Does Heisenberg's Uncertainty Collapse at the Planck Scale? Heisenberg's Uncertainty Principle Becomes the Certainty Principle

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Abstract

In this paper we show that Heisenberg's uncertainty principle, combined with key principles from Max Planck and Einstein, indicates that uncertainty collapses at the Planck scale. In essence we suggest that the uncertainty principle becomes the certainty principle at the Planck scale. This can be used to find the rest-mass formula for elementary particles consistent with what is already known. If this interpretation is correct, it means that Einstein's intuition that "God Does Not Throw Dice with the Universe" could also be correct. We interpret this to mean that Einstein did not believe the world was ruled by strange uncertainty phenomena at the deeper level, and we will claim that this level is the Planck scale, where all uncertainty seems to collapse. The bad news is that this new-found certainty can only can last for one Planck second! We are also questioning, without coming to a conclusion, if this could have implications for Bell's theorem and hidden variable theories.

Key words: Heisenberg's uncertainty principle, Planck length, Planck particle, Planck momentum.

1 The Three Giants

In 1899, Max Planck introduced what he called natural units, namely the Planck length, the Planck mass, the Planck second, and the Planck energy [1, 2]. He derived these fundamental units from Newton's gravitational constant [3], the speed of light, and the Planck constant. In 1905, Albert Einstein introduced special relativity theory [4]. In 1927, Heisenberg [5] introduced his uncertainty principle. The Heisenberg uncertainty principle is one of the cornerstones in quantum mechanics. The Planck constant is also a key here. However, the Planck length, the Planck mass, the Planck energy, and the Planck time have never been really understood or directly linked to a consistent quantum theory.

Albert Einstein is, of course, also one of the founders of quantum theory, in particular with his insight on the photoelectric effect. However, he was very skeptical on much of what followed in quantum physics, especially in relation to strange uncertainty phenomena. It was not necessarily the case that he did not believe in such models, but he felt that the theories did not capture the full picture of reality. Einstein is famous for his statement, see [6]

God Does Not Throw Dice with the Universe

From the derivations and logical reasoning that we are working with here, it looks like Einstein was right, even though many have maintained that he was wrong on this point. We will use concepts from special relativity theory, Max Planck, and Heisenberg, and we find that the unification of these three Giants of Physics seems to lead to a breakdown of uncertainty at the Planck scale. Further, this can be used to derive well-known formulas for the rest-mass of particles.

2 Does Uncertainty Collapse at the Planck Scale?

Heisenberg's uncertainty principle is given by

$$\Delta p \Delta x \geq \hbar$$

Lloyd Motz, while working at the Rutherford Laboratory in 1962, [7, 8, 9] suggested that there was probably a very fundamental particle with a mass equal to the Planck mass; today it is known as the Planck mass particle. The momentum of a Planck mass particle must also follow the relativistic mass "rule" and be

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$$p_p = \frac{m_p v}{\sqrt{1-\frac{v^2}{c^2}}} = 0 \tag{1}$$

Haug [10, 11, 12] has shown that the maximum velocity any particle with rest-mass likely can attain is

$$v_{max} = c\sqrt{1-\frac{l_p^2}{\bar{\lambda}^2}} \tag{2}$$

where $\bar{\lambda}$ is the reduced Compton wavelength of the particle and l_p is the Planck length. Only for the Planck mass particle does $\bar{\lambda} = l_p$, and only for the Planck mass particle do we have maximum velocity of zero:

