

# **Detailing Coherent , Minimum Uncertainty States of Gravitons, as Semi Classical Components of Gravity Waves, and how squeezed states affect upper limits to graviton mass**

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## **Abstract**

This document will outline what the authors suppose is relevant to squeezed states of initial space time and how that affects both the composition of relic GW, and also gravitons. A side issue to consider is if gravitons can be configured as semi classical “particles”, which is akin to the Pilot model of Quantum Mechanics as embedded in a larger non linear ‘deterministic’ background. In addition, as the main author has discussed with Stuart Allen in long evening talks, the relative classical embedding of QM will be linkable to upper bounds to the graviton mass, for reasons brought up in the manuscript.

## **Introduction**

. Gravitons may be decomposed via an instanton – anti instanton structure.i.e. that the structure of SO(4) gauge theory is initially broken due to the introduction of vacuum energy, and that after a second-order phase transition, the instanton-anti-instanton structure of relic gravitons is reconstituted. This will be crucial to link graviton production with entropy, provided we have sufficiently HFGW at the origin of the big bang. The linkage to SO(4) gauge theory and gravitons was brought up by [1] Kuchiev, M. Yu, and we think it leads to a kink-anti kink pair tie in for attendant gravitons . Note that [Kuchiev](#) [1] writes that “Conventional non-Abelian SO(4) gauge theory is able to describe gravity provided the gauge field possesses a specific polarized vacuum state. In this vacuum the instantons and anti-instantons have a preferred direction of orientation.”, and furthermore “Gravitons appear as the mode describing propagation of the gauge field which strongly interacts with the oriented instantons” Furthermore, as given by [Ivan Andrić](#), [Larisa Jonke](#) and [Danijel Jurman](#),[2] in a Classical and quantum gravity article, 2006, what is called an  $n$ -soliton solution is shown to have an equivalence with the following, namely “semiclassical solutions corresponding to giant gravitons described by matrix models obtained in the framework of AdS/CFT correspondence” . Solitons have a kink- anti kink structure, even in low dimensions, as was worked out by Beckwith (2006) in a condensed matter application. The string theory methodology is merely extending much the same thinking up to higher than four dimensional situations..

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1. Modeling of entropy, generally, as kink-anti-kinks pairs with  $\tilde{N}$  the number of the kink-anti-kink pairs. This number,  $\tilde{N}$  is, initially in tandem with entropy production, as will be explained later,
2. The tie in with entropy and gravitons is this: The two structures are related to each other in terms of kinks and anti-kinks. It is asserted that how they form and break up is due to the same phenomenon: a large insertion of vacuum energy leads to an initial breakup of both entropy levels and gravitons. When a second-order phase transition occurs, there is a burst of relic gravitons. Similarly, there is an initial breakup of net entropy levels, and after a second-order phase transition, another rapid increase in entropy.

The supposition we are making here is that the value of  $N$  so obtained is actually proportional to a numerical graviton density we will refer to as  $\langle n \rangle$ , provided that there is a bias toward HFGW, which would mandate a very small value for  $V \approx R_H^3 \approx \lambda^3$ . Furthermore, structure formation arguments, as given by Perkins [3] give ample evidence that if we use an energy scale,  $m$ , over a Planck mass value  $M_{Planck}$ , as well as contributions from field amplitude  $\phi$ , and using the contribution of scale factor behavior  $\frac{\dot{a}}{a} \equiv H \approx -m \cdot \frac{\phi}{3 \cdot \dot{\phi}}$ , where we assume  $\ddot{\phi} \cong 0$  due to inflation

$$\frac{\Delta \rho}{\rho} \sim H \Delta t \sim \frac{H^2}{\dot{\phi}} \sim \left( \frac{m}{M_{Planck}} \right) \times \left( \frac{\phi}{M_{Planck}} \right) \sim 10^{-5} \quad (1)$$

At the very onset of inflation,  $\phi \ll M_{Planck}$ , and if  $m$  ( assuming  $\hbar = c = 1$  ) is due to inputs from a prior universe, we have a wide range of parameter space as to ascertain where  $\Delta S \approx \Delta N_{gravitons} \neq 10^{88}$  comes from and plays a role as to the development of entropy in cosmological evolution. In the next Chapter, we will discuss if or not it is feasible / reasonable to have data compression of prior universe ‘information’. It suffices to say that if  $S_{initial} \sim 10^5$  is transferred from a prior universe to our own universe at the onset of inflation,, at times less than Planck time  $t_p \sim 10^{-44}$  seconds, that enough information **MAY** exit for the preservation of the prior universe’s cosmological constants, i.e.  $\hbar, G, \alpha$  (fine structure constant) and the like. Confirmation of this hypothesis depends upon models of how much ‘information’  $\hbar, G, \alpha$  actually require to be set in place, at the onset of our universe’s inflation, a topic which we currently have no experimental way of testing at this current time.

### **Is each ‘particle count unit’ as brought up by Ng, is equivalent to a brane-anti brane ‘unit in brane treatments of entropy? How does this tie in with string/ brane theory treatments of entropy?**

It is useful to state this convention for analyzing the resulting entropy calculations, because it is a way to explain how and why the number of instanton – anti instanton pairs, and their formulation and break up can be linked to the growth of entropy. If, as an example, there is a linkage between quantum energy level components of the quantum gas as brought up by Glinka [4] (2007) and the number of instanton- anti instanton pairs, then it is possible to ascertain a linkage between a Wheeler De Witt worm hole introduction of vacuum energy [5] from a prior universe to our present universe, and the resulting brane- anti brane (instanton- anti instanton) units of entropy. Such an approach may permit asking how information is transferred from a prior to the present universe. What would be ideal would be to make an equivalence between a quantum number,  $n$ , say of a quantum graviton gas, as entering a worm hole, i.e. going back to the Energy ( quantum gas )  $\approx n \cdot \hbar \omega$ , and the number  $\langle n \rangle$  of pairs of brane- anti brane pairs showing up in an entropy count, and the growth of entropy. We are fortunate that Dr. Jack Ng’s research into entropy [5] not only used the Shannon entropy model, but also as part of his quantum infinite statistics lead to a quantum counting algorithm with entropy proportional to ‘emergent field’ particles. If as an example a quantum graviton gas exists, as suggested by Glinka[4] (2007), if each quantum gas ‘particle’ is equivalent to a graviton, and that graviton is an ‘emergent’ from quantum vacuum entity, then we fortuitously connect our research with gravitons with Shannon entropy, as given by  $S \sim \ln[\text{partition} - \text{function}]$ . This is a counter part as to what Asakawa et al,[6] (2001, 2006) suggested for quark gluon gases, and the 2<sup>nd</sup> order phase transition written up by [Torrieri](#) et al [7] (2008) brought up at the nuclear physics Erice (2008) school, in discussions with the author.

Furthermore, finding out if or not it is either a drop in viscosity [6],[7] when  $\left| \frac{\eta}{s} \approx \varepsilon^+ \right| \ll \frac{1}{4\pi}$ , or a major increase in entropy density may tell us how much information is, indeed, transferred from a prior universe to our present. If it is  $s \rightarrow \infty$ , for all effective purposes, at the moment after the pre big bang configuration, likely then there will be a high degree of ‘information’ from a prior universe exchanged to our present universe. If on the other hand,  $\eta \rightarrow 0^+$  due to restriction of ‘information from four dimensional ‘geometry’ to a variable fifth dimension, so as to indicate almost infinite collisions with a closure of a fourth dimensional ‘portal’ for information flow, then it is likely that significant data compression has occurred. While stating this, it is note worthy to state that the Penrose-Hawking singularity theorems do not give precise answers as to information flow from a prior to the present universe. Hawking's singularity theorem is for the whole universe, and works backwards-in-time: it guarantees that the big-bang has infinite density. This theorem is more restricted, it only holds when matter obeys a stronger energy condition, called the *dominant energy condition*, which means that the energy is bigger than the pressure. All ordinary matter, with the exception of a vacuum expectation value of a scalar field, obeys this condition.

This leaves open the question of if or not there is ‘infinite’ density of ordinary matter, or if or not there is a fifth dimensional leakage of ‘information’ from a prior universe to our present. If there is merely infinite ‘density’, and possibly infinite entropy ‘density/ disorder at the origin, then perhaps no information from a prior universe is transferred to our present universe. On the other hand, having  $\eta \rightarrow 0^+$ , or at least be very small may indicate that data compression is a de rigor way of treating how information for cosmological parameters, such as  $\hbar$ , G, and the fine structure constant.  $\alpha$  arose, and may have been recycled from a prior universe. Details about this have to be worked out, and this because that as of present one of the few tools which is left to formulation and proof of the singularity theorems is the [Raychaudhuri equation](#), which describes the divergence  $\theta$  of a [congruence](#) (family) of geodesics, which has a lot of assumptions behind it, as stated by [Naresh Dadhich](#) [8] (2005). As indicated by Hawking's theorem, infinite density is its usual modus operandi, for a singularity, and this assumption may have to be revisited. Natário, J.[9] (2006) has more details on the different type of singularities involved. The supposition is that the value of N is proportional to a numerical DM density referred to as  $\langle n \rangle_{\text{Dark-matter}}$ . HFGW would play a role if

$V \approx R_H^3 \approx \lambda^3$  has each  $\lambda$  of the order of being within an order of magnitude of the Planck length value, as implied by Beckwith (2009)[10]. examined, and linked to modeling gravity as an effective theory, as well as giving credence to how to avoid  $dS/dt = \infty$  at  $S=0$ . If so, then one can look at the research results of Mathur [11] (2007). This is part of what has been developed in the case of massless radiation, where for D space-time dimensions, and E, the general energy is

$$S \sim E^{(D-1/D)} \quad (2)$$

This suggests that entropy scaling is proportional to a power of the vacuum energy, i.e., entropy  $\sim$  vacuum energy, if  $E \sim E_{total}$  is interpreted as a total net energy proportional to vacuum energy, as given below. Conventional brane theory actually enables this instanton structure analysis, as can be seen in the following. This is adapted from a lecture given at the ICGC-07 conference by Beckwith [12]

$$\frac{\Lambda_{Max} V_4}{8 \cdot \pi \cdot G} \sim T^{00} V_4 \equiv \rho \cdot V_4 = E_{total} \quad (3)$$

The approximation we are making, in this treatment initially is that  $E_{total} \propto V(\phi)$  where we are looking at a potential energy term.[13]

What we are paying attention to, here is the datum that for an exponential potential ( effective potential energy)

$$V(\phi) = g \cdot \phi^\alpha \quad (4)$$

De facto, what we come up with pre, and post Planckian space time regimes, when looking at consistency of the emergent structure is the following. Namely,

$$V(\phi) \propto \phi^{|\alpha|} \quad \text{for } t < t_{Planck} \quad (4a)$$

Also, we would have 
$$V(\phi) \propto 1/\phi^{|\alpha|} \quad \text{for } t \gg t_{Planck} \quad (4b)$$

The switch between Eq. (4a) and Eq. (4b) is not justified analytically. I.e. it breaks down. Beckwith et al (2011) designated this as the boundary of a causal discontinuity.

Now according to Weinberg [13], if  $\epsilon = \frac{\lambda^2}{16\pi G}$ ,  $H = 1/\epsilon t$  so that one has a scale factor behaving as

$$a(t) \propto t^{1/\epsilon} \quad (5)$$

Then, if

$$|V(\phi)| \ll (4\pi G)^{-2} \quad (6)$$

there are no quantum gravity effects worth speaking of. I.e., if one uses an exponential potential a scalar field could take the value of  $\phi$ , when there is a drop in a field from  $\phi_1$  to  $\phi_2$  for flat space geometry and times  $t_1$  to  $t_2$  [13]

$$\phi(t) = \frac{1}{\lambda} \ln \left[ \frac{8\pi G g \epsilon^2 t^2}{3} \right] \quad (7)$$

Then the scale factors, from Planckian time scale as [13]

$$\frac{a(t_2)}{a(t_1)} = \left( \frac{t_2}{t_1} \right)^{1/\epsilon} = \exp \left[ \frac{(\phi_2 - \phi_1) \lambda}{2 \epsilon} \right] \quad (8)$$

The more  $\frac{a(t_2)}{a(t_1)} \gg 1$ , then the less likely there is a tie in with quantum gravity. Note those that the way

this potential is defined is for a flat, Robertson-Walker geometry, and that if and when  $t_1 < t_{Planck}$  then what is done in Eq. (8) no longer applies, and that one is no longer having any connection with even an octonionic Gravity regime. If so, as indicated by Beckwith, et al (2011)[15] one may have to tie in graviton production due to photonic (“light”) inputs from a prior universe, i.e. a causal discontinuity, with consequences which will show in both GW and graviton production.

