre inflationary physics of $f_{GW} \sim 10^{22} \text{ Hertz}$ when $\lambda_{GW} \sim 10^{-14}\text{ meters}$, i.e. a change of
$\sim 10^{13}$ orders of magnitude in about $10^{-25}$ seconds, or less. The challenge, next will be to come up with an
input model which will justify a generation of data points, i.e. a new data model, since the pre inflationary
models and their other related inferences are all ready being spelled out.[1],[16]

Table 3, how to identify the commensurate metric models which are consistent with Eq.
(13a) above as far as conventional cosmology models

To summarize, what we expect is that appropriate strain sensitivity values plus predictions as to frequencies
may confirm or falsify each of these four inflationary candidates, and perhaps lead to completely new model
insights. Note that in the following table, we assume that $\Omega_{GW}$ are essentially not measurable in the relic GW
sense for the classic GR model.
TABLE 3: Variance of the $\Omega_{GW}$ parameters as given by the above mentioned cosmology models. [18], [19], [20], [21], [22], [23], [24], [25], [38] and referring to Appendix A below

<table>
<thead>
<tr>
<th>Relic pre big bang</th>
<th>QIM</th>
<th>Cosmic String model</th>
<th>Ekpyrotic</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Omega_{GW} \sim 6.9 \times 10^{-6}$</td>
<td>$\Omega_{GW} \sim 10^{-6}$</td>
<td>$\Omega_{GW} \sim 4 \times 10^{-6}$</td>
<td>$\Omega_{GW} \sim 10^{-15}$</td>
</tr>
<tr>
<td>when $f \geq 10^{-1} \text{Hz}$</td>
<td>$1GH &lt; f &lt; 10GH$</td>
<td>$f \propto 10^{-6} \text{Hz}$</td>
<td>$10^7 \text{Hz} &lt; f &lt; 10^8 \text{Hz}$</td>
</tr>
<tr>
<td>$\Omega_{GW} &lt;&lt; 10^{-6}$</td>
<td></td>
<td>$\Omega_{GW} \sim 0$</td>
<td>$\Omega_{GW} \sim 0$</td>
</tr>
<tr>
<td>when $f &lt; 10^{-1} \text{Hz}$</td>
<td></td>
<td>otherwise</td>
<td>otherwise</td>
</tr>
</tbody>
</table>

The best targets of opportunity, for viewing $\Omega_{GW} \sim 10^{-6}$ are in the $1\text{Hz} < f < 10 \text{GHz}$ range, with another possible target of opportunity in the $f \propto 10^{-6} \text{Hz}$ range. Other than that, it may be next to impossible to obtain relic GW signatures. Now that we have said it, it is time to consider the next issue. See Appendix D for a description of these cosmology models.

2.4 A new idea extending Penrose’s suggestion of cyclic universes, black hole evaporation, and the embedding structure our universe is contained within

Beckwith strongly suspects that there are no fewer than $N$ universes undergoing Penrose ‘infinite expansion’ [16],[17] and all these are contained in a mega universe structure. Furthermore, each of the $N$ universes has black hole evaporation, with the Hawking radiation from decaying black holes. If each of the $N$ universes is defined by a partition function, we can call $\{\Xi_i\}_{i=1}^{\infty} \equiv \Xi$, then there exist an information minimum ensemble of mixed minimum information roughly correlated as about $10^7 - 10^8$ bits of information per partition function in the set $\{\Xi_i\}_{i=1}^{\infty} \equiv \Xi$, so minimum information is conserved between a set of partition functions per each universe [26],[27] \[
\left\{\Xi_i\right\}_{i=1}^{\infty} \equiv \left\{\Xi_i\right\}_{i=1}^{\infty} \right.$$ \text{after} \\
\left\{\Xi_i\right\}_{i=1}^{\infty} \equiv \left\{\Xi_i\right\}_{i=1}^{\infty} \right.$$ \text{before} \\
\left\{\Xi_i\right\}_{i=1}^{\infty} \equiv \left\{\Xi_i\right\}_{i=1}^{\infty} \right.$ (14)