$$v_{max} = c\sqrt{1-\frac{l_p^2}{l_p^2}} = 0 \tag{3}$$

This remarkably also means the Planck mass particle always has zero momentum. However it is normally assumed the Planck mass momentum is $p_p = m_p c$. This we do not disagree with, but we think the correct interpretation is that there is a rest-mass momentum equal to mc when a particle stands still, and that the Planck mass particle always stand still when it exist, and only have rest-mass momentum. It also only have rest-mass energy and no kinetic energy. No particle with rest mass can anyway move at the speed of light, as one mistakenly could suspect is indicated by $p_p = m_p c$. A rest mass particle moving at the speed of light would mean infinite kinetic energy, which is impossible. The key is that the Planck mass particle must stand still we will claim that the Planck mass particle only last for one Planck second. We also get a hint about the lifetime of a Planck particle from the Planck acceleration, $a_p = \frac{c^2}{l_p} \approx 5.56092 \times 10^{51}\ m/s^2$. The Planck acceleration is assumed to be the maximum possible acceleration by several physicists; see [14, 15], for example. The velocity of a particle that undergoes Planck acceleration will actually reach the speed of light within one Planck second: $a_p t_p = \frac{c^2}{l_p}\frac{l_p}{c} = c$. However, we know that nothing with rest-mass can travel at the speed of light, so no "normal" particle can undergo Planck acceleration if the shortest possible acceleration time interval is the Planck second. The solution is simple. The Planck acceleration is an internal acceleration inside the Planck particle that within one Planck second turns the Planck mass particle into pure energy. This also explains why the Planck momentum is so special, namely always $m_p c$, unlike for any other particles, which can take a wide range of velocities and therefore a wide range of momentums.

All other known particles have maximum velocities extremely close to that of the speed of light, but these far exceed what can be achieved at the Large Hadron Collider today, making empirical work difficult. This maximum velocity and view that the Planck mass particle must stand absolutely still mean that the Lorentz symmetry must be broken at the Planck scale, something that also is predicted by several quantum gravity theories [13].

All other particles can show a wide range of momentum, because they can have significant variations in their velocity and therefore, they also have uncertainty in their momentum.

As long as we assume that the Planck particle has a known momentum of $m_p c$, then we find that

$$\begin{aligned} \Delta p_p \Delta x &\geq \hbar \\ m_p c \Delta x &\geq \hbar \\ m_p c &\geq \frac{\hbar}{\Delta x} \\ m_p &\geq \frac{\hbar}{\Delta x}\frac{1}{c} \end{aligned} \tag{4}$$

We know that the mass of any elementary particle can be written in the form

$$m = \frac{\hbar}{\bar{\lambda}}\frac{1}{c} \tag{5}$$

and since the reduced Compton wavelength of the Planck mass particle is $\bar{\lambda} = l_p$ then we must have

$$m_p = \frac{\hbar}{l_p}\frac{1}{c} \tag{6}$$

Inputting formula 6 into formula 4 and solving with respect to Δx we get

$$\begin{aligned} \frac{\hbar}{l_p}\frac{1}{c} &\geq \frac{\hbar}{\Delta x}\frac{1}{c} \\ \Delta x &\geq l_p \end{aligned} \tag{7}$$

This gives two important insights. Many (perhaps even most) physicists are of the opinion that the Planck length is the minimum distance we can measure, and from the analysis above, this would mean that we cannot have an uncertainty smaller than the Planck length. This has several important implications; for example, it means the speed limit of just $v < c$ cannot hold for anything with rest-mass, as the highest relativistic mass must now be the Planck mass; see [16] for detailed discussion on this point. Instead, we get the exact speed limit given by Haug's maximum speed limit for anything with rest-mass. This speed limit is, for any known observed particle, very close to the speed of light, except for the special case of the Planck particle where it "surprisingly" is zero. Because there is no uncertainty in the Planck momentum due to there being no uncertainty in the velocity of the Planck particle, we will claim there is no longer an uncertainty in its position. This corresponds well with the points above, where we have shown that the Planck particle must stand absolutely still, but only for one Planck second. So, its position is simply the shortest possible distance we can measure, even hypothetically, which is the Planck length. That is to say, only for the Planck mass particle can we know the momentum and the position at the same time and, in fact, we only need one of them and then we can deduce the other one. This means that at the Planck scale Heisenberg's uncertainty principle breaks down and becomes the certainty principle as recently showed in quantum mechanical calculation in [17]. This seems to also indicate that the minimum uncertainty in position for all other particles seems to be limited by the Planck length

$$\Delta x_{minimum} = l_p \tag{8}$$

To reiterate, we claim all uncertainty will likely disappear at the Planck scale, but this world is certain for only one Planck second. The Planck momentum is linked to the speed of light and no mass can move at the speed of light. However, a Planck particle can and must dissolve into pure energy within one Planck second.

