## Electrostatic Force and Charge Structure

Preston Guynn

Guynn Engineering, 1776 Heritage Center Drive, Suite 204
Wake Forest, North Carolina, United States 27587
guynnengineering@gmail.com

In our previous report, Electromagnetic Effects and Structure of Particles due to Special Relativity, we proved that electromagnetic effects are due to special relativity by showing 11 significant digits of correspondence between the maximum value of rotation minus precession and the fine structure constant. We now provide the theoretical basis for the correspondence and its relationship to the previously derived electron and proton structure.

## Introduction

Because time dilation occurs only in the direction of motion, and not in the transverse direction, an angle observed during motion differs from an angle observed when stationary according to ${ }^{1}$

$$
\begin{equation*}
\frac{\Delta \theta}{2 \pi}=\gamma-1 \tag{1}
\end{equation*}
$$

where $\gamma$ is the Lorentz factor. Angular rotation, $\omega$, results in angular precession, $\omega_{P}$, according to ${ }^{1}$

$$
\begin{equation*}
\frac{\omega_{P}}{\omega}=\frac{\Delta \theta}{2 \pi}=\gamma-1 \tag{2}
\end{equation*}
$$

The sense of angular precession is of a secondary rotation in the opposite direction of the primary angular rotation. Angular rotation minus angular precession gives a difference angular velocity

$$
\begin{equation*}
\omega_{d}=\omega-\omega_{P}=\omega(2-\gamma) \tag{3}
\end{equation*}
$$

This can be thought of as effective angular velocity with regard to angular momentum and kinetic energy. Multiplying Equation 3 by radius, we can write difference velocity in terms of rotation velocity.

$$
\begin{equation*}
v_{d}=v(2-\gamma) \tag{4}
\end{equation*}
$$

Figure 1 shows difference velocity graphed from Equation 4.


Fig 1. Difference velocity as a function of rotation velocity

When we solve for the maximum difference velocity we find

$$
\begin{equation*}
v_{m}=\left(2^{2 / 3}-1\right)^{3 / 2} c \cong 134965504.63776 \mathrm{~m} / \mathrm{s} \tag{5}
\end{equation*}
$$

where $c$ is the speed of light.

## Analysis

The magnitude of the electrostatic force between two charged particles separated by distance $r$ can be written as

$$
\begin{equation*}
F(r)=\frac{2 \pi}{r^{2} c}\left(\frac{\frac{\sqrt{3}}{2} \hbar k_{1}}{\frac{1}{2} m_{e} v_{m}^{2}}+\sqrt{2} \hbar v_{m} k_{2}\right) \tag{6}
\end{equation*}
$$

where

$$
\begin{align*}
& k_{1} \equiv \mathrm{~kg} \mathrm{~m}^{4} / \mathrm{s}^{4}  \tag{7}\\
& k_{2} \equiv \mathrm{~m} / \mathrm{s} \tag{8}
\end{align*}
$$

and $m_{e}$ is electron mass, and $h$ is the reduced Planck constant. Note that $k_{1}$ and $k_{2}$ effect unit transformations, which will be described below. Constants $c$ and $v_{m}$ are exact values.

The uncertainty of the calculation is only that of the reported values of $h$ and $m_{e}$. The value obtained using Equation 6 matches the value from Coulomb's law applied to two elementary charges to 11 significant digits.

The first term in parenthesis in Equation 6 is charge total angular momentum divided by the kinetic energy of electron mass rotating with difference velocity $v_{m}$, modified by a unit transformation. The second term in parenthesis in Equation 6 is photon total angular momentum multiplied by $v_{m}$, modified by a different unit transformation.

We see from Equation 2 that $\Delta \theta=2 \pi$ when $\omega=\omega_{\mathrm{P} \text {. The physical interpretation of this is }}$ that an angle perceived when rotating differs by $2 \pi$ from the same angle perceived while stationary when the rotation angular velocity equals the precession angular velocity. This condition exists when rotation velocity equals $\sqrt{3} / 2 c$ so $\gamma=2$. This rotation velocity is labeled $v_{0}$ in Figure 1. In other words, at rotation velocity $v_{0}$ the difference velocity is 0 because rotation minus precession equals 0 , so there is no kinetic energy or angular momentum. The angular difference is the source of the $2 \pi$ factor in Equation 6.