However, that there is non uniqueness of information put into each partition function $\{\Xi_i\}_{i=1}^{\infty} \equiv \Xi$. Furthermore Hawking radiation from the black holes is collated via a strange attractor collection in the mega universe structure to form a new big bang for each of the $N$ universes as represented by $\{\Xi_i\}_{i=1}^{\infty} \equiv \Xi$. Verification of this mega structure compression and expansion of information with a non unique venue of information placed in each of the $N$ universes favors Ergodic mixing treatments of initial values for each of $N$ universes expanding from a singularity beginning. The $n_f$ value, will be used to algorithm of [1],[15], [28] $S_{\text{energy}} \sim n_f \cdot$. How to tie in this energy expression, as in Eq. (15) will be to look at the formation of a non trivial gravitational measure which we can state as a new big bang for each of the $N$ universes as by [9], and $n(E_i)$- the density of states at a given energy $E_i$ for a partition function. [1], [29]
\[
\{\Xi_j\}_i^{i=N} \propto \left\{ \int \frac{dE_i}{0} n(E_i) \cdot e^{-E_i} \right\}_j^{i=N}.
\] (15)

Each of the terms \( E_i \) would be identified with Eq.(12a) above, with the following iteration for N universes [1],

\[
\frac{1}{N} \cdot \sum_{j=1}^{N} \Xi \bigg|_{j\text{-before-nucleation-regime}} \xrightarrow{\text{vacuum-nucleation-transfer}} \Xi \bigg|_{j\text{-fixed-after-nucleation-regime}}
\] (16)

For N number of universes, with each \( \Xi |_{j\text{-before-nucleation-regime}} \) for \( j = 1 \) to N being the partition function of each universe just before the blend into the RHS of Eq. (16) above for our present universe. Also, each of the independent universes given by \( \Xi |_{j\text{-before-nucleation-regime}} \) would be constructed by the absorption of one million black holes sucking in energy. I.e. in the end [1], [26], [27]

\[
\Xi |_{j\text{-before-nucleation-regime}} \approx \sum_{k=1}^{\text{Max}} \Xi \bigg|_{\text{black-holes-}j\text{-universe}}
\] (17)

3.0: Providing a curve for the fifth cosmology model, as a modification / extension of the Penrose model talked about above

We can look now at the following approximate model for the discontinuity put in, due to the heating up implied in Table 1 above, namely This is adapted from a lecture given at the ICGC-07 conference by Beckwith [30] We will start off with

\[
\frac{\Lambda_{\text{Max}} V_4}{8 \cdot \pi \cdot G} \sim T_0^{00} V_4 = \rho \cdot V_4 = E_{\text{total}}
\] (18)

The approximation we are making, in this treatment initially is that \( E_{\text{total}} \propto V(\phi) \) where we are looking at a potential energy term. [1] What we are paying attention to, here is that for an exponential potential (effective potential energy) [1], [31]

\[
V(\phi) = g \cdot \phi^\alpha
\] (19)

De facto, what we come up with pre, and post Planckian space time regimes, when looking at consistency of the emergent structure is the following. Namely, [1], [31]

\[
V(\phi) \propto \phi^{\left|\epsilon\right|} \quad \text{for} \quad t < t_{\text{Planck}}
\] (19a)

Also, we would have

\[
V(\phi) \propto 1/\phi^{\left|\epsilon\right|} \quad \text{for} \quad t >> t_{\text{Planck}}
\] (19b)

The switch between Eq. (19a) and Eq. (19b) is not justified analytically. I.e. it breaks down. Beckwith (2011) designated this as the boundary of a causal discontinuity. Now according to Weinberg [31], if

\[
\epsilon = \frac{\lambda^2}{16\pi G}, H = 1/\epsilon \quad t
\]

so that one has a scale factor behaving as [1],[31]
\[ a(t) \propto t^{1/e} \]  \hspace{1cm} (19c)

Then, if \([1],[31]\)

\[ |V(\phi)| \ll (4\pi G)^{-2} \] \hspace{1cm} (20)

There are no quantum gravity effects worth speaking of. I.e., if one uses an exponential potential a scalar field could take the value of, when there is a drop in a field from \(\phi_1\) to \(\phi_2\) for flat space geometry and times \(t_1\) to \(t_2\) \([1],[31]\)

\[ \phi(t) = \frac{1}{\lambda} \ln \left[ \frac{8\pi G g e^2 t^2}{3} \right] \] \hspace{1cm} (21)

Then the scale factors, from Planckian time scale as \([1],[31]\)

\[ \frac{a(t_2)}{a(t_1)} = \left( \frac{t_2}{t_1} \right)^{1/e} = \exp \left[ \frac{(\phi_2 - \phi_1)\lambda}{2 e} \right] \] \hspace{1cm} (22)

The more \(\frac{a(t_2)}{a(t_1)} \gg 1\), then the less likely there is a tie in with quantum gravity. Note those that the way this potential is defined is for a flat, Roberson-Walker geometry, and that if and when \(t_1 < t_{\text{planck}}\) then what is done in Eq. (22) no longer applies, and that one is no longer having any connection with even an octonionic Gravity regime.

