

k-Factorial

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Let n and k be positive integers, with $1 \leq k \leq n-1$.

As a generalization of the factorial and double factorial one defines the k -factorial of n as the below product of all possible strictly positive factors:

$$SKF(n) = n(n-k)(n-2k)\dots$$

Particular Cases:

$S1F(n)$ is just the well-known factorial of n , i.e. $n! = n(n-1)(n-2)\dots 1$.

$S2F(n)$ is just the well-known double factorial of n , i.e. $n!! = n(n-2)(n-4)\dots$.

$S3F(n)$ is the triple factorial of n , i.e. $n!!! = n(n-3)(n-6)\dots$.

$S4F(n)$ is the fourth factorial of n , i.e. $S4F(n) = n(n-4)(n-8)\dots$.

Examples:

$$S3F(7) = 7(7-3)(7-6) = 28.$$

$$S4F(8) = 8(8-4) = 32.$$

$$S10F(27) = 27(27-10)(27-20) = 27(17)7 = 3213.$$

Remark:

Many Smarandache type functions, such as the Smarandache (classical) function, double factorial function, ceil functions, etc. can be extended/transformed to this k -factorial definition.