Now that we have established the significance of all of the individual components in Equation 6, we turn to the relationship between the components and the previously derived models of the physical structure and behavior of the electron and proton.

First, as a brief review of our previous report, both electron and proton consist of three mutually orthogonal rings of rotating mass. The electron rings' difference velocity remains between $+/-v_{m}$, with each ring's angular momentum $S_{Z}=+/-\mathrm{h} / 2$ at $+/-v_{m}$. This is shown in Figure 2.


Fig 2. Electron ring difference velocity as a function of rotation velocity, with angular momentum annotated.

The proton maximum difference velocity is

$$
\begin{equation*}
v_{m p}=v_{m} \sqrt{\frac{m_{e}}{m_{p}}} \cong 3149694.18144 \mathrm{~m} / \mathrm{s} \tag{9}
\end{equation*}
$$

where $m_{p}$ is proton mass. The proton rings' difference velocity remains between $+/-v_{m p}$, with each ring's angular momentum $S_{Z}=+/-\mathrm{h} / 2$ at $+/-v_{m p}$. This is shown in Figure 3.


Fig 3. Proton ring difference velocity as a function of rotation velocity, with angular momentum annotated.

Having reviewed some of the model of structure and behavior of electron and proton from our previous work, we move on to the relationship between the components of Equation 6. The denominator of the first tem in parenthesis in Equation 6 takes the form of kinetic energy. The kinetic energy of one of an electron's three mutually orthogonal rings when rotating at $v_{m}$ is

$$
\begin{equation*}
E_{k e}=\frac{1}{2} \frac{m_{e}}{3} v_{m}^{2} \cong 2.7655614 \mathrm{e}-15 \text { Joules } \tag{10}
\end{equation*}
$$

The kinetic energy of one of a proton's three mutually orthogonal rings when rotating at $v_{m p}$ is

$$
\begin{equation*}
E_{k p}=\frac{1}{2} \frac{m_{p}}{3} v_{m p}^{2} \cong 2.7655614 \mathrm{e}-15 \text { Joules } \tag{11}
\end{equation*}
$$

Equations 10 and 11 show that the kinetic energy of electron and proton rings is equal when they are rotating with their difference velocities each at maximum. So we see that the denominator of the first term in parenthesis of Equation 6 is the sum of the kinetic energy of all three rings of either the electron or proton. This is consistent since Equation 6 can be used to calculate the magnitude of the electrostatic force between either two electrons or two protons or one proton and one electron.

The magnitude of the first term in parenthesis in Equation 6 is equivalent to a change in total angular momentum from maximum to 0 , divided by a change in kinetic energy from maximum to 0 . This change occurs for both angular momentum and kinetic energy when $v_{d}$ transitions from the charge's maximum to 0 , resulting in the mass rotating at the velocity labeled $v_{0}$ in Figure 1.

As described in our previous report, angular momentum is conserved, so when a charge's angular momentum is decreased, the angular momentum in the space adjacent to the charge is increased. That increase in the angular momentum of space adjacent to the electron takes the form of a photon, which explains the second term in parenthesis in Equation 6.

The magnitude of the second term in parenthesis of Equation 6 is the angular momentum of a photon between two charges multiplied by $v_{m}$. The $v_{m}$ factor is because the photon's maximum difference velocity is $v_{m}$ with respect to charge rotation at $v_{0}$. In measuring the electrostatic force between two charged particles, there are three components as noted with Equation 6. There are the two charged particles, and a photon between the particles.

Unit modifiers $k_{1}$ and $k_{2}$ are required because force is not simply mass multiplied by acceleration. At the particle level, force has a $2 \pi$ magnitude component from an angular difference due to special relativity. The asymmetrical effect of time dilation extends the conditions under which force results. Units under the SI system are not functions of velocity and angle, so the effects of particles rotating in the ranges shown in Figures 2 and 3 , and the effect of a stationary photon, require unit modifiers.