### 3.1 We are then going to get the following expression for the energy / frequency spread in the Penrose alternation of the big ‘crunch’ model

Start with working with the expression given beforehand as \([1],[32]\)

\[ E_{\text{thermal}} \approx \frac{1}{2} k_B T_{\text{temperature}} \propto \tilde{\beta} \]

This is for having for a time \(\tilde{T} \sim 0^+\) to \(10^{-44}\) seconds, \(\Omega G_{\text{GW}} \sim 10^6\), and a variance of frequency of

\[ \Omega_0 e^{1 \text{GHz}, 10 \text{GHz}} \] \hspace{1cm} (23)

This is due to \(T_{\text{temperature}} \sim 10^{32}\) Kelvin at the point of generation of the discontinuity leading to a discontinuity for a signal generation as given by \(\delta_0\) at about \(\tilde{T} \sim 10^{-44}\) seconds. This is for inputs into the relatively constant

\[ \left[ \Omega_0 \tilde{T} \right] \sim \tilde{\beta} \] \hspace{1cm} (24)
The assumption is that the discontinuity, as given by $\delta_0$ will be as of about temperature
$T_{\text{temperature}} \sim 10^{32}$ Kelvin, for $\Omega_{GW} \sim 10^6$, meaning that the peak curve of frequency will be between 1 to 10 GHz for $\Omega_{GW} \sim 10^6$, with a rapidly falling value of $\Omega_{GW}$ for frequencies $< 1$ GHz.

4.1: 1st part of conclusion. Can we justify / Isolate out an appropriate $T^{(i)}_{uv}$ if one has non zero graviton rest mass?

It is difficult. It depends upon understanding what is meant by emergent structure, as a way to generalize what is known in mathematics as the concept of “self-organized criticality” put forward by the Santa Fe school. [33] as well as the concept of negator algebra referring to topos-theoretic results. In (2001) Zimmermann and Voelcker [34] refer to a pure abstract mathematical self organized criticality structure... We assert that the mathematical self organized criticality structure is akin to a definition as to how Dp branes arise at the start of inflation. What is the emergent structure permitting $(i)_{0x}$ to hold? What is the self organized criticality structure leading to forming an appropriate $(i)_{0x}$ if one has non zero graviton rest mass? Answering such questions will permit us to understand how to link finding $(i)_{0x}$ in a GW detector, its full analytical linkage to $\tilde{\beta}$ in Eq (13a), and Eq. (13b). The following construction is used to elucidate how a EM Gaussian sense beam can perhaps be used to eventually help in isolating $(i)_{0x}$ in a GW detector. This construction below is to be used to investigate ‘massive gravitons’/ and also the initial structure of self organized criticality, in the aftermath of graviton/ gravitational wave generation. Further details can be accessed in Appendix F as to a GW detection system which may be able to help us isolate $(i)_{0x}$.

4.2: 2nd part of conclusion: In terms of the Planckian evolution, as well as the feed into it from different universes

We wish to summarize what we have presented in an orderly fashion. This mapping requires a deterministic quantum limit as similar to what tHooft included in his embedding of Quantum physics in a larger, non linear theory [35]. This is approximated by current Pilot model build up of an embedding of QM within a more elaborate super structure.In particular, in order to verify the above one may have to make analogies with detection via the proposed and planned detection systems (SEMCs and SEMCS II), for frequency ranges centering on $10^9$ to $10^{10}$ Hz uniquely corresponds to maxima for pre-big-bang and quintessential inflation models. This for $\Omega_{GW} \sim 10^7$ as the ratio of the density of GW radiation over $\rho_c =$ critical density. Theoretically, what Eq. (16) and Eq. (17) are to develop considerations based upon different initial conditions in phase space, requiring experimental input. If what the author suspects, i.e. ergodic characteristics, along the lines of [36]

$$p_0(x) = \left\{ \begin{array}{ll} \frac{1}{\delta \cdot x_0} & \text{when } x \in [x_0, x_0 + \delta \cdot x] \\ 0 & \text{otherwise} \end{array} \right.$$  

(25)

Appendix A, Establishing GW astronomy in terms of a choice between models

We view in geometry that there is a change of $\sim 10^{13}$ orders of magnitude in about $10^{25}$ seconds, or less in terms of one of the variants of inflation. As has been stated else where [18],[19], [20], [21], [22], [23], [24], [25], [38] particularly in a publication under development, there are several models which may be affecting this change of magnitude. The following is a summary of what may be involved: We seek to keep the direction of time to be one directional. I.e. [37]
A1) The relic GWs in the pre-big-bang model.