### **Linking Instanton-anti Instanton Construction in both Entropy generation and Gravitons**

Here is a quick review of how to have an instanton – anti instanton construction for entropy, and then proposing a similar construction for gravitons. Afterwards, we will analyze squeezed states. It is the authors conviction that semi classical treatment of Gravitons, if gravitons are in an instanton-anti instanton pairing is equivalent to the break down of the “thin wall approximation” used in density wave physics. In what

may be by some peoples visualization, an outrageous simplification, the issue of squeezing of graviton states is similar to what happens with the break down of the purely quantum mechanical analogy done for initially non squeezed states, which when squeezed have their own non quantum mechanical flavor.

We will start first looking at entropy, as an instanton – anti instanton construction and go from there:

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Traditionally, minimum length for space-time benchmarking has been via the quantum gravity modification of a minimum Planck length for a grid of space-time of Planck length, whereas this grid is changed to something bigger  $l_p \sim 10^{-33} \text{ cm} \xrightarrow{\text{Quantum-Gravity-threshold}} \tilde{N}^\alpha \cdot l_p$ . So far, we this only

covers a typical string gas model for entropy.  $\tilde{N}$  is assigned as the as numerical density of branes and anti-branes. A brane-antibrane pair corresponds to solitons and anti-solitons in density wave physics. The branes are equivalent to instanton kinks in density wave physics, whereas the antibranes are an anti-instanton structure. First, a similar pairing in both black hole models and models of the early universe is examined, and a counting regime for the number of instanton and anti-instanton structures in both black holes and in early universe models is employed as a way to get a net entropy-information count value. One can observe this in the work of [Gilad Lifschytz](#) [14] in 2004. Lifschytz (2004) codified thermalization equations of the black hole, which were recovered from the model of branes and antibranes and a contribution to total vacuum energy. In lieu of assuming an antibrane is merely the charge conjugate of say a Dp brane. Here,  $M_{p,j,0}$  is the number of branes in an early universe configuration, while  $M_{\bar{p},j,0}$  is anti-

brane number. I.e., there is a kink in the given  $brane \sim M_{p,j,0} \leftrightarrow CDW e^-$  electron charge and for

the corresponding anti-kink  $anti-brane \sim M_{\bar{p},j,0} \leftrightarrow CDW e^+$  positron charge. Here, in the bottom

expression,  $\tilde{N}$  is the number of kink-anti-kink charge pairs, which is analogous to the simpler CDW structure.

$$S_{Total} \sim \tilde{a} \cdot \left[ \frac{E_{Total}}{2^n} \right]^\lambda \cdot \prod_{j=1}^{\tilde{N}} \left( \sqrt{M_{p,j,0}} + \sqrt{M_{\bar{p},j,0}} \right) \quad (9)$$

This expression for entropy (based on the number of brane-anti-brane pairs) has a net energy value of  $E_{Total}$  as expressed in Eq (9) above, where  $E_{Total}$  is proportional to the cosmological vacuum energy parameter; in string theory,  $E_{Total}$  is also defined via

$$E_{Total} = 4\lambda \cdot \sqrt{M_{p,j,0} \cdot M_{\bar{p},j,0}} \quad (10)$$

Equation 10 can be changed and rescaled to treating the mass and the energy of the brane contribution along the lines of Mathur's CQG article [15] (2007) where he has a string winding interpretation of energy: putting as much energy  $E$  into string windings as possible via  $[n_1 + \bar{n}_1]LT = [2n_1]LT = E/2$ , where there are  $n_1$  wrappings of a string about a cycle of the torus, and  $\bar{n}_1$  being "wrappings the other way", with the torus having a cycle of length  $L$ , which leads to an entropy defined in terms of an energy value of

mass of  $m_i = T_p \prod L_j$  ( $T_p$  is the tension of the  $i$ th brane, and  $L_j$  are spatial dimensions of a complex torus structure). The toroidal structure is to first approximation equivalent dimensionally to the minimum effective length of  $\tilde{N}^\alpha \cdot l_p \sim \tilde{N}^\alpha$  times Planck length  $\propto 10^{-35}$  centimeters

$$E_{Total} = 2 \sum_i m_i n_i \quad (11)$$

The windings of a string are given by figure 6.1 of Becker et al [16], as the number of times the strings wrap about a circle midway in the length of a cylinder. The structure the string wraps about is a compact

object construct Dp branes and anti-branes. Compactness is used to roughly represent early universe conditions, and the brane-anti brane pairs are equivalent to a bit of “information.” This leads to entropy expressed as a strict numerical count of different pairs of Dp brane-Dp anti-branes, which form a higher-dimensional equivalent to graviton production. The tie in between Eqn. (12) below and Jack Ng’s treatment of the growth of entropy is as follows: First, look at the expression below, which has  $\tilde{N}$  as a stated number of pairs of Dp brane-antibrane pairs: The suffix  $\tilde{N}$  is in a 1-1 relationship with  $\Delta S \approx \Delta N_{gravitons}$

$$S_{Total} = A \cdot \prod_i^{\tilde{N}} \sqrt{n_i} \quad (12)$$

Now, how do we make sense of the following entropy values? Note the following

As an example of present confusion, please consider the following discussion where leading cosmologists, i.e. Sean Carroll [17](2005) asserted that there is a distinct possibility that mega black holes in the center of spiral galaxies have more entropy, in a calculated sense, i.e. up to  $10^{90}$  in non dimensional units. This has to be compared to Carroll’s (2005)[17] stated value of up to  $10^{88}$  in non dimensional units for observable non dimensional entropy units for the observable universe. Assume that there are over one billion spiral galaxies, with massive black holes in their center, each with entropy  $10^{90}$ , and then there is due to spiral galaxy entropy contributions  $10^6 \times 10^{90} = 10^{96}$  entropy units to contend with, vs.  $10^{88}$  entropy units to contend with for the observed universe. I.e. at least a ten to the eight order difference in entropy magnitude to contend with. The author is convinced after trial and error that the standard which should be used is that of talking of information, in the Shannon sense, for entropy, and to find ways to make a relationship between quantum computing operations, and Shannon information. Making the identification of entropy as being written as  $S \sim \ln[\textit{partition} - \textit{function}]$ . This is Shannon information theory with regards to entropy, and the convention will be the core of this text. What is chosen as a partition function will vary with our chosen model of how to input energy into our present universe. This idea as to an input of energy, and picking different models of how to do so leading to partition functions models is what motivated research in entropy generation. From now on, there will be an effort made to identify different procedural representations of the partiton function, and the log of the partion function with both string theory representations, i.e. the particle count algorithm of Y.Jack Ng,[ 5 ] and the Wheeler De Witt version of the log of the partition function as presented by Glinka (2007).[ 4 ] Doing so may enable researchers to eventually determine if or not gravity/ gravitational waves are an emergent field phenomenon.

A further datum to consider is that Eq (8) with its variance of density fluctuations may eventually be linkable to Kolmogrov theory as far as structure formation. If we look at R. M. S. Rosa [18],[19] (2006), and energy cascades of the form of the ‘energy dissipation law’, assuming  $u_0, l_0$  are minimum velocity and length, with velocity less than the speed of light, and the length at least as large, up to  $10^6$  time larger than Planck length  $l_{Planck}$

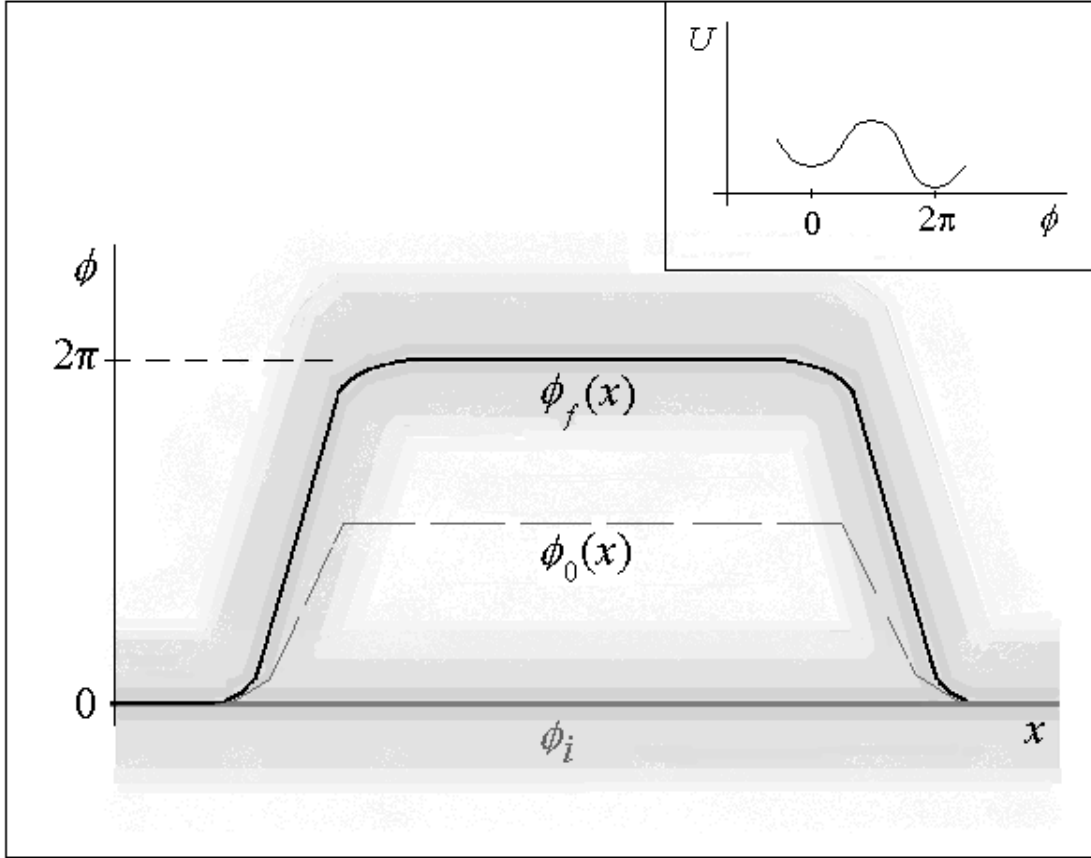
$$\varepsilon \approx \frac{u_0^3}{l_0} \quad (13)$$

Eq. (13) above can be linked to an eddy break down process, which leads to energy dissipated by viscosity. If applied appropriately to structures transmitted through a ‘worm hole’ from a prior to a present universe, it can explain

- 1) How there could be a break up of ‘encapsulating’ structure which may initially suppress additional entropy beyond  $S_{initial} \sim 10^5$ , in the onset of inflation
- 2) Provide a ‘release’ mechanism for  $\Delta S \approx \Delta N_{gravitons} < 10^{54} \ll 10^{88}$ , with  $\Delta S \approx \Delta N_{gravitons} \sim 10^{21}$  perhaps a starting point for increase in entropy in

$\Delta t \approx t_{planck} \sim 5 \times 10^{-44}$  sec , rising to  $\Delta S \approx \Delta N_{gravitons} \leq 10^{54} \ll 10^{88}$  for times up to 1000 seconds after the big bang.

Here is, in a nutshell the template for the Gravitons which will examine, and eventually link to Gravitational waves, and entropy.