Still, for all non-Planck particles we have

$$\begin{aligned} \Delta p \Delta x &\geq \hbar \\ \Delta \frac{mv}{\sqrt{1-\frac{v^2}{c^2}}} \Delta x &\geq \hbar \end{aligned} \tag{9}$$

If we now assume we know the rest-mass of the particle in question, an electron, for example, then the uncertainty in momentum must come from the uncertainty in the velocity. This means we have

$$\frac{m\Delta v}{\sqrt{1-\frac{(\Delta v)^2}{c^2}}} \geq \frac{\hbar}{\Delta x} \tag{10}$$

Now if we set Δx to what we know is the minimum possible uncertainty in it, namely the Planck length, and we know the rest-mass of the particle, then it is even more clear that what is causing the uncertainty in the momentum is the uncertainty in the velocity:

$$\begin{aligned} \frac{m\Delta v}{\sqrt{1-\frac{(\Delta v)^2}{c^2}}} l_p &\geq \hbar \\ \frac{\frac{\hbar}{\bar{\lambda}}\frac{1}{c}\Delta v}{\sqrt{1-\frac{(\Delta v)^2}{c^2}}} l_p &\geq \hbar \\ \frac{\frac{1}{c}\Delta v}{\sqrt{1-\frac{(\Delta v)^2}{c^2}}} &\geq \frac{\bar{\lambda}}{l_p} \\ \frac{\Delta v}{\sqrt{1-\frac{(\Delta v)^2}{c^2}}} &\geq \frac{\bar{\lambda}}{l_p} c \end{aligned} \tag{11}$$

Solved with respect to Δv this gives

$$\begin{aligned}
\frac{v^2}{1-\frac{(\Delta v)^2}{c^2}} &\geq \frac{\bar{\lambda}^2}{l_p^2}c^2 \\
(\Delta v)^2 &\leq \frac{\bar{\lambda}^2}{l_p^2}c^2\left(1-\frac{(\Delta v)^2}{c^2}\right) \\
(\Delta v)^2\left(1+\frac{\bar{\lambda}^2}{l_p^2}\right) &\leq \frac{\bar{\lambda}^2}{l_p^2}c^2 \\
(\Delta v)^2 &\leq \frac{\frac{\bar{\lambda}^2}{l_p^2}c^2}{\left(1+\frac{\bar{\lambda}^2}{l_p^2}\right)} \\
\Delta v &\leq \frac{c}{\sqrt{1+\frac{l_p^2}{\bar{\lambda}^2}}} \qquad (12)
\end{aligned}$$

This is basically the same derivation as given by Haug in a working paper previously [16]. What is new in this paper is that we are showing how Heisenberg's uncertainty principle likely leads to a breakdown of uncertainty at the Planck scale.

3 Future Research: Bell's Theorem

Several researchers have pointed out that by implicitly assuming all possible Bell measurements occur simultaneously, then all proofs of Bell's Theorem [18] violate Heisenberg's uncertainty principle [19]. We wonder what it could mean for the interpretation of Bell's Theorem if the Heisenberg uncertainly principle breaks down at the Planck scale and we then go from uncertainty to certainty (determinism). If Heisenberg?s uncertainty principle breaks down at the Planck scale, could this open up the possibility of hidden variables as suggested by Einstein, Podolsk and Rosen in 1935? See [20].

Clover, as cited above, claims that

> *Only time-independent classical local hidden variable theories are forbidden by violations of the original Bell inequalities; time-dependent quantum local hidden variable theories can satisfy this new bound and agree with experiment.*

Further Clover interestingly states [21]

> *By implicitly assuming that all measurements occur simultaneously, Bell's Theorem only applied to local theories that violated Heisenberg's Uncertainty Principle.*

We are currently studying more about Bell's theorem and hidden variable ideas. Although it is too early to draw any conclusions at this point, we encourage others to see if the extended version of Heisenberg's uncertainty principle presented in this paper can provide further insights here.

4 Conclusion

In this paper, we have shown that Heisenberg's uncertainty principle likely collapses to a certainty principle at the Planck scale. This indicates that Einstein was right when he claimed "God Does Not Throw Dice." The Planck mass particle is unique and is the only particle that has a known momentum equal to $p = mc$. There is likely no room for uncertainty in the velocity of a Planck mass particle, simply because it is at absolute rest, even as observed across different reference frames. This hypothesis is supported by quantum mechanical derivations and is ready for evaluation by other researchers.

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