Here, the relic GWs have a broad peak bandwidth from 1 Hz to 10 GHz. We can refer to other such publications for equivalent information as in the pre big model [19], [20]. In this spectral region the upper limit of energy density of relic GWs is almost a constant $\Omega_{gw} \sim 6.9 \times 10^{-6}$, but it will rapidly decline in the region from 1 Hz to $10^{-3}$ Hz. Thus direct detection of the relic GWs should be focused in intermediate and high-frequency bands. Amplitude upper limits of relic GWs range from $h \sim 10^{-23}$ at frequencies around 100 Hz to $h \sim 10^{-30}$ at frequencies around 2.9 GHz. This means that frequencies around 100 Hz and frequencies around 2.9 GHz would be two key detection windows.

A2) The relic GWs in the quintessential inflationary model (QIM).

The peak and maximal signal of relic GWs in the QIM are localized in the GHz band, and the strength of relic GWs in both the QIM and the pre-big-bang model in the GHz band have almost the same magnitude (e.g., $h \sim 10^{-30}$ at 2.9 GHz). But the peak bandwidth of the QIM (from 1 GHz to 10 GHz) [21] is less than that of the pre-big-bang model (from 1 Hz to 10 GHz) [22] [23].

A3) The relic GWs in the cosmic string model.

Unlike relic GWs in the pre-big-bang model and in the QIM, the peak energy density $\Omega_{gw}$ of relic GWs in the cosmic string model is in the low-frequency region of $\sim 10^{-7}$ Hz to $10^{-1}$ Hz, and the upper limit of $\Omega_{gw}$ may be $\sim 4 \times 10^{-6}$ at frequencies around $10^{-6}$ Hz. When $\nu < 10^{-7}$ Hz, the energy density decays quickly. Therefore, LISA and ASTROD will have sufficient sensitivity to detect low-frequency relic GWs in the region of $\sim 10^{-7}$ Hz $< \nu < 10^{-3}$ Hz predicted by the model [22], [23]. Moreover, the energy density of relic GWs is an almost constant $\Omega_{gw} \sim 10^{-8}$ from $10^{-1}$ Hz to $10^{10}$ Hz, and the relic GWs at frequencies around 100 Hz should be detectable by advanced LIGO, but the amplitude upper limit of relic GWs in the GHz band may be only $h \sim 10^{-31}$ to $10^{-32}$, which cannot be directly detected by current technologies.

A4) The relic GWs in the ekpyrotic scenario

Relic GWs in the ekpyrotic scenario [38] and in the pre-big-bang [22], [23] model have some common and similar features. The initial state of universe described by both is a large, cold, nearly empty universe, and there is no beginning of time in both, and they are faced with the difficult problem of making the transition between the pre- and post-big bang phase. However, the difference of physical behavior of relic GWs in both is obvious. First, the peak energy density of relic GWs in the ekpyrotic scenario is $\Omega_{gw} \sim 10^{-15}$, and localized in frequencies around $10^{7}$ Hz to $10^{8}$ Hz. Therefore the peak of $\Omega_{gw}$ is less than corresponding value in the latter.

A5) The relic GWs in the ordinary inflationary model

Also, for ordinary inflation [20] the energy density of relic GWs holds constant ($\Omega_{gw} \sim 10^{-14}$) in a broad bandwidth from $10^{-16}$ Hz to $10^{10}$ Hz, but the upper limit of the energy density is less than that in the pre-big-bang model from $10^{-3}$ Hz to $10^{10}$ Hz, in the cosmic string model from $10^{-7}$ Hz to $10^{10}$ Hz, and in the QIM from $10^{-1}$ Hz to $10^{10}$ Hz. For example, this model predicts $h_{\text{max}} \sim 10^{-27}$ at 100 Hz, $h_{\text{max}} \sim 10^{-33}$ at 100 MHz and $h_{\text{max}} \sim 10^{-35}$ at 2.9 GHz.
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