**Fig 1:** Here, the left hand side corresponds to a soliton, the right hand side is an anti soliton[20]

### Different scenarios for Entropy growth depending upon If or not we have Low to high Frequency GW from the big bang.

As mentioned above, there is a question of what frequency range of GW is dominant during the onset of the big bang. To begin with let us look at frequency range of GW from relic conditions. As given by for a peak amplitude as stated by Tina Kahniashvili (2007).[21] Now for the amplitude of a GW, as detected today

$$h_c(f) = 1.62 \times 10^{-18} \left( \frac{T_*}{100 \text{ GeV}} \right) \left( \frac{g_*}{100} \right)^{-5/6} \left( \frac{\gamma}{0.01} \right)^{3/2} \left( \frac{\zeta}{0.01} \right)^{1/2} [k_0^3 f H_{ijij}(2\pi f, 2\pi f)]^{1/2}. \quad (14)$$

The equation , as given by Kahniashvili [21] (2007) with a frequency  $f$  given below in Eq. (15) which is for today's detected GW frequency a detector would observe, whereas  $\omega_*$  is the frequency of a process synthesizing GW during a 2<sup>nd</sup> order phase transition in the early universe. Also,  $T_*$  is a mean temperature during that 2<sup>nd</sup> order phase transition. If as an example  $T_*$  is many times larger than 100 GeV, which is the case if GW nucleation occurred at the ORIGIN of the big bang, i.e. at temperatures  $\sim 10^{32}$  Kelvin, then it is likely that  $f$  in Eq. 10 below is capable of approaching values of the order of what was predicted by Grishkuk [22] (2007), i.e. approaching 10 Giga Hertz. Eq (8) and Eq(9) **above**, would have either a small, or a huge  $T_*$ , which would play a role as to how large the amplitude of a GW would be, detected today, as opposed to what it would be at the origin, say, of the big bang. . The larger  $f$  is, the more likely the amplitude is, of Eqn (14) would be very large. In both Eq (14) above, and Eq. (15) below,  $g_*$  is a degree of freedom for spatial conditions factor, which has, according to Kolb and Turner [23](1991) high values of the order of 100 right after the big bang, to values closer to 2 and/or 3 in the modern era. I.e. the degrees of freedom radically dropped in the evolution of space time.

$$f = 1.55 \times 10^{-3} \text{ Hz} \left( \frac{\omega_*}{k_0} \right) \left( \frac{g_*}{100} \right)^{1/6} \left( \frac{\gamma}{0.01} \right)^{-1} \left( \frac{T_*}{100 \text{ GeV}} \right), \quad (15)$$

Here, in this choice of magnitude  $h$  of a GW today, and frequency  $f$  detected today, as presumed by using a factor given by Kahniashvili [21] (2007) as

$$H_{ijkl}(\mathbf{x}', \mathbf{k}, \omega) = \frac{1}{(2\pi)^4} \int d^3\xi d\tau e^{i(\omega\tau - \mathbf{k}\xi)} R_{ijkl}(\mathbf{x}', \xi, \tau). \quad (16)$$

Why? The factor  $H_{ijkl}$  is due to complicated physics which gives a tensor/scalar ratio

As well as

$$R_{ijkl}(\mathbf{x}', \xi, \tau) = \frac{1}{w^2} \langle S_{ij}(\mathbf{x}', t) S_{kl}(\mathbf{x}'', t + \tau) \rangle, \quad (17)$$

Why? Eqn (17) is a two correlation point function, much in the spirit of calculations of two point correlation functions, i.e. greens functions of Quantum field theory. See [24] Peskin's (1995) QFT reference as to how such functional calculations are to show the degree of interaction between  $S_{i,j}(\mathbf{x}', t)$  &  $S_{k,l}(\mathbf{x}'', t + \tau)$ , with each individual  $S_{i,j}$  defined as part of a GR 'stress tensor' contribution of

$$S_{ij}(\mathbf{x}, t) = T_{ij}(\mathbf{x}, t) - \frac{1}{3} \delta_{ij} T_k^k(\mathbf{x}, t), \quad (18)$$

This is where, commonly, we have a way to interpret  $h_{i,j}$  in terms of  $S_{i,j}$  via

$$h_{ij}(\mathbf{x}, t) = 4G \int d^3\mathbf{x}' \frac{S_{ij}(\mathbf{x}', t - |\mathbf{x} - \mathbf{x}'|)}{|\mathbf{x} - \mathbf{x}'|}. \quad (19)$$



As well as a wave equation we can write as

$$\nabla^2 h_{ij}(\mathbf{x}, t) - \frac{\partial^2}{\partial t^2} h_{ij}(\mathbf{x}, t) = -16\pi G S_{ij}(\mathbf{x}, t). \quad (1) \quad (20)$$

What is above, is a way for making sense of GW ‘density’ as given by the formula

$$\rho_{GW}(\omega) \equiv \frac{d\rho_{GW}}{d \ln \omega} = 16\pi^3 \omega^3 G_{\text{w}}^2 \tau_T H_{ijij}(\omega, \omega). \quad (21)$$

Here, the temperature  $T_*$  for the onset of a phase transition, i.e. usually interpreted as a 2<sup>nd</sup> order phase transition plays a major role as to if or not the frequency,  $f$ , for today is very low, or higher, and if or not energy density is high, or low, as well as the attendant amplitude of a GW, as given by Eq. (19) above is important. Furthermore appropriate calculations of Eqn. (21) very much depend upon the correlation function as given by Eq (17) is correctly done, allowing for a minimization of sources of noise, of the sort alluded to by [25] Michelle Maggiore (2008). Possibly though, cosmological evolution is so subtle that no simple use of correlation functions will be sufficient to screen noise by typical field theory derived methods. If temperature  $T_*$  for the onset of a phase transition, is very high, it is almost certain that we are looking at HFGW, and relic gravitons which are severely energized, i.e.  $\omega^*$  would be enormous. If so, then for high  $T_*$  and enormous  $\omega^*$ , at the onset of inflation, we are looking at HFGW, and that [5]

$$\Delta S \approx \Delta N_{\text{gravitons}} \quad (22)$$

If the frequency is much lower, we will see, if the particle-wave duality has large  $\lambda$ , for DM candidates

$$\Delta S \approx \Delta N_{\text{DM-Candidates}} \quad (23)$$

This graviton counting as given in Eq. (22) will next be connected to information counting which will be a necessary and sufficient condition for information exchanged from a prior to the present universe.

### Minimum amount of information needed to initiate placing values of fundamental cosmological parameters

A.K. Avessian’s [26] article (2009) about alleged time variation of Planck’s constant from the early universe depends heavily upon initial starting points for  $\hbar(t)$ , as given below, where we pick our own values for the time parameters, for reasons we will justify in this manuscript:

$$\hbar(t) \equiv \hbar_{\text{initial}} [t_{\text{initial}} \leq t_{\text{Planck}}] \cdot \exp[-H_{\text{macro}} \cdot (\Delta t \sim t_{\text{Planck}})] \quad (24)$$

The idea is that we are assuming a granular, discrete nature of space time. Furthermore, after a time we will state as  $t \sim t_{\text{Planck}}$  there is a transition to a present value of space time, which is then probably going to be held constant.

It is easy to, in this situation, to get an inter relationship of what  $\hbar(t)$  is with respect to the other physical parameters, i.e. having the values of  $\alpha$  written as  $\alpha(t) = e^2 / \hbar(t) \cdot c$ , as well as note how little the fine structure constant actually varies. Note that if we assume an unchanging Planck’s mass  $m_{\text{Planck}} = \sqrt{\hbar(t)c/G(t)} \sim 1.2 \times 10^{19} \text{ GeV}$ , this means that  $G$  has a time variance, too.

This leads to us asking what can be done to get a starting value of  $\hbar_{initial} [t_{initial} \leq t_{Planck}]$  recycled from a prior universe, to our present universe value. What is the initial value, and how does one insure its existence?

We obtain a minimum value as far as ‘information’ via appealing to Hogans [27] (2002) argument where we have a maximum entropy as

$$S_{max} = \pi/H^2 \quad (25)$$

, and this can be compared with A.K. Avessian’s article [26] (2009) value of, where we pick  $\Lambda \sim 1$

$$H_{macro} \equiv \Lambda \cdot [H_{Hubble} = H] \quad (26)$$

I.e. a choice as to how  $\hbar(t)$  has an initial value, and entropy as scale valued by  $S_{max} = \pi/H^2$  gives us a ball park estimate as to compressed values of  $\hbar_{initial} [t_{initial} \leq t_{Planck}]$  which would be transferred from a prior universe, to today’s universe. If  $S_{max} = \pi/H^2 \sim 10^5$ , this would mean an incredibly small value for the INITIAL  $H$  parameter, i.e. in pre inflation, we would have practically NO increase in expansion, just before the introduction vacuum energy, or emergent field energy from a prior universe, to our present universe.

Typically though, the value of the Hubble parameter, during inflation itself is HUGE, i.e.  $H$  is many times larger than 1, leading to initially very small entropy values. This means that we have to assume, initially, for a minimum transfer of entropy/ information from a prior universe, that  $H$  is negligible. If we look at Hogan’s holographic model, this is consistent with a non finite event horizon [27]

$$r_0 = H^{-1} \quad (27)$$

This is tied in with a temperature as given by

$$T_{black-hole} = (2\pi \cdot r_0)^{-1} \quad (28)$$

Nearly infinite temperatures are associated with tiny event horizon values, which in turn are linked to huge Hubble parameters of expansion. Whereas initially nearly zero values of temperature can be arguably linked to nearly non existent  $H$  values, which in term would be consistent with  $S_{max} = \pi/H^2 \sim 10^5$  as a starting point to entropy. We next then must consider how the values of initial entropy are linkable to other physical models. I.e. can there be a transfer of entropy/ information from a pre inflation state to the present universe. Doing this will require that we keep in mind, as Hogan writes, that the number of distinguishable states is writable as [27]

$$N = \exp(\pi H^{-2}) \quad (29)$$

If, in this situation, that  $N$  is proportional to entropy, i.e.  $N$  as  $\sim$  number of entropy states to consider, then as  $H$  drops in size, as would happen in pre inflation conditions, we will have opportunities for  $N \sim 10^5$

### **How the CMBR permits , via maximum frequency, and maximum wave amplitude values, an upper bound value for massive graviton mass $m_g$**

Camp and Cornish [28] (2004) , as does Fangyu Li [29] (2008) use the typical transverse gravitational gauge  $h_{ij}$  with a typically traceless value summed as  $0 + h_+ - h_+ + 0$  and off diagonal elements of  $h_x$  on each side of the diagonal to mix with a value of

$$h_{ij} \equiv \frac{G_N}{c^4} \cdot \frac{2}{r} \cdot \left[ \frac{d^2}{dt^2} Q_{ij} \right]_{retarded}^{TT} \quad (30)$$

This assumes  $r$  is the distance to the source of gravitational radiation, with the *retarded* designation on the Eq. (30) denoting  $\frac{d}{dt}$  replaced by a retarded time derivative  $\frac{d}{d[t-(r/c)]}$ , while TT means take the transverse projections and subtract the trace. Here, we call the quadrupole moment, with  $\rho(t, x)$  a density measurement. Now, the following value of the  $Q_{ij}$  as given gives a luminosity function  $L$ , where  $R$  is the ‘characteristic size’ of a gravitational wave source. Note that if  $M$  is the mass of the gravitating system

$$Q_{ij} = \int d^3x \left[ x_i x_j - \frac{1}{3} \cdot \delta_{ij} \cdot x^2 \right] \cdot \rho(t, x) \quad (31)$$

$$L \approx \frac{1}{5} \cdot \frac{G_N}{c^5} \cdot \frac{d^3 Q_{ij}}{dt^3} \cdot \frac{d^3 Q^{ij}}{dt^3} \cong \frac{\pi \cdot c^5}{G_N} \cdot \left( \frac{G_N M}{R \cdot c^2} \right)^2 \quad (32)$$

After certain considerations reported by Camp and Cornish [28](2004), one can recover a net GW amplitude

$$h \sim 2 \cdot \left[ \frac{G_N \cdot M}{R \cdot c^2} \right] \cdot \left[ \frac{G_N \cdot M}{r \cdot c^2} \right] \quad (33)$$

This last equation requires that  $R > R_G = \frac{G_N M}{c^2} \equiv$  gravitational radius of a system, with a black hole resulting if one sets  $R < R_G = \frac{G_N M}{c^2}$ . Note that when  $R \sim R_G = \frac{G_N M}{c^2}$  we are at an indeterminate boundary where one may pick our system as having black hole properties.

Now for stars, Camp and Cornish [28] (2004) give us that

$$h \approx 10^{-21} \cdot \left[ \frac{15 \cdot Mpc}{r} \right] \cdot \left[ \frac{M}{2.8 M_{solar-mass}} \right]^2 \cdot \left( \frac{90km}{R} \right) \quad (34)$$

$$f \equiv \text{frequency} \approx \sqrt{\frac{M}{2.8 M_{solar-mass}}} \cdot \sqrt{\frac{90km}{R}} \cdot 100Hz \quad (35)$$

As well as a mean time  $\tau_{GW}$  for half of gravitational wave potential energy to be radiated away as

$$\tau_{GW} \approx \frac{R}{2\pi \cdot c} \cdot \left[ \frac{G_N M}{R \cdot c^2} \right]^{-3} \sim \left( \frac{R}{90km} \right)^4 \cdot \left[ \frac{2.8 M_{solar-mass}}{M} \right]^3 \cdot \left( \frac{1}{2} \cdot \text{sec} \right) \quad (36)$$

The assumption we make is that if we model  $R \sim R_G = \frac{G_N M}{c^2}$ , for a sufficiently well posed net mass  $M$

that the star formulas roughly hold for early universe conditions, provided that we can have a temperature  $T$  for which we can use the approximation  $\approx \sqrt{\frac{M}{2.8M_{solar-mass}}} \cdot \sqrt{\frac{90km}{R}} \cdot 100Hz$  that we also have

$\left[ \frac{T}{TeV} \right] \sim 10^{13}$  or higher, so, that at a minimum we recover Grishchuck's [22] (2007) value of

$$f_{Peak} \approx (10^{-3} Hz) \cdot \left[ \frac{T}{TeV} \right] \sim 10^{10} Hz \quad (37)$$

$$\approx \sqrt{\frac{M}{M_{solar-mass}}} \cdot \sqrt{\frac{90km}{R}}$$

Eq (36) places, for a specified value of  $R$ , which can be done experimentally, an upper bound as far as far as what a mass  $M$  would be. Can this be exploited to answer the question of if or not there is a minimum value for the Graviton mass?