## Discussion

Equations 10 and 11 show that the kinetic energies of the electron and proton, when each $v_{d}$ is at maximum, are equal. We now consider the maximum difference angular velocity of electron and proton.

In order to find the maximum difference angular velocity of the electron, we use the electron radius, which was derived in our previous report ${ }^{2}$. $R_{e} \cong 1.2866358293764310^{-12}$ m . The electron maximum difference angular velocity can be written as

$$
\begin{equation*}
\omega_{m}=v_{m} / R_{e} \cong 1.04897983995310^{20} \tag{12}
\end{equation*}
$$

In order to find the maximum difference angular velocity of the proton, we use the proton radius which was derived in our previous paper ${ }^{2}$. $R_{p} \cong 3.0026260386277210^{-14} \mathrm{~m}$. The electron maximum difference angular velocity can be written as

$$
\begin{equation*}
\omega_{m p}=v_{m p} / R_{p} \cong 1.04897983995310^{20} \tag{13}
\end{equation*}
$$

Equations 12 and 13 show that the maximum difference angular velocities of electron and proton are equal.

Charge is conserved because mass with angular difference velocity in the range $+/-\omega_{m}$ is a particle which is always coupled to space, exhibiting the effects of charge, and it always remains in that range.

## Conclusion

In our model charged particles consist of three mutually orthogonal rings of rotating mass. The difference angular velocity for both electron and proton remains between +/$\omega_{m}$, while the difference velocity ranges are shown in Figures 2 and 3 . The equation for the magnitude of electrostatic force between two charged particles is written in terms of the structure and behavior of our model in Equation 6, and the result of Equation 6 exactly matches the result of applying Coulomb's law to two elementary charges.

We have proven that charge structure and electrostatic force are due to special relativity. With a direct interpretation of the physical meaning of previously known Equation 2, and with a simple extension, we arrived at Equation 4 and its graph in Figure 1. The maximum value and the zero crossing of the difference velocity graphed in Figure 1 lead to every component of Equation 6, which results in an 11 significant digit correspondence with the experimentally established electrostatic force.

The components of Equation 6 have clear and concise meaning within the structural model, and the relationship between the components is reasonable only within the structural model. The inner consistency of the components of Equation 6, their direct correspondence to each other and the model, and 11 significant digits of correspondence to experimental results is the strongest confirmation of the theoretical basis of any physical law of which the author is aware. The number of assumptions is few. The special relativistic effect of precession is well established. The exact match between the theoretical model, the equation based on it, and the measured value of electrostatic force all assure us that the electron and proton have the structure and behavior described in the model.

The development of Equation 6 is confirmation of our previous work in Electromagnetic Effects and Structure of Particles due to Special Relativity. The models of particle structure and their rotational behavior explain the origin of charge, conservation of charge, and its effects. The model clearly explains electron and proton per axis and total angular momentum, photon emission, spin, spin-flip, difference between electron and proton spin-flip, why there are no magnetic monopoles, how the neutron has magnetic moment though it has no charge, the negative edge of the neutron, the Larmor formula
for radiated power, and many other characteristics. The current model without extension or modification explains anti-matter by orientation and counter rotation. Anti-matter may be described more fully in a future work, but it is easily understood from considering the third graph in Appendix A. The very simple and straightforward model described in our previous work and supported theoretically herein, appears capable of explaining most particle physics, material physics, and chemistry.

The discovery of electron structure and knowledge of charged particle structure and behavior in general will lead to advances in practically every area of physics. However, that the electron is now known to have structure and has been proven not to be a point particle has broad implications for previous research. Physics research that was based on the concept of the electron as a point particle can now be seen to have a very limited domain of validity. The author welcomes other researchers to study this and our previous work and join in applying the structural models, which have a solid theoretical basis.

## References

1) Smoot, G. F. (1998, February) Physics 139 Relativity Thomas Precession. Retrieved from https://jila.colorado.edu/arey/sites/default/files/files/seven(1).pdf
2) Guynn P. L., viXra [v3] 2017-06-12 15:13:52, 'Electromagnetic Effects and Structure of Particles due to Special Relativity', p. 7

## Appendix A



Electron rotation velocity range $v(v / c)$