The key to the following discussion will be that  $\sqrt{\frac{M}{2.8M_{solar-mass}}} \cdot \sqrt{\frac{90km}{R}} \approx 10^8$ , or larger.

### **Inter relationship between graviton mass $m_g$ and the problem of a sufficient number of bits of $\hbar$ from a prior universe, to preserve continuity between fundamental constants from a prior to the present universe**

P. Tinyakov [30] (2006) gives that there is, with regards to the halo of sub structures in the local Milky Way galaxy an amplitude factor for gravitational waves of

$$\langle h_{ij} \rangle \sim 10^{-10} \cdot \left[ \frac{2 \cdot 10^{-4} Hz}{m_{graviton}} \right] \quad (38)$$

If we use LISA values for the Pulsar Gravitational wave frequencies, this may mean that the massive graviton is ruled out. On the other hand  $\sqrt{\frac{M}{2.8M_{solar-mass}}} \cdot \sqrt{\frac{90km}{R}} \approx 10^8$  leads to looking at, if

$$\langle h_{ij} \rangle \sim h \sim 10^{-5} \cdot \left[ \frac{15Mpc}{r} \right]^{1/2} \cdot \left[ \frac{M}{2.8 \cdot M_{solar-mass}} \right]^{1/2} \approx 10^{-30} \quad (39)$$

If the radius is of the order of  $r \geq 10$  billion light-years  $\sim 4300 Mpc$  or much greater, so then we have, as

an example  $\langle h_{ij} \rangle \sim 10^{-10} \cdot \left[ \frac{2 \cdot 10^{-4} Hz}{m_{graviton}} \right] \approx 5.9 \cdot 10^{-7} \cdot \left[ \frac{M}{2.8 \cdot M_{solar-mass}} \right]^{1/2}$

$$\left[ \frac{10^{-7} Hz}{m_{graviton}} \right] \approx \left[ \frac{5.9}{\sqrt{5.6}} \right] \cdot \sqrt{\frac{M}{M_{solar-mass}}} \quad (40)$$

This Eq. (40) is in units where  $\hbar = c = 1$ .

If  $10^{-60}$  grams per graviton, and 1 electron volt is in rest mass , so

$1.6 \times 10^{-33}$  grams  $\Rightarrow$  gram =  $6.25 \times 10^{32}$  eV . Then

$$\left[ \frac{10^{-7} \text{ Hz}}{m_{\text{graviton}}} \right] \equiv \left[ \frac{10^{-7} \text{ Hz} \cdot [6.582 \times 10^{-15} \text{ eV} \cdot \text{s}]}{[10^{-60} \text{ grams} \equiv 6.25 \times 10^{-28} \text{ eV}] \cdot [2.99 \times 10^9 \text{ meter / sec}]^2} \right] \sim \frac{10^{-22}}{10^{-9}} \sim 10^{-13}$$

Then, exist

$$M \sim 10^{-26} M_{\text{solar-mass}} \approx 1.99 \times 10^{33-26} \equiv 1.99 \times 10^7 \text{ grams} . \quad (41)$$

If each photon, as stated above is  $3.68 \times 10^{-48}$  grams per photon,[31] then

$$M \sim 5.44 \times 10^{54} \text{ initially transmitted photons.} \quad (42)$$

Futhermore, if there are , today for a back ground CMBR temperature of 2.7 degrees Kelvin  $5 \times 10^8$  photons / cubic – meter , with a wave length specified as  $\lambda_{\text{max}} \approx 1 \cdot \text{cm}$  . This is for a numerical density of photons per cubic meter given by

$$n_{\text{photon}} := \frac{\sigma \cdot (T)^4 \cdot (\lambda_{\text{max}})}{h \cdot c^2} \quad (43)$$

As a rough rule of thumb, if , as given by Weinberg (1973) [32] that early quantum effects , for quantum gravity take place at a temperature  $T \approx 10^{33}$  Kelvin, then, if there was that temperature for a cubic meter of space, the numerical density would be , roughly  $10^{132}$  times greater than what it is today. Forget it. So what we have to do is to consider a much smaller volume area. If the radii of the volume area is  $r \cong 4 \times 10^{-35}$  meters  $\equiv l_p = \text{Planck - length}$  ,then we have to work with a de facto initial volume  $\approx 64 \times 10^{-105} \sim 10^{-103} (\text{meters})^3$  . I.e. the numerical value for the number of photons at  $T \approx 10^{33}$  , if we have a per unit volume area based upon Planck length, in stead of meters, cubed is  $10^{29} \times (5 \times 10^8) \approx 5 \times 10^{37}$  photons for a cubic area with sides  $r \cong 4 \times 10^{-35}$  meters  $\equiv l_p$  at  $T|_{\text{quantum-effects}} \approx 10^{33}$  Kelvin However,  $M \sim 5.44 \times 10^{54}$  initially transmitted photons! Either the minimum distance ,i.e. the grid is larger, or  $T|_{\text{quantum-effects}} \gg 10^{33}$  Kelvin

We have, now, so far linked entropy, gravitons, and also information with certain qualifications. Next, we will attempt to quantify the treatment of gravitons , as given in Fig 1 above, with thin wall ( box shape ) treatment of quantum mechanics rendition of a Graviton . When the thin wall approximation fails, we approach having a semi classical embedding for Gravitons. Corresponding to squeezed states, for gravitons, we will introduce coherent states of gravitons.

The next part of our discussion will be in linking sequeezed states, with a break down of the purely quantum mechanical modeling of gravitons.

## Issues about Coherent state of Gravitons (linking gravitons with GW)

In the quantum theory of light (quantum electrodynamics) and other bosonic quantum field theories , coherent states were introduced by the work of [33] Roy J. Glauber in 1963 Now, what is appropriate for presenting gravitons as coherent states ? Coherent states , to first approximation are retrievable as minimum uncertainty states. If one takes string theory as a reference, the minimum value of uncertainty becomes part of a minimum uncertainty which can be written as given by Veneziano [34] (1993), where  $l_s \cong 10^\alpha \cdot l_{Planck}$  , with  $\alpha > 0$ , and  $l_{Planck} \approx 10^{-33}$  centimeters

$$\Delta x > \frac{\hbar}{\Delta p} + \frac{l_s^2}{\hbar} \cdot [\Delta p] \quad (44)$$

To put it mildly, if we are looking at a solution to minimize graviton position uncertainty, we will likely be out of luck if string theory is the only tool we have for early universe conditions. Mainly, the momentum will not be small, and uncertainty in momentum will not be small either. Either way, most likely,  $\Delta x > l_s \cong 10^\alpha \cdot l_{Planck}$  In addition, it is likely, as Klaus Kieffer [35] in the book “ Quantum Gravity” on page 290 of that book that if gravitons are excitations of closed strings, then one will have to look for conditions for which a coherent state of gravitons, as stated by [36] Mohaupt (2003) occurs. What Mohaupt is referring to is a string theory way to reproduce what Ford gave in 1995, i.e. conditions for how Gravitons in a squeezed vacuum state, the natural result of quantum creation in the early universe will introduce metric fluctuations. Ford’s [37] (1995) treatment is to have a metric averaged retarded Green’s function for a massless field becoming a Gaussian. The condition of Gaussianity is how to obtain semi classical , minimal uncertainty wave states, in this case de rigor for coherent wave function states to form. Ford uses gravitons in a so called ‘squeezed vacuum state’ as a natural template for relic gravitons. I.e. the squeezed vacuum state (a **squeezed coherent state**) is any state such that the uncertainty principle is saturated.: In QM coherence would be when  $\Delta x \Delta p = \hbar/2$ . In the case of string theory it would have to

be  $\Delta x \Delta p = \frac{\hbar}{2} + \frac{l_s^2}{2 \cdot \hbar} \cdot [\Delta p]^2$ . Putting it mildly, the string theory case is far more difficult. And that is

the problem, with regards to string theory, what is an appropriate vacuum expectation value for treating a template of how to nucleate gravitons into a coherent state with respect to relic conditions. [37] Ford, in 1994, wrote a squeezed state operation  $S(\zeta)$  via  $|\zeta\rangle = S(\zeta) \cdot |0\rangle$  , Here, the operator  $\cdot |0\rangle$  is a ground state, and frequently, as Ford did, in 1994, there is a definition of a root mean squared fluctuation of a graviton / gravitational wave state via use of an average scalar field  $\Phi$  , where

$$h^2 = \frac{1}{30} \cdot \langle h_{ij} h^{ij} \rangle = \frac{1}{15} \cdot \langle \Phi^2 \rangle \equiv \frac{1}{180} \cdot T^2 \Big|_{Thermal-bath} \quad (45)$$

Here, the value  $T \Big|_{Thermal-bath}$  has yet to be specified, and that actually for energy values approximately of

the order of  $10^{15} GeV$  which may be the mean temperature for the expanding universe mid way, to the end of inflation, which does not equal current even smaller string theory estimates as presented by Li et al

$h \Big|_{THERMAL-BATH} \approx 10^{-18} / \sqrt{Hz} \neq h_{rms} \sim 10^{-30} - 10^{-34} / \sqrt{Hz} \equiv$  string theory values for inflationary

Gravitational amplitudes. I.e. the more modern treatments are predicting almost infinitesimal GW fluctuations. It is not clear from Ford’s 1995 [37] treatment of gravitons, and fluctuations, if he is visualizing fluctuation of gravitons/ GW, but if one takes literally Eq. (45) as a base line, and then considering what would be the optimal way to obtain a way to obtain coherent states of gravitons, going to

the Li stated value of  $h_{rms} \sim 10^{-39} / \sqrt{Hz}$  for solar plasma from the sun as a graviton source, would be a

way of obtaining fluctuations  $10^{-5} - 10^{-9}$  times weaker , i.e. going to  $h_{rms}$  values so small that the

requirement for a minimum fluctuation , in line with not contradicting  $\Delta x \Delta p = \frac{\hbar}{2} + \frac{l_s^2}{2 \cdot \hbar} \cdot [\Delta p]^2$  , if we

consider experimental conditions for obtaining  $\Delta x \approx h_{rms} \sim 10^{-39} / \sqrt{Hz}$  . Note that this would put severe restrictions upon the variations in momentum. A subject which will be referenced in whether or not

the Li- Baker detector can suitably obtain such small values of  $\Delta x \approx h_{rms} \sim 10^{-39} / \sqrt{Hz}$  in detection capacity. To do so will require an investigation into extreme sensitivity requirements, for this very low value of  $h_{rms}$ . Fanguy Li. et al (2009) [38] reports in their PRD document  $h_{rms} \sim 10^{-26} - 10^{-30} / \sqrt{Hz}$  would require up to  $10^5$  seconds in evaluative time for a clean signal, for GW. What will be asked in further sections is if or not the  $10^5$  seconds in evaluative time for a clean signal can evaluate additional data. I.e. what if one would have to do to distinguish if or not coherent states of gravitons which merge to form GW may be measured via the protocols brought up by Li et al [38](2009) for relic GW. Now what could be said about forming states close to classical representations of gravitons? Venkatartnam, and Suresh, 2007 [39] built up a coherent state via use of a displacement operator  $D(\alpha) \equiv \exp(\alpha \cdot a^+ - \alpha^* \cdot a)$ , applied to a vacuum state, where  $\alpha$  is a complex number, and  $a, a^+$  as annihilation, and creation operations  $[a, a^+] = 1$ , where one has

$$|\alpha\rangle = D(\alpha) \cdot |0\rangle \quad (46)$$

However, what one sees in string theory, is a situation where a vacuum state as a template for graviton nucleation is built out of an initial vacuum state,  $|0\rangle$ . To do this though, as Venkatartnam, and Suresh [39] did, involved using a squeezing operator  $Z[r, \mathcal{G}]$  defining via use of a squeezing parameter  $r$  as a strength of squeezing interaction term, with  $0 \leq r \leq \infty$ , and also an angle of squeezing,  $-\pi \leq \mathcal{G} \leq \pi$  as used in  $Z[r, \mathcal{G}] = \exp\left[\frac{r}{2} \cdot \left([\exp(-i\mathcal{G})] \cdot a^2 - [\exp(i\mathcal{G})] \cdot a^{+2}\right)\right]$ , where combining the  $Z[r, \mathcal{G}]$  with (47) leads to a single mode squeezed coherent state, as they define it via

$$|\zeta\rangle = Z[r, \mathcal{G}]|\alpha\rangle = Z[r, \mathcal{G}]D(\alpha) \cdot |0\rangle \xrightarrow{\alpha \rightarrow 0} Z[r, \mathcal{G}] \cdot |0\rangle \quad (48)$$

The right hand side of Rq. (48) given above becomes a highly non classical operator, i.e. in the limit that the super position of states  $|\zeta\rangle \xrightarrow{\alpha \rightarrow 0} Z[r, \mathcal{G}] \cdot |0\rangle$  occurs, there is a many particle version of a ‘vacuum state’ which has highly non classical properties. Squeezed states, for what it is worth, are thought to occur at the onset of vacuum nucleation, but what is noted for  $|\zeta\rangle \xrightarrow{\alpha \rightarrow 0} Z[r, \mathcal{G}] \cdot |0\rangle$  being a super position of vacuum states, means that classical analog is extremely difficult to recover in the case of squeezing, and general non classical behavior of squeezed states. Can one, in any case, faced with  $|\alpha\rangle = D(\alpha) \cdot |0\rangle \neq Z[r, \mathcal{G}] \cdot |0\rangle$

do a better job of constructing coherent graviton states, in relic conditions, which may not involve squeezing?. Note L. Grishchuk [40] wrote in (1989) in ‘‘On the quantum state of relic gravitons’’, where he claimed in his abstract that ‘It is shown that relic gravitons created from zero-point quantum fluctuations in the course of cosmological expansion should now exist in the squeezed quantum state. The authors have determined the parameters of the squeezed state generated in a simple cosmological model which includes a stage of inflationary expansion. It is pointed out that, in principle, these parameters can be measured experimentally’. Grishchuk [40], et al, (1989) reference their

version of a cosmological perturbation  $h_{nlm}$  via the following argument. How we work with the argument will affect what is said about the necessity, or lack of, of squeezed states in early universe cosmology. From[40] Class. Quantum Gravity: 6 (1989), L 161-L165, where  $h_{nlm}$  has a component  $\mu_{nlm}(\eta)$  obeying a parametric oscillator equation, where  $K$  is a measure of curvature which is  $= \pm 1, 0$ ,  $a(\eta)$  is a scale factor of a FRW metric, and  $n = 2\pi \cdot [a(\eta)/\lambda]$  is a way to scale a wavelength,  $\lambda$ , with  $n$ , and with  $a(\eta)$

$$h_{nlm} \equiv \frac{l_{Planck}}{a(\eta)} \cdot \mu_{nlm}(\eta) \cdot G_{nlm}(x) \quad (49)$$

$$\mu_{nlm}''(\eta) + \left( n^2 - K - \frac{a''}{a} \right) \cdot \mu_{nlm}(\eta) \equiv 0 \quad (50)$$

If  $y(\eta) = \frac{\mu(\eta)}{a(\eta)}$  is picked, and a Schrodinger equation is made out of the Lagrangian used to formulate Eq.

(50) above, with  $\hat{P}_y = \frac{-i}{\partial y}$ , and  $M = a^3(\eta)$ ,  $\Omega = \frac{\sqrt{n^2 - K^2}}{a(\eta)}$ ,  $\tilde{a} = [a(\eta)/l_{Planck}] \cdot \sigma$ , and  $F(\eta)$  an

arbitrary function.  $y' = \partial y / \partial \eta$ . Also, we have a finite volume  $V_{finite} = \int \sqrt{^{(3)}g} d^3x$

Then the Lagrangian for deriving Eq. (50) is ( and leads to a Hamiltonian which can be **also** derived from the Wheeler De Witt equation), with  $\zeta = 1$  for zero point subtraction of energy

$$L = \frac{M \cdot y'^2}{2a(\eta)} - \frac{M^2 \cdot \Omega^2 a \cdot y^2}{2} + a \cdot F(\eta) \quad (51)$$

$$\frac{-1}{i} \cdot \frac{\partial \psi}{a \cdot \partial \eta} \equiv \hat{H} \psi \equiv \left[ \frac{\hat{P}_y^2}{2M} + \frac{1}{2} \cdot M \Omega^2 \hat{y}^2 - \frac{1}{2} \cdot \zeta \cdot \Omega \right] \cdot \psi \quad (52)$$

then there are two possible solutions to the S.E. Grushchuk [40] created in 1989, one a non squeezed state, and another a squeezed state. So in general we work with

$$y(\eta) = \frac{\mu(\eta)}{a(\eta)} \equiv C(\eta) \cdot \exp(-B \cdot y) \quad (53)$$

The **non squeezed state** has a parameter  $B|_{\eta \rightarrow \eta_b} \rightarrow B(\eta_b) \equiv \omega_b/2$  where  $\eta_b$  is an initial time, for which the Hamiltonian given in Eq. (52) in terms of raising/ lowering operators is ‘diagonal’, and then the rest of the time for  $\eta \neq \eta_b$ , the **squeezed state** for  $y(\eta)$  is given via a parameter B for squeezing which when looking at a squeeze parameter r, for which  $0 \leq r \leq \infty$ , then Eq. (53) has, instead of  $B(\eta_b) \equiv \omega_b/2$

$$B|_{\eta \rightarrow \eta_b} \rightarrow B(\omega, \eta \neq \eta_b) \equiv \frac{i}{2} \cdot \frac{(\mu/a(\eta))'}{(\mu/a(\eta))} \equiv \frac{\omega}{2} \cdot \frac{\cosh r + [\exp(2i\vartheta)] \cdot \sinh r}{\cosh r - [\exp(2i\vartheta)] \cdot \sinh r} \quad (54)$$

Taking Grishchuk’s formalism [40] literally, a state for a graviton/ GW is not affected by squeezing when we are looking at an initial frequency, so that  $\omega \equiv \omega_b$  initially corresponds to a non squeezed state which may have coherence, but then right afterwards, if  $\omega \neq \omega_b$  which appears to occur whenever the time

evolution,  $\eta \neq \eta_b \Rightarrow \omega \neq \omega_b \Rightarrow B(\omega, \eta \neq \eta_b) \equiv \frac{i}{2} \cdot \frac{(\mu/a(\eta))'}{(\mu/a(\eta))} \neq \frac{\omega_b}{2}$  A reasonable research task

would be to determine, whether or not  $B(\omega, \eta \neq \eta_b) \neq \frac{\omega_b}{2}$  would correspond to a vacuum state being initially formed right after the point of nucleation, with  $\omega \equiv \omega_b$  at time  $\eta \equiv \eta_b$  with an initial



cosmological time some order of magnitude of a Planck interval of time  $t \approx t_{Planck} \propto 10^{-44}$  seconds The next section will be to answer whether or not there could be a point of no squeezing, as Grishchuk implied, for initial times, and initial frequencies, and an immediate transition to times, and frequencies afterwards, where squeezing was mandatory. Note that in 1993, Grischchuk [41] further extended his analysis, with respect to the same point of departure, ie. What to do with when  $|\alpha\rangle = D(\alpha) \cdot |0\rangle \neq Z[r, \mathcal{G}] \cdot |0\rangle$ . Having  $|\alpha\rangle = D(\alpha) \cdot |0\rangle$  with  $D(\alpha)$  a possible displacement operator, seems to be in common with  $B(\eta_b) \equiv \omega_b/2$ , whereas  $|\alpha\rangle = Z[r, \mathcal{G}] \cdot |0\rangle$  which is highly non classical seems to be in common with a solution for which  $B(\omega_b) \neq (\omega_b/2)$  This leads us to the next section, i.e. does  $B(\eta_b) \equiv \omega_b/2$  when of time  $t \approx t_{Planck} \propto 10^{-44}$  seconds, and then what are the initial conditions for forming ‘frequency’  $\omega \equiv \omega_b$  ?

### **Necessary and sufficient conditions for String/ Brane theory graviton coherent states?**

A curved spacetime is a coherent background of gravitons, and therefore in string theory is a coherent state Joseph Gerard Polchinski [42] starting with the typical small deviation from flat space times as can be written up by  $G_{uv}(X) = \eta_{uv} + h_{uv}(X)$ , with  $\eta_{uv}$  flat space time, and the Polyakov action, is generalized as follows, the  $S_\sigma$  Polyakov action is computed and compared with exponentiated values

$$S_\sigma = \frac{1}{4\pi\alpha'} \cdot \int_M d^2\sigma \cdot \sqrt{g} \cdot g^{ab} \cdot G_{uv}(X) \cdot \partial_a X^\mu \partial_b X^\nu \quad (55)$$

becomes

$$\exp(-S_\sigma) = [\exp(-S_p)] \cdot \left[ 1 - \frac{1}{4\pi\alpha'} \cdot \int_M d^2\sigma \cdot \sqrt{g} \cdot g^{ab} \cdot h_{uv}(X) \cdot \partial_a X^\mu \partial_b X^\nu + \dots \right] \quad (56)$$

Polochinski writes that the term of order  $h$  in Eq. (56) is the vertex operator for the graviton state of the string, with  $h_{uv}(X) \equiv -4\pi g_c \cdot \exp[-ikX_{S_w}]$ , and the action of  $S_\sigma$  a coherent state of a graviton. Now the important question to ask, is if this coherent state of a graviton, as mentioned by Polochinski can hold up in relic, early universe conditions. R Dick [43], in 2001, argued as stating that the “graviton multiplet as one particular dark matter source in heterotic string theory. In particular, it is pointed out that an appreciable fraction of dark matter from the graviton multiplet requires a mass generating phase transition around  $T_c \approx 10^8$  GeV, where the symmetry partners of the graviton would evolve from an ultrahard fluid to pressureless dark matter. indicates  $m \approx 10$  MeV for the massive components of the graviton multiplet”. This has a counter part in a presentation made by Berkenstein (2004) [44] with regards to BPS states, and SHO models for  $AdS_5 \times S^5$  geometry. The upshot is that string theory appears to construct coherent graviton states, but it has no answer to the problem that Ford [37] (1995), wrote on if the existing graviton coherent states would be squeezed into non classical configurations in relic conditions.

### **Does LQG give us more direct arguments as to coherent states, squeezed states, and the break down of classical behavior at the onset of inflation ?**

Carlo Rovelli,[45] in 2006, in a PRL article states that a vertex amplitude that contributes to a coherent graviton state is the exponential of the Regge action: the other terms, that have raised doubts on the physical viability of the model, are suppressed by the phase of the vacuum state, and Rovelli writes a coherent vacuum state as given by a Gaussian peaked on parts of the boundary  $\Sigma_d$  of a four dimensional sphere.

$$\Psi_q[s] = \Psi_q(\Gamma, j_{m,n}) \quad (57)$$

Rovelli [45] states that “bad” contributions to the behavior of Eq. (57) are cancelled out by an appropriate (Gaussian?) vacuum wave functional which has ‘appropriately’ chosen contributions from the boundary  $\Sigma_d$  of a four dimensional sphere. This is to avoid trouble with “bad terms” from what is known as the Barret – Crane vertex amplitude contributions, which are can be iminized by an appropriate choice of vacuum state amplitude being picked. Rovelli [45]calculated some components of the graviton two-point function and found that the Barrett-Crane vertex yields a wrong long-distance limit. A problem, as stated by Lubos Motel (2007) [46], that there are infinitely many other components of the correlators in the LQG that are guaranteed not to work unless an infinite number of adjustments are made. The criticism is harsh, but until one really knows admissible early universe geometry one cannot rule out the Rovelli approach, or confirm it. In addition, Jakub Mielczarek [47] (2009) considered tensor gravitational perturbations produced at a bounce phase in presence of the holonomy corrections. Here bounce phase and holonomy corrections originate from Loop Quantum Cosmology . What comes to the fore are corrections due to what is called quantum holonomy, l. A comment about the quantum bounce. i.e. what is given by Dah-Wei Chiou, Li-Fang Li,[48] (2009) is that there is a branch match up between a prior to a present set of Wheeler De Witt equations for a prior to present universe, as far as modeling how the quantum bounce links the two Wheeler De Witt solution branches, i.e. one Wheeler De Witt wave function for a prior univers, and another wave function for a present universe. Furthermore, Abhay Ashtekar [49] ( 2006) wrote a simple treatment of the Bounce causing Wheeler De Witt equation along the lines of , for  $\rho_* \approx const \cdot (1/8\pi G\Delta)$  as a critical density, and  $\Delta$  the eignvalue of a minimum area operator. Small values of  $\Delta$  imply that gravity is a repulsive force, leading to a bounce effect.

$$\left(\frac{\dot{a}}{a}\right)^2 \equiv \frac{8\pi G}{3} \cdot \rho \cdot (1 - (\rho/\rho_*)) + H.O.T. \quad (58)$$

Furthermore, Bojowald [50, 51] (2008) specified a criteria as to how to use an updated version of  $\Delta$  and  $\rho_* \approx const \cdot (1/8\pi G\Delta)$  in his GRG manuscript on what could constitute grounds for the existence of generalized squeezed initial (graviton ?) states. Bojowald [51] (2008) was referring to the existence of squeezed states, as either being necessarily, or NOT necessarily a consequence of the quantum bounce. As Bojowald [51] (2008) wrote it up, in both his equation (26) which has a quantum Hamiltonian  $\langle \hat{V} \rangle \approx H$ , with

$$\left. \frac{d\langle \hat{V} \rangle}{d\phi} \right|_{\phi \approx 0} \xrightarrow{\text{existence-of-un-squeezed-states} \Leftrightarrow \phi \approx 0} 0 \quad (59)$$

and  $\hat{V}$  is a ‘volume’ operator where the ‘ volume’ is set as  $V$  , Note also, that Bojowald has , in his initial Friedman equation, density values  $\rho \equiv \frac{H_{matter}(a)}{a^3}$  , so that when the Friedman equation is quantized, with an initial internal time given by  $\phi$  , with  $\phi$  becoming a more general evolution of state variable than ‘internal time’. If so, Bojowald (2008) writes, when there are squeezed states[51]

$$\left. \frac{d\langle \hat{V} \rangle}{d\phi} \right|_{\phi \neq 0} \xrightarrow{\text{existence-of-squeezed-states}} N(\text{value}) \neq 0 \quad (60)$$

for his equation (26), which is incidently when links to classical behavior break down , and when the bounce from a universe contracting goes to an expanding present universe,. Bojowald [51] also writes that if one is looking at an isotropic universe, that as the large matter ‘H’ increases, that in certain cases, one

observes more classical behavior, and a reduction in the strength of a quantum bounce.. Bojowalds [51] states that “Especially the role of squeezed states is highlighted. The presence of a bounce is proven for uncorrelated states, but as squeezing is a dynamical property and may change in time” The upshot is that although it is likely in a quantum bounce state that the states should be squeezed, it is not a pre requisite for the states to always start off as being squeezed states. .So a physics researcher can ,look at if an embedding of the present universe in a higher dimensional structure which could have lead to a worm hole from a prior universe to our present for re introduction of inflationary growth

### **Other models. Do worm hole bridges between different universes allow for initial un squeezed states? Wheeler De Witt solution with pseudo time component added in.**

This discussion is to present a not so well known but useful derivation of how instanton structure from a prior universe may be transferred from a prior to the present universe.. This discussion is partly rendered in [15] , but is reproduced here due to the relatively unknown feature of a pseudo time component to the Wheeler de Witt equation

1. The solution as taken from L. Crowell’s (2005)[52] book, and re produced here, as referenced by Beckwith (2008,2009) has many similarities with the WKB method. I.e. it is semi CLASSICAL.
2. left unsaid is what embedding structure is assumed
3. A final exercise for the reader. Would a WKB style solution as far as transfer of ‘material’ from a prior to a present universe constitute procedural injection of non compressed states from a prior to a present universe ? Also if uncompressed, coherent states are possible, how long would they last in introduction to a new universe ?

This is the Wheeler-De-Witt equation with pseudo time component added. From Crowell

$$-\frac{1}{\eta r} \frac{\partial^2 \Psi}{\partial r^2} + \frac{1}{\eta r^2} \cdot \frac{\partial \Psi}{\partial r} + r R^{(3)} \Psi = (r \eta \dot{\phi} - r \ddot{\phi}) \cdot \Psi \quad (61)$$

This has when we do it  $\phi \approx \cos(\omega \cdot t)$ , and frequently  $R^{(3)} \approx \text{constant}$ , so then we can consider

$$\phi \cong \int_0^{\infty} d\omega \left[ a(\omega) \cdot e^{ik_{\sigma} x^{\mu}} - a^+(\omega) \cdot e^{-ik_{\sigma} x^{\mu}} \right] \quad (62)$$

In order to do this, we can write out the following for the solutions to Eq (61) above.

$$C_1 = \eta^2 \cdot \left( 4 \cdot \sqrt{\pi} \cdot \frac{t}{2\omega^5} \cdot J_1(\omega \cdot r) + \frac{4}{\omega^5} \cdot \sin(\omega \cdot r) + (\omega \cdot r) \cdot \cos(\omega \cdot r) \right) + \frac{15}{\omega^5} \cos(\omega \cdot r) - \frac{6}{\omega^5} Si(\omega \cdot r) \quad (63)$$

And

$$C_2 = \frac{3}{2 \cdot \omega^4} \cdot (1 - \cos(\omega \cdot r)) - 4e^{-\omega r} + \frac{6}{\omega^4} \cdot Ci(\omega \cdot r) \quad (64)$$

This is where  $Si(\omega \cdot r)$  and  $Ci(\omega \cdot r)$  refer to integrals of the form  $\int_{-\infty}^x \frac{\sin(x')}{x'} dx'$  and  $\int_{-\infty}^x \frac{\cos(x')}{x'} dx'$  . .

Next, we should consider whether or not the instanton so formed is stable under evolution of space-time leading up to inflation. To model this, we use results from Crowell [52] (2005) on quantum fluctuations in space-time, which gives a model from a pseudo time component version of the Wheeler-De-Witt equation, with use of the Reinsner-Nordstrom metric to help us obtain a solution that passes through a thin shell separating two space-times. The radius of the shell  $r_0(t)$  separating the two space-times is of length  $l_p$  in approximate magnitude, leading to a domination of the time component for the Reissner – Nordstrom metric

$$dS^2 = -F(r) \cdot dt^2 + \frac{dr^2}{F(r)} + d\Omega^2 \quad (65)$$

This has:

$$F(r) = 1 - \frac{2M}{r} + \frac{Q^2}{r^2} - \frac{\Lambda}{3} \cdot r^2 \xrightarrow{T \rightarrow 10^{32} \text{ Kelvin} \rightarrow \infty} -\frac{\Lambda}{3} \cdot (r = l_p)^2 \quad (66)$$

This assumes that the cosmological vacuum energy parameter has a temperature dependence as outlined by Park (2003), leading to

$$\frac{\partial F}{\partial r} \sim -2 \cdot \frac{\Lambda}{3} \cdot (r \approx l_p) \equiv \eta(T) \cdot (r \approx l_p) \quad (67)$$

as a wave functional solution to a Wheeler-De-Witt equation bridging two space-times, similar to two space-times with “instantaneous” transfer of thermal heat, as given by Crowell (2005)

$$\Psi(T) \propto -A \cdot \{\eta^2 \cdot C_1\} + A \cdot \eta \cdot \omega^2 \cdot C_2 \quad (68)$$

This has  $C_1 = C_1(\omega, t, r)$  as a pseudo cyclic and evolving function in terms of frequency, time, and spatial function. This also applies to the second cyclical wave function  $C_2 = C_2(\omega, t, r)$ , where

$C_1 = \text{Eq (63)}$  and  $C_2 = \text{Eqn. (64)}$  then we get that Eqn. (68) is a solution to the pseudo time WDM equation.

The question which will be investigated is if Eq. (68) is a way to present either a squeezed or un squeezed state. A way forward is to note that Prado Martin-Moruno, Pedro F. Gonzalez-Diaz in July [53] (2009) wrote up about thermal phantom-like radiation process coming from the wormhole throat. Note that the Crowell construction of a worm hole bridge is in some ways similar to Carco Cavaglià's [54] (1994 )

treatment of use of conjugate momentum  $\pi^{ij}$  of  $h_{ij}$  generalized momentum variables, also known as conjugate momenta  $\hat{\pi}^{ij} \equiv \frac{\hbar}{i} \cdot \frac{\partial}{\partial \cdot h_{ij}}$ , leading to the sort of formalism as attributed to Luis J. Garay's

(1991)[55] article , of

$$\Psi(h_{ij}) \approx \left[ \exp \int d^3 x \cdot \pi^{ij} \cdot h_{ij} \right]_r \quad (69)$$

Now in the case of what can be done with the worm hole used by Crowell [52] , with, if  $\hbar \equiv 1$ ,  $\hat{\pi}^{ij} \equiv -i \frac{\delta}{\delta \cdot g_{ij}}$

,  $\hat{\pi}^{\theta\theta} \equiv -\frac{i}{2r} \frac{\partial}{\partial \cdot r}$ ,  $\hat{\pi}^{tt} \equiv -i \cdot \left( \frac{\partial F(r)}{\partial r} \right)^{-1} \cdot \frac{\partial}{\partial \cdot r}$ , and a kinetic energy value as given of the form

$\hat{\pi}^{\theta\theta} \hat{\pi}^{tt} + \hat{\pi}^{tt} \hat{\pi}^{\theta\theta}$ . The supposition which we have the worm hole wave functional may be like, so, use the wave functional looking like  $\Psi(g_{ij}) \approx \left[ \exp \int d^3 x \cdot [\pi^{ij}] \cdot g_{ij} \right]_r$  where the  $g_{ij}$  for the Weiner-Nordstrom metric will be

$$dS^2 = -F(r) \cdot dt^2 + \frac{dr^2}{F(r)} + d\Omega^2 \equiv g^{ij} dx^i dx^j \equiv \frac{\Lambda}{3} \cdot (r = l_p)^2 \cdot dt^2 - \frac{dr^2}{\frac{\Lambda}{3} \cdot (r = l_p)^2} + d\Omega^2$$

### Unanswered questions, and what this suggests for future research endeavors

As far back as 1982, Linde, [56] when analyzing a potential of the form

$$V(\phi) = \frac{m^2 \phi^2}{2} + \lambda \phi^4 + V(0) \quad (70)$$

This is when the ‘mass’ has the form, (here M is the bare mass term of the field  $\phi$  in de Sitter space, which does not take into account quantum fluctuations)

$$m^2(t) = M^2 + \frac{3\lambda H^3}{4\pi} \cdot (t - t_0) \quad (71)$$

Specified non linearity of  $\langle \phi^2 \rangle$  at a time from the big bang, of the form

$$\Delta t_1 \approx \frac{3H}{2M} \quad (72)$$

The question raised repeatedly in whether or not i) if higher dimensions are necessary, and whether or not ii) mass gravitons are playing a role as far as the introduction of DE speed up of cosmological expansion may lead to an improvement over what was specified for density fluctuations and structure formation (the galaxy hierarchy problem ) of density fluctuations given as

$$\frac{\delta\rho}{\rho} \sim 10^{-4} \Leftrightarrow \lambda \leq 10^{-10} \quad (73)$$

Eq (73) is for four space, a defining moment as to what sort of model would lead to density fluctuations. It totally fails as to give useful information as to the galaxy hierarchy problem as given in figure 1, above. Secondly, to what degree is the relative speed up of the  $q(z)$  function is impacted by various inter plays between , say a MODIFIED version of, say a KK DM model, using a MODIFIED mass hierarchy to get suitable DM masses of the order of 100 GeV or more. Giving a suitable definition as to  $q(z)$  as well as the inter play between DM values, 4 Dim Graviton mass issues, and /or what really contributes to the speed up of the universe will in the end dramatically improve the very crude estimate given by Eq. (70) above which says next to nothing about how the problems illustrated by the break down of the galaxy mass formation/ hierarchy can be fixed. Furthermore is considering the spectral index problem, where the spectral index is

$$n_s - 1 \cong -\frac{3}{8\pi} \cdot \left(\frac{V_\phi}{V}\right)^2 + \frac{1}{4\pi} \cdot \left(\frac{V_{\phi\phi}}{V}\right)^2 \quad (74)$$

Usual experimental values of density fluctuations experimentally are  $\frac{\delta\rho}{\rho} \sim 10^{-5}$  , instead of

$\frac{\delta\rho}{\rho} \sim 10^{-4}$  , and this is assuming that  $\lambda$  is extremely small. In addition, Linde[56] (1982) had

$\frac{d}{d\phi^2} V = m^2 \leq \frac{H}{40} = \frac{1}{40} \cdot \frac{\dot{a}}{a}$  inside a false vacuum bubble. If something other than the Klein Gordon

relationship  $\frac{\dot{a}}{a} \Rightarrow \ddot{\phi} + 3H\dot{\phi} + m^2\phi = 0$  occurs, then different models of how density fluctuation may have to be devised. A popular model of density fluctuations with regards to the horizon is

$$\left(\frac{\delta\rho}{\rho}\right)_{Horizon} \cong \frac{k^{3/2} |\delta_k|}{\sqrt{2\pi}} \propto \frac{k^{(3/2)+3\alpha-3/2}}{\sqrt{2\pi}} \approx (1/\sqrt{2\pi}) \cdot k^{3\alpha} \quad (75)$$

, where  $-0.1 < \alpha < 0.2$  , and  $\alpha \cong 0 \Leftrightarrow n_s \cong 1$  and to first order,  $k \cong Ha$  . The values, typically of

$n_s \neq 1$  If working with  $H^2 = \left(\frac{\dot{a}}{a}\right)^2 = \left[\left(\frac{\rho}{3M_4^2} + \frac{\rho^2}{36M_{Planck}^2}\right) + \frac{C}{a^4}\right]$  , and with a density value

$\rho \cong \rho_0 \cdot \left(\frac{a_0}{a}\right)^3 - \left[\frac{m_g c^6}{8\pi G \hbar^2}\right] \cdot \left(\frac{a^4}{14} + \frac{2a^2}{5} - \frac{1}{2}\right)$  where  $m_g \approx 10^{-65}$  grams, and  $\alpha < 0.2$  is usually

picked to avoid over production of black holes, a very complex picture emerges. Furthermore, if working with  $\alpha < 0.2$  and  $\alpha \neq 0$

$$\left(\frac{\delta\rho}{\rho}\right)_{Horizon} \cong (1/\sqrt{2\pi}) \cdot k^{3\alpha} \sim \frac{H^2}{\dot{\phi}} \propto 10^{-4} - 10^{-5} \quad (76)$$

The above equation gives inter relationships between the time evolution of a pop up inflaton field  $\phi$ , and a Hubble expansion parameter  $H$ , and a wave length parameter  $\lambda = (2\pi/k) \cdot a(t)$  for a mode given as  $\delta_k$ . What should be considered is the inter relationship of the constituent components of Eq. (76) and  $\lambda \leq H^{-1}$ . What the author thinks is of particular import is to look at whether or not the more general expression, as given by the below equation also holds.[57]

$$\left(\frac{\delta\rho}{\rho}\right) \cong Ak^{\left(\frac{n_s-1}{2}\right)} \propto 10^{-4} - 10^{-5} \quad (77)$$

To first order, variations of  $\alpha < 0.2$  and  $\alpha \neq 0$ , should be compared with admissible values of  $\left(\frac{n_s - 1}{2}\right)$  which would closely correspond to  $\alpha \neq 0$  and  $0 < \alpha \ll 0.2$ . I.e. the precise values of this may help us out in determining how to unravel what is going on in the galaxy formation I.e. how can we have earlier than expected galaxy formation ?.

### Conclusions, as to how to look at early universe topology and later flat space

One of the aspects of early universe topology we need to consider is how to introduce a de facto break down of quantization in curved space time geometries, and this is a problem which would permit a curved space treatment of  $\Psi \sim [R/R_{eq}]^{3/2}$ . I.e. as  $R$  gets of the order of  $R \sim \mathcal{G}(l_p)$ , say that the spatial geometry of early universe expansion is within a few orders of magnitude of Planck length, then how can we recover a field theory quantization condition for  $\Psi \sim [R/R_{eq}]^{3/2}$  in terms of path integrals. We claim that deformation quantization, if applied successfully will eventually lead to a great refinement of the above Wheeler De Witt wave functional value, as well as allow a more thorough match up of a time independent solution of the Wheeler De Witt equation, with the more subtle pseudo time dependent evolution of the wave functional as Crowell wrote up. I.e. the linkage between time independent treatments of the wave functional of the universe, with what Lawrence Crowell [52] wrote up in 2005, will be made more explicit. This will, in addition allow us to understand better how graviton production in relic conditions may add to entropy, as well as how to link the number of gravitons, say  $10^{12}$  gravitons per photon, as information as a way to preserve the continuity of  $\hbar$  values from a prior universe to the present universe.

**The author claims that in order to do this rigorously, that use of the material in [58]Gutt, and Waldmann will be necessary, especially to investigate if quantization of severely curved space time conditions is possible. We claim that it is not. [15]**

Resolution of which add more detail to  $\Psi \sim [R/R_{eq}]^{3/2}$ . Having said this, it is now important to consider what can be said about how relic gravitons/ information can pass through minimum vales of  $R \sim \mathcal{G}(l_p)$ .

We shall reference what the AW. Beckwith (2008) presented in 2008 STAIF [59], which we think still has current validity for reasons we will elucidate upon in this document. We use a power law relationship first presented by Fontana [60] (2005), who used Park's earlier (1955) [61] derivation: when

$$E_{eff} \equiv \langle n(\omega) \rangle \cdot \omega \equiv \omega_{eff}$$

$$P(power) = 2 \cdot \frac{m_{graviton}^2 \cdot \widehat{L}^4 \cdot \omega_{net}^6}{45 \cdot (c^5 \cdot G)} \quad (78)$$

This expression of power should be compared with the one presented by Massimo Giovannini (2008) on averaging of the energy-momentum pseudo tensor to get his version of a gravitational power energy density expression, namely [62]

$$\bar{\rho}_{GW}^{(3)}(\tau, \tau_0) \cong \frac{27}{256 \cdot \pi^2} H^2 \cdot \left(\frac{H}{M}\right)^2 \cdot \left[1 + \mathcal{G} \cdot \left(\frac{H^4}{M^4}\right)\right] \quad (79)$$

Giovannini states that should the mass scale be picked such that  $M \sim m_{planck} \gg m_{graviton}$ , that there are doubts that we could even have inflation. However, it is clear that gravitational wave density is faint, even if we make the approximation that  $H \equiv \frac{\dot{a}}{a} \cong \frac{m\phi}{\sqrt{6}}$  as stated by [63] Linde (2008), where we are following

$\dot{\phi} = -m\sqrt{2/3}$  in evolution, so we have to use different procedures to come up with relic gravitational wave detection schemes to get quantifiable experimental measurements so we can start predicting relic gravitational waves. This is especially true if we make use of the following formula for gravitational radiation, as given by L.Kofman [64] (2008), with  $M = V^{1/4}$  as the energy scale, with a stated initial inflationary potential V. This leads to an initial approximation of the emission frequency, using present-day gravitational wave detectors.

$$f \cong \frac{(M = V^{1/4})}{10^7 GeV} Hz \quad (80)$$

What we would like to do for future development of entropy would be to consider a way to ascertain if or not the following is really true, and to quantify it by an improvement of a supposition advanced by [65] Kiefer, Polarski, and Starobinsky as of (2000). I.e. the author, Beckwith, has in this document presented a general question of how to avoid having  $dS/dt = \infty$  at  $S=0$ .

- 1, Removes any chance that early universe nucleation is a quantum based emergent field phenomena
2. Goldstone gravitons would arise in the beginning due to a violation of Lorentz invariance. I.e. we have a causal break, and merely having the above condition does not qualify for a Lorentz invariance breakdown

Kiefer, Polarski, and Starobinsky as of (2000) [65] presented the idea of presenting the evolution of relic entropy via the evolution of phase spaces, with  $\Gamma/\Gamma_0$  being the ratio of ‘final (future)’ / ‘initial’ phase space volume, for k modes of secondary GW background.

$$S(k) = \ln \frac{\Gamma}{\Gamma_0} \quad (81)$$

If the phase spaces can be quantified, as a starting point of say  $l_{min-length-string} \equiv 10^\alpha \cdot l_{Planck}$ , with  $l_{Planck}$  being part of how to form the ‘dimensions’ of  $\Gamma_0$ , and  $l_{min-length-string}$  part of how to form the dimensions of  $\Gamma$ , and  $10^\alpha$  being, for a given  $\alpha > 0$ , and in certain cases  $\alpha \gg 0$ , then avoiding having  $dS/dt = \infty$  at  $S=0$  will be straight forward. We hope to come up with an emergent structure for gravitational fields which is congruent with obtaining  $10^\alpha$  naturally, so this sort of procedure is non controversial, and linked to falsifiable experimental measurement protocol, so quantum gravity becomes a de facto experimental science. This will mean looking at Appendix B, fully. Appendix C, and Appendix D give further issues we describe later on in future publications. We give them as pertinent information for the future development of this project.

## Appendix A: Bounds upon Graviton mass, and making use of the difference between Graviton propagation speed and HFGW transit speed to observe post Newtonian corrections to Gravitational potential fields.

The author presents a post Newtonian approximation based upon an earlier argument / paper by Clifford Will as to Yukawa revisions of gravitational potentials in part initiated by gravitons with explicit mass dependence in their Compton wave length.

### Introduction

Post Newtonian approximations to General relativity have given physicists a view as to how and why inflationary dynamics can be measured via deviation from simple gravitational potentials. One of the simplest deviations from the Newtonian inverse power law gravitational potential being a Yukawa potential modification of gravitational potentials. So happens that the mass of a graviton would factor directly into the Yukawa exponential term modification of gravity . This appendix indicates how a smart experimentalist could use the Li-Baker detector as a way to obtain more realistic upper bounds as to the mass of a graviton and to use it as a template to investigate modifications of gravity along the lines of a Yukawa potential modification as given by Clifford Will [66] .

### Giving an upper bound to the mass of a graviton.

The easiest way to ascertain the mass of a graviton is to investigate if or not there is a slight difference in the speed of graviton ‘particle’ propagation and of HFGW in transit from a ‘source’ to the detector. Visser’s [67] (1998) mass of a graviton paper [68] presents a theory which passes the equivalence test, but which has problem with depending upon a non-dynamical background metric. I.e. gravitons are assumed by both him, and also Clifford Will’s [66] write up of experimental G.R. to have mass. This document accepts that there is a small graviton mass, which the author has estimated to be on the order of  $10^{-60}$  kilograms. Small enough so the following approximation is valid. Here,  $v_g$  is the speed of graviton ‘propagation’,  $\lambda_g$  is the Compton wavelength of a graviton with  $\lambda_g = h/m_g c$ , and  $f \approx 10^{10}$  Hertz in line with L. Grischuck’s treatment of relic HFGW’s [22]. In addition, the high value of relic HFGW’s leads to naturally fulfilling  $hf \gg m_g c^2$  so that [66]

$$(v_g/c)^2 \approx 1 - (c/\lambda_g f)^2 \quad (A1)$$

But equation (1) above is an approximation of a much more general result which may be rendered as

$$(v_g/c)^2 \equiv 1 - (m_g c^2/E)^2 \quad (A2)$$

The terms  $m_g$  and E refers to the graviton rest mass and energy, respectively. Now specifically in line with applying the Li Baker detector, [38] physics researchers can ascertain what E is, with experimental data from the Li Baker detector, and then the next question needs to be addressed, namely if D is the distance between a detector, and the source of a HFGW/ Graviton emitter source

$$1 - v_g/c = 5 \times 10^{-17} \cdot \left[ \frac{200 \text{Mpc}}{D} \right] \cdot \left( \frac{\Delta t}{1 \text{sec}} \right) \quad (A3)$$

The above formula depends upon  $\Delta t \equiv \Delta t_a - (1+Z)\Delta t_e$ , with where  $\Delta t_a$  and  $\Delta t_e$  are the differences in arrival time and emission time of the two signals ( HFGW and Graviton propagation ), respectively, and  $Z$  is the redshift of the source.  $Z$  is meant to be the red shift. Specifically, the situation for HFGW is that for early universe conditions, that  $Z \geq 1100$ , in fact for very early universe conditions in the first few milli seconds after the big bang, that  $Z \sim 10^{25}$ . An enormous number.



The first question which needs to be asked is, if or not the Visser [67] non-dynamical background metric correct, for early universe conditions so as to avoid the problem of the limit of small graviton mass does not coincide with pure GR, and the predicted perihelion advance, for example, violates experiment . A way forward would be to configure data sets so in the case of early universe conditions that one is examining appropriate  $Z \gg 1100$  but with extremely small  $\Delta t_e$  times, which would reflect upon generation of HFGW before the electro weak transition, and after the INITIAL onset of inflation.

I.e. the Li – Baker detector system should be employed [38] as to pin point experimental conditions so to high accuracy , the following is an adequate presentation of the difference in times,  $\Delta t$  . I.e.

$$\Delta t \equiv \Delta t_a - (1 + Z)\Delta t_e \rightarrow \Delta t_a - \varepsilon^+ \approx \Delta t_a \quad (\text{A4})$$

The closer the emission times for production of the HFGW and Gravitons are to the time of the initial nucleation of vacuum energy of the big bang, the closer we can be to experimentally using equation (4) above as to give experimental criteria for stating to very high accuracy the following.

$$1 - v_g/c \cong 5 \times 10^{-17} \cdot \left[ \frac{200 \text{Mpc}}{D} \right] \cdot \left( \frac{\Delta t_a}{1 \text{sec}} \right) \quad (\text{A5})$$

More exactly this will lead to the following relationship which will be used to ascertain a value for the mass of a graviton. By necessity, this will push the speed of graviton propagation very close to the speed of light. In this, we are assuming an enormous value for D

$$v_g/c \cong 1 - 5 \times 10^{-17} \cdot \left[ \frac{200 \text{Mpc}}{D} \right] \cdot \left( \frac{\Delta t_a}{1 \text{sec}} \right) \quad (\text{A6})$$

This Eq. (A6) relationship should be placed into  $\lambda_g = h/m_g c$  with a way to relate this above value of

$(v_g/c)^2 \cong 1 - (m_g c^2/E)^2$ , with an estimated value of E coming from the Li- Baker detector[38] and field theory calculations, as well as to make the following argument rigorous, namely

$$\left[ 1 - 5 \times 10^{-17} \cdot \frac{200 \text{Mpc}}{D} \cdot \frac{\Delta t_a}{1 \text{sec}} \right]^2 \cong 1 - \left( \frac{m_g c^2}{E} \right)^2 \quad (\text{A7})$$

A suitable numerical treatment of this above equation, with data sets could lead to a range of bounds for  $m_g$ , as a refinement of the result given by Clifford Will [66] for graviton Compton wavelength bounded behavior for a lower bound to the graviton mass, assuming that  $h$  is the Planck's constant.

$$\begin{aligned} \lambda_g \equiv \frac{h}{m_g c} &> 3 \times 10^{12} \text{ km} \cdot \left( \frac{D}{200 \text{Mpc}} \cdot \frac{100 \text{Hz}}{f} \right)^{1/2} \cdot \left( \frac{1}{f \Delta t} \right)^{1/2} \\ &\cong 3 \times 10^{12} \text{ km} \cdot \left( \frac{D}{200 \text{Mpc}} \cdot \frac{100 \text{Hz}}{f} \right)^{1/2} \cdot \left( \frac{1}{f \Delta t_a} \right)^{1/2} \end{aligned} \quad (\text{A8})$$

The above Eq.(A8) gives an upper bound to the mass  $m_g$  as given by

$$m_g < \left(\frac{c}{h}\right) / 3 \times 10^{12} \text{ km} \cdot \left(\frac{D}{200 \text{ Mpc}} \cdot \frac{100 \text{ Hz}}{f}\right)^{1/2} \cdot \left(\frac{1}{f \cdot \Delta t_a}\right)^{1/2} \quad (\text{A9})$$

Needless to say that an estimation of the bound for the graviton mass  $m_g$ , and the resulting Compton wavelength  $\lambda_g$  would be important to get values of the following formula, namely

$$V(r)_{\text{gravity}} \cong \frac{MG}{r} \exp(r/\lambda_g) \quad (\text{A10})$$

Clifford Will gave for values of frequency  $f \equiv 100$  Hertz enormous values for the Compton wave length, i.e. values like  $\lambda_g > 6 \times 10^{19}$  kilometers. Such enormous values for the Compton wave length make experimental tests of Eq. (A10) practically infeasible. Values of  $\lambda_g \approx 10^{-5}$  centimeters or less for very high HFGW data makes investigation of Eq. (A10) above far more tractable.

### **Application to Gravitational Synchrotron radiation, in accelerator physics**

Eric Davis, quoting Pisen Chen's article [69] written in 1994 estimates that a typical storage ring for an accelerator will be able to give approximately  $10^{-6} - 10^3$  gravitons per second. Quoting Pisen Chen's [69] 1994 article, the following for graviton emission values for a circular accelerator system, with  $m$  the mass of a graviton, and  $M_p$  being Planck mass.  $N$  as mentioned below is the number of 'particles' in a ring for an accelerator system, and  $n_b$  is an accelerator physics parameter for bunches of particles which for the LHC is set by Pisen Chen [69] as of the value 2800, and  $N$  for the LHC is about  $10^{11}$ . And, for the LHC Pisen Chen sets  $\gamma$  as  $.88 \times 10^2$ , with  $\rho[m] \approx 4300$ . Here,  $m \sim m_{\text{graviton}}$  acts as a mass charge.

$$N_{\text{GSR}} \sim 5.6 \cdot n_b^2 \cdot N^2 \cdot \frac{m^2}{M_p^2} \cdot \frac{c \cdot \gamma^4}{\rho} \quad (\text{A11})$$

The immediate consequence of the prior discussion would be to obtain a more realistic set of bounds for the graviton mass, which could considerably refine the estimate of  $10^{11}$  gravitons produced per year at the LHC, with realistically  $365 \times 86400 \text{ seconds} = 31536000 \text{ seconds in a year, leading to } 3.171 \times 10^3 \text{ gravitons produced per second. Refining an actual permitted value of bounds for the accepted graviton mass, } m, \text{ as given above, while keeping } M_p \sim 1.2209 \times 10^{19} \text{ GeV}/c^2 \text{ would allow for a more precise set of gravitons per second which would significantly enhance the chance of actual detection, since right now for the LHC there is too much general uncertainty as to the likelihood of where to place a detector for actually capturing / detecting a graviton.}$

### **Conclusion, falsifiable tests for the Graviton are closer than the physics community thinks**

*The physics community now has an opportunity to experimentally infer the existence of gravitons as a knowable and verifiable experimental datum with the onset of the LHC as an operating system. Even if the LHC is not used, Pisen Chens parameterization of inputs from his table [69] right after his equation (8) as inputs into Eq. (A11) above will permit the physics community to make progress as to detection of Gravitons for, say the Brookhaven site circular ring accelerator system. Tony Rothman's [70] predictions as to needing a detector the size of Jupiter to obtain a single experimentally falsifiable set of procedures is*

defensible only if the wave- particle duality induces so much uncertainty as to the mass of the purported graviton, that worst case model building and extraordinarily robust parameters for a Rothman style graviton detector have to be put in place.

The Li- Baker detector[71] can help with bracketing a range of masses for the graviton, as a physical entity subject to measurements. Such an effort requires obtaining rigorous verification of the approximation used to the effect that  $\Delta t \equiv \Delta t_a - (1 + Z)\Delta t_e \rightarrow \Delta t_a - \varepsilon^+ \approx \Delta t_a$  is a defensible approximation.

Furthermore, obtaining realistic inputs for distance  $D$  for inputs into Eq (A9) above is essential. The expected pay offs of making such an investment would be to determine the range of validity of Eq. (A10) , i.e. to what degree is gravitation as a force is amendable to post Newtonian approximations. The author asserts that equation (10) can only be realistically be tested and vetted for sub atomic systems, and that with the massive Compton wavelength specified by Clifford Will cannot be done with low frequency gravitational waves.

Furthermore, a realistic bounding of the graviton mass would permit a far more precise calibration of Eq. (A11) as given by Pisen Chen in his 1994 article.[69]

## Appendix B. Basic physics of achieving minimum

$l_{\text{min-length-string}} \equiv 10^\alpha \cdot l_{\text{Planck}}$  **precision in CMBR power spectra measurements**

Begin first of all looking at

$$\frac{\Delta T}{T} \equiv \sum_{l,m} a_{lm} Y_{l,m}(\theta, \phi) \quad (\text{B1})$$

This leads to consider what to do with

$$C_l = \left\langle |a_{l,m}|^2 \right\rangle \quad (\text{B2})$$

Samtleben et al (2007) [71] consider then what the experimental variance in this power spectrum, to the tune of an achievable precision given by

$$\frac{\Delta C_l}{C_l} = \sqrt{\frac{2}{2l+1}} \cdot \left( \frac{1}{\sqrt{f_{\text{sky}}}} + \frac{4\pi \cdot (\Delta T_{\text{exp}})^2}{C_l} \cdot \sqrt{f_{\text{sky}}} \cdot e^{l^2 \sigma_b^2} \right) \quad (\text{B3})$$

$f_{\text{sky}}$  is the fraction of the sky covered in the measurement , and  $\Delta T_{\text{exp}}$  is a measurement of the total experimental sensitivity of the apparatus used. Also  $\sigma_b$  is the width of a beam , while we have a minimum value of  $l_{\text{min}} \approx (1/\Delta\Theta)$  which is one over the fluctuation of the angular extent of the experimental survey.

I.e. contributions to  $C_l$  uncertainty from sample variance is equal to contributions to  $C_l$  uncertainty from noise. The end result is

$$4\pi \cdot f_{sky} = C_l \cdot (\exp[-l^2 \sigma^2]) / (\Delta T)^2 \quad (B4)$$

### Appendix C : Cosmological perturbation theory and tensor fluctuations (Gravity waves)

Durrer [72] (2004) reviews how to interpret  $C_l$  in the region where we have  $2 < l < 100$ , roughly in the region of the Sachs-Wolf contributions due to gravity waves. We begin first of all by looking at an initial perturbation, using a scalar field treatment of the 'Bardeen potential'  $\Psi$ . This can lead us to put up, if  $H_i$  is the initial value of the Hubble expansion parameter

$$k^3 |\Psi|^2 \cong \left( \frac{H_i}{M_p} \right)^2 \quad (C1)$$

And

$$\langle |\Psi|^2 \rangle \cdot k^3 = A^2 k^{n-1} \cdot \eta_0^{n-1} \quad (C2)$$

Here we are interpreting  $A$  = amplitude of metric perturbations at horizon scale, and we set  $k = 1/\eta_0$ , where  $\eta$  is the conformal time, according to  $dt \equiv a d\eta$  = physical time, where we have  $a$  as the scale factor. Then for  $2 < l < 100$ , and  $-3 < n < 3$ , and a pure power law given by

$$\langle |H(k, \eta = 1/k)|^2 \rangle \cdot k^3 = A_T^2 k^{n_T} \cdot \eta_0^{-n_T} \quad (C3)$$

We get for tensor fluctuation, i.e. gravity waves and a scale invariant spectrum with  $n_T = 0$

$$C_l^{(T)} \approx \frac{A_T^2}{(l+3) \cdot (l-2)} \cdot \frac{1}{15\pi} \quad (C4)$$

### Appendix D: Linking the thin shell approximation, Weyl quantization, and the Wheeler De Witt equation

This is a recapitulation of what is written by S. Capozziello, et al (2000) [73] for physical review A, which is assuming a generally spherically symmetric line element. The upshot is that we obtain a dynamical evolution equation, similar in part to the Wheeler De Witt equation which can be quantified as  $H|\Psi\rangle = 0$

Which in turn will lead to, with qualifications, for thin shell approximations  $|x| \ll 1$ ,

$$\Psi'' + a^2 x^4 \Psi = 0 \quad (D1)$$

so that  $Z_{1/6}$  is a spherical Bessel equation for which we can write

$$\Psi \equiv \sqrt{x} Z_{1/6} \left( \frac{a}{3} x^3 \right) \sim x^{2/3} \quad (D2)$$

Similarly,  $|x| \gg 1$  leads to

$$\Psi \equiv \sqrt{x} Z_{1/6} \left( \frac{a}{3 \cdot \sqrt{2}} x^3 \right) \quad (D3)$$

Also, when  $x \cong 1$

$$\Psi \equiv \left[ \sqrt{2a^2 \cdot (x-1)} \right]^3 Z_{-3/4} \left( \frac{8}{3} \cdot a \cdot (x-1)^{3/2} \right) \quad (D4)$$

Realistically, in terms of applications, we will be considering very small  $x$  values, consistent with conditions near a singularity/ worm hole bridge between a prior to our present universe. This is for  $x \equiv R/R_{equilibrium}